# Non-Clairvoyant Dynamic Mechanism Design: Experimental Evidence

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July, 2023 AMES

# Main Takeaways

### What do we do?

- ▶ Bring Non-Clairvoyant Environment (Mirrokni et al., 2020) into Lab.
- ▶ Test the optimal Non-Clairvoyant dynamic mechanism (NC).
- ► Compare the performance with Repeated Static optimal mechanism (RS).

### What do we find?

- ▶ Dynamic NC works well as theory predicts More revenue in some scenarios.
- ▶ Participants overbid less in NC.
- ightharpoonup Risk aversion  $\rightarrow$  No full participation  $\rightarrow$  Revenue loss in NC.

# Optimal Dynamic Mechanism Design

- ▶ How the seller establishes rules of allocation and price over **multi-period** for the best revenue, as the buyer receives private information over time.
  - ► Long-term principal-agent relationship
  - Repeated selling of perishable goods
- ▶ Dynamic mechanism improves revenues and efficiency (Baron & Besanko, 1984).

# Non-Clairvoyance

# Clairvoyance: Future demand is known at the beginning.

- ▶ Complicated, non-intuitive, lack of General Form.
- ▶ Buyers tend to have biased forecast on future demand (DellaVigna & Malmendier, 2006).

### Non-Clairvoyance: Future demand is not accessible at the beginning.

- ▶ No need to share unbiased belief.
- ► General Form.



 $F_2$  is unknown in Day 1



 $v_1 \sim F_1$ 



 $v_2 \sim F_2$ ?

# Mechanisms under Non-Clairvoyant Environment

 $\Rightarrow$  Optimal clairvoyant revenue  $Rev^*$  is unachieveble.

# RS: Repeated Static optimal mechanism (Myerson, 1981)

▶ Rules in two days are independent of each other

Maximize intra-period revenue for each period separately.

 $\Rightarrow \frac{Rev^{RS*}}{Rev^*}$  could be arbitrarily small (Papadimitriou et al., 2016)

# NC: Non-Clairvoyant optimal dynamic mechanism (Mirrokni et al., 2020)

▶ Rules in Day 2 depends on bid in day 1

Best Revenue Guarantee: 
$$\Rightarrow \frac{Rev^{NC*}}{Rev^*} \ge \frac{1}{\alpha}$$

Achieve at least  $\frac{1}{2}$  revenue produced by optimal clairvoyant mechanism under all scenarios in **two-period single-buyer** case.

# When can Non-Clairvoyant dynamic mechanism do better?

Theoretically, Non-Clairvoyant mechanism can not always outperform.

### Optimal Intra-period Revenue Inter-period Revenue

RS	100%	zero
NC	$\geq 50\%$	$\geq 50\%$

Relative size of inter-period revenues is the key.

- $\triangleright$  Scenario A: Inter period revenue is larger  $\Rightarrow$  NC outperforms.
- ightharpoonup Scenario B: Optimal intra period revenue is larger  $\Rightarrow$  RS outperforms.

# Experimental Design 2 \* 2

### Two Mechanisms

- ▶ Non-Clairvoyant Dynamic Mechanism (NC)
- ► Repeated Static Mechanism (RS)

### Two Scenarios

$$F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_A = 3.$$

$$F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_B = 6.$$

▶ Scenario A  $(S_A)$ : NC generates more revenue than RS.

$$F_1 = F_A, \ F_2 = F_B \implies REV^{RS} = 4, \ REV^{NC} = 4.5 \uparrow 12.5\%$$

▶ Scenario B  $(S_B)$ : NC generates less revenue than RS.

$$F_1 = F_B, \ F_2 = F_A \implies REV^{RS} = 4, \ REV^{NC} = 3.5 \downarrow 12.5\%$$



# Non-Clairvoyant Environment

- **Buyer**: Participant
- ▶ **Robot Seller**: Experimenter, c = 0
- **Two periods**: Buyer can buy one item in each period from seller, t = 1, 2.
- ▶ Non-clairvoyance: The distribution of buyer's value  $(F_t)$  is common knowledge only in that period
- ► Incomplete Information :
  - 1. Only buyer knows his value for the item in each period,  $v_t$ .
  - 2. Buyer's value is drawn **independently**.

### Variables for Environment

▶ Endowment: E = 50

# Mechanism - Repeated Static (RS)

### Period 1

- $\triangleright$  Seller sets a reserve price  $r_1$  based on the distributional knowledge  $F_1$ .
- ▶ Buyer learns his value  $(v_1)$ , makes a bid :  $b_1$
- ▶ Buyer can get the item only when  $b_1 \ge r_1$  and pay  $p_1 = r_1$ .

