

Neural oscillations level sets for activity constancy: from single neurons to networks



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Abstract

Neural oscillatory patterns can be characterized by a number of attributes, whose value is determined by the interplay of the participating currents. Experimental and theoretical work has shown that multiple combinations of parameters can generate patterns with the same attributes [1-4]. This endows neurons and networks with flexibility to adapt to changing environments and is substrate for homeostatic regulation [4].

At the same time, it presents modelers with the phenomenon of unidentifiability in parameter estimation. Attribute level sets (LSs) in parameter are manifolds on parameter space for which a given attribute is constant. Whether and under what circumstances the attribute LSs for individual neurons are conserved in the networks in which they are embedded and what additional network level sets emerge is not well understood.

In this work we describe a canonical (C-) model for oscillations LSs for single cells. Under certain conditions, the LSs for individual C-cells are preserved in networks of C-cells. Moreover new LSs emerge in these networks. We characterize them for both homogeneous and heterogeneous networks, where individual cells are identical or not.

Methods

The mathematical oscillator (C-model) used to represent the behavior of a neuron is given by

Neuron model
$$\frac{dx}{dt} = \lambda x - \omega y - (bx + ay)(x^2 + y^2)$$

$$\frac{dy}{dt} = \omega x + \lambda x + (ax - by)(x^2 + y^2)$$

It is a type of the so-called Lambda-Omega systems with a single limit circle in which degeneracy is easily characterized. Amplitude and frequency LSs are given by

- Amplitude level sets $\rightarrow \frac{\lambda}{L} = K_a$
- Frequency level sets $\rightarrow \omega + a \frac{\lambda}{I} = K_f$

The general form of the linear connectivity networks of Lambda-Omega systems are

Network model
$$\begin{cases} \frac{dx_k}{dt} = \lambda_k x_k - \omega_k y_k - (b_k x_k + a_k y_k)(x_k^2 + y_k^2) + \sum_{j=1}^N \alpha_{k,j} x_j \\ \frac{dy_k}{dt} = \omega_k x_k + \lambda_k x_k + (a_k x_k - b_k y_k)(x_k^2 + y_k^2) \end{cases}$$

where $A = \{\alpha_{k,i}\}$ is the connectivity matrix

Introduction

Degeneracy in Biological Systems

The Activity-dependent homeostatic regulation (ADHR) mechanism constitute a negative feedback system through which neurons are able to restore their properties and compensate changes due to perturbations. It allows neurons to maintain their so-called target activity level.

The idea a given that target activity level can be achieved with different parameter combinations and that almost identical activity can arise from different intrinsic properties has both experimental and theoretical evidence [1,5].

Figure 1. Similar neuron activity, From [5]

Neuronal activity properties need to be constrained in order to achieve the target activity level of any ADHR. Usually, these constraints result in regions on parameter space which generate a desired neuron behavior. When characterized by certain attributes, attribute LSs can represent these regions.

Parameter Estimation Unidentifiability

Neuronal parameter optimization is the process of identifying sets of parameters that lead to a desired electrical activity pattern in a given neuron or neuronal network model that is not fully determined by experimental data.

Structural degeneracy (of a given parameter model) refers to the situations where multiple sets of parameters values can produce the same observable output, therefore making the inverse problem ill-posed. It is only based on the inherent structure of a given model

If we create ground truth (fake) data using a particular set of parameters values, it is not clear (¿?) how to retrieve the biophysical parameter values used.

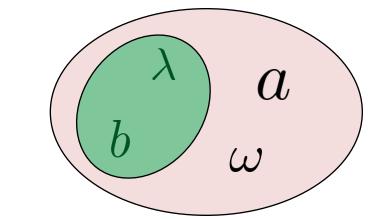


Figure 2. Degeneracy scheme for the neuron model

Conclusions

heterogeneous networks (cells belong to different

✓ Gap junctions do not preserve LSs on type-II

amplitude LS). However a readjust in self-

connectivities guarantees LSs preservation.

✓ The type of network (homogeneous or

affect predictions in [3].

parameter of the system.

✓ Several LSs have been computed (1,2-dimensional

heterogeneous) and the model structure does

*Prediction in [3]: If a particular homeostatic

characteