

Surplus and Equilibrium (Ch14/15/16)

Shan Gui

Shanghai University of Finance and Economics

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Consumption Theory

What We Have Learned

- Consider non-extreme preferences. Given p_1, p_2 and m .

	$p_1 \uparrow$	$p_1 \downarrow$
Consumption of Good 1	Substitution: - Income: -/+	Substitution: + Income: +/-
Consumption of Good 2	Substitution: + Income: -/+	Substitution: - Income: +/-
Consumer's Utility	?	?

Table 1: Effect of rise/fall of p_1 in two good economy

Measuring Gains and Losses from a Change

- Why is $u^{new} - u^{old}$ not a good measure?

Outline

Part I. Monetary Measures of Welfare Change

- ▶ The Relationship Triangle: Preferences, Choices, and Utilities
- ▶ Three Monetary Measures: Compensating Variation (CV), Equivalent Variation (EV), and Change in Consumer Surplus (ΔCS) (Ch14)

Part II. From Consumer Surplus to Consumers' Surplus

- ▶ Aggregate individual demand to derive market demand. (Ch15)
- ▶ Competitive equilibrium maximizes social surplus. (Ch16)
- ▶ Who bears the tax burden more? \Rightarrow Depends on the price elasticity of demand and supply.

Part I: Monetary Measures of Gain/Loss from a Price Change

Why is $u^{new} - u^{old}$ not a good measure?

- ▶ The Relationship Triangle: Preferences, Choices, and Utilities

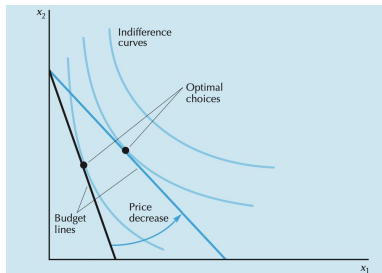
Three Monetary Measures:

- ▶ Compensating Variation (CV)
- ▶ Equivalent Variation (EV)
- ▶ Change in Consumer Surplus (ΔCS)

Consumer will never Worse-off if Price Decreases

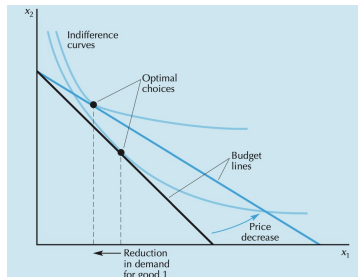
A Price Decrease Expands the Budget Set

- ▶ *Ceteris paribus*, more options lead to a higher utility: $u^{new} > u^{old}$.
- ▶ Conversely, a price increase never benefits the consumer.



An ordinary good. Ordinarily, the demand for a good increases when its price decreases, as is the case here.

Good 1 is an Ordinary Good



A Giffen good. Good 1 is a Giffen good, since the demand for it decreases when its price decreases.

Good 1 is a Giffen Good

Choices Reveal Preferences, Utility Functions Represent Preferences

Choices: $x(\mathbf{p}, m)$

- ▶ Choices \Leftarrow Preferences + Budget Constraints
- ▶ Choices are observable.

Collecting choices under different prices \Rightarrow Individual demand curve.

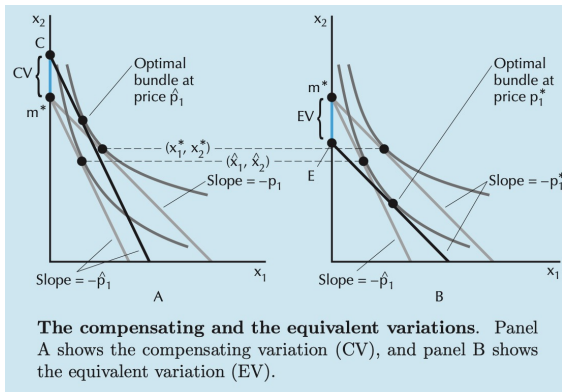
Utility Function: $u(\mathbf{x})$

- ▶ Utility functions label indifference curves.
- ▶ Different utility functions can represent the same preferences.
- ▶ **Lexicographical preferences** cannot be represented by a utility function.

For example, $(x_1^A, x_2^A) \succeq (x_1^B, x_2^B)$ if $x_1^A > x_1^B$ or $(x_1^A = x_1^B \text{ and } x_2^A \geq x_2^B)$.

