Time Series Analysis

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Importing the required bibs for work

```
library(tseries)
## Registered S3 method overwritten by 'quantmod':
##
    as.zoo.data.frame zoo
require(urca)
## Loading required package: urca
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.6 v purr 0.3.4

## v tibble 3.1.7 v dplyr 1.0.9

## v tidyr 1.2.0 v stringr 1.4.0

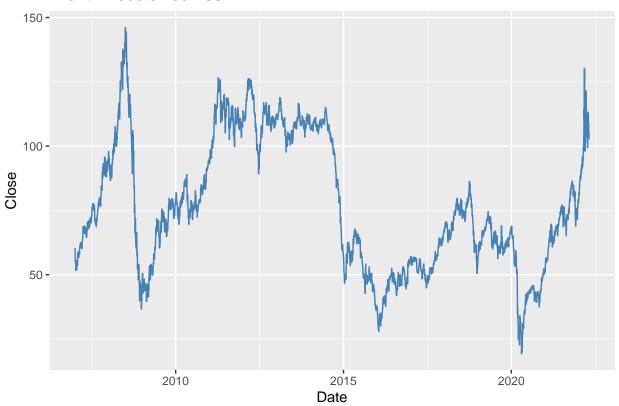
## v readr 2.1.2 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(fpp2)
## -- Attaching packages ------ fpp2 2.4 --
## v forecast 8.16 v expsmooth 2.3
## v fma
             2.4
##
library(vars)
## Loading required package: MASS
```

```
##
## Attaching package: 'MASS'
## The following objects are masked from 'package:fma':
##
##
       cement, housing, petrol
## The following object is masked from 'package:dplyr':
##
##
       select
## Loading required package: strucchange
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Attaching package: 'strucchange'
## The following object is masked from 'package:stringr':
##
##
       boundary
## Loading required package: lmtest
library(forecast)
require(lmtest)
library(readxl)
suppressWarnings(expr)
## function (expr)
## {
##
       enexpr(expr)
## }
## <bytecode: 0x7fe22e040508>
## <environment: namespace:rlang>
Importing the data
brent_prices <- read_xlsx("brent_prices.xlsx")</pre>
Petr4_prices <- read_xlsx("Petr4_prices.xlsx")</pre>
```

Brent Oil Prices Graph

```
ggplot(brent_prices, aes(x=Date)) +
  geom_line(aes(y = Close), color = "steelblue") +
  labs(title = 'Brent Prices since 2007')
```

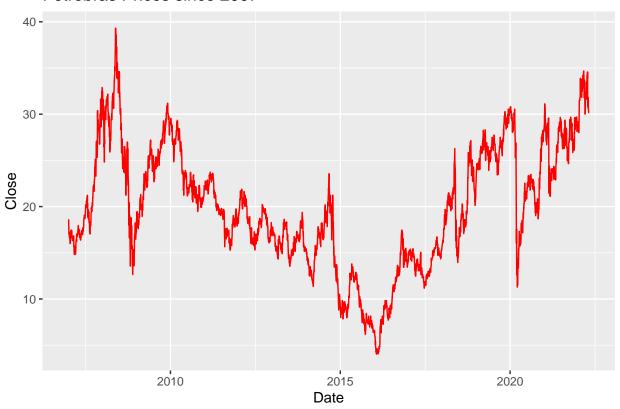
Brent Prices since 2007



Petrobrás stock prices graph

```
ggplot(Petr4_prices, aes(x=Date)) +
  geom_line(aes(y = `Close`), color = "red") +
  labs(title = 'Petrobras Prices since 2007')
```

Petrobras Prices since 2007



Managing the data

```
final_data <- merge(Petr4_prices, brent_prices, by = 'Date')
names(final_data) <- c('Date', 'Petrobras', 'Brent Oil Prices')
normalized_final_data <- data_frame(final_data$Date,final_data[,2] / final_data[1,2],final_data[,3]/fin

## Warning: 'data_frame()' was deprecated in tibble 1.1.0.

## Please use 'tibble()' instead.

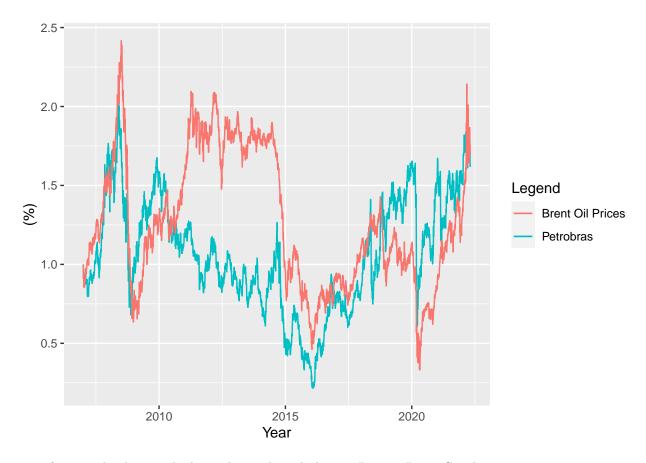
## This warning is displayed once every 8 hours.

## Call 'lifecycle::last_lifecycle_warnings()' to see where this warning was generated.

names(normalized_final_data) <- c('Date', 'Petrobras', 'Brent Oil Prices')</pre>
```

