CSC 112: Computer Operating Systems Lecture 6

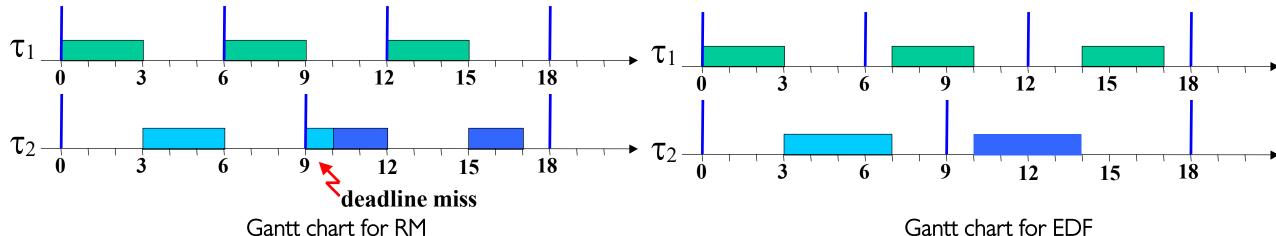
Real-Time Scheduling Exercises ANS

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- Determine schedulability of the following tasksets under (1) Rate Monotonic (RM) scheduling, using Utilization Bound test and/or Response Time Analysis (RTA) to determine taskset schedulability. (2) Earliest Deadline First (EDF) scheduling, using Utilization Bound test. We use the notation $\tau_i(C_i, T_i, D_i)$ to denote task τ_i with WCET C_i Period T_i , Deadline D_i (c.f. Slide 33 in Lecture 6)
- 1) Taskset $\tau_1(3, 6, 6), \tau_2(4, 9, 9)$
- 2) Taskset $\tau_1(3, 6, 6), \tau_2(3, 9, 9)$
- 3) Taskset $\tau_1(3, 6, 6), \tau_2(2, 9, 9)$
- 4) Taskset $\tau_1(2, 4, 4), \tau_2(4, 8, 8)$
- 5) Taskset $\tau_1(2, 5, 5), \tau_2(4, 7, 7)$
- 6) Taskset $\tau_1(1, 2, 2), \tau_2(2.5, 5, 5)$

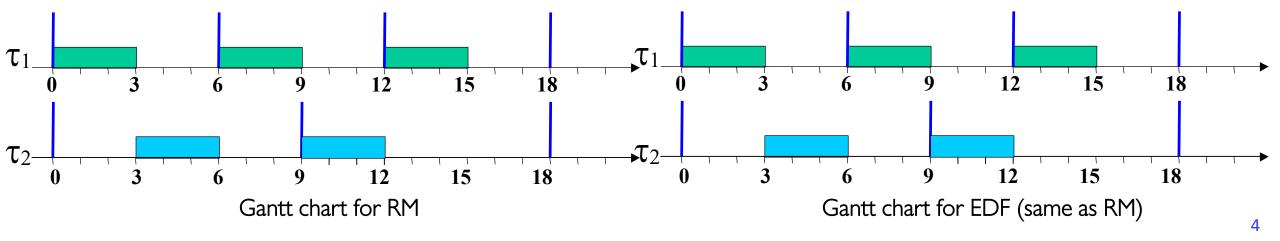
# Tasks	RM Util Bound
1	1.00
2	0.828
3	0.780

- 1) Taskset $\tau_1(3, 6, 6), \tau_2(4, 9, 9)$
- System utilization $U=\frac{3}{6}+\frac{4}{9}=0.944>0.828$ (UB for 2 tasks under RM). Since utilization exceeds the RM bound, we cannot determine its schedulability under RM, so we perform RTA to compute WCRT of each task, by solving $R_i = C_i + \sum_{\forall j \in hp(i)} \left| \frac{\kappa_i}{T_i} \right| C_j$
- For higher-priority (smaller period) task $\tau_1, R_1 = C_1 = 3 \le D_1 = 6$, hence τ_1 is schedulable
- For lower-priority (larger period) task τ_2 , $R_2 = C_2 + \left\lceil \frac{R_2}{T_1} \right\rceil C_1 = 4 + \left\lceil \frac{R_2}{6} \right\rceil \cdot 3$, solving it iteratively gives $R_2 = 10 > D_2 = 9$, hence τ_2 is not schedulable
- This taskset is unschedulable under RM.
- System utilization $U = \frac{3}{6} + \frac{4}{9} = 0.944 \le 1$ (UB under EDF), hence this taskset is schedulable under EDF
- (You are not required to draw the Gantt charts below, they are FYI only.)

