

Non-Clairvoyant Dynamic Mechanism Design: Experimental Evidence

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Main Takeaways

What do we do?

- ▶ Bring Non-Clairvoyant Environment (Mirrokni et al., 2020) into Lab.
- ▶ Test the optimal Non-Clairvoyant dynamic mechanism (NC).
- ▶ Compare the performance with Repeated Static optimal mechanism (RS).

What do we find?

- ▶ Dynamic NC works well as theory predicts - More revenue in some scenarios.
- ▶ Participants overbid less in NC.
- ▶ Risk aversion \rightarrow No full participation \rightarrow Revenue loss in NC.

Optimal Dynamic Mechanism Design

- ▶ How the seller establishes the rules of allocation and price over **multi-period** for the best revenue, as the buyer receives private information over time.
 - ▶ Long-term principal-agent relationship
 - ▶ **Repeated selling of perishable goods**
- ▶ Dynamic mechanism improves revenues and efficiency (Baron & Besanko, 1984).

Non-Clairvoyance

Clairvoyance: Future demand is known at the beginning.

- ▶ Complicated, non-intuitive, lack of General Form.
- ▶ Buyers tend to have biased forecast on future demand (DellaVigna & Malmendier, 2006).

Non-Clairvoyance: Future demand is not accessible at the beginning.

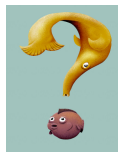
- ▶ No need to share unbiased belief.
- ▶ General Form.



F_2 is unknown in Day 1



$v_1 \sim F_1$



$v_2 \sim F_2$?

Mechanisms under Non-Clairvoyant Environment

\Rightarrow Optimal clairvoyant revenue Rev^* is unachievable.

RS: Repeated Static optimal mechanism (Myerson, 1981)

- Rules in two days are independent of each other

Maximize **intra-period revenue** for each period separately.

$\Rightarrow \frac{Rev^{RS*}}{Rev^*}$ could be arbitrarily small (Papadimitriou et al., 2016)

NC: Non-Clairvoyant optimal dynamic mechanism (Mirrokni et al., 2020)

- Rules in Day 2 depends on bid in day 1

Best Revenue Guarantee: $\Rightarrow \frac{Rev^{NC*}}{Rev^*} \geq \frac{1}{\alpha}$

Achieve at least $\frac{1}{2}$ revenue produced by optimal clairvoyant mechanism under all scenarios in **two-period single-buyer** case.

When can Non-Clairvoyant dynamic mechanism do better?

Theoretically, Non-Clairvoyant mechanism can not always outperform.

	Optimal Intra-period Revenue	Optimal Inter-period Revenue
RS	100%	zero
NC	$\geq 50\%$	$\geq 50\%$

Relative size of optimal intra- and inter-period revenues is the key.

- ▶ Scenario A: Optimal inter - period revenue is larger \Rightarrow NC outperforms.
- ▶ Scenario B: Optimal intra - period revenue is larger \Rightarrow RS outperforms.

Experimental Design 2 * 2

Two Mechanisms

- ▶ Non-Clairvoyant Dynamic Mechanism (NC)
- ▶ Repeated Static Mechanism (RS)

Two Scenarios

$$F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_A = 3.$$

$$F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_B = 6.$$

- ▶ Scenario A (S_A): NC generates more revenue than RS.

$$F_1 = F_A, F_2 = F_B \Rightarrow REV^{RS} = 4, REV^{NC} = 4.5 \uparrow 12.5\%$$

- ▶ Scenario B (S_B): NC generates less revenue than RS.

$$F_1 = F_B, F_2 = F_A \Rightarrow REV^{RS} = 4, REV^{NC} = 3.5 \downarrow 12.5\%$$

Non-Clairvoyant Environment

- ▶ **Buyer:** Participant
- ▶ **Robot Seller:** Experimenter, $c = 0$
- ▶ **Two periods :** Buyer can buy one item in each period from seller, $t = 1, 2$.
- ▶ **Non-clairvoyance :** The distribution of buyer's value (F_t) is common knowledge **only in that period**
- ▶ **Incomplete Information :**
 1. **Only buyer** knows his value for the item in each period, v_t .
 2. Buyer's value is drawn **independently**.