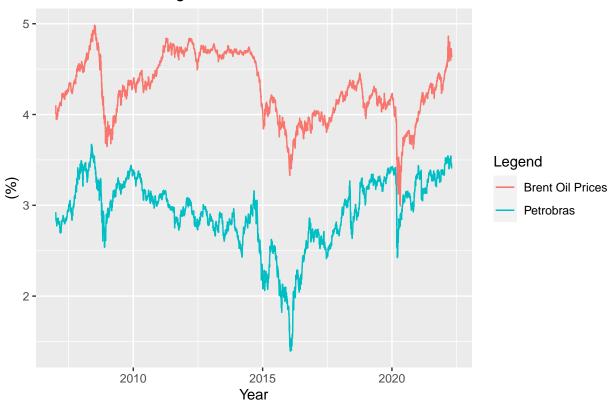
Brent x Petrobrás Graph in normalized scale

```
ggplot(normalized_final_data, aes(x = Date)) +
  geom_line(aes(y = Petrobras, color = "Petrobras")) +
  geom_line(aes(y = `Brent Oil Prices`, color = "Brent Oil Prices")) +
  labs(x = "Year",
      y = "(%)",
      color = "Legend")
```



Transforming the data to the logarithm scale and plotting Petr4 x Brent Graph

PETR4 x Brent Logarithm



Augmented dickey fuller test for Brent Prices

```
adf_test_brent <- ur.df(log_data$`Brent Oil Prices`,selectlags = "BIC")
summary(adf_test_brent)</pre>
```

```
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression none
##
##
## Call:
## lm(formula = z.diff \sim z.lag.1 - 1 + z.diff.lag)
##
## Residuals:
##
                     Median
       Min
                1Q
                                        Max
##
  -0.277534 -0.010297 0.000714 0.010998 0.192156
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## z.lag.1
            2.063e-05 9.136e-05
                               0.226
                                       0.821
                                       0.291
## z.diff.lag -1.718e-02 1.627e-02 -1.056
## Residual standard error: 0.02415 on 3778 degrees of freedom
```

```
## Multiple R-squared: 0.0003075, Adjusted R-squared: -0.0002218
## F-statistic: 0.581 on 2 and 3778 DF, p-value: 0.5594
##
##
## Value of test-statistic is: 0.2258
##
## Critical values for test statistics:
        1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
Augmented dickey fuller test for Brent Prices with drift
adf_test_brent <- ur.df(log_data$`Brent Oil Prices`,type="drift",selectlags = "BIC")</pre>
summary(adf_test_brent)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression drift
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + z.diff.lag)
## Residuals:
                  10
                        Median
## -0.278572 -0.010430 0.000732 0.011012 0.189506
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.009944
                        0.004846
                                  2.052
                                          0.0402 *
## z.lag.1
             -0.002284
                         0.001127 -2.027
                                          0.0427 *
## z.diff.lag -0.015984
                         0.016269 -0.982
                                          0.3259
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.02414 on 3777 degrees of freedom
## Multiple R-squared: 0.001382,
                                 Adjusted R-squared: 0.0008529
## F-statistic: 2.613 on 2 and 3777 DF, p-value: 0.07345
##
## Value of test-statistic is: -2.027 2.1311
## Critical values for test statistics:
        1pct 5pct 10pct
## tau2 -3.43 -2.86 -2.57
## phi1 6.43 4.59 3.78
```

Augmented dickey fuller test for Brent Prices with trend

```
adf_test_brent <- ur.df(log_data$`Brent Oil Prices`,type="trend",selectlags = "BIC")
summary(adf_test_brent)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression trend
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + tt + z.diff.lag)
## Residuals:
##
       Min
                 1Q
                      Median
                                  30
## -0.278335 -0.010410 0.000744 0.011055 0.189507
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.188e-02 5.583e-03
                                2.128
                                        0.0334 *
            -2.616e-03 1.223e-03 -2.139
                                        0.0325 *
## z.lag.1
            -2.731e-07 3.905e-07 -0.699
                                        0.4844
## z.diff.lag -1.576e-02 1.627e-02 -0.969
                                        0.3328
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.02414 on 3776 degrees of freedom
## Multiple R-squared: 0.001511, Adjusted R-squared: 0.0007177
## F-statistic: 1.905 on 3 and 3776 DF, p-value: 0.1266
##
## Value of test-statistic is: -2.1394 1.5836 2.2987
##
## Critical values for test statistics:
       1pct 5pct 10pct
##
## tau3 -3.96 -3.41 -3.12
## phi2 6.09 4.68 4.03
## phi3 8.27 6.25 5.34
Augmented dickey fuller test for Petrobrás stock prices
adf_test_petr <- ur.df(log_data$Petrobras,type="none", selectlags = "BIC")
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
## Test regression none
```