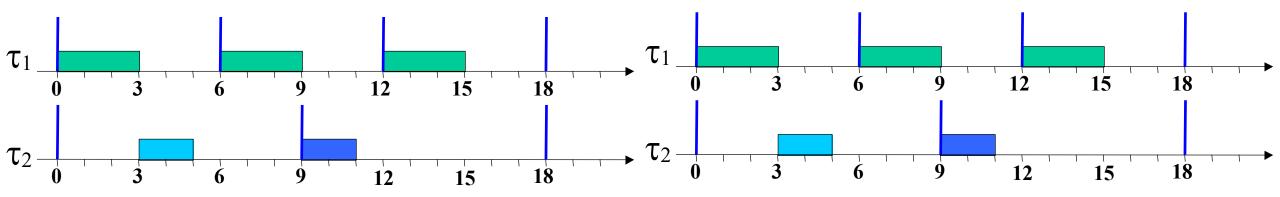


Gantt chart for EDF

- 2) Taskset $\tau_1(3, 6, 6), \tau_2(3, 9, 9)$
- System utilization $U=\frac{3}{6}+\frac{3}{9}=0.833>0.828$. Since utilization exceeds the RM bound, we cannot determine its schedulability under RM, so we perform RTA to compute WCRT of each task, by solving $R_i=C_i+\sum_{\forall j\in hp(i)}\left|\frac{R_i}{T_j}\right|C_j$
- For higher-priority (smaller period) task $\tau_1, R_1 = C_1 = 3 \le D_1 = 6$, hence τ_1 is schedulable
- For lower-priority (larger period) task τ_2 , $R_2 = C_2 + \left\lceil \frac{R_2}{T_1} \right\rceil C_1 = 3 + \left\lceil \frac{R_2}{6} \right\rceil \cdot 3$, solving it iteratively gives $R_2 = 6 \le D_2 = 9$, hence τ_2 is schedulable
 - $R_2=9$ is another possible solution for the recursive equation, but we consider the minimum fixed-point solution of $R_2=6$
- We determine this taskset to be schedulable under RM.
- System utilization $U = \frac{3}{6} + \frac{4}{9} = 0.833 \le 1$, hence this taskset is schedulable under EDF



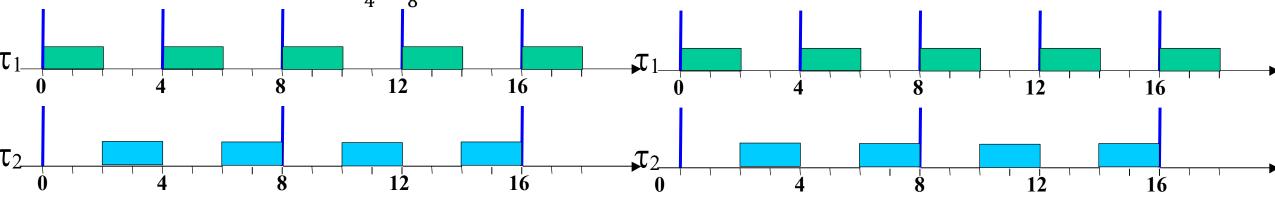
- 3) Taskset $\tau_1(3, 6, 6), \tau_2(2, 9, 9)$
- System utilization $U=\frac{3}{6}+\frac{2}{9}=0.722\leq0.828$. Since utilization is within the RM bound, we determine this taskset to be schedulable under RM, without the need for RTA
- System utilization $U = \frac{3}{6} + \frac{2}{9} = 0.722 \le 1$, hence this taskset is schedulable under EDF



Gantt chart for RM

Gantt chart for EDF (same as RM)