Monetary Measure of Welfare Loss under Rise of Price

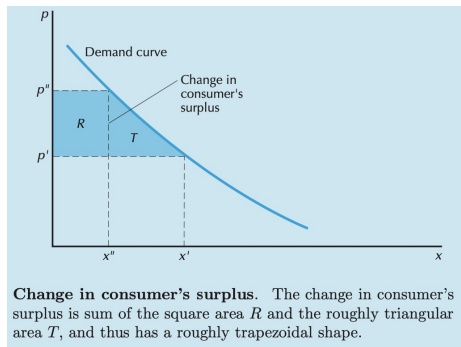
Compensating Variation (CV) Equivalent Variations (EV)



- ▶ **Compensating Variation:**
How much income is needed to maintain the original utility?
- ▶ $CV = e(p_1^{new}, p_2, v) - m$
- ▶ e : the minimum expenditure given prices and utility (v)
- ▶ **Equivalent Variation:** How much income loss is equivalent to this price change?
- ▶ $EV = m - e(p_1, p_2, v^{new})$

Monetary Measure of Welfare Loss under Rise of Price

Change in Consumer's Surplus (ΔCS)



- ▶ Optimal consumption: $x_1^*(p_1, p_2, m)$
- ▶ Inverse demand function: $p(x)$, write p_1 as a function of x_1 , viewing p_2, m as constant.
- ▶ Gross Surplus at (x', p') : area under demand curve, $\int_0^{x'} p(x) dx$
- ▶ (Net) Surplus: area under demand curve and above market price line (p'),
 $\int_0^{x'} [p(x) - p'] dx$
- ▶ p' to p'' :
$$\Delta CS = \int_0^{x''} [p(x) - p'] dx - \int_0^{x'} [p(x) - p'] dx$$
$$\Delta CS = \int_{p'}^{p''} x(p) dp$$

Relationship Among CV , EV , and ΔCS

Marshallian Demand Curve and Hicksian Demand Curve

- ▶ Marshallian Demand: $x_1^*(p_1, p_2, m)$, given income \Rightarrow normal demand curve
 ΔCS : Trapezoidal area under Marshallian demand curve
- ▶ Hicksian Demand: $x_1^*(p_1, p_2, u)$, holding the utility the same
 CV, EV : Trapezoidal area under Hicksian demand curves

For a normal good

- ▶ Hicksian demand curve is steeper than Marshallian demand curve. Why?
- ▶ For a price increase: $CV > -\Delta CS > EV > 0$
- ▶ For a price decrease: $0 > CV > -\Delta CS > EV$

If $U(x_1, x_2) = v(x_1) + x_2$

- ▶ No income effect on Good 1 if income is enough.
- ▶ $CV = -\Delta CS = EV = -\Delta U$

Part II. From Consumer Surplus to Consumers' Surplus

Aggregate individual demand to derive market demand

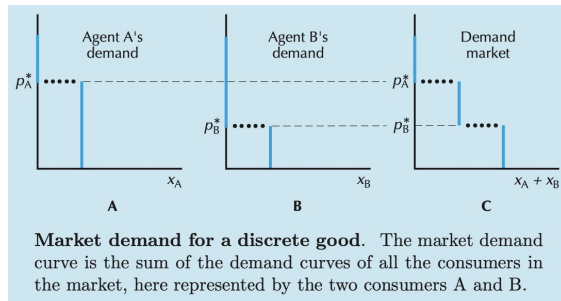
- ▶ Consumers' Surplus

Market Demand, Market Supply, and Equilibrium

- ▶ Competitive equilibrium maximizes social surplus. (Ch16)
- ▶ Who bears the tax burden more? \Rightarrow Depends on the price elasticity of demand and supply.

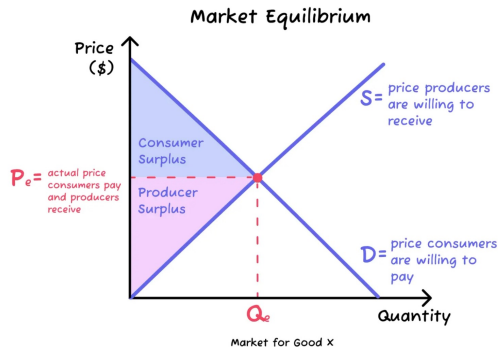
From Individual to Market Demand

Summing the Demand Curves Horizontally



- ▶ Market Demand Function for Good 1:
$$X^1(p_1, p_2, m_1, m_2 \dots m_n)$$
$$= \sum_{i=1}^n x_i^1(p_1, p_2, m_i)$$
- ▶ Market Demand Curve: $p_1(X^1)$, viewing p_1, m_1, \dots, m_m as constant
- ▶ Market Supply: aggregation of individual supply

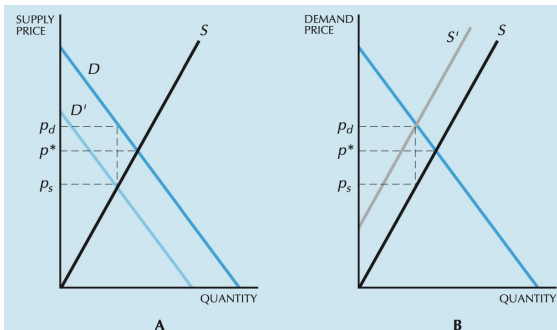
From Consumer's Surplus to Consumers' Surplus



- **Consumers' Surplus:** area under market demand curve and above market price line (p^e),
$$\int_0^{x^e} [p(x) - p^e] dx$$
- **Producers' Surplus:** area under market supply curve and below market price line (p^e),
$$\int_0^{x^e} [p(x) - p^e] dx$$
- **Social Surplus:** Consumers' Surplus + Producers' Surplus + (Government's Revenue)

Who Bears the Tax More?

