

## **Jukes-Cantor DNA Evolution**

	$\rightarrow A$	$\to G$	$\to C$	$\to T$	Α —
$\overline{A}$	$1-3\epsilon$	$\epsilon$	$\epsilon$	$\epsilon$	
G	$\epsilon$	$1 - 3\epsilon$ $\epsilon$	$\epsilon$	$\epsilon$	6
C	$\epsilon$	$\epsilon$	$1 - 3\epsilon$	$\epsilon$	C
T	$\epsilon$	$\epsilon$	$\epsilon$	$1 - 3\epsilon$	Т
	I				time

- Probability of mutation is  $O(\varepsilon)$  per generation.
- mutations will appear at rate of once every  $O(1/\epsilon)$  generations.
- Measuring time in units of  $1/\epsilon$  leads to a continuous-time Markov chain.
- In each time step of length  $\varepsilon$ , total probability of a mutation is  $3\varepsilon$ .

$$P = \begin{pmatrix} 1 - 3\epsilon & \epsilon & \epsilon & \epsilon \\ \epsilon & 1 - 3\epsilon & \epsilon & \epsilon \\ \epsilon & \epsilon & 1 - 3\epsilon & \epsilon \\ \epsilon & \epsilon & \epsilon & 1 - 3\epsilon \end{pmatrix} = I + \epsilon \begin{pmatrix} -3 & 1 & 1 & 1 \\ 1 & -3 & 1 & 1 \\ 1 & 1 & -3 & 1 \\ 1 & 1 & 1 & -3 \end{pmatrix}$$