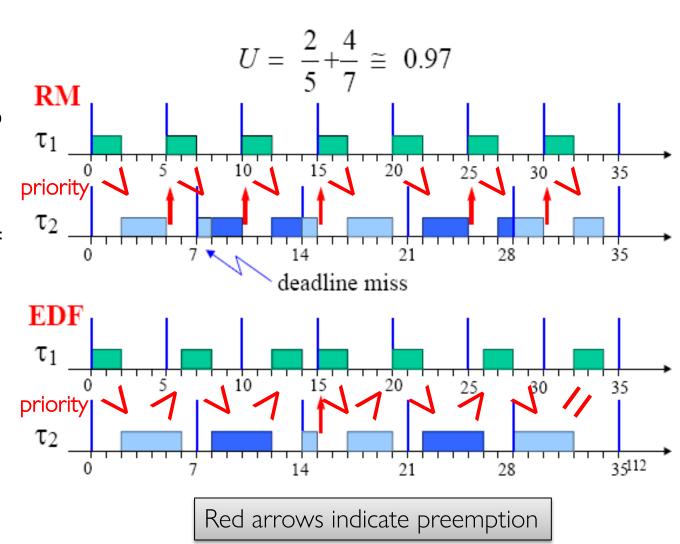
- 4) Taskset $\tau_1(2, 4, 4), \tau_2(4, 8, 8)$
- System utilization $U=\frac{2}{4}+\frac{4}{8}=1.0>0.828$. Since utilization exceeds the RM bound, we cannot determine its schedulability under RM, so we perform RTA to compute WCRT of each task, by solving $R_i=C_i+\sum_{\forall j\in hp(i)} \left|\frac{R_i}{T_j}\right| C_j$
- For higher-priority (smaller period) task $\tau_1, R_1 = C_1 = 2 \le D_1 = 4$, hence τ_1 is schedulable
- For lower-priority (larger period) task τ_2 , $R_2 = C_2 + \left\lceil \frac{R_2}{T_1} \right\rceil C_1 = 4 + \left\lceil \frac{R_2}{4} \right\rceil \cdot 2$, solving it iteratively gives $R_2 = 8$, hence τ_2 is schedulable
- We determine this taskset to be schedulable under RM.
 - We can also skip RTA, and use this condition to this taskset to be schedulable under RM. "If periods are harmonic (larger periods divisible by smaller periods), then utilization bound is 1."
- System utilization $U = \frac{2}{4} + \frac{4}{8} = 1.0 \le 1$, hence this taskset is schedulable under EDF



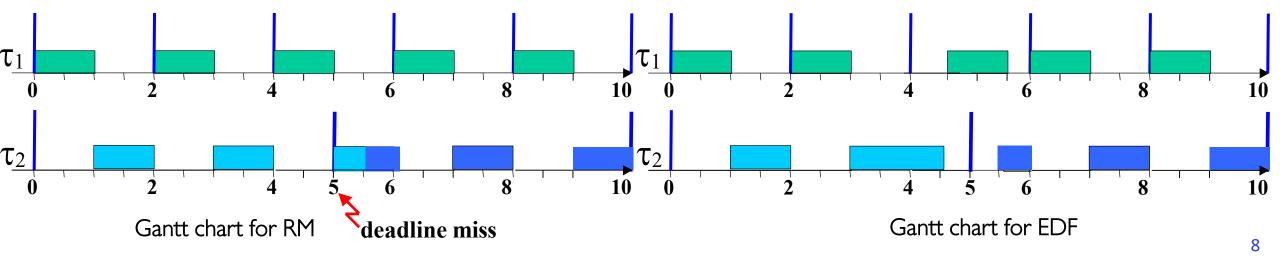
Gantt chart for RM

Gantt chart for EDF (same as RM)

- 5) Taskset $\tau_1(2, 5, 5), \tau_2(4, 7, 7)$
- System utilization $U = \frac{2}{5} + \frac{4}{7} = 0.97 > 0.828$. Since utilization exceeds the RM bound, we cannot determine its schedulability under RM, so we perform RTA to compute WCRT of each task, by solving $R_i = C_i + \sum_{\forall j \in hp(i)} \left[\frac{R_i}{T_i}\right] C_j$
- For higher-priority (smaller period) task $\tau_1, R_1 = C_1 = 2 \le D_1 = 5$, hence τ_1 is schedulable
- For lower-priority (larger period) task τ_2 , $R_2 = C_2 + \left\lceil \frac{R_2}{T_1} \right\rceil C_1 = 4 + \left\lceil \frac{R_2}{5} \right\rceil \cdot 2$, solving it iteratively gives $R_2 = 8 > D_2 = 7$, hence τ_2 is not schedulable
- This taskset is unschedulable under RM
- System utilization $U = \frac{2}{5} + \frac{4}{7} = 0.97 \le 1$, hence this taskset is schedulable under EDF



- 6) Taskset $\tau_1(1, 2, 2), \tau_2(2.5, 5, 5)$
- System utilization $U=\frac{1}{2}+\frac{2.5}{5}=1>0.828$. Since utilization exceeds the RM bound, we cannot determine its schedulability under RM, so we perform RTA to compute WCRT of each task, by solving $R_i=C_i+\sum_{\forall j\in hp(i)} \left|\frac{R_i}{T_j}\right| C_j$
- For higher-priority (smaller period) task $\tau_1, R_1 = C_1 = 1 \le D_1 = 2$, hence τ_1 is schedulable
- For lower-priority (larger period) task τ_2 , $R_2 = C_2 + \left\lceil \frac{R_2}{T_1} \right\rceil C_1 = 2.5 + \left\lceil \frac{R_2}{2} \right\rceil \cdot 1$, solving it iteratively gives $R_2 = 5.5 > D_2 = 5$, hence τ_2 is not schedulable
- This taskset is unschedulable under RM
- System utilization $U = \frac{1}{2} + \frac{2.5}{5} = 1 \le 1$, hence this taskset is schedulable under EDF

