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 $http://www.math.berkeley.edu/\sim mgu/MA170Spring2020$ 

## Math170 Term Project Mathematical Methods for Optimization

There is an interactive canonical LP solver you can download from the class becourses site. It automatically generates a random LP with a basic feasible solution for the given numbers of constraints and variables, and then solves it. Modify this code so it can solve any given canonical LP with the **Phase I** and **Phase II** solution process.

There are two parts to this project.

1. You should turn in a .m file LPxxx.m which contains a matlab function of the form

function [data, info] = LPxxx(A,b,c)

to solve a given canonical LP. Here xxx is your student id. On output (case sensitive):

- If info.run = Failure, then
  - info.msg: Explain where and how the failure occured
     (in Phase I or Phase II, failure due to arithmetic exceptions or degeneracy)
- If info.run = Success
  - info.case = 1, 2, 3, for LP feasible with optimal solution, LP feasible without optimal solution, or LP infeasible.
  - Whenever applicable,
    - (a) For **Phase I**:
      - \* data.PhaseI.obj = the optimal objective value
      - \* data.PhaseI.x = optimal primal solution as column vector.
    - (b) For **Phase II**:
      - \* data.PhaseII.Primalobj, data.PhaseII.Dualobj = the optimal objective values
      - \* data.PhaseII.x, data.PhaseII.y, data.PhaseII.z = optimal primal and dual solutions, as column vectors, with  $\mathbf{z} = \mathbf{c} A^T \mathbf{y} \ge \mathbf{0}$ .
      - \* In case 2, data.PhaseII.x and data.PhaseII.t are a basic feasible solution and a search direction in which the object value approaches  $-\infty$  with feasible solution data.PhaseII.x $-\lambda$ \*data.PhaseII.t.
    - (c) info.PhaseI.loop, info.PhaseII.loop should contain numbers of steps in Phase I and Phase II loops.
- 2. Use your code to solve George Stigler's Diet Problem as developed in his paper, accessible on the class becourses site. Take your input data from Table 1 and Table A. Output the optimal diet and associated daily cost.

Due Monday April 13, 2020 on gradescope.