##

```
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
                                        Max
## -0.35544 -0.01446 0.00077 0.01486 0.19378
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## z.lag.1
             1.575e-06 1.638e-04
                                 0.010
                                          0.9923
## z.diff.lag -3.002e-02 1.626e-02 -1.846
                                          0.0649 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02972 on 3778 degrees of freedom
## Multiple R-squared: 0.0009016, Adjusted R-squared: 0.0003727
## F-statistic: 1.705 on 2 and 3778 DF, p-value: 0.182
##
##
## Value of test-statistic is: 0.0096
## Critical values for test statistics:
        1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
Augmented dickey fuller test for Petrobrás stock prices with drift
adf_test_petr <- ur.df(log_data$Petrobras,type="drift", selectlags = "BIC")
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression drift
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + z.diff.lag)
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
## -0.35487 -0.01459 0.00065 0.01476 0.19289
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.008233
                        0.003760
                                  2.189
                                          0.0286 *
## z.lag.1
             -0.002764
                         0.001274 - 2.170
                                          0.0301 *
## z.diff.lag -0.028561
                         0.016266 -1.756
                                          0.0792 .
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

```
##
## Residual standard error: 0.0297 on 3777 degrees of freedom
## Multiple R-squared: 0.002147, Adjusted R-squared: 0.001618
## F-statistic: 4.063 on 2 and 3777 DF, p-value: 0.01727
##
## Value of test-statistic is: -2.1699 2.3964
##
## Critical values for test statistics:
        1pct 5pct 10pct
## tau2 -3.43 -2.86 -2.57
## phi1 6.43 4.59 3.78
Augmented dickey fuller test for Petrobrás stock prices with trend
adf_test_petr <- ur.df(log_data$Petrobras,type="trend", selectlags = "BIC")
summary(adf_test_petr)
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression trend
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + tt + z.diff.lag)
##
## Residuals:
       Min
                1Q Median
                                 3Q
## -0.35511 -0.01455 0.00066 0.01472 0.19265
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 7.882e-03 3.874e-03 2.035
                                          0.0419 *
## z.lag.1
            -2.753e-03 1.275e-03 -2.160
                                          0.0308 *
             1.674e-07 4.429e-07 0.378
                                          0.7055
## z.diff.lag -2.861e-02 1.627e-02 -1.759
                                          0.0787 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02971 on 3776 degrees of freedom
## Multiple R-squared: 0.002185, Adjusted R-squared: 0.001392
## F-statistic: 2.756 on 3 and 3776 DF, p-value: 0.04095
##
## Value of test-statistic is: -2.1599 1.6449 2.425
## Critical values for test statistics:
        1pct 5pct 10pct
##
## tau3 -3.96 -3.41 -3.12
## phi2 6.09 4.68 4.03
## phi3 8.27 6.25 5.34
```

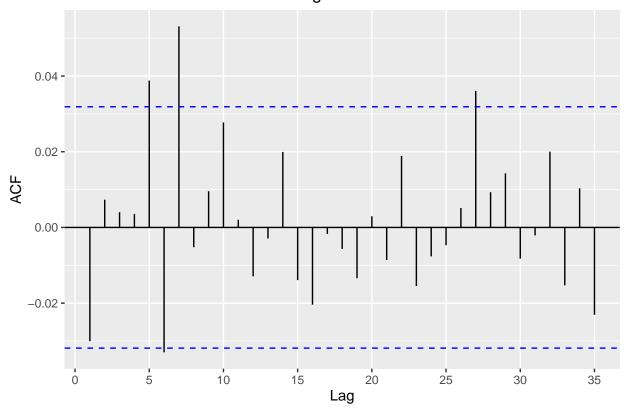
Log Returns for the data