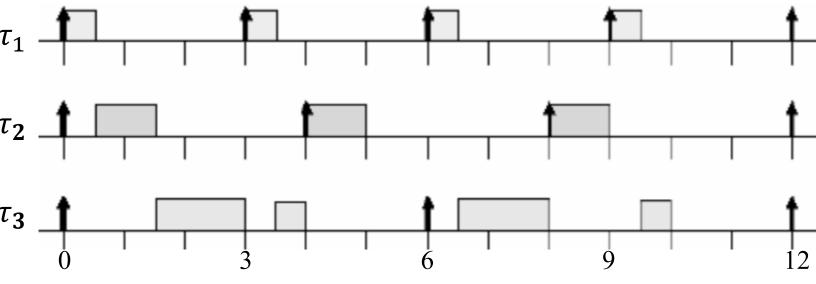


Q2. Schedulability under RM, DM, or EDF

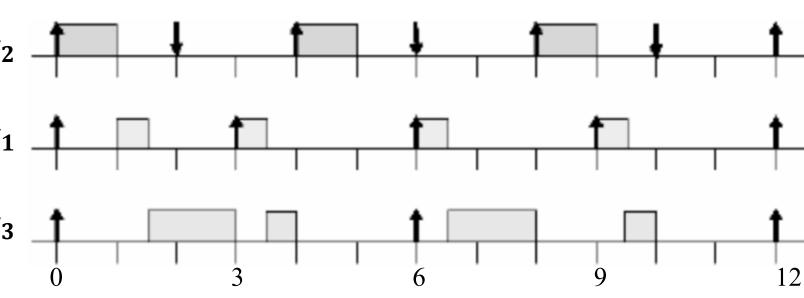
- Determine schedulability of the following tasksets under (1) Rate Monotonic (RM) scheduling, using Utilization Bound test and/or Response Time Analysis (RTA) to determine taskset schedulability. (2) Deadline Monotonic (DM) scheduling (3) Earliest Deadline First (EDF) scheduling, using Utilization Bound test.
- 1) Taskset $\tau_1 = (0.5, 3, 3), \tau_2 = (1, 4, 4), \tau_3 = (2, 6, 6)$
- 2) Taskset $\tau_1 = (0.5, 3, 3), \tau_2 = (1, 4, 2), \tau_3 = (2, 6, 6)$
- 3) Taskset $\tau_1 = (1, 3, 3), \tau_2 = (1, 4, 2), \tau_3 = (2, 6, 6)$

Recall: RM vs. DM Example

- Three tasks: $\tau_1 = (0.5, 3, 3), \tau_2 = (1, 4, 4), \tau_3 = (2, 6, 6)$
- Under RM (or DM), priority ordering $au_1 > au_2 > au_3$



- Three tasks with au_2 assigned a smaller deadline of $D_2=2$: $au_1=(0.5,3,3), au_2=(1,4,2), au_3=(2,6,6)$
- Under DM, priority ordering $au_2 > au_1 > au_3$



- Three tasks: $\tau_1 = (0.5, 3, 3), \tau_2 = (1, 4, 4), \tau_3 = (2, 6, 6)$
 - For RM: priority ordering $au_1 > au_2 > au_3$
 - » System utilization $U = \frac{0.5}{3} + \frac{1}{4} + \frac{2}{6} = 0.75 \le 0.780$ (UB for 2 tasks under RM), hence the taskset is schedulable under RM
 - For DM: priority ordering $au_1 > au_2 > au_3$
 - » Since $D_i = T_i$, DM scheduling is the same as RM scheduling, hence it is also schedulable under DM
 - For EDF: System utilization $U=\frac{0.5}{3}+\frac{1}{4}+\frac{2}{6}=0.75\leq 1$ (UB for EDF), hence the taskset is schedulable under EDF

- Three tasks: $\tau_1 = (0.5, 3, 3), \tau_2 = (1, 4, 2), \tau_3 = (2, 6, 6)$
- No Utilization Bound test for RM or DM, for taskset with $D_i < T_i$; need to use Response Time Analysis (RTA)
- For RM: priority ordering $au_1 > au_2 > au_3$

$$-R_1 = C_1 + 0 = 0.5 + 0 = 0.5 \le D_1 = 3$$

$$-R_2 = C_2 + \left[\frac{R_1}{T_1}\right] \cdot C_1 = 1 + \left[\frac{R_1}{3}\right] \cdot 0.5 = 1.5 \le D_2 = 2$$

$$-R_3 = C_3 + \left[\frac{R_3}{T_1}\right] \cdot C_1 + \left[\frac{R_3}{T_2}\right] \cdot C_2 = 2 + \left[\frac{R_3}{3}\right] \cdot 0.5 + \left[\frac{R_3}{4}\right] \cdot 1 = 4 \le D_3 = 6$$