### Period 2

 $ightharpoonup F_2 \Rightarrow r_2, v_2 \Rightarrow b_2, \text{ pays } p_2 = r_2 \text{ if } b_2 \geq r_2$ 

### Myerson's Auction

monopoly price: 
$$r_1 = r_2 = 2$$
  $r_A = 2 \in \{arg \max_r r \cdot P(v_A > r)\}, \quad r_B = 2 \in \{arg \max_r r \cdot P(v_B > r)\}$ 



# Mechanism - Non-Clairvoyant Dynamic (NC)

How the dynamic mechanism work?



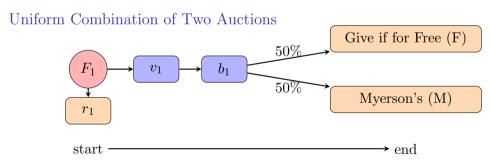
Half chance of free item in period 1



Half chance of upfront fee in period 2

# Non-Clairvoyant Mechanism in Period 1

- $\triangleright$  Seller sets a fixed reserve price  $r_1$  based on the distribution  $F_1$ .
- ▶ Buyer learns his value  $(v_1)$ , makes a bid :  $b_1$
- Buyer has 50% chance to get the item for free:  $p_1 = 0$ ; Otherwise, buyer can get the item only when  $b_1 \ge r_1$  and pay  $p_1 = r_1$ .



# Non-Clairvoyant Mechanism in Period 2

- ▶ Seller sets an upfront fee  $s_2 = \min(b_1, E(v_2))$ .
- $\triangleright$  Buyer decides pay or leave. If buyer leave (enter = 0), game over.
- ▶ If buyer pays, (enter = 1),
  - ▶ Buyer learns his value,  $v_2$ , and makes a bid:  $b_2$
  - ▶ Buyer has 50% chance to get refund on the upfront fee (luck = 1).
  - Seller sets two reserve prices  $(r_2)$  based on the  $F_2$ , luck for each given  $m_2$ , Buyer can get the item only when  $b_2 \geq r_2$  and pay  $p_2 = r_2$

# Uniform Combination of Two Auctions Zero expected payoff for buyer $b_1$ $v_2$ $b_2$ $v_3$ $v_4$ $v_5$ $v_6$ $v_7$ $v_8$ $v_9$ v

# Hypotheses

### Hypothesis 1 - On Revenue Comparison

- ▶ In Scenario A  $(S_A)$ , the non-clairvoyant mechanism (NC) generates greater revenue than the repeated static mechanism (RS);
- ▶ In  $S_B$ , NC generates less revenue than RS.

# Hypothesis 2 - On Individual Rationality

▶ Some buyers choose not to pay the upfront fee, such that the experimental revenue of the non-clairvoyant mechanism is less than its theoretical prediction.

### Hypothesis 3 - On Incentive Compatibility

▶ Participants' bids are closer to true value under NC than RS.

# Experiments

▶ 256 George Mason Students. September to November 2021.

<b></b>	${\bf Scenario}{\bf A}$			ario B
Treatment	Non-Clairvoyant	Repeated Static	NC	$\mathbf{RS}$
Age	21.6	22.3	21.9	22.7
Gender (Male=1)	0.48	0.44	0.52	0.47
Risk aversion	4.46	4.90	4.55	4.63
Observation	64	64	64	64

Table 1: Summary Statistic

### Results

### Result 1.

Experimental observations match theoretical predictions.

- ▶ In  $S_A$ , the non-clairvoyant dynamic mechanism gains more revenue than the repeated static mechanism.
- ▶ In  $S_B$ , the non-clairvoyant dynamic mechanism gains less revenue than the repeated static mechanism. mechanism.

# Experimental Revenue Comparison - Period 1

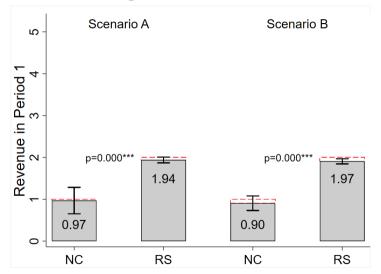


Figure 3: Revenues of Period 1 in each Treatment

# Experimental Revenue Comparison - Period 1 & Period 2

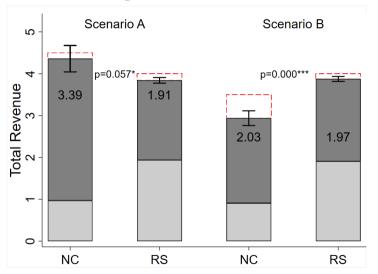


Figure 4: Revenues in each Treatment

### Results

### Result 2.

Risk aversion deters buyers from participating in the second period in NC.

