

CSC 112: Computer Operating Systems

Lecture 4

Deadlocks Exercises

Department of Computer Science,
Hofstra University

Quiz: Deadlocks II

- Is there a possible deadlock?

```
1  Semaphore L1=1, L2=1, L3=1;
2
3  // Thread 1:
4  L1.wait();
5  L2.wait();
6  // critical section requiring L1 and L2 locked.
7  L2.post();
8  L1.post();
9
10 // Thread 2:
11 L3.wait();
12 L1.wait();
13 // critical section requiring L3 and L1 locked.
14 L1.post();
15 L3.post();
16
17 // Thread 3:
18 L2.wait();
19 L3.wait();
20 // critical section requiring L2 and L3 locked.
21 L3.post();
22 L2.post();
```

Quiz: Banker's Algorithm I

- 4 processes P1 through P5; 3 resource types R1, R2, R3 with 7, 3, 6 instances each.
- Run Banker's algorithm to check if the current state is safe. If yes, give a safe sequence of process completions and fill in the table with the sequence of process completions without deadlock, and available resources after the completion of each process.
- (You will be graded on "Need matrix", and "Available resources after completion of each process".)

$$R = \begin{bmatrix} 7 & 5 & 3 \\ 3 & 2 & 2 \\ 9 & 0 & 2 \\ 2 & 2 & 2 \\ 4 & 3 & 3 \end{bmatrix}$$

$$E = \begin{bmatrix} 7 & 3 & 6 \end{bmatrix}$$

$$C = \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 0 \\ 3 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 2 \end{bmatrix}$$

Available resources after completion of each process

	R1	R2	R3
Init			

Quiz: Banker's algorithm II

- ❁ 4 processes P1, P2, P3; 3 resource types R1, R2, R3 with 8, 6, 4 instances each.
- ❁ 1) Run Banker's algorithm to check if the current state is safe. If yes, give a safe sequence of process completions and fill in the table with the sequence of process completions without deadlock, and available resources after the completion of each process.
- ❁ 2) Starting from the initial state, if P1 makes request for 2 more instances of resource 3, should we grant it?
- ❁ 3) Starting from the initial state, if P2 makes request for 2 more instances of resource 1, should we grant it?

Max	Allocation
$\begin{bmatrix} 8 & 4 & 3 \\ 6 & 2 & 0 \\ 3 & 3 & 3 \end{bmatrix}$	$\begin{bmatrix} 0 & 0 & 1 \\ 3 & 2 & 0 \\ 2 & 2 & 1 \end{bmatrix}$

Total
 $E = [8 \quad 6 \quad 4]$

Available resources after completion of each process

	R1	R2	R3
Init			

Banker's Algorithm: 4 philosophers each holding his left fork

$$R = \begin{array}{c|ccccc} & \text{Max} & & & & \\ & 1 & 1 & 0 & 0 & 0 \\ & 0 & 1 & 1 & 0 & 0 \\ & 0 & 0 & 1 & 1 & 0 \\ & 0 & 0 & 0 & 1 & 1 \\ & 1 & 0 & 0 & 0 & 1 \end{array} \quad C = \begin{array}{c|ccccc} & \text{Allocation} & & & & \\ & 1 & 0 & 0 & 0 & 0 \\ & 0 & 1 & 0 & 0 & 0 \\ & 0 & 0 & 1 & 0 & 0 \\ & 0 & 0 & 0 & 1 & 0 \\ & 0 & 0 & 0 & 0 & 0 \end{array} \quad R - C = \begin{array}{c|ccccc} & \text{Need} & & & & \\ & 0 & 1 & 0 & 0 & 0 \\ & 0 & 0 & 1 & 0 & 0 \\ & 0 & 0 & 0 & 1 & 0 \\ & 0 & 0 & 0 & 0 & 1 \\ & 1 & 0 & 0 & 0 & 1 \end{array}$$

$$E = \begin{array}{c|ccccc} & \text{Total} & & & & \\ & 1 & 1 & 1 & 1 & 1 \end{array} \quad A = \begin{array}{c|ccccc} & \text{Available} & & & & \\ & 0 & 0 & 0 & 0 & 1 \end{array}$$

Suppose we have 5 philosophers P1-P5, and 5 forks R1-R5; philosopher P_i has left fork R_i , and right fork $R_{(i+1)\%5}$. Philosophers P1-P4 each is holding his left fork.