- Since all tasks meet their deadlines, the taskset is schedulable
- For DM: priority ordering $au_2 > au_1 > au_3$

$$-R_2 = C_2 + 0 = 1 + 0 = 1 \le D_2 = 2$$

$$-R_1 = C_2 + \left[\frac{R_1}{T_2}\right] \cdot C_2 = 0.5 + \left[\frac{R_1}{4}\right] \cdot 1 = 1.5 \le D_1 = 3$$

$$-R_3 = C_3 + \left[\frac{R_3}{T_2}\right] \cdot C_2 + \left[\frac{R_3}{T_1}\right] \cdot C_1 = 2 + \left[\frac{R_3}{4}\right] \cdot 1 + \left[\frac{R_3}{3}\right] \cdot 0.5 = 4 \le D_3 = 6$$

- Since all tasks meet their deadlines, the taskset is schedulable
- For EDF:
 - System density $\Delta = \frac{0.5}{3} + \frac{1}{2} + \frac{2}{6} = 1.0 \le 1$, hence this taskset is schedulable under EDF

- Three tasks: $\tau_1 = (1, 3, 3), \tau_2 = (1, 4, 2), \tau_3 = (2, 6, 6)$
- No Utilization Bound test for RM or DM, for taskset with $D_i < T_i$; need to use Response Time Analysis (RTA)
- For RM: priority ordering $au_1 > au_2 > au_3$

$$-R_1 = C_1 + 0 = 1 + 0 = 1 \le D_1 = 3$$

$$- R_2 = C_2 + \left[\frac{R_1}{T_1}\right] \cdot C_1 = 1 + \left[\frac{R_1}{3}\right] \cdot 1 = 2 \le D_2 = 2$$

$$-R_3 = C_3 + \left[\frac{R_3}{T_1}\right] \cdot C_1 + \left[\frac{R_3}{T_2}\right] \cdot C_2 = 2 + \left[\frac{R_3}{3}\right] \cdot 1 + \left[\frac{R_3}{4}\right] \cdot 1 = 6 \le D_3 = 6$$

- Since all tasks meet their deadlines, the taskset is schedulable
- For DM: priority ordering $\tau_2 > \tau_1 > \tau_3$

$$-R_2 = C_2 + 0 = 1 + 0 = 1 \le D_2 = 2$$

$$-R_1 = C_2 + \left[\frac{R_1}{T_2}\right] \cdot C_2 = 1 + \left[\frac{R_1}{4}\right] \cdot 1 = 2 \le D_1 = 3$$

$$-R_3 = C_3 + \left[\frac{R_3}{T_2}\right] \cdot C_2 + \left[\frac{R_3}{T_1}\right] \cdot C_1 = 2 + \left[\frac{R_3}{4}\right] \cdot 1 + \left[\frac{R_3}{3}\right] \cdot 1 = 6 \le D_3 = 6$$

- Since all tasks meet their deadlines, the taskset is schedulable
- Three tasks: $\tau_1 = (1, 3, 3), \tau_2 = (1, 4, 2), \tau_3 = (2, 6, 6)$ under EDF
 - System density $\Delta=\frac{1}{2}+\frac{1}{6}+\frac{2}{6}=1.17>1$, hence we CANNOT determine this taskset's schedulability under EDF

Q3 RM, EDF, LLF

 Consider the set of 2 periodic tasks whose period, deadline and WCET parameters are given.

• 1. For each scheduling algorithm (RM, EDF, LLF), draw the Gantt chart by filling in the table with the task ID that runs in each time slot until time 10, and calculate the WCRT for each task.

• 2. Under RM scheduling, use utilization bound and Response Time Analysis (RTA) to

determine taskset schedulability.

Task ID	T=D	С	RM Resp. Time	•	LLF Resp. Time
1	8	3			
2	10	4			

RM					
EDF					
LLF					

Time 0 1 2 3 4 5 6 7 8 9 10 Gantt Chart

Time	тı Laxity	т ₂ Laxity	Running Task
t=0			
t=1			
t=2			
t=3			
t=4			
t=5			
t=6			
t=7			
t=8			
T=9			

Q3 RM, EDF, LLF ANS

- Consider the set of 2 periodic tasks whose period, deadline and WCET parameters are given.
- 1. For each scheduling algorithm (RM, EDF, LLF), draw the Gantt chart by filling in the table with the task ID that runs in each time slot until time 10, and calculate the WCRT for each task.

