

## Aprendizagem 2024

# **Lab 2: Decision Trees**

### **Practical exercises**

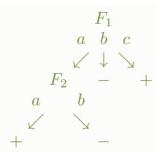
#### I.

# **Decision tree learning**

	У1	<b>У</b> 2	<b>y</b> 3	clas s
<b>X</b> 1	а	а	а	+
<b>X</b> 2	С	b	С	+
<b>X</b> 3	С	а	С	+
<b>X</b> 4	b	а	а	_
<b>X</b> 5	а	b	С	_
<b>X</b> 6	b	b	С	_

Consider the following dataset:

Plot the learned decision tree using information gain (Shannon entropy). Show your calculus.



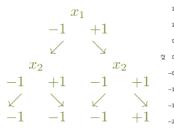
## Brief notes:

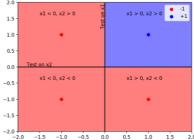
 $\mathbf{y_1}$  provides the highest gain,  $IG(y_{out} \, \Big| \, y_1) = 1 - 0.33$ , hence selected.

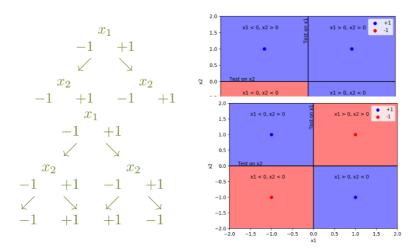
 ${f y_1}$  correctly classifies all observations when  $y_1=b$  and  $y_1=c$  Entropies of  $y_2$  and  $y_3$  for  $(y_1=a)$ -conditional data are both zero, so we can select either.

There is no more uncertainty.

- 1. Show if a decision tree can learn the following logical functions and, if so, plot the corresponding decision boundaries.
  - a) AND
  - b) OR







2. Consider the following testing targets, z, and the corresponding predictions,  $\hat{z}$ , by a decision tree:

$$z = [A A A B B B C C C C]$$

$$\overset{\wedge}{z} = [B B A C B A C A B C]$$

a) Draw the confusion matrix

b) Compute the accuracy and sensitivity/recall per class

$$acccuracy = 0.4, \ sensitivity_A = \frac{1}{3}, \ sensitivity_B = \frac{1}{3}, \ sensitivity_C = \frac{1}{2}$$

c) Considering class C, identify precision and  $F_1$ -measure

$$precision_C = \frac{2}{3}, \ F1_C = 0.57$$

d) Identify the accuracy, sensitivity, and precision of the random classifier

$$accuracy_{random} = 0.(3), \ recall_{random}(A) = 0.(3), \ recall_{random}(B) = 0.(3), \ recall_{random}(C) = 0.(3)$$
 
$$precision_{random}(A) = 0.3, \ precision_{random}(B) = 0.3, \ precision_{random}(C) = 0.4$$

Consider a dataset composed by 374 records, described by 6 variables, and classified according to the decision tree below. Each leaf in the tree shows the label, number of classified records with the label, and total number of observations in the leaf. The positive class is the minority class.

A (66/66) **A** (19/19) A (14/16) -67

a) Compute the confusion matrix.

#
$$A = 66 + 19 + 14 + 15 + 18 = 132$$
 $A (14/16)$ 
 $Y_4$ 
 $A = 66 + 19 + 14 + 15 + 18 = 132$ 
 $A (15/19)$ 
 $A (15/19)$ 
 $A (15/19)$ 

The minority class is A, hence is seen as positive.

		True		
		<b>P</b> (A)	<b>N</b> (B)	
Predicted	<b>P</b> (A)	114	6	
	<b>N</b> (B)	18	236	

b) Compare the accuracy of the given tree versus a pruned tree with only two nodes.

Is there any evidence towards overfitting?

Considering training accuracy: 
$$accuracy_{depth=4} = 0.936$$
,  $accuracy_{depth=2} = 0.874$ 

Without the testing accuracy, there is no sufficient evidence to assume the tree is prone to overfit input data.

c) [optional] Are decision trees learned from high-dimensional data susceptible to underfitting?

Why an ensemble of decision trees minimizes this problem?

Assuming a limited depth, relevant data may be discarded due to a focus on a compact subset of overall input variables. In ensemble models, such as random forests, different decision trees can be learned from data subsamples and subspaces, leading to decisions that consider a broader set of input variables.

# **Programming quests**

5. Following the provided Jupyter notebook on *Classification*, learn and evaluate a decision tree classifier on the breast.w.arff dataset (available at the webpage) using sklearn.

Considering a 80-20 train-test split:

- a) visualize the decision tree learned from the training observations with default parameters
- b) compare the train and test accuracy of decision trees with a varying maximum depth