

**UGR | Metaheurística**

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# YIN-YANG-PAIR OPTIMIZATION

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# MOTIVATION

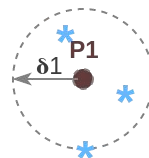
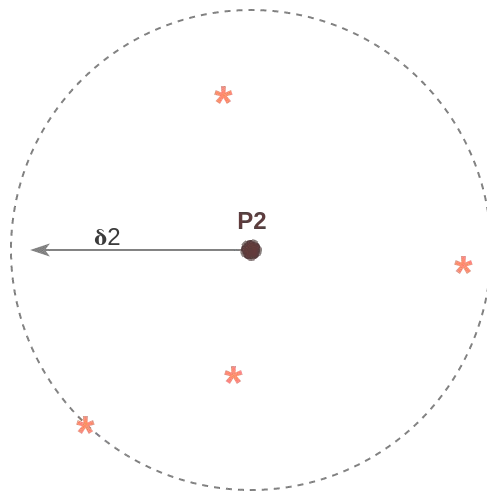
- Exploitation - Exploration **balance**
- Same **navigation** mechanism
- Low **complexity**



## KEY VALUES

$\delta$  - Initial radius

$\alpha$  - Transformation speed



## MAIN FEATURES

### TWO POINTS

P1 exploits  $\longrightarrow$   $\delta_1$  shrinks

P2 explores  $\longrightarrow$   $\delta_2$  grows

### RADII

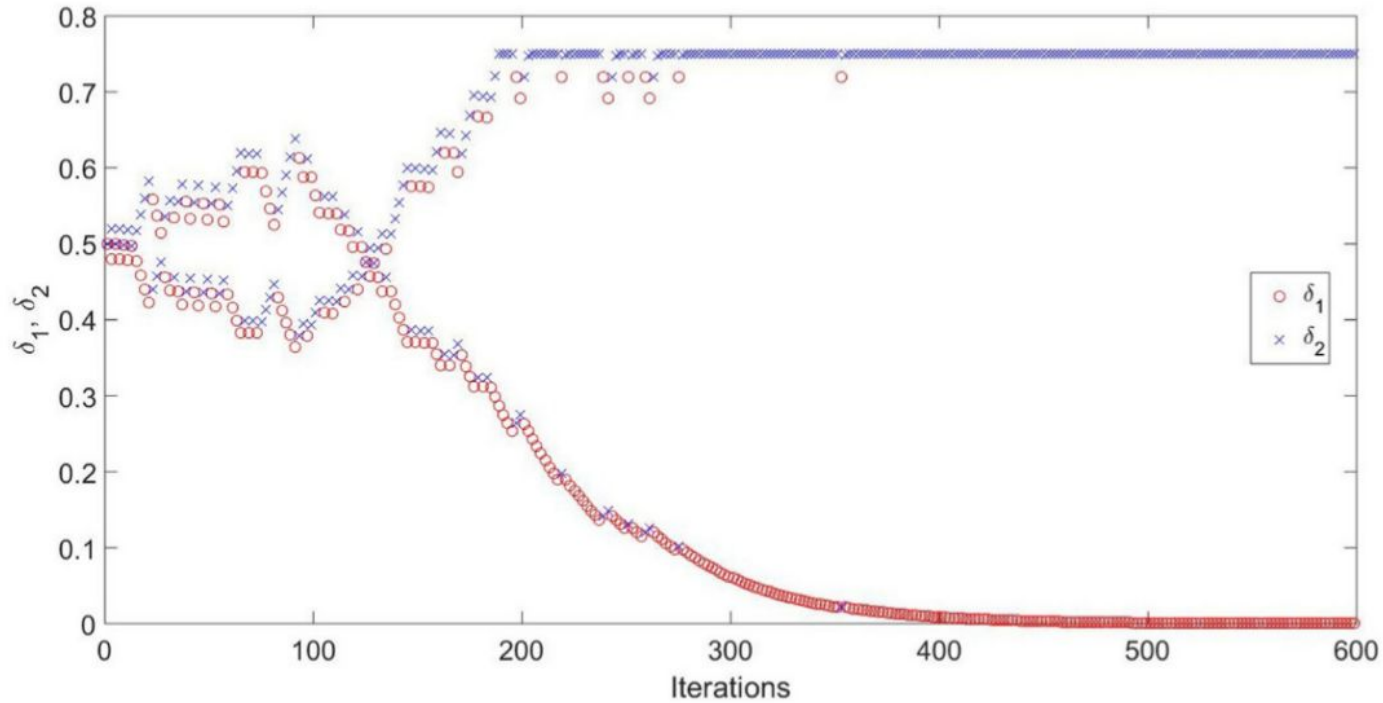
### $\alpha$ FACTOR

$$\delta_1 = d_1 - (d_1/\alpha)$$

$$\delta_2 = d_2 - (d_2/\alpha)$$

If fitter they exchange **positions** and **radius**

# MAIN FEATURES



**Fig. 3.** Variation of  $\delta_1$  and  $\delta_2$  with iterations.

## KEY VALUES

$I$  - Archive stage interval

# MAIN FEATURES

## SPLITTING STAGE

Saves in the archive  
the current solution

Generates 2D new  
solutions for each  
point

Selects the fittest

$I$  iterations

## ARCHIVE STAGE

Selects the two fittest  
solutions from the  
archive (last  $2I$   
points)