2. Under RM scheduling, determine taskset schedulability using utilization bound and/or Response Time Analysis (RTA) to

Task ID	T=D	С	RM Resp. Time		LLF Resp. Time
1	8	3	3	3	5
2	10	4	7	7	7

RM	1	1	1	2	2	2	2	X	1	1
EDF	1	1	1	2	2	2	2	X	1	1
LLF	1	1	2	2	1	2	2	X	1	1

10 Time **Gantt Chart**

Time	тı Laxity	т ₂ Laxity	Running Task
t=0	8-0-3=5	10-0-4=6	1
t=1	8-1-2=5	10-1-4=5	1 (tie)
t=2	8-2-1=5	10-2-4=4	2
t=3	8-3-1=4	10-3-3=4	2 (tie)
t=4	8-4-1=3	10-4-2=4	1
t=5	T1 done	10-5-2=3	2
t=6	T1 done	10-6-1=3	2
t=7	T1 done	T2 done	X
t=8	16-8-3=5	T2 done	1
T=9	16-9-2=5	T2 done	1

Q3 RM, EDF, LLF ANS

- System utilization $U=\frac{3}{8}+\frac{4}{10}=0.775\leq 0.828$. Since utilization is within the RM bound, we determine this taskset to be schedulable under RM, without the need for RTA
- System utilization $U = \frac{3}{8} + \frac{4}{10} = 0.775 \le 1.0$, hence this taskset is schedulable under EDF and LLF

Recall: PCP Blocking Time

A given task i is blocked (or delayed) by at most one critical section of any lower priority task locking a semaphore with priority ceiling greater than or equal to the priority of task i. We can explain that mathematically using the notation:

$$B_i = \max_{\{k,s \mid k \in lp(i) \land s \in used_by(k) \land ceil(s) \geq pri(i)\}} cs_{k,s}$$

$$(4.5)$$

- Consider all lower-priority tasks (k∈lp(i)), and the semaphores they can lock (s)
- Select from those semaphores (s) with ceiling higher than or equal to $pri(i) = P_i$
- Take max length of all tasks (k)'s critical sections that lock semaphores (s)
- (Note: this formula applies only when task i requests some semaphore. If task i does not require any semaphores itself, then it does not experience any blocking time, i.e., $B_i = 0$.)

Q5. Schedulability with Shared Resources

- Consider the set of 8 periodic tasks scheduled with RM, with period, deadline, priority (larger number denotes higher priority), and WCET parameters given in the table. The tasks may require one or more of the 5 semaphores.
- 1) Calculate priority ceilings of the semaphores
- 2) Calculate worst-case blocking time B_i , and WCRT R_i of all tasks based on RTA for RM $R_i = C_i + B_i + \sum_{\forall j \in hp(i)} \left[\frac{R_i}{T_j}\right] C_j$

Q5. Schedulability with Shared Resources

Task	Т	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1		
В	500	200	50	7	S ₃	4		
С	800	400	90	6	S ₁	30		
D	800	800	20	5	S ₁ ,S ₂ ,S ₄	9,3,3		
E	1000	1000	50	4	S ₃	4		
F	2000	2000	10	3	S ₅	7		
G	2000	2000	10	2	/	/		
Н	2000	2000	30	1	S ₂ ,S ₅	13,7		

Sem	Ceiling
S_1	
S ₂	
S ₃	
S ₄	
S ₅	

Q5. Schedulability with Shared Resources ANS

Task	Т	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	S ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	S ₁ ,S ₂ ,S ₄	9,3,3	13	187
E	1000	1000	50	4	S ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	S ₂ ,S ₅	13,7	0	288

Sem	Ceiling
S ₁	6
S ₂	5
S ₃	7
S ₄	8
S ₅	3

Q5. Schedulability with Shared Resources ANS

• Each semaphore is assigned a ceiling, equal to maximum priority of all tasks that require it: $C(s_k) = \max\{P_j: \tau_j \text{ uses } s_k\}$. Hence we can fill in the semaphore ceiling table.

