

# **Circuit Theory and Electronics Fundamentals**

T4 Laboratory Report

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**Group 61**

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# 1 Introduction

In this laboratory assignment, we analysed, using both a theoretical and simulation analysis, a Sound Amplifier made of Bipolar Junction Transistors. It was made up of two different stages, a Gain stage, with the goal of having the maximum gain possible, and an output stage, whose goal was to lower the impedance. The circuit is presented in ??.

As mentioned above, we analysed the circuit theoretically, combining Operating Point, allowing us to derive important values used in the incremental analysis.

Simultaneously, the circuit is analysed by computational simulation tools, via *Ngspice*, and the results are compared to the theoretical results obtained, in Section 2. The conclusions of this study are outlined in Section 4.

We also used Ngspice to analyse the circuit by computational tools, and then compared with the results obtained in 2. The results of this comparison are outlined in 4.

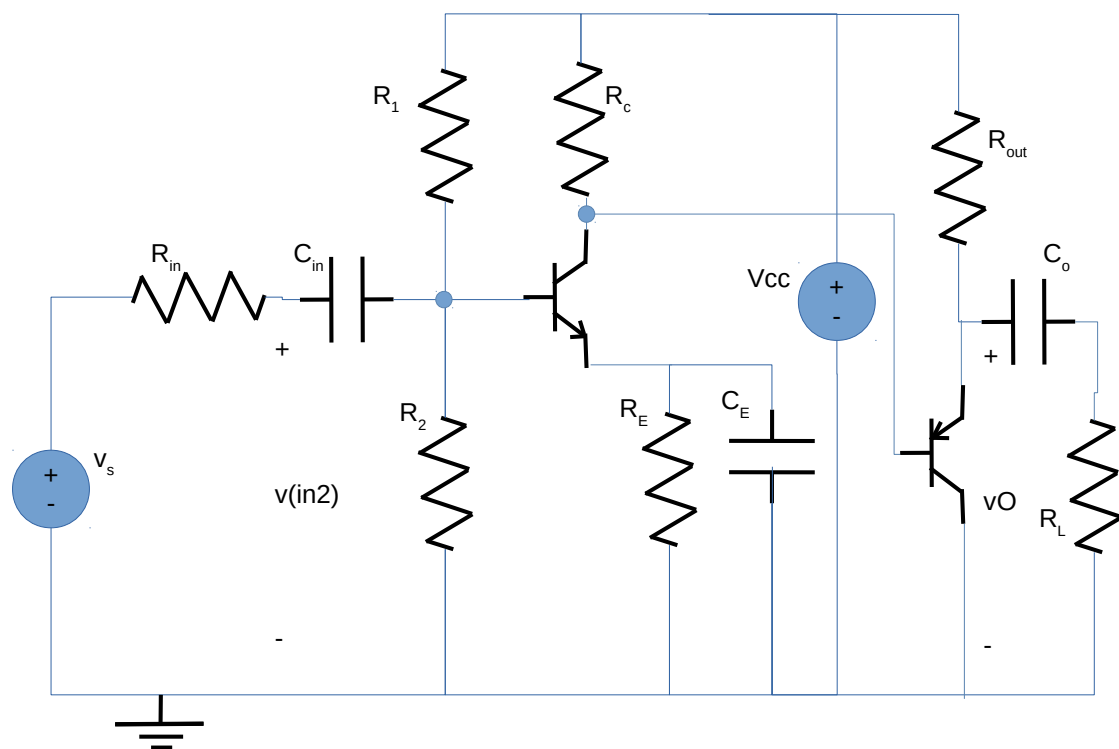


Figure 1: BJT Amplifier

## 2 Theoretical and Simulation Analysis

We will be dealing with the simulation and theoretical analysis at the same time. Next we present a table of constants that will be used.

Name	Value	Units
$R_1$	33.7	$k\Omega$ [kOhms]
$R_2$	3.6	$k\Omega$ [kOhms]
$R_C$	3.8	$k\Omega$ [kOhms]
$R_E$	200	$\Omega$ [Ohms]
$R_{out}$	400	$\Omega$ [Ohms]
$C_{in}$	800	$\mu F$ [ $\mu$ Farads]
$C_E$	800	$\mu F$ [ $\mu$ Farads]
$C_o$	600	$\mu F$ [ $\mu$ Farads]

Table 1: Constants Values

### 2.1 Gain Stage

The Gain Stage of the circuit is responsible for insuring a high input voltage so the input signal is not degraded through the circuit. It has an elevated gain and is the part responsible for signal amplification.

There are 3 types of elements: a NPN BJT, resistors and capacitors.

The first capacitor,  $C_{in}$ , is a coupling capacitor, as it acts as a DC Block, so that  $V_{in}$  doesn't impose a DC component of 0, that would change the OP of the transistor.

The second capacitor,  $C_E$ , acts as a bypass capacitor, for it ensures that for low frequencies all the current flows through  $R_E$ , and for high frequencies, it passes through the capacitor.

The output impedance of this stage ( $Z_{O1}$ ) is high.

### 2.2 Output Stage

The Gain Stage has a high  $Z_{O1}$  so to counter this, we connect a circuit with low output impedance to the first one. This circuit presents similar components but with very distinct results.

Instead of a NPN BJT, we use a PNP BJT, because it has a higher  $\beta_F$ , which lowers the output impedance.

Another capacitor,  $C_o$ , is used with a similar goal as the previous coupling capacitor. If we didn't use such component, the gain stage would impose a DC voltage of 0 to the second stage, which would ruin the transistor's OP.

As we'll see, we end up with a lower output impedance in this stage and a higher input impedance (when compared to the output impedance of the gain stage).

When combining both stages, we need to ensure that there is a compatibility between the impedances, the input impedance of the second stage should be much greater than the output impedance of the first one.

## 2.3 Theoretical Analysis

In the theoretical analysis we will evaluate the four impedances associated with the two stages ( $Z_{I1}$ ,  $Z_{O1}$ ,  $Z_{I2}$  and  $Z_{O2}$ ) and the two gains in each stage ( $A_{V1}$  and  $A_{V2}$ ).

### 2.3.1 Impedances

In the first stage we can find the input and output impedances ( $\{Z_{I1}, Z_{O1}\}$ ) using KVL and KCL.

$$Z_{I1} = R_B // r_{\pi 1} \quad (1)$$

where  $R_B = R_1 // R_2$ .

We assume  $R_E \simeq 0$  (capacitors are short-circuited). The first stage input matches the total input impedance of the circuit.

The first stage output impedance can be obtained by:

$$Z_{O1} = r_o // R_C \quad (2)$$

For the second stage, by analysing the circuit we get:

$$Z_{I2} = \frac{(g_{m2} + g_{\pi 2} + g_{o2} + g_{E2})}{g_{\pi 2}(g_{\pi 2} + g_{o2} + g_{E2})} \quad (3)$$

$$Z_{O2} = \frac{1}{(g_{m2} + g_{\pi 2} + g_{o2} + g_{E2})} \quad (4)$$

And finally, the total output impedance:

$$Z_{OT} = \frac{v_o}{i_o} = \frac{1}{g_{o2} + g_{m2} \frac{r_{\pi 2}}{r_{\pi 2} + Z_{O1}} + g_{E2} + \frac{1}{r_{\pi 2} + Z_{O1}}} \quad (5)$$

The 4 values are presented below,

Impedances	Ohms ( $\Omega$ )
$Z_{I1}$	1290.209759
$Z_{O1}$	3411.452239
$Z_{I2}$	37245.135442
$Z_{O2}$	1.375831
$Z_{OT}$	15.566019

Table 2: Theoretical Impedances

Remembering that  $Z_{O1}$  needs to be much lower than  $Z_{I2}$ , we end up with good results. This is needed so that there is no signal degradation or loss between these stages.

### 2.3.2 Gain

To calculate the total gain ( $A_V$ ) we performed a simple multiplication  $A_V = A_{V1} A_{V2}$ . The real interaction between both stages is negligible, and so we can compute the gain as if it was the total gain of both separate stages.

To acquire a better comparison between theory and simulation, besides this approach, that considers the gain to be constant through all the frequencies, we also performed the *Time constant method* for the lower cut-off frequency.

We calculate the lower cut-off frequency ( $\omega_L = 2\pi f_{CO_L}$ ) as,

Gain	Value
$G_1$	-264.565721
$G_2$	0.991532
$G_T$	-252.275561
$G_{T_{dB}}$	48.037504

Table 3: Theoretical upper gain bound results

Gain	Value
$G_1$	-17.126226
$G_2$	0.991532
$G_T$	-16.330643
$G_{T_{dB}}$	24.260066

Table 4: Theoretical lower gain bound results

$$\omega_L = 1/R_{eq_i}C_i + 1/R_{eq_e}C_e + 1/R_{eq_o}C_o \implies f_{CO_L} = 2\pi\omega_L \quad (6)$$

where  $R_{eq} \equiv$  equivalent resistor as seen by each capacitor when the others are short-circuits.

We have,

$$R_{eq_{in}} = R_{in} + Z_{I1} \quad (7)$$

$$R_{eq_e} = R_E // \left( \frac{1}{\frac{1}{R_s || R_B + r_\pi} + \frac{g_m r_\pi}{R_s || R_B + r_\pi}} \right) \simeq R_E // \left( \frac{r_\pi + R_s || R_B}{r_\pi} \frac{1}{g_m} \right) \simeq 1/g_m \quad (8)$$

$$R_{eq_o} = R_L + Z_O \quad (9)$$

The theoretical value of the lower cut-off frequency is presented in the table below.

Name	Value [Hz]
Lower CO freq	28.296662

Table 5: Theoretical Lower Cut-off frequency

## 2.4 Simulation Analysis

In the Simulation Analysis, we want to get the two impedances associated with the circuit, the two cut-off frequencies,  $f_{CO_L}$  and  $f_{CO_H}$ , the bandwidth and the total gain,  $A_V$ . We also check whether the BJT's are on the Forward Active Region (FAR), by comparing  $V_{CE}$  and  $V_{BE}$  for the NPN, and, analogously,  $V_{EC}$  and  $V_{EB}$  for PNP.

Name	Value
V(CE)	3.41818
V(BE)	0.667497
V(CE) greater than V(BE)	Yes

Table 6: NPN voltages and FAR confirmation

Name	Value
V(EC)	4.59871
V(EB)	0.730469
V(EC) greater than V(EB)	Yes

Table 7: PNP voltages and FAR confirmation

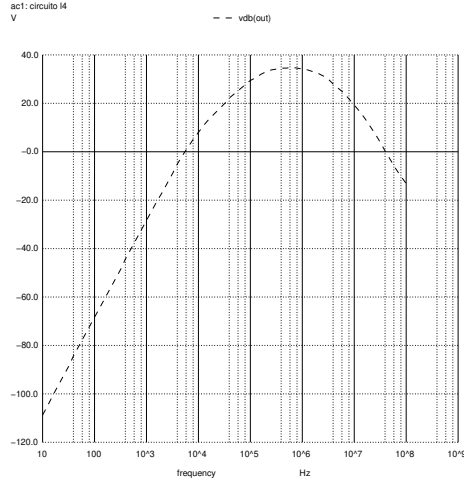
The results are presented in the table below:

Name	Value	Units
Gain (dB)	36.1296	dB
Gain	63.8779	
Lower CO Freq	19.9163	Hz
Higher CO Freq	1.37411E+06	Hz
Bandwidth	1.37409E+06	Hz

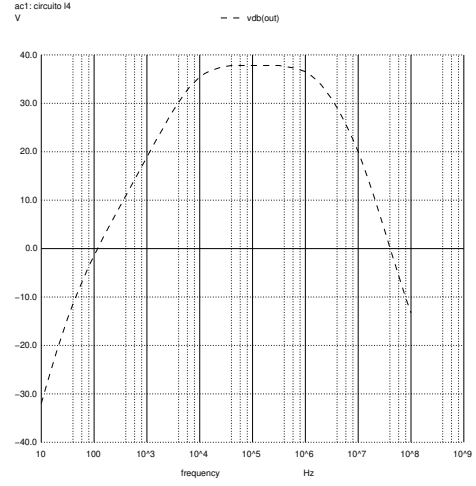
Table 8: Simulation results

### 2.4.1 Coupling Capacitors

To be able to analyse the circuit, we need to understand the Coupling Capacitor's behaviour. In our amplifier we have two coupling capacitors,  $C_O$  and  $C_{in}$ , but due to the analog nature of the functions, we will focus on the capacitor  $C_{in}$ . The two figures of the frequency response analysis are presented below.



(a)  $C_i$  low ( $1nF$ )



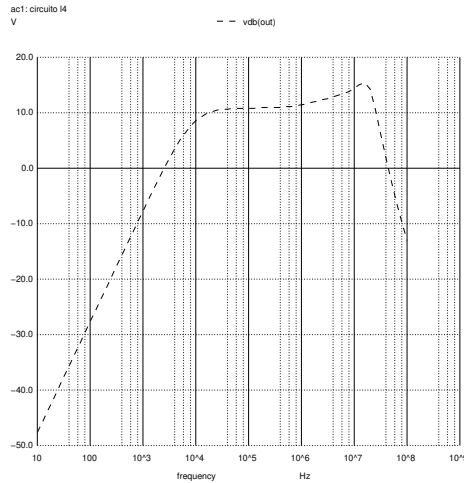
(b)  $C_i$  high ( $1F$ )

Figure 2:  $C_{in}$  influence

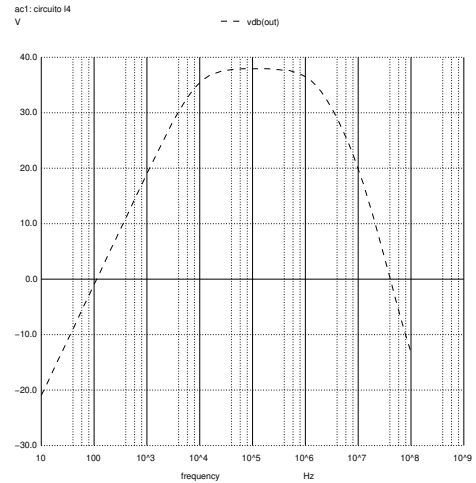
We can see that the increase of the capacitance pushes the cut-off frequency to the left and, without altering the higher cut-off frequency, anticipating it, which generates a larger bandwidth. As discussed previously, as  $\omega \rightarrow 0$ ,  $Z(C_{in}) \rightarrow \infty$ , this is not surprising, so this capacitor prevents the transistor from entering the cut-off regions or the saturation, by blocking the DC component of the Audio In source. This helps the transistor operate at lower frequencies by maintaining the OP of the transistor, as  $C_{in}$  increases.

## 2.4.2 Bypass Capacitor

The two figures of the frequency response analysis, by changing the parameter  $C_E$ , are presented below.



(a) Low  $C_E$  effect on Gain ( $1nF$ )



(b) High  $C_E$  effect on Gain ( $1F$ )

Figure 3:  $C_E$  influence

Due to the placement of the bypass capacitor in parallel with  $R_E$ , this resistor becomes short for high and medium frequencies. The amplifier's first stage gain being inversely dependent on this resistance leads to the bypass capacitor playing an extremely important role in maximizing the gain for high and medium frequencies.



### 2.4.3 $R_C$

To conclude, we need to analyse the role of  $R_C$  on the total gain of the circuit. We also present asymptotical situations in order to fully understand that behaviour.

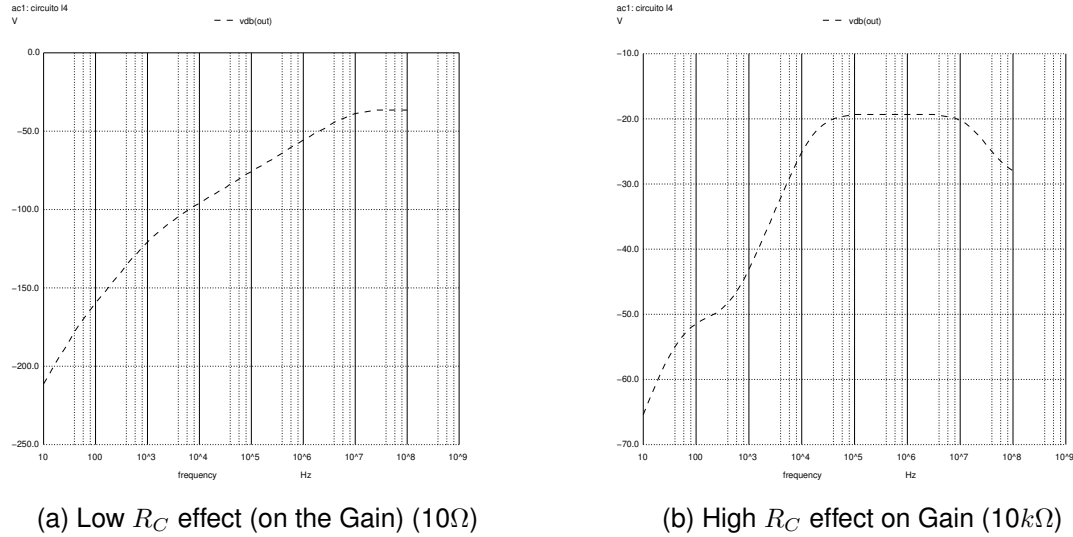


Figure 4:  $R_C$  influence (on the Gain)

We can see that the gain increases with  $R_C$  and also anticipates the passband. This behaviour matches the predictions given by the theoretical analysis on the gain, due to being proportional to  $R_C$ .

To guarantee a high compatibility with speakers and AUDIO IN, we simulate the input and output impedances of the circuit. The good compatibility is guaranteed with a high input impedance,  $Z_I$ , and a low output impedance,  $Z_O$ . The results are presented in the tables below.

Name	Value [ $\Omega$ ]
Input Imp	$-1233.51 + 277.892j$
Absolute Value	1264.42

Table 9: Simulation Input Impedance

Name	Value [ $\Omega$ ]
Output Imp	$21.808 + 0.737357j$
Absolute value	21.8204

Table 10: Simulation Output Impedance

In similarity with the theoretical analysis, the simulation gives off a slightly high output impedance. This is due to the compromises needed for the merit system.

## 2.5 Comparison

We are now going to compare theoretical and simulation values.

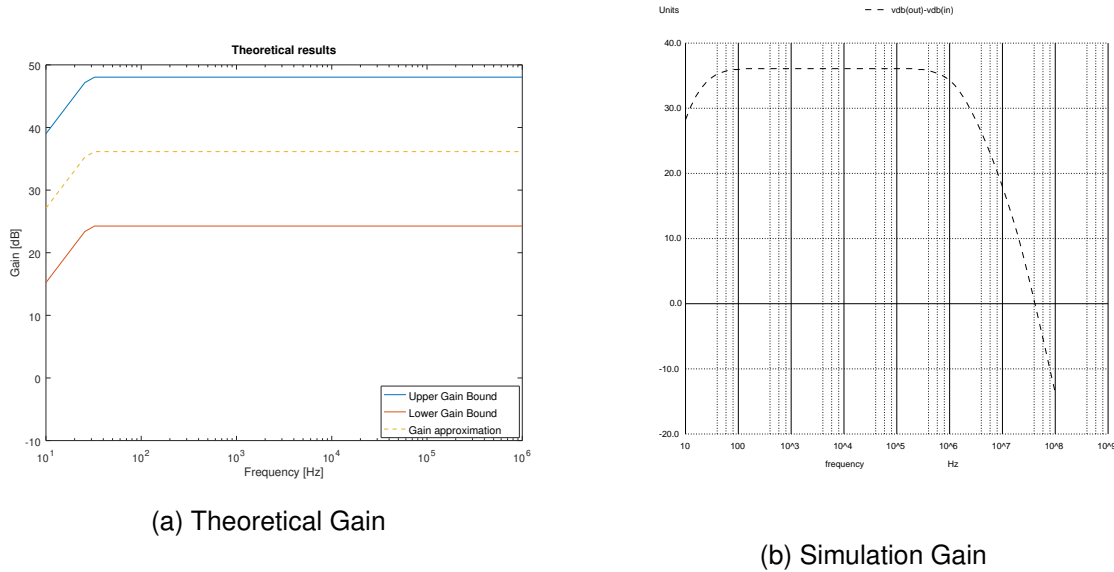


Figure 5: Gain

Above we can see theoretical and simulation graphs of the gain.

In this case, the comparison of the shape can only be done on the left side, since we don't have the theoretical higher cut-off frequency. For this reason, there's no point in plotting the theoretical gain any further than  $1MHz$ .

The theoretical analysis takes in account that all capacitors are short-circuted or open-circuted, leading to two different plots one in blue and the other one in orange, respectively. This leaves us with a region of acceptance for the simulation gain, that fits in this region for the interval in study. The yellow plot is the average gain, wich should be a better approximation of the real gain. Considering both graphs we can also comment on their similar shape that confirms the match of our theoretical aproach. Looking back on the studied values of each the theoretical and the simulation analysis ( $Z_I$  and  $Z_O$ ,  $A_v$  and  $f_{CO_L}$ ), we can confirm that they have the similar orders of magnitude, wich gives us an aproximation within reason.

## 3 Merit Results

From the results obtained through the Ngspice simulation (see Section 2.5) and considering we used the data shown in Section 1, we can compute the price and the merit using the *formulae* given in the lab assignment:

Name	Value
price	2242.01
merit	1965.72

Table 11: Total Price and Merit

For our strategy, we opted to firstly understand what each component would produce when its values changed dramatically . So we analysed the circuit *asymptotically* in order to acquire a bigger picture of the influence of each component.

After understanding that, we then made small adjustments to further perfect our results, which in turn made the merit figure rise. In this approach, we left the cost as a second thought.

To conclude, we began decreasing the cost until we found out the perfect compromise for us, giving the results shown in table 11.

## 4 Final Conclusion and General Notes

As a conclusion, we can state that, alike the previous lab assignment, there is not a major degree of similarity between both analysis, in terms of precision. This was expected due to the fact that the circuit is non-linear and the model used by *Ngspice* is far more complex than the theoretical model used - the Incremental Analysis one, presented on classes, only includes 2 resistors and a dependent current source. Despite these differences, as previously discussed, the theoretical model gives an overview of the behaviour, so it is useful when we don't have any simulation tools available or even to quickly verify the simulation results obtained.

With all this in mind, this laboratory enabled us to deepen our knowledge regarding BJTs and how they can be implemented to develop circuits with various purposes - in our case, an AUDIO Amplifier, even though the real model amplifiers are far more complex than the circuit implemented, achieving gains of around 115 dB. Besides, we used new concepts such as the *Time constant method*, the incremental models, the input and output impedances and the gain (these, even though already familiar, allowed us to gain flexibility and easiness).

Regarding our results, especially the simulation ones, the main goal was to have a high gain and a large enough bandwidth that would cover at least 20Hz to 20kHz, since this is the human hearing range. We can state that we obtained results that more than cover said range and would be suitable for a real audio amplifier. Given that, one possible improvement to our circuit would be to increase the gain even more, which we were not able to do.