Variables for Environment

- ▶ **Endowment:** $E = 50$

Mechanism - Repeated Static (RS)

Period 1

- ▶ Seller sets a reserve price r_1 based on the distributional knowledge F_1 .
- ▶ Buyer learns his value (v_1), makes a bid : b_1
- ▶ Buyer can get the item only when $b_1 \geq r_1$ and pay $p_1 = r_1$.

Period 2

- ▶ $F_2 \Rightarrow r_2$, $v_2 \Rightarrow b_2$, pays $p_2 = r_2$ if $b_2 \geq r_2$

Myerson's Auction

monopoly price: $r_1 = r_2 = 2$

$$r_A = 2 \in \{\arg \max_r r \cdot P(v_A > r)\}, \quad r_B = 2 \in \{\arg \max_r r \cdot P(v_B > r)\}$$

Mechanism - Non-Clairvoyant Dynamic (NC)

How the dynamic mechanism work?



Half chance of free item in period 1

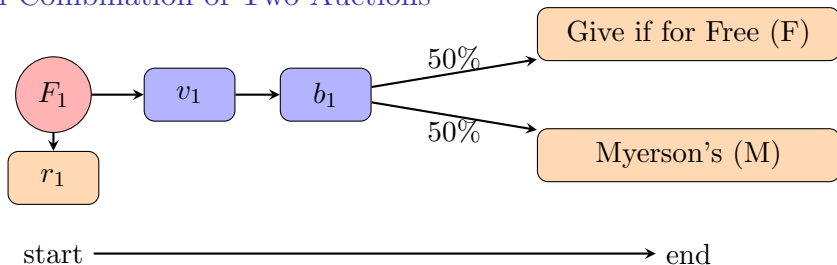


Half chance of upfront fee in period 2

Non-Clairvoyant Mechanism in Period 1

- ▶ Seller sets a fixed reserve price r_1 based on the distribution F_1 .
- ▶ Buyer learns his value (v_1), makes a bid : b_1
- ▶ Buyer has 50% chance to get the item for free: $p_1 = 0$;
Otherwise, buyer can get the item only when $b_1 \geq r_1$ and pay $p_1 = r_1$.

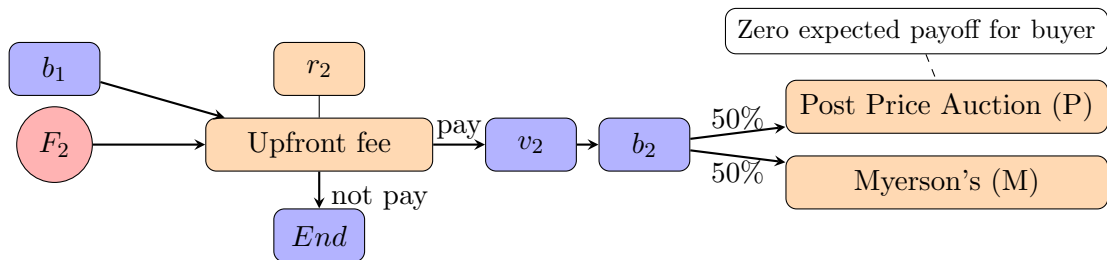
Uniform Combination of Two Auctions



Non-Clairvoyant Mechanism in Period 2

- ▶ Seller sets an upfront fee $s_2 = \min(b_1, E(v_2))$.
- ▶ Buyer decides pay or leave. If buyer leave ($enter = 0$), game over.
- ▶ If buyer pays, ($enter = 1$),
 - ▶ Buyer learns his value, v_2 , and makes a bid: b_2
 - ▶ Buyer has 50% chance to get refund on the upfront fee ($luck = 1$).
 - ▶ Seller sets two reserve prices (r_2) based on the $F_2, luck$ for each given m_2 ,
Buyer can get the item only when $b_2 \geq r_2$ and pay $p_2 = r_2$

Uniform Combination of Two Auctions



Hypotheses

Hypothesis 1 - On Revenue Comparison

- ▶ In Scenario A (S_A), the non-clairvoyant mechanism (NC) generates greater revenue than the repeated static mechanism (RS);
- ▶ In S_B , NC generates less revenue than RS.

Hypothesis 2 - On Individual Rationality

- ▶ Some buyers choose not to pay the upfront fee, such that the experimental revenue of the non-clairvoyant mechanism is less than its theoretical prediction.

Hypothesis 3 - On Incentive Compatibility

- ▶ Participants' bids are closer to true value under NC than RS.