Tax on Producers or Consumers: It Doesn't Matter

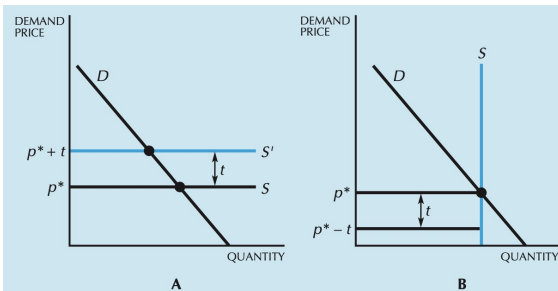


The imposition of a tax. In order to study the impact of a tax, we can either shift the demand curve down, as in panel A, or shift the supply curve up, as in panel B. The equilibrium prices paid by the demanders and received by the suppliers will be the same either way.

- ▶ A tax $t = p^d - p^s$
- ▶ Tax on consumer: shift the demand curve down
- ▶ Tax on producer: shift the supply curve up
- ▶ \Rightarrow same equilibrium quantity, same purchasing price p^d , same price received by supplier p^s .
- ▶ Who Bears the Tax More?
 $p^d - p^* = \Delta p = ?$

Extreme Cases

Perfectly Elastic Supply and Perfectly Inelastic Supply

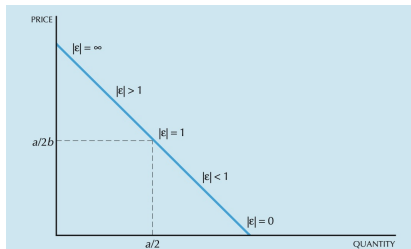


Special cases of taxation. (A) In the case of a perfectly elastic supply curve the tax gets completely passed along to the consumers. (B) In the case of a perfectly inelastic supply none of the tax gets passed along.

- ▶ Consumers bear all tax:
 $\Delta p = p^d - p^* = t$
 - Perfectly Elastic Supply
 - Perfectly Inelastic Demand
- ▶ Producers bear all tax:
 $\Delta p = p^d - p^* = 0$
 - Perfectly Inelastic Supply
 - Perfectly Elastic Demand

Tax Incidence Depends on Price Elasticity of Demand and Supply

Price elasticity: $\epsilon = \frac{\Delta q/q}{\Delta p/p}$:



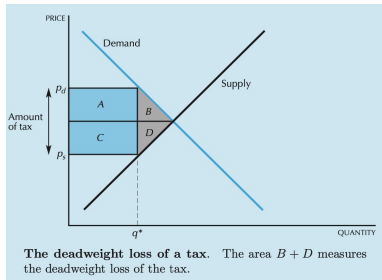
The elasticity of a linear demand curve. Elasticity is infinite at the vertical intercept, one halfway down the curve, and zero at the horizontal intercept.

- ▶ **Price Elasticity:** percentage change in quantity when price changes by one percent
- ▶ Price Elasticity of Demand: $\epsilon^D = \frac{\Delta D/D}{\Delta p/p}$
- ▶ Price Elasticity of Supply: $\epsilon^S = \frac{\Delta S/S}{\Delta p/p}$
- ▶ Before Tax: $S(p) = D(p)$, $\Delta t \Rightarrow \Delta p$
- ▶ After Tax: $S(p + \Delta p) = D(p + \Delta p + \Delta t)$
$$\Rightarrow \frac{\Delta p}{\Delta p} = \frac{D'(p)}{S'(p) - D'(p)} = \frac{\epsilon^D}{\epsilon^S - \epsilon^D}$$

The more elastic the market demand, the smaller the tax burden on consumers.

Deadweight Loss of a Tax

Less Than Market Equilibrium Quantity



- ▶ Competitive Equilibrium: Maximum Social Surplus
- ▶ Output has been decreased by this tax.
Change in Consumers' Surplus: $-(A+B)$
Change in Producers' Surplus: $-(C+D)$
Change in Government's Revenue: $+(A+C)$
- ▶ Deadweight Loss of a tax: area $B+D$
- ▶ subsidy = - tax
- ▶ The Deadweight Loss of a subsidy?

End of Consumer Theory

Midterm Exam

- ▶ Date: Monday, April 7th, during class time
- ▶ Location: Classroom 1-204
- ▶ Format: Closed book; answers may be written in English or Chinese.
- ▶ Chapters Covered: Ch. 1–6, Ch. 8, Ch. 14–16

- ▶ Good luck!

Good luck!

Thank You!