Every  $I$  iterations

Reduces  $\delta$

## KEY VALUES

***P*** - Splitting probability (0.5)

# NAVIGATION MECHANISM

## ONE-WAY SPLITTING

Explore the hypersphere in 1 dimension

NP = Matrix 2DxD

$$NP_j^j = P^j + r\delta \quad \text{and}$$

$$NP_{D+j}^j = P^j - r\delta, \quad \text{where } j = 1, 2, 3 \dots D$$

## D-WAY SPLITTING

Explore the hypersphere in several dimensions

B = Matrix 2DxD

$$NP_k^j = P^j + r\left(\delta/\sqrt{2}\right) \quad \text{if } B(k, j) = 1,$$

$$NP_k^j = P^j - r\left(\delta/\sqrt{2}\right) \quad \text{else.}$$

where  $k = 1, 2, 3 \dots 2D$  and  $j = 1, 2, 3 \dots D$

# NAVIGATION MECHANISM

Rastrigin function

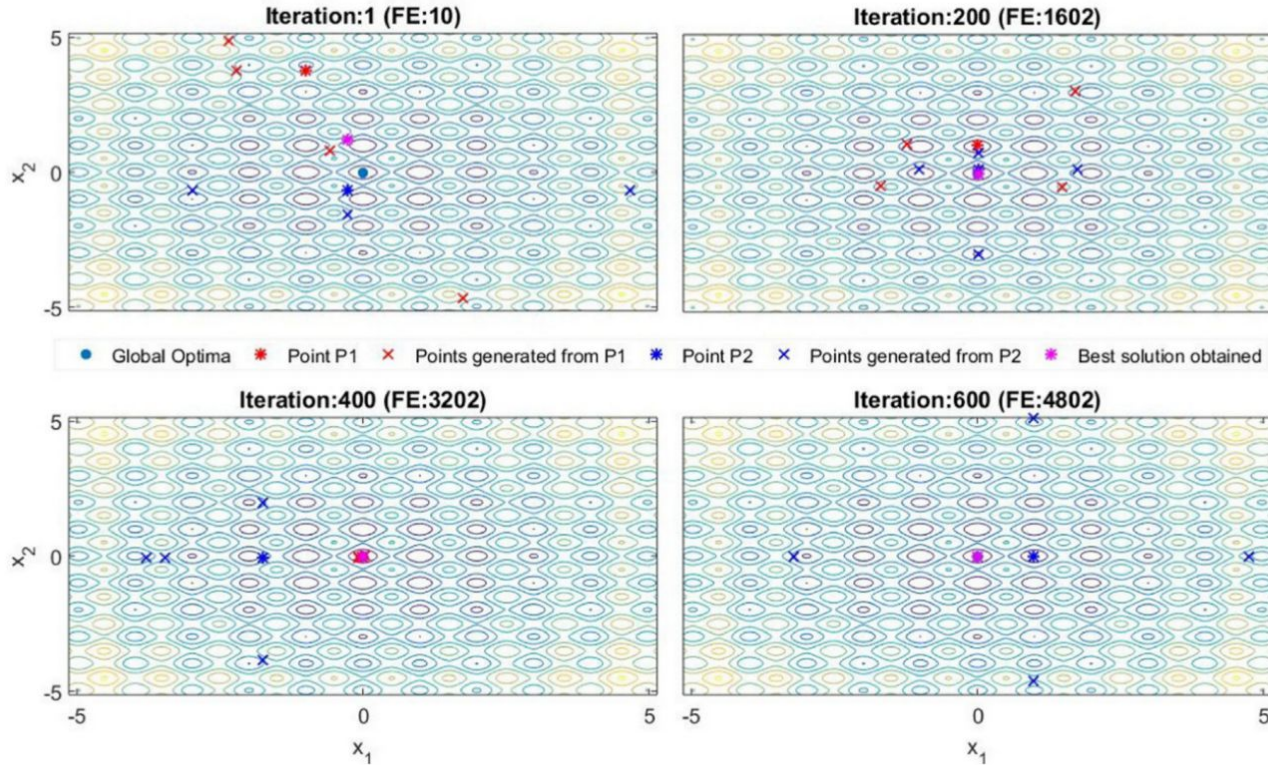
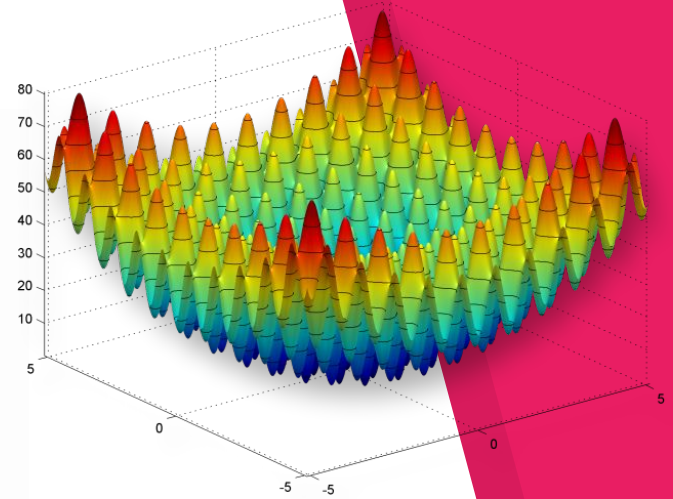
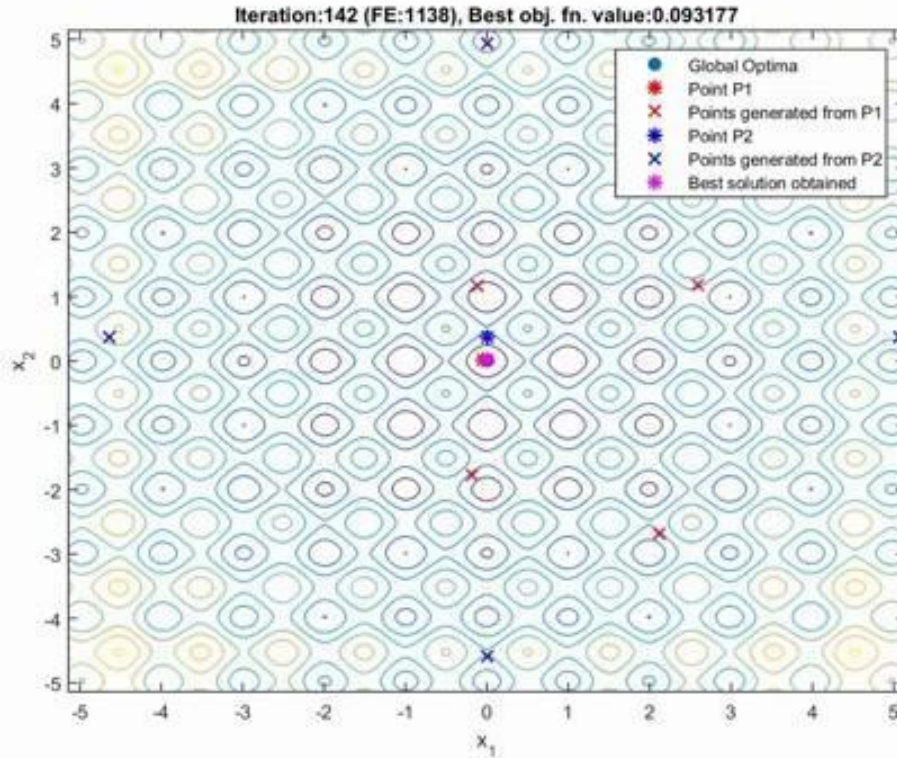


Fig. 2. Convergence of YYPO for the Rastrigin function.



# NAVIGATION MECHANISM

Rastrigin function



# CEC-2013 Results

Performance of YYPO on the 50D test functions.