Experiments

- ▶ 256 George Mason Students. September to November 2021.

Treatment	Scenario A		Scenario B	
	Non-Clairvoyant	Repeated Static	NC	RS
Age	21.6	22.3	21.9	22.7
Gender (Male=1)	0.48	0.44	0.52	0.47
Risk aversion	4.46	4.90	4.55	4.63
Observation	64	64	64	64

Table 1: Summary Statistic

Results

Result 1.

Experimental observations match theoretical predictions.

- ▶ In S_A , the non-clairvoyant dynamic mechanism gains more revenue than the repeated static mechanism.
- ▶ In S_B , the non-clairvoyant dynamic mechanism gains less revenue than the repeated static mechanism. mechanism.

Experimental Revenue Comparison - Period 1

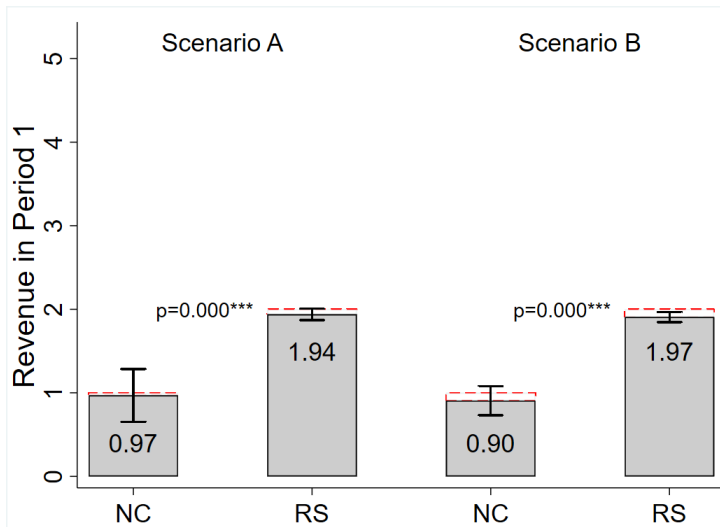


Figure 3: Revenues of Period 1 in each Treatment

Experimental Revenue Comparison - Period 1 & Period 2

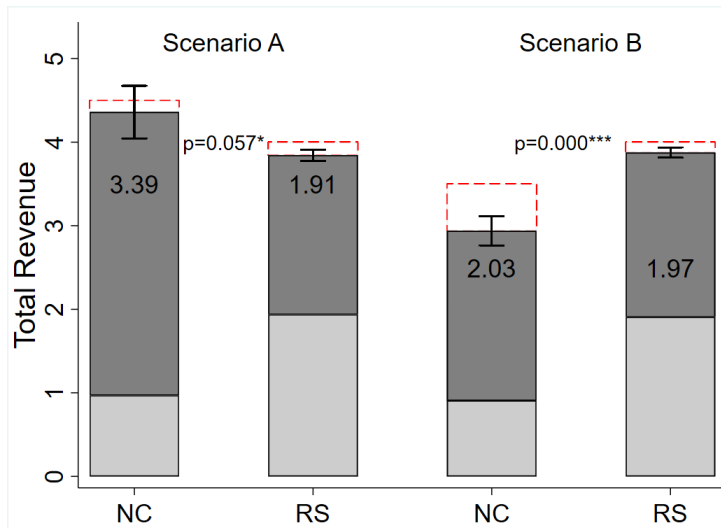


Figure 4: Revenues in each Treatment

Results

Result 2.

Risk aversion deters buyers from participating in the second period in NC.

- ▶ In S_A , 4 buyers quit the second period, and the number doubles in S_B .
- ▶ Revenue from NC being less than theoretically predicted.

Revenue Loss Decomposition

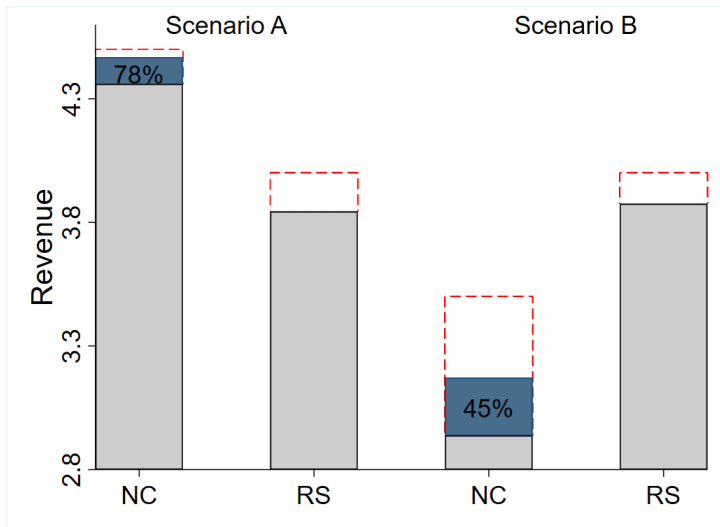


Figure 5: Revenues Increase if all Buyers enter in Period 2.

Why not Pay the Upfront Fee (membership fee)

- ▶ “Since I got a profit the first time I didn’t want to go again with my luck”
- ▶ “Risk vs Reward..... I got lucky and did not have to pay.”
- ▶ “Based on the membership fee. ”
- ▶ “didn’t want to take any big risks so I just lowballed my offers and refused to take the membership”
- ▶ “i read the instructions carefully. i think the second period isn’t worth losing the points - i had to pay membership fee and could only get the item by bidding higher than the price set by the seller..... honestly, i haven’t been feeling lucky so i’d rather not take my chances. so i tried not to lose money in the first period and just left it as is.”

Risk Aversion Affects Second-period Participation Indirectly

	DV: Enter in Period 2 (=1)	
	(1)	(2)
Scenario A (=1)	0.17** (0.08)	0.25* (0.13)
<i>notfree</i> ₁ (= 1)	0.07 (0.07)	0.08 (0.11)
Scenario A * <i>notfree</i> ₁	-0.18* (0.10)	-0.14 (0.17)
risk aversion	-0.01 (0.01)	-0.03 (0.02)
<i>payoff</i> ₁	0.00 (0.01)	0.00 (0.01)
<i>upfront</i> ₂	-0.01 (0.03)	-0.03 (0.05)
Controls		✓

Standard errors in parentheses. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.1$.

Table 2: Regression of Participation Choice on Risk attitude.

Results

Result 3.

- ▶ Generally overbid.
- ▶ Buyers overbid less under Non-Clairvoyant mechanism when the distribution of their valuation has low variance.

Bid-Value Ratio Comparison

Bid/value	Non-Clairvoyant Dynamic	Repeated Static	(p-value) ¹
F_A (Low variance)	1.264 (0.04)	1.379 (0.04)	0.060*
F_B (High variance)	1.194 (0.05)	1.251 (0.04)	0.392
(p-value)	0.116	0.008***	

Table 3: Bid-Value Ratio Comparison

¹We report two-sided p-value under t-test.

Conclusions

- ▶ We find the experimental observations are consistent with theoretical predictions: the optimal Non-Clairvoyant dynamic mechanism outperforms the optimal Repeated Static mechanism when it is predicted to do so.
- ▶ Buyers' risk attitudes matter in the success of Non-Clairvoyant mechanism.
- ▶ Randomization in non-clairvoyant mechanism leads buyers to overbid less.

Discussion

How should sellers choose between mechanisms?

- ▶ NC generates more revenue when the scenario is “good”.
- ▶ NC encourages more accurate valuation information.
- ▶ NC works better when buyers are not risk-averse.

Future work

- ▶ Can participants (human sellers) set up correct rules?
- ▶ Experiments on multi-buyer with more than 2 periods.

Thank you!

Requirements of Mechanisms under Non-clairvoyant Environment

Seller sets up:

- ▶ Allocation rule $x \in \{0, 1\}$: whether buyer can get the item or not
- ▶ Price rule $p \in \mathcal{R}$: how much to pay if buyer gets the item

Buyer: $\max_{\{b_1, b_2\}} u_1 + u_2 = (x_1 v_1 - p_1) + (x_2 v_2 - p_2)$

- ▶ Dynamic Incentive Compatibility (DIC)

For a buyer, it is optimal to bid true value in each period

- ▶ Ex-post Individual Rationality (EPIR)

$u_1 + u_2 \geq 0$, for all realization of v_1, v_2

Intra-period Revenue & Inter-period Revenue

- ▶ Intra-period revenue: independent revenue, using information within that period \Rightarrow bounded by Myerson's revenue.
- ▶ Inter-period revenue: dependent revenue, linking past periods with current period \Rightarrow bounded by current-period expected value.