- ▶ In  $S_A$ , 4 buyers quit the second period, and the number doubles in  $S_B$ .
- ▶ Revenue from NC being less than theoretically predicted.

# Revenue Loss Decomposition

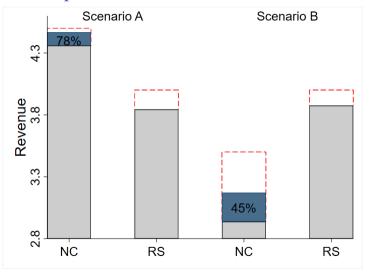


Figure 5: Revenues Increase if all Buyers enter in Period 2.

# Why not Pay the Upfront Fee (membership fee)

- ▶ "Since I got a profit the first time I didn't want to go again with my luck"
- ▶ "Risk vs Reward..... I got lucky and did not have to pay."
- ▶ "Based on the membership fee."
- "didn't want to take any big risks so I just lowballed my offers and refused to take the membership"
- "i read the instructions carefully. i think the second period isn't worth losing the points i had to pay membership fee and could only get the item by bidding higher than the price set by the seller..... honestly, i haven't been feeling lucky so i'd rather not take my chances. so i tried not to lose money in the first period and just left it as is."

# Risk Aversion Affects Second-period Participation Indirectly

	DV: Enter in Period 2	` /
	(1)	(2)
Scenario A (=1)	0.17**	$0.25^{*}$
	(0.08)	(0.13)
$notfree_1 (= 1)$	0.07	0.08
	(0.07)	(0.11)
Scenario A * $notfree_1$	$-0.18^*$	-0.14
	(0.10)	(0.17)
risk aversion	-0.01	-0.03
	(0.01)	(0.02)
$pay of f_1$	0.00	0.00
	(0.01)	(0.01)
$upfront_2$	-0.01	-0.03
	(0.03)	(0.05)
Controls		$\checkmark$

Table 2: Regression of Participation Choice on Risk attitude.

### Results

### Result 3.

- ► Generally overbid.
- ▶ Buyers overbid less under Non-Clairvoyant mechanism when the distribution of their valuation has low variance.

# Bid-Value Ratio Comparison

Bid/value	Non-Clairvoyant Dynamic	Repeated Static	(p-value) $^1$
$F_A$ (Low variance)	$1.264 \ (0.04)$	1.379(0.04)	0.060*
$F_B$ (High variance)	$1.194\ (0.05)$	$1.251 \ (0.04)$	0.392
(p-value)	0.116	0.008***	

Table 3: Bid-Value Ratio Comparison

### Conclusions

- ▶ We find the experimental observations are consistent with theoretical predictions: the optimal Non-Clairvoyant dynamic mechanism outperforms the optimal Repeated Static mechanism when it is predicted to do so.
- ▶ Buyers' risk attitudes matter in the success of Non-Clairvoyant mechanism.
- ► Randomization in non-clairvoyant mechanism leads buyers to overbid less.

### Discussion

### How should sellers choose between mechanisms?

- ▶ NC generates more revenue when the scenario is "good".
- ▶ NC encourages more accurate valuation information.
- ▶ NC works better when buyers are not risk-averse.

### Future work

- ► Can participants (human sellers) set up correct rules?
- Experiments on multi-buyer with more than 2 periods.

# Thank you!

# Requirements of Mechanisms under Non-clairvoyant Environment

### Seller sets up:

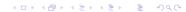
- ightharpoonup Allocation rule  $x \in \{0,1\}$ : whether buyer can get the item or not
- ▶ Price rule  $p \in \mathcal{R}$ : how much to pay if buyer gets the item

Buyer: 
$$\max_{\{b_1,b_2\}} u_1 + u_2 = (x_1v_1 - p_1) + (x_2v_2 - p_2)$$

- Dynamic Incentive Compatibility (DIC)
   For a buyer, it is optimal to bid true value in each period
- Ex-post Individual Rationality (EPIR)  $u_1 + u_2 > 0$ , for all realization of  $v_1, v_2$

# Intra-period Revenue & Inter-period Revenue

- ▶ Intra-period revenue: independent revenue, using information within that period ⇒bounded my Myerson's revenue.
- ► Inter-period revenue: dependent revenue, linking past periods with current period ⇒ bounded by current-period expected value.