	Prob. ID (Optima)	Best	Worst	Median	Mean	Std. dev.
Unimodal	CEC1 (−1400)	2.82E−08	6.57E−07	1.12E−07	1.45E−07	1.21E−07
	CEC2 (−1300)	1.13E+06	7.26E+06	3.69E+06	3.55E+06	1.48E+06
	CEC3 (−1200)	1.21E+07	2.51E+09	3.38E+08	5.43E+08	6.10E+08
	CEC4 (−1100)	1.83E+03	1.25E+04	4.55E+03	5.40E+03	2.63E+03
	CEC5 (−1000)	6.71E−04	4.43E−03	3.74E−03	3.58E−03	6.95E−04
Basic multimodal	CEC6 (−900)	4.34E+01	1.41E+02	4.72E+01	6.36E+01	2.80E+01
	CEC7 (−800)	5.75E+01	1.44E+02	1.04E+02	1.01E+02	2.07E+01
	CEC8 (−700)	2.10E+01	2.12E+01	2.11E+01	2.11E+01	2.98E−02
	CEC9 (−600)	2.77E+01	6.14E+01	4.50E+01	4.50E+01	7.51E+00
	CEC10 (−500)	4.17E−06	9.60E−02	2.96E−02	3.47E−02	2.13E−02
	CEC11 (−400)	3.57E−07	4.97E+00	1.99E+00	1.78E+00	1.18E+00
	CEC12 (−300)	1.63E+02	6.08E+02	3.69E+02	3.76E+02	1.22E+02
	CEC13 (−200)	2.53E+02	6.45E+02	4.07E+02	4.28E+02	8.82E+01
	CEC14 (−100)	1.59E+00	1.96E+01	1.01E+01	1.02E+01	3.84E+00
	CEC15 (100)	6.12E+03	1.07E+04	8.25E+03	8.29E+03	1.02E+03
	CEC16 (200)	9.67E−01	2.98E+00	1.79E+00	1.84E+00	4.37E−01
	CEC17 (300)	5.34E+01	6.26E+01	5.75E+01	5.77E+01	2.17E+00
	CEC18 (400)	2.03E+02	4.42E+02	3.24E+02	3.22E+02	6.49E+01
	CEC19 (500)	1.57E+00	4.20E+00	3.16E+00	3.10E+00	5.78E−01
	CEC20 (600)	1.93E+01	2.40E+01	2.10E+01	2.12E+01	1.08E+00
Composition	CEC21 (700)	2.00E+02	1.12E+03	8.36E+02	7.78E+02	3.94E+02
	CEC22 (800)	2.17E+01	2.45E+02	3.21E+01	8.78E+01	8.68E+01
	CEC23 (900)	7.21E+03	1.15E+04	9.34E+03	9.47E+03	1.04E+03
	CEC24 (1000)	2.64E+02	3.83E+02	3.28E+02	3.27E+02	2.47E+01
	CEC25 (1100)	3.23E+02	4.45E+02	3.91E+02	3.87E+02	2.74E+01
	CEC26 (1200)	2.00E+02	2.08E+02	2.00E+02	2.01E+02	1.29E+00
	CEC27 (1300)	1.02E+03	1.95E+03	1.56E+03	1.55E+03	2.00E+02
	CEC28 (1400)	4.00E+02	3.71E+03	4.00E+02	8.29E+02	1.09E+03

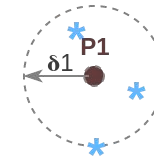
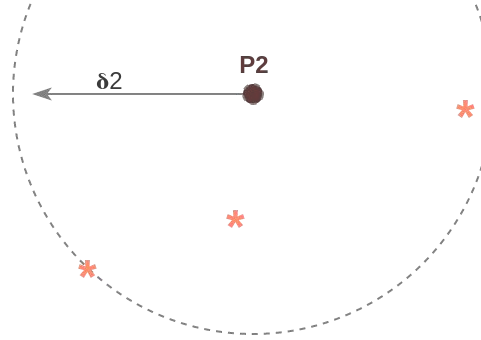
# CEC-2013 Results

Wilcoxon signed rank test results.

YYPO vs.	10D			30D		
	R+	R–	p-Value	R+	R–	p-Value
ABC	235	171	4.66E–01	284	122	6.51E–02
ALO	400	6	7.26E–06	390	16	2.06E–05
DE	361	45	3.21E–04	319	87	8.25E–03
GWO	351	55	7.51E–04	307	99	1.79E–02
MDS	385	21	3.41E–05	361	45	3.21E–04
PS	393	13	1.51E–05	361	45	3.21E–04
PSO	388	18	2.52E–05	315	91	1.08E–02

YYPO vs.	50D		
	R+	R–	p-Value
ABC	284	122	6.51E–02
ALO	278	128	8.77E–02
DE	311	95	1.39E–02
GWO	318	88	8.83E–03
MDS	359	47	3.82E–04
PS	345	61	1.22E–03
PSO	324	82	5.86E–03

**ABC** Artificial Bee Colony  
**ALO** Ant-Lion Optimizer  
**DE** Differential Evolution  
**GWO** Grey Wolf Optimizer  
**MDS** Multiobjective Direct Search  
**PS** Pattern Search  
**PSO** Particle Swarm Optimization



## ROOM FOR IMPROVEMENT

- Local search **almost** already implemented
- **Dynamic** splitting probability <sup>[1]</sup>

$$P_M = (D/(D + 5))^2$$

$$P_U = 1 - P_M$$

- Dynamic **load balance** (P1/P2)
- **Several explorer** points
- **Genetic stage** before archive stage

[1] V. Punnathanam and P. Kotecha, "Adaptive Yin-Yang-Pair Optimization on CEC 2016 functions," 2016 IEEE Region 10 Conference (TENCON), Singapore, 2016, pp. 2296-2299.