Run Banker's algorithm to check if the current state is safe. If yes, give a safe sequence of process completions and fill in the table with the sequence of process completions without deadlock, and available resources after the completion of each process.

Available resources after completion of each process

	R1	R2	R3	R4	R5
	0	0	0	0	1

Banker's Algorithm: 5 philosophers each holding his left fork

	Max						Allocation						Need				
$R =$	1	1	0	0	0	$C =$	1	0	0	0	0	$C =$	0	1	0	0	0
	0	1	1	0	0		0	1	0	0	0		0	0	1	0	0
	0	0	1	1	0		0	0	1	0	0		0	0	0	1	0
	0	0	0	1	1		0	0	0	1	0		0	0	0	0	1
	1	0	0	0	1		0	0	0	0	1		1	0	0	0	0

Total					Available						
$E =$	1	1	1	1	1	$A =$	0	0	0	0	0

Run Banker's algorithm to check if the current state is safe.

Multi-Armed Lawyers

- Consider a large table with identical multi-armed alien lawyers. There is a pile of chopsticks at the center of the table. In order to eat, a lawyer must have one chopstick in each hand. Assume total number of chopsticks \geq number of hands of each lawyer, so at least one lawyer can eat.
- It is not a generalization of the 2-armed Dining Philosophers problem. Since the chopsticks are in a pile at center of the table, we should model them as a single resource with multiple instances, instead of multiple resources for the Dining Philosophers, where each fork (chopstick) has a fixed position in-between two philosophers. Hence the R and C matrices have a single column.

Example: 5 Lawyers, each with 2 arms, 5 chopsticks

Max: $\begin{vmatrix} 2 \\ 2 \\ 2 \\ 2 \\ 2 \end{vmatrix}$, Allocation: $\begin{vmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{vmatrix}$, Total: |5|, Available: |5|

- Initially, all chopsticks are free.

Max: $\begin{vmatrix} 2 \\ 2 \\ 2 \\ 2 \\ 2 \end{vmatrix}$, Allocation: $\begin{vmatrix} 2 \\ 2 \\ 0 \\ 0 \\ 0 \end{vmatrix}$, Total: |5|, Available: |1|

- Two lawyers each grab two chopsticks and start eating. No other lawyers can eat.

Quiz: Dining Lawyers I

- If each lawyer has 2 arms, and there is a pile of chopsticks at the center of the table. Assume there are at least 2 chopsticks, so at least one lawyer can eat. Each lawyer follows the following steps:
 - (1) Pick up a chopstick
 - (2) Pick up another chopstick
 - (3) Eat
 - (4) Return both chopsticks to the pile
- Q: Can the system be deadlocked?

Quiz: Dining Lawyers II

- If each lawyer has 2 arms, and there is a pile of knives and forks at center of the table. Assume there are at least 1 knife and 1 fork, so at least one lawyer can eat. Each lawyer follows the following steps:
 - (1) Pick up a knife
 - (2) Pick up a fork
 - (3) Eat
 - (4) Return the knife and fork to the pile
- Q: Can the system be deadlocked?

Quiz: Dining Lawyers III

- If each lawyer has 4 arms, and there is a pile of knives and forks at center of the table. Assume there are at least 2 knives and 2 forks, so at least one lawyer can eat. Each lawyer follows the following steps:
 - (1) Pick up 2 knives atomically
 - (2) Pick up 2 forks atomically
 - (3) Eat
 - (4) Return the knives and forks to the pile
- Q: Can the system be deadlocked?

Quiz: Dining Lawyers III

- If each lawyer has 4 arms, and there is a pile of knives and forks at center of the table. Assume there are at least 2 knives and 2 forks, so at least one lawyer can eat. Each lawyer follows the following steps:
 - (1) Pick up a knife
 - (2) Pick up another knife
 - (3) Pick up a fork
 - (4) Pick up another fork
 - (5) Eat
 - (6) Return the knife and fork to the pile
- Q1: Can the system be deadlocked?
- Q2: What if each lawyer may have a different number of arms, and may request a different ratio of knives vs. forks?