# Revenue Comparison in Scenario A

$$F_1 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\} \mathbb{E}_1 = 3.$$

$$F_2 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E} = 6.$$

▶ Non-Clairvoyant Mechanism increases revenue, ↑ 12.5%

Revenue in $S_A$	Non-clairvoyant Dynamic		Repeated Static			
Period 1	Give for Free (F) Myerson's Auction (M)	0 2	Myerson's Auction (M)	2		
Period 2	Posted Price Auction (P) Myerson's Auction (M)	5 2	Myerson's Auction (M)	2		
Total		4.5		4		
Intra-period Revenue Inter-period Revenue		2 2.5		4 0		

Table 4: Theoretical Revenues in Scenario A.

# Revenue Comparison in Scenario B

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \ \mathbb{E}_1 = 6.$$

$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \ \mathbb{E}_2 = 3.$$

▶ Non-Clairvoyant Mechanism decreases revenue, ↓ 12.5%

Revenue in $S_B$	Non-clairvoyant Dynamic		Repeated Static		
Period 1	Give for Free (F) Myerson's Auction (M)	0 2	Myerson's Auction (M)	2	
Period 2	Posted Price Auction (P) Myerson's Auction (M)	3 2	Myerson's Auction (M)	2	
Total		3.5		4	
Intra-period Revenue Inter-period Revenue		2 1.5		4 0	

Table 5: Theoretical Revenues in Scenario B.

# Reserve price $(r_1, r_2)$ in Scenario A

$$\begin{array}{l} F_1=F_A=\{v,p(v)\}=\{(2,\frac{1}{2}),(4,\frac{1}{2})\},\ \mathbb{E}_1=3.\\ F_2=F_B=\{v,p(v)\}=\{(2,\frac{1}{2}),(4,\frac{1}{4}),(8,\frac{1}{8}),(16,\frac{1}{16}),(32,\frac{1}{16})\},\ \mathbb{E}_2=6. \end{array}$$

### Period 1

▶ Myserson's Auction:  $r_1 = 2$ 

### Period 2

- ▶ If luck = 1, Myserson's Auction:  $r_2 = 2$
- ▶ If luck = 0, Posted Price Auction:  $r_2$  satisfies

$$E_{v_2}[(v_2 - r_2)^+] = min(b_1, E(v_2)) = upfrong \ fee.$$

Piece-wise function:  $r_2^P = 0$  if  $b_1 \ge 6$ ,  $r_2^P = 2$  if  $b_1 = 4$ ,  $r_2^P = 8$  if  $b_1 = 2$ , and  $r_2^P = 32$  if  $b_1 = 0$ .

# Reserve price $(r_1, r_2)$ in Scenario B

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \ \mathbb{E}_1 = 6.$$

$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \ \mathbb{E}_2 = 3.$$

### Period 1

▶ Myserson's Auction:  $r_1 = 2$ 

### Period 2

- ▶ If luck = 1, Myserson's Auction:  $r_2 = 2$
- ▶ If luck = 0, Posted Price Auction:  $r_2$  satisfies

$$E_{v_2}[(v_2 - r_2)^+] = min(b_1, E(v_2)) = upfront \ fee.$$

Piece-wise function:  $r_2^P = 0$  if  $b_1 \ge 3$ ,  $r_2^P = 1$  if  $b_1 = 2$  and  $r_2^P = 4$  if  $b_1 = 0$ .

# Experimental Revenue Decomposition in Scenario A

<b>D</b>	Non-clairvoyant Dynamic			Repeated Static		
Revenue in $S_A$	Theory		Experiment	Theory		Experiment
D 1 1	Give it for free	0	0	Μ	0	1.04(0.04)
Period 1	Myerson's auction	2	1.94(0.06)	Myerson's	2	1.94(0.04)
Period 2	Posted Price Auction	<b>5</b>	4.84(0.47)	Myerson's	9	1.91(0.05)
	Myerson's auction	2	1.94(0.06)	Myerson s	4	1.91(0.00)
Total		5	4.35(0.32)		4	3.84(0.07)

Table 6: Revenue decomposition in  $S_A$ 

# Experimental Revenue Decomposition in Scenario B

<b>D</b>	Non-clairvoyant Dynamic			Repeated Static		
Revenue in $S_B$	Theory		Experiment	Theory		Experiment
D. 1. 1.1	Give it for free	0	0	N.f	0	1.01(0.05)
Period 1	Myerson's auction	2	1.93(0.06)	Myerson's	2	1.91(0.05)
Period 2	Posted Price Auction	3	2.25(0.21)	Myerson's	2	1.97(0.03)
r eriod 2	Myerson's auction	2	1.75(0.12)	Myerson s	2	1.97 (0.03)
Total		3.5	<b>2.91</b> (0.18)		4	3.88(0.06)

Table 7: Revenue decomposition in  $S_B$