

Lecture 9-red-black trees

1. What type of data structure is a Red-Black Tree?

- a) Array
- b) Linked List
- c) Balanced Binary Search Tree
- d) Hash Table

Answer: c) Balanced Binary Search Tree

2. In a Binary Search Tree, where are items smaller than a given node placed?

- a) To the left
- b) To the right
- c) Above
- d) Below

Answer: a) To the left

3. What is the guaranteed height of a balanced search tree with n items?

- a) $O(n)$
- b) $O(\log n)$
- c) $O(n^2)$
- d) $O(1)$

Answer: b) $O(\log n)$

4. How many colors can a node in a Red-Black Tree have?

- a) 1
- b) 2
- c) 3
- d) 4

Answer: b) 2

5. What color are the root and leaves (NIL) in a Red-Black Tree?

- a) Red
- b) Black
- c) Either red or black
- d) No color

Answer: b) Black

6. If a node is red in a Red-Black Tree, what color must its children be?

- a) Red
- b) Black

- c) Either red or black
- d) No color

Answer: b) Black

7. In a Red-Black Tree, all paths from a node to its NIL descendants contain:

- a) The same number of red nodes
- b) The same number of black nodes
- c) An equal number of red and black nodes
- d) No specific pattern

Answer: b) The same number of black nodes

8. What is the maximum ratio between the longest and shortest path in a Red-Black Tree?

- a) 1:1
- b) 2:1
- c) 3:1
- d) 4:1

Answer: b) 2:1

9. What is the time complexity of search, insert, and remove operations in a Red-Black Tree?

- a) $O(1)$
- b) $O(n)$
- c) $O(\log n)$
- d) $O(n^2)$

Answer: c) $O(\log n)$

10. What technique is used to fix violations after inserting or removing nodes in a Red-Black Tree?

- a) Sorting
- b) Rotations
- c) Splitting
- d) Merging

Answer: b) Rotations

11. What is the primary goal of rotations in a Red-Black Tree?

- a) To increase the height of the tree
- b) To decrease the height of the tree
- c) To change the color of nodes
- d) To remove nodes

Answer: b) To decrease the height of the tree

12. What is the time complexity of a rotation operation?

- a) $O(1)$
- b) $O(\log n)$
- c) $O(n)$
- d) $O(n^2)$

Answer: a) $O(1)$

13. How many main scenarios are there after inserting a node Z in a Red-Black Tree?

- a) 2
- b) 3
- c) 4
- d) 5

Answer: c) 4

14. In Case 0 of insertion, what action is taken when Z is the root?

- a) Color Z red
- b) Color Z black
- c) Rotate Z
- d) No action needed

Answer: b) Color Z black

15. In Case 1 of insertion, what is done when Z's uncle is red?

- a) Rotate Z
- b) Recolor Z's parents and grandparent
- c) Remove Z
- d) No action needed

Answer: b) Recolor Z's parents and grandparent

16. In Case 2 of insertion (triangle case), what action is taken?

- a) Rotate Z
- b) Rotate Z's parent
- c) Rotate Z's grandparent
- d) No rotation needed

Answer: b) Rotate Z's parent

17. In Case 3 of insertion (line case), what actions are taken?

- a) Rotate Z's grandparent only
- b) Recolor Z's parents and grandparent only
- c) Rotate Z's grandparent and recolor Z's parents and grandparent

d) No action needed

Answer: c) Rotate Z's grandparent and recolor Z's parents and grandparent

18. What is the overall time complexity of inserting a node in a Red-Black Tree?

- a) $O(1)$
- b) $O(\log n)$
- c) $O(n)$
- d) $O(n^2)$

Answer: b) $O(\log n)$

19. Which of the following is NOT an application of Red-Black Trees?

- a) Java's TreeMap
- b) C++ STL's map
- c) Linux kernel's completely fair scheduler
- d) Python's list implementation

Answer: d) Python's list implementation

20. What property of Red-Black Trees makes them efficient for use as system symbol tables?

- a) They use only two colors
- b) They guarantee $O(\log n)$ time complexity for basic operations
- c) They always have a black root
- d) They require frequent rotations

Answer: b) They guarantee $O(\log n)$ time complexity for basic operations