Sem	Ceiling
S_1	5
S ₂	5
S ₃	7
S ₄	8
S ₅	3

Q5. Task A

- Consider task A:
- The set of lower priority tasks Ip(A) includes tasks B, C, D, E, F, G, H
- The set of semaphores used/required by these tasks includes s_1 , s_2 , s_3 , s_4 , and s_5
- Ceilings $C(s_4)=8 \ge prio(A)=8$
- Maximum blocking time of task A is $B_A = cs(D, s4) = 3$
 - Task D has a CS with length 3, associated with s₄
- $R_A = C_A + B_A = 14 + 3 = 17 \le D_A = 50$
- Hence task A is schedulable

Task	Т	D	С	Prio	sems	CS	В	R
						Len		
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	S ₃	4	4	68
С	800	400	90	6	1	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
Е	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	1	/	13	271
Н	2000	2000	30	1	s _{2,} s ₅	13,7	0	288

Ceiling
6
5
7
8
3

Q5. Task B

- Consider task B:
- The set of lower priority tasks Ip(B) includes tasks C, D, E, F, G, H
- The set of semaphores used/required by these tasks includes s_1 , s_2 , s_3 , s_4 , and s_5
- Ceilings $C(s_3)=7$, $C(s_4)=8 \ge prio(B)=7$
- Maximum blocking time of task B is $B_B = \max\{cs(D, s4), cs(E, s3)\} = \max(3, 4) = 4$

•
$$R_B = C_B + B_B + \left[\frac{R_B}{T_A}\right] C_A = 50 + 4 + \left[\frac{R_B}{250}\right] 14 = 68 \le D_B = 200$$

Hence task B is schedulable

Task	Т	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	s ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
E	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	S _{2,} S ₅	13,7	0	288

Sem	Ceiling			
s ₁	6			
s ₂	5			
s ₃	7			
S ₄	8			
S ₅	3			

Q5. Task C

- Consider task C:
- The set of lower priority tasks Ip(C) includes tasks D, E, F, G, H
- The set of semaphores used/required by these tasks includes s_1 , s_2 , s_3 , s_4 , and s_5
- Ceilings $C(s_3)=7$, $C(s_4)=8 \ge prio(C)=6$
- Maximum blocking time of task C is $B_C = \max\{cs(D, s4), cs(E, s3)\} = \max(3, 4) = 4$

•
$$R_C = C_C + B_C + \left[\frac{R_C}{T_A}\right] C_A + \left[\frac{R_C}{T_B}\right] C_B = 90 + 4 + \left[\frac{R_C}{250}\right] 14 + \left[\frac{R_C}{500}\right] 50 = 158 \le D_C = 400$$

Hence task C is schedulable

Task	Т	D	С	Prio	sems	CS	В	R
						Len		
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	s ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
Е	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s _{2,} s ₅	13,7	0	288

Sem	Ceiling
s ₁	6
s ₂	5
S ₃	7
S ₄	8
S ₅	3

Q5. Task D

- Consider task D:
- The set of lower priority tasks Ip(D) includes tasks E, F, G, H
- The set of semaphores used/required by these tasks includes s_2 , s_3 and s_5
- Ceilings of $C(s_2)=5$, $C(s_3)=7 \ge prio(D)=5$
- Maximum blocking time of task D is $B_D = \max\{cs(E, s3), cs(H, s2)\} = \max(4, 13) = 13$
 - Task E has a CS with length 4, associated with s₃
 - Task H has a CS with length 13, associated with s₂
 - (Note that task B has higher priority than D, so it is not included even though it also requires s_3)

•
$$R_D = C_D + B_D + \left[\frac{R_D}{T_A}\right] C_A + \left[\frac{R_D}{T_B}\right] C_B + \left[\frac{R_D}{T_C}\right] C_C = 20 + 13 + \left[\frac{R_D}{250}\right] 14 + \left[\frac{R_D}{500}\right] 50 + \left[\frac{R_D}{800}\right] 90 = 187 \le D_D = 800$$

• Hence task D is schedulable

Task	T	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	S ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
Е	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s _{2,} s ₅	13,7	0	288

Sem	Ceiling			
s ₁	6			
s ₂	5			
s ₃	7			
S ₄	8			
S ₅	3			

Q5. Task E

- Consider task E:
- The set of lower priority tasks Ip(E) includes tasks F, G, H
- The set of semaphores used/required by these tasks includes s₂ and s₅
- Ceiling $C(s_2)=5 \ge prio(E)=4$
- Maximum blocking time of task E is $B_E = cs(H, s2) = 13$

•
$$R_E = C_E + B_E + \left[\frac{R_E}{T_A}\right] C_A + \left[\frac{R_E}{T_B}\right] C_B + \left[\frac{R_E}{T_C}\right] C_C + \left[\frac{R_E}{T_D}\right] C_D = 50 + 13 + \left[\frac{R_E}{250}\right] 14 + \left[\frac{R_E}{500}\right] 50 + \left[\frac{R_E}{800}\right] 90 + \left[\frac{R_E}{800}\right] 20 = 237 \le D_E = 1000$$

• Hence task E is schedulable

Task	Т	D	С	Prio	sems	CS	В	R
						Len		
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	S ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
Е	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	s ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s ₂ ,s ₅	13,7	0	288