```
log_ret_petr <- diff(log_data$Petrobras)
log_ret_brent <- diff(log_data$`Brent Oil Prices`)</pre>
```

ACF, PACF and series of returns for Petrobras

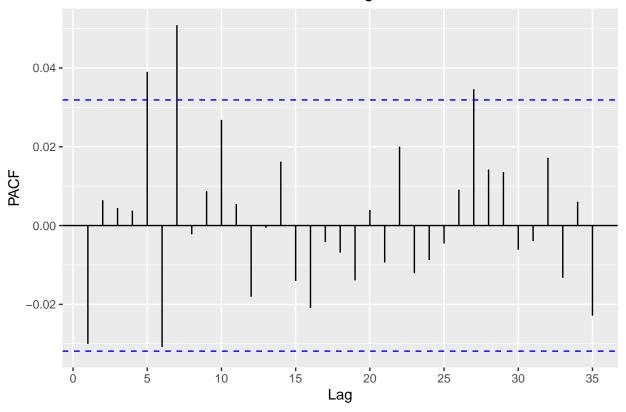
```
ggAcf(log_ret_petr) + labs(title = "AutoCorrelation for Petrobras Log Diff")
```

AutoCorrelation for Petrobras Log Diff

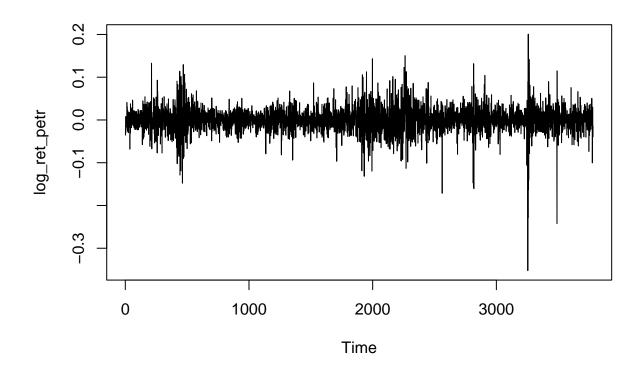


ggPacf(log_ret_petr) + labs(title = "Partial AutoCorrelation for Petrobras Log Diff")

Partial AutoCorrelation for Petrobras Log Diff



```
ts.plot(log_ret_petr) %>%
  labs(title = "Log of returns for Petrobras")
```

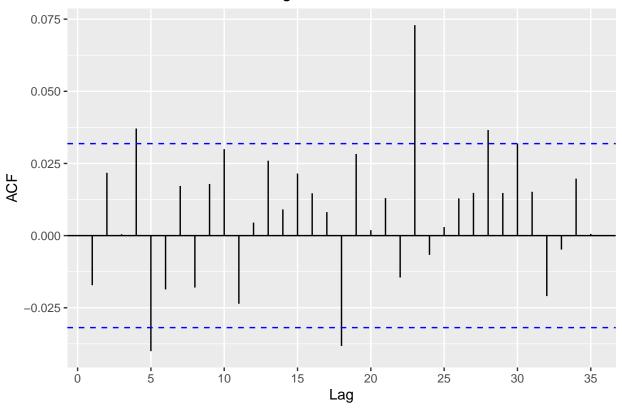


```
## [[1]]
## NULL
##
## $title
## [1] "Log of returns for Petrobras"
##
## attr(,"class")
## [1] "labels"
```

ACF, PACF and series of returns for Petrobras

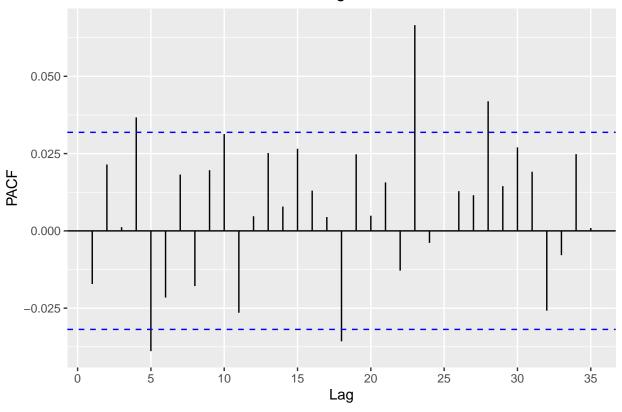
```
log_ret_brent <- diff(log_data$`Brent Oil Prices`)
ggAcf(log_ret_brent) + labs(title = "AutoCorrelation for Brent Log Diff")</pre>
```

AutoCorrelation for Brent Log Diff

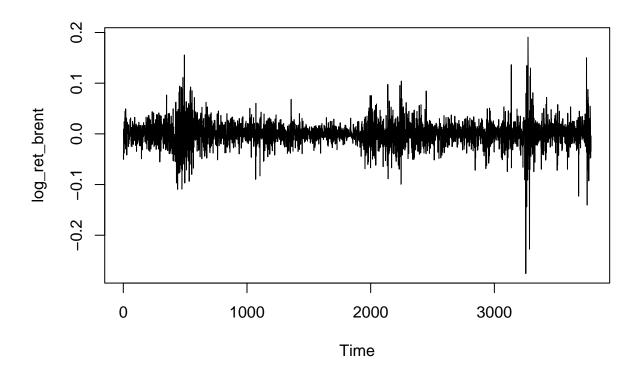


ggPacf(log_ret_brent) + labs(title = "Partial AutoCorrelation for Brent Log Diff")

Partial AutoCorrelation for Brent Log Diff



```
ts.plot(log_ret_brent) %>%
labs(title = "Log of returns for Brent Oil Prices")
```



```
## [[1]]
## NULL
##
## $title
## [1] "Log of returns for Brent Oil Prices"
##
## attr(,"class")
## [1] "labels"
```

After the transformation of data, we need to test the new data (log return scaled) for stationarity. Augmented dickey fuller test for Petrobrás stock prices with drift

```
adf_test_petr <- ur.df(log_ret_petr,type="drift", selectlags = "BIC")
summary(adf_test_petr)</pre>
```

```
## lm(formula = z.diff ~ z.lag.1 + 1 + z.diff.lag)
##
## Residuals:
##
       Min
                    Median
                1Q
                                 3Q
                                         Max
## -0.35520 -0.01451 0.00063 0.01472 0.19428
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.0001457 0.0004835
                                   0.301
                                            0.763
                                            <2e-16 ***
## z.lag.1
             -1.0236688 0.0233588 -43.824
## z.diff.lag -0.0064274 0.0162734 -0.395
                                            0.693
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.02972 on 3776 degrees of freedom
## Multiple R-squared: 0.5152, Adjusted R-squared: 0.5149
## F-statistic: 2006 on 2 and 3776 DF, p-value: < 2.2e-16
##
##
## Value of test-statistic is: -43.8237 960.2569
##
## Critical values for test statistics:
        1pct 5pct 10pct
##
## tau2 -3.43 -2.86 -2.57
## phi1 6.43 4.59 3.78
Augmented dickey fuller test for Petrobrás stock prices with trend
adf_test_petr <- ur.df(log_ret_petr,type="trend", selectlags = "BIC")</pre>
summary(adf_test_petr)
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression trend
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + tt + z.diff.lag)
##
## Residuals:
##
       Min
                1Q
                    Median
                                 3Q
## -0.35545 -0.01456 0.00062 0.01472 0.19402
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.937e-04 9.677e-04 -0.200
                                            0.841
## z.lag.1
             -1.024e+00 2.336e-02 -43.821
                                           <2e-16 ***
              1.795e-07 4.433e-07
                                    0.405
                                            0.686
## z.diff.lag -6.372e-03 1.628e-02 -0.392
                                            0.695
## ---
```

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02972 on 3775 degrees of freedom
## Multiple R-squared: 0.5152, Adjusted R-squared: 0.5148
## F-statistic: 1337 on 3 and 3775 DF, p-value: < 2.2e-16
##
## Value of test-statistic is: -43.8206 640.0842 960.1262
## Critical values for test statistics:
        1pct 5pct 10pct
## tau3 -3.96 -3.41 -3.12
## phi2 6.09 4.68 4.03
## phi3 8.27 6.25 5.34
Augmented dickey fuller test for Petrobrás stock prices
adf_test_petr <- ur.df(log_ret_petr,type="none", selectlags = "BIC")</pre>
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
## Test regression none
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
## Residuals:
                    Median
       Min
                1Q
                                 3Q
                                        Max
## -0.35505 -0.01437 0.00077 0.01486 0.19443
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
            -1.023621
                        0.023355 -43.828
## z.lag.1
## z.diff.lag -0.006451
                        0.016271 -0.396
                                          0.692
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.02972 on 3777 degrees of freedom
## Multiple R-squared: 0.5152, Adjusted R-squared: 0.5149
## F-statistic: 2007 on 2 and 3777 DF, p-value: < 2.2e-16
##
## Value of test-statistic is: -43.8279
##
## Critical values for test statistics:
##
        1pct 5pct 10pct
```

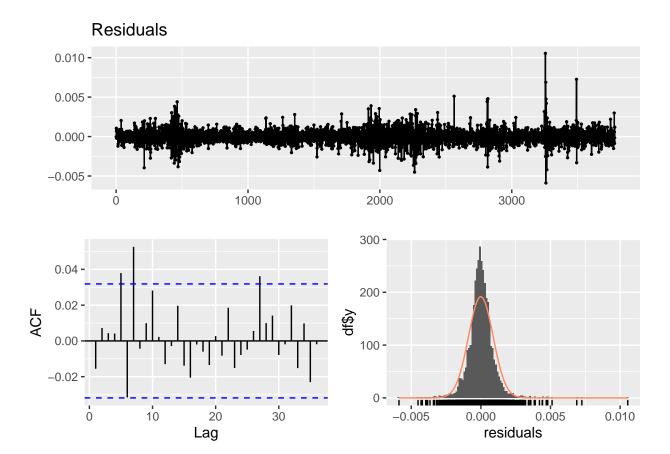
Augmented dickey fuller test for Brent prices with drift

tau1 -2.58 -1.95 -1.62

```
adf_test_petr <- ur.df(log_ret_brent,type="drift", selectlags = "BIC")</pre>
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression drift
##
## Call:
## lm(formula = z.diff ~ z.lag.1 + 1 + z.diff.lag)
## Residuals:
##
       Min
                1Q
                     Median
## -0.277196 -0.010377 0.000572 0.010925 0.192128
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.0001641 0.0003927
                                0.418
                                        0.676
## z.lag.1
            <2e-16 ***
## z.diff.lag -0.0214655 0.0162584 -1.320
                                        0.187
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.02414 on 3776 degrees of freedom
## Multiple R-squared: 0.5095, Adjusted R-squared: 0.5092
## F-statistic: 1961 on 2 and 3776 DF, p-value: < 2.2e-16
##
##
## Value of test-statistic is: -42.9529 922.477
## Critical values for test statistics:
       1pct 5pct 10pct
## tau2 -3.43 -2.86 -2.57
## phi1 6.43 4.59 3.78
Augmented dickey fuller test for Brent prices with trend
adf_test_petr <- ur.df(log_ret_brent,type="trend", selectlags = "BIC")
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression trend
##
##
## Call:
```

```
## lm(formula = z.diff ~ z.lag.1 + 1 + tt + z.diff.lag)
##
## Residuals:
##
                        Median
        Min
                  1Q
                                     3Q
                                             Max
## -0.277234 -0.010379 0.000589 0.010915 0.192090
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 1.114e-04 7.859e-04
                                   0.142
                                            0.887
             -9.963e-01 2.320e-02 -42.947
## z.lag.1
                                            <2e-16 ***
## tt
              2.791e-08 3.600e-07
                                    0.078
                                            0.938
## z.diff.lag -2.146e-02 1.626e-02 -1.320
                                            0.187
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.02414 on 3775 degrees of freedom
## Multiple R-squared: 0.5095, Adjusted R-squared: 0.5091
## F-statistic: 1307 on 3 and 3775 DF, p-value: < 2.2e-16
##
##
## Value of test-statistic is: -42.9471 614.8248 922.2369
## Critical values for test statistics:
        1pct 5pct 10pct
##
## tau3 -3.96 -3.41 -3.12
## phi2 6.09 4.68 4.03
## phi3 8.27 6.25 5.34
Augmented dickey fuller test for Brent prices
adf_test_petr <- ur.df(log_ret_brent,type="none", selectlags = "BIC")</pre>
summary(adf_test_petr)
##
## # Augmented Dickey-Fuller Test Unit Root Test #
##
## Test regression none
##
##
## Call:
## lm(formula = z.diff ~ z.lag.1 - 1 + z.diff.lag)
##
## Residuals:
##
                        Median
        Min
                  1Q
## -0.277026 -0.010214 0.000735 0.011092 0.192289
##
## Coefficients:
##
            Estimate Std. Error t value Pr(>|t|)
            -0.99623
                        0.02319 -42.956
## z.lag.1
                                         <2e-16 ***
## z.diff.lag -0.02151
                        0.01626 -1.323
                                         0.186
## ---
```

```
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 0.02414 on 3777 degrees of freedom
## Multiple R-squared: 0.5094, Adjusted R-squared: 0.5092
## F-statistic: 1961 on 2 and 3777 DF, p-value: < 2.2e-16
##
##
## Value of test-statistic is: -42.9556
## Critical values for test statistics:
        1pct 5pct 10pct
## tau1 -2.58 -1.95 -1.62
Specifying ARIMA model for log returns of Petrobras
petr_model <- arima(log_ret_petr, order=c(1,0,1), include.mean = FALSE, method = "ML")</pre>
summary(petr_model)
##
## Call:
## arima(x = log_ret_petr, order = c(1, 0, 1), include.mean = FALSE, method = "ML")
## Coefficients:
##
             ar1
                      ma1
        -0.0152 -0.0146
##
         0.4903
                  0.4868
## s.e.
##
## sigma^2 estimated as 0.0008827: log likelihood = 7929.89, aic = -15853.77
##
## Training set error measures:
                                               MAE MPE MAPE
##
                                   RMSE
                                                                 MASE
## Training set 0.0001310876 0.02971103 0.02052066 NaN Inf 0.6882743
                         ACF1
## Training set -4.157921e-05
coeftest(petr_model)
##
## z test of coefficients:
##
       Estimate Std. Error z value Pr(>|z|)
## ar1 -0.015218  0.490292 -0.031  0.9752
## ma1 -0.014590
                 0.486827 -0.030 0.9761
checkresiduals(fitted(petr_model))
## Warning in modeldf.default(object): Could not find appropriate degrees of
## freedom for this model.
```



Specifying ARIMA model for log returns of Brent

```
brent_model <- arima(log_ret_brent, order=c(2,0,0), include.mean = FALSE, method = "ML")
summary(brent_model)</pre>
```

```
##
## Call:
  arima(x = log_ret_brent, order = c(2, 0, 0), include.mean = FALSE, method = "ML")
##
##
##
  Coefficients:
##
             ar1
                     ar2
##
         -0.0168
                  0.0215
## s.e.
                  0.0163
          0.0163
##
## sigma^2 estimated as 0.0005831: log likelihood = 8713.72, aic = -17421.44
##
## Training set error measures:
                                   RMSE
                                               MAE MPE MAPE
##
## Training set 0.0001392721 0.02414819 0.01613219 NaN Inf 0.6792112
## Training set -7.694423e-05
```

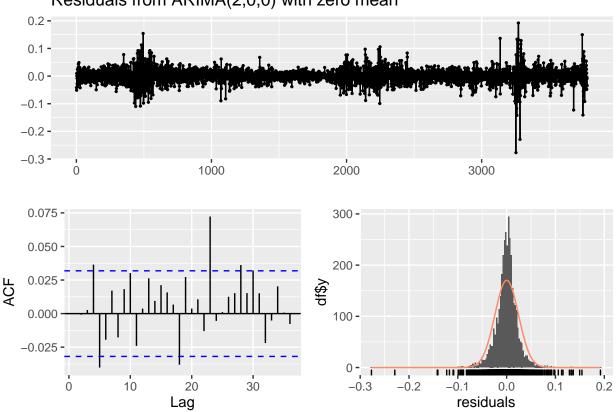
##

coeftest(brent_model)

```
## z test of coefficients:
##
## Estimate Std. Error z value Pr(>|z|)
## ar1 -0.016759   0.016268 -1.0302   0.3029
## ar2   0.021542   0.016275   1.3236   0.1856
```

checkresiduals((brent_model))

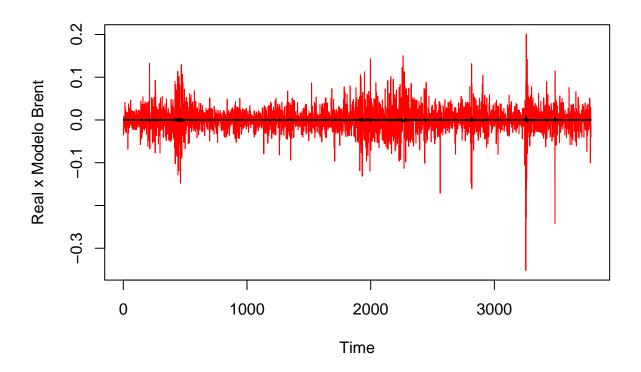
Residuals from ARIMA(2,0,0) with zero mean



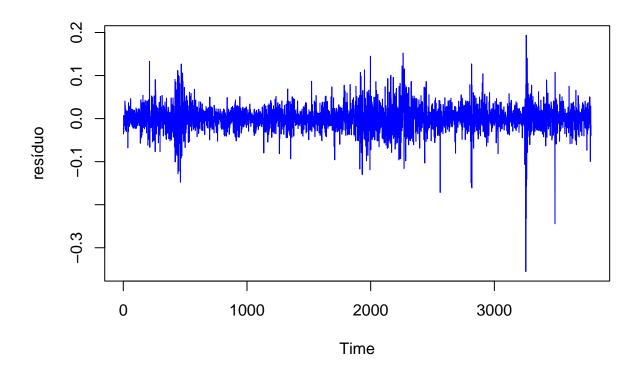
```
##
## Ljung-Box test
##
## data: Residuals from ARIMA(2,0,0) with zero mean
## Q* = 19.619, df = 8, p-value = 0.01188
##
## Model df: 2. Total lags used: 10
```

Real time series x Fitted Values for the model specified for Petrobras

```
ts.plot(log_ret_petr, fitted(petr_model), col=c("red", "black"), ylab = "Real x Modelo Brent")
```

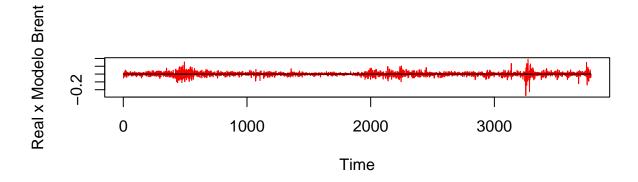


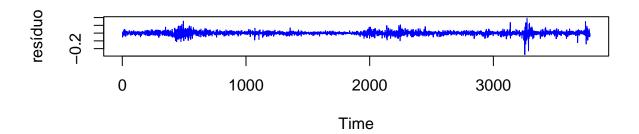
ts.plot(residuals(petr_model), col="blue", ylab="residuo")



Real time series **x** Fitted Values for the model specified for Brent

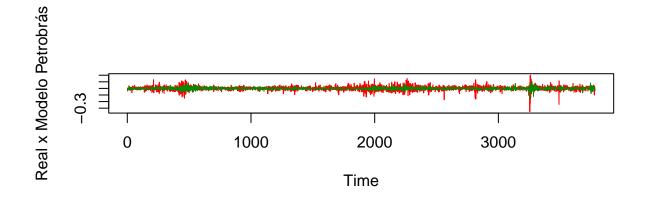
```
par(mfrow = c(2,1))
ts.plot(log_ret_brent, fitted(brent_model), col=c("red", "black"), ylab = "Real x Modelo Brent")
ts.plot(residuals(brent_model), col="blue", ylab="residuo")
```

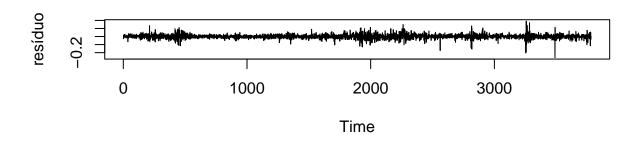




Specifying and model to predict Petrobras prices with Brent Prices

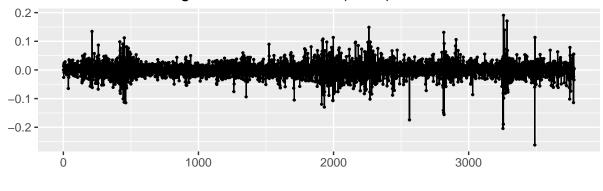
```
par(mfrow=c(2,1))
model_arimax <- Arima(log_ret_petr, order = c(0,1,1), xreg =log_ret_brent, include.constant = FALSE)
ts.plot(log_ret_petr, fitted(model_arimax), col=c("red", "green4"), ylab = "Real x Modelo Petrobrás")
ts.plot(residuals(model_arimax), col="black", ylab="resíduo")</pre>
```

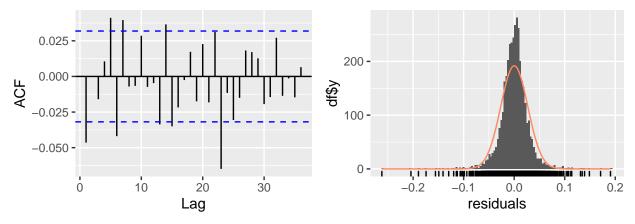




checkresiduals(model_arimax)

Residuals from Regression with ARIMA(0,1,1) errors



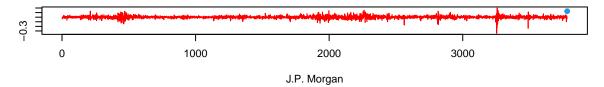


```
##
## Ljung-Box test
##
## data: Residuals from Regression with ARIMA(0,1,1) errors
## Q* = 31.989, df = 8, p-value = 9.356e-05
##
## Model df: 2. Total lags used: 10
```

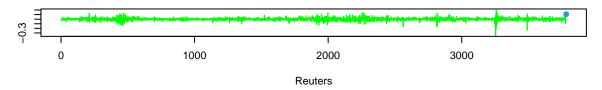
For the forecast produce, we gonna get the J.P Morgan, Reuters and Barclays forecasts for Brent Oil prices for 2022. The information are available at the following links:

- J.P Morgan: 'https://www.thestreet.com/investing/oil-will-hit-125-a-barrel-in-2022-150-in-2023-jpmorgan'
- \bullet Reuters: 'https://www.reuters.com/business/energy/oil-prices-drop-demand-worries-rising-supplies-2021-11-16/'
- $\bullet \ \, \text{Barclays:} \ \, \text{`https://boereport.com/} 2022/01/24/\text{barclays-hikes-2022-oil-price-view-by-5-bbl-on-depressed-inventories/'}$

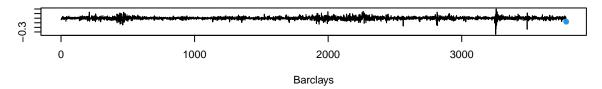
Forecasts from Regression with ARIMA(0,1,1) errors



Forecasts from Regression with ARIMA(0,1,1) errors



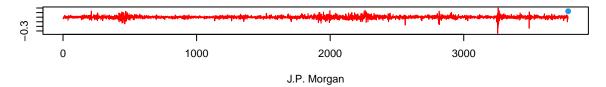
Forecasts from Regression with ARIMA(0,1,1) errors



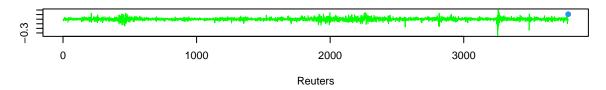
Since Brazil is going throught an election year, we decide to add a auto-regressive component, since the PETR4 stock price can pass to depend to previous values.

```
par(mfrow=c(3,1))
plot(jpm_forecast_elections, col = c("red"), xlab = "J.P. Morgan")
plot(reuters_forecast_elections, col = c("green"), xlab = 'Reuters')
plot(barclays_forecast_elections, xlab = "Barclays")
```

Forecasts from Regression with ARIMA(0,1,2) errors



Forecasts from Regression with ARIMA(0,1,2) errors



Forecasts from Regression with ARIMA(0,1,2) errors