Revenue Comparison in Scenario A

$$F_1 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\} \quad \mathbb{E}_1 = 3.$$

$$F_2 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \quad \mathbb{E} = 6.$$

- Non-Clairvoyant Mechanism increases revenue, $\uparrow 12.5\%$

Revenue in S_A	Non-clairvoyant Dynamic		Repeated Static	
Period 1	Give for Free (F) Myerson's Auction (M)	0 2	Myerson's Auction (M)	2
Period 2	Post Price Auction (P) Myerson's Auction (M)	5 2	Myerson's Auction (M)	2
Total		4.5		4
Intra-period Revenue		2		4
Inter-period Revenue		2.5		0

Table 4: Theoretical Revenues in Scenario A.

Revenue Comparison in Scenario B

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \mathbb{E}_1 = 6.$$

$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \mathbb{E}_2 = 3.$$

- Non-Clairvoyant Mechanism decreases revenue, $\downarrow 12.5\%$

Revenue in S_B	Non-clairvoyant Dynamic		Repeated Static	
Period 1	Give for Free (F) Myerson's Auction (M)	0 2	Myerson's Auction (M)	2
Period 2	Post Price Auction (P) Myerson's Auction (M)	3 2	Myerson's Auction (M)	2
Total		3.5		4
Intra-period Revenue		2		4
Inter-period Revenue		1.5		0

Table 5: Theoretical Revenues in Scenario B.

Reserve price (r_1, r_2) in Scenario A

$$F_1 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \quad \mathbb{E}_1 = 3.$$

$$F_2 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \quad \mathbb{E}_2 = 6.$$

Period 1

- Myerson's Auction: $r_1 = 2$

Period 2

- If $luck = 1$, Myerson's Auction: $r_2 = 2$
- If $luck = 0$, Posted Price Auction: r_2 satisfies

$$E_{v_2}[(v_2 - r_2)^+] = \min(b_1, E(v_2)) = \text{upfront fee}.$$

Piece-wise function: $r_2^P = 0$ if $b_1 \geq 6$, $r_2^P = 2$ if $b_1 = 4$, $r_2^P = 8$ if $b_1 = 2$, and $r_2^P = 32$ if $b_1 = 0$.

Reserve price (r_1, r_2) in Scenario B

$$F_1 = F_B = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{4}), (8, \frac{1}{8}), (16, \frac{1}{16}), (32, \frac{1}{16})\}, \quad \mathbb{E}_1 = 6.$$
$$F_2 = F_A = \{v, p(v)\} = \{(2, \frac{1}{2}), (4, \frac{1}{2})\}, \quad \mathbb{E}_2 = 3.$$

Period 1

- Myerson's Auction: $r_1 = 2$

Period 2

- If $luck = 1$, Myerson's Auction: $r_2 = 2$
- If $luck = 0$, Posted Price Auction: r_2 satisfies

$$E_{v_2}[(v_2 - r_2)^+] = \min(b_1, E(v_2)) = \text{upfront fee}.$$

Piece-wise function: $r_2^P = 0$ if $b_1 \geq 3$, $r_2^P = 1$ if $b_1 = 2$ and $r_2^P = 4$ if $b_1 = 0$.

Experimental Revenue Decomposition in Scenario A

Revenue in S_A	Non-clairvoyant Theory	Dynamic Experiment	Repeated Static Theory	Static Experiment
Period 1	Give it for free	0	0	
	Myerson's auction	2	1.94(0.06)	Myerson's 2 1.94(0.04)
Period 2	Post Price Auction	5	4.84(0.47)	
	Myerson's auction	2	1.94(0.06)	Myerson's 2 1.91(0.05)
Total		5	4.35(0.32)	4 3.84(0.07)

Table 6: Revenue decomposition in S_A

Experimental Revenue Decomposition in Scenario B

Revenue in S_B	Non-clairvoyant		Dynamic		Repeated Static	
	Theory		Experiment		Theory	Experiment
Period 1	Give it for free	0	0	Myerson's	2	1.91(0.05)
	Myerson's auction	2	1.93(0.06)			
Period 2	Post Price Auction	3	2.25(0.21)	Myerson's	2	1.97(0.03)
	Myerson's auction	2	1.75(0.12)			
Total		3.5	2.91 (0.18)		4	3.88 (0.06)

Table 7: Revenue decomposition in S_B