Sem	Ceiling
s ₁	6
s ₂	5
s ₃	7
S ₄	8
S ₅	3

Q5. Task F

- Consider task F:
- The set of lower priority tasks lp(F) includes tasks G, H
- The set of semaphores used/required by these tasks includes s_2 and s_5
- Ceilings $C(s_2)=5$, $C(s_5)=3 \ge prio(F)=3$
- Maximum blocking time of task E is $B_F = \max(cs(H, s2), cs(H, s5)) = \max(13, 7) = 13$

•
$$R_F = C_F + B_F + \left[\frac{R_F}{T_A}\right] C_A + \left[\frac{R_F}{T_B}\right] C_B + \left[\frac{R_F}{T_C}\right] C_C + \left[\frac{R_F}{T_D}\right] C_D + \left[\frac{R_F}{T_E}\right] C_E = 10 + 13 + \left[\frac{R_E}{250}\right] 14 + \left[\frac{R_E}{500}\right] 50 + \left[\frac{R_E}{800}\right] 90 + \left[\frac{R_E}{800}\right] 20 + \left[\frac{R_E}{1000}\right] 50 = 247 \le D_F = 2000$$

Hence task F is schedulable

Task	Т	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	S ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
E	1000	1000	50	4	S ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s _{2,} s ₅	13,7	0	288

Sem	Ceiling
s ₁	6
s ₂	5
s ₃	7
S ₄	8
S ₅	3

Q5. Task G

- Consider task G:
- The set of lower priority tasks lp(G) includes task H
- The set of semaphores used/required by these tasks includes $\rm s_2$ and $\rm s_5$
- Ceilings $C(s_2)=5$, $C(s_5)=3 \ge prio(G)=2$
- Maximum blocking time of task E is $B_E = \max(cs(H, s2), cs(H, s5)) = \max(13, 7) = 13$

•
$$R_G = C_G + \left[\frac{R_G}{T_A}\right] C_A + \left[\frac{R_G}{T_B}\right] C_B + \left[\frac{R_G}{T_C}\right] C_C + \left[\frac{R_G}{T_D}\right] C_D + \left[\frac{R_G}{T_E}\right] C_E + \left[\frac{R_G}{T_F}\right] C_F = 10 + 13 + \left[\frac{R_G}{250}\right] 14 + \left[\frac{R_G}{500}\right] 50 + \left[\frac{R_G}{800}\right] 90 + \left[\frac{R_G}{800}\right] 20 + \left[\frac{R_G}{1000}\right] 50 + \left[\frac{R_G}{2000}\right] 10 = 271 \le D_G = 2000$$

Hence task G is schedulable

Task	Т	D	С	Prio	sems	CS Len	В	R
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	s ₃	4	4	68
С	800	400	90	6	/	/	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
E	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	s ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s _{2,} s ₅	13,7	0	288

Sem	Ceiling
s ₁	6
s ₂	5
s ₃	7
S ₄	8
S ₅	3

Q5. Task H

- Consider task H:
- Task H is the lowest priority task, so it does not experience any blocking $B_H=0$

•
$$R_H = C_H + \left[\frac{R_H}{T_A}\right] C_A + \left[\frac{R_H}{T_B}\right] C_B + \left[\frac{R_H}{T_C}\right] C_C + \left[\frac{R_H}{T_D}\right] C_D + \left[\frac{R_H}{T_E}\right] C_E + \left[\frac{R_H}{T_F}\right] C_F + \left[\frac{R_H}{T_G}\right] C_G = 30 + \left[\frac{R_H}{250}\right] 14 + \left[\frac{R_H}{500}\right] 50 + \left[\frac{R_H}{800}\right] 90 + \left[\frac{R_H}{800}\right] 20 + \left[\frac{R_H}{1000}\right] 50 + \left[\frac{R_H}{2000}\right] 10 + \left[\frac{R_H}{2000}\right] 10 = 288 \le D_H = 2000$$

Hence task H is schedulable

Task	Т	D	С	Prio	sems	CS	В	R
						Len		
Α	250	50	14	8	S ₄	1	3	17
В	500	200	50	7	s ₃	4	4	68
С	800	400	90	6	s ₁	30	4	158
D	800	800	20	5	s ₁ ,s ₂ ,s ₄	9,3,3	13	187
E	1000	1000	50	4	s ₃	4	13	237
F	2000	2000	10	3	S ₅	7	13	247
G	2000	2000	10	2	/	/	13	271
Н	2000	2000	30	1	s ₂ ,s ₅	13,7	0	288

Sem	Ceiling
s_1	5
s ₂	5
s ₃	7
S ₄	8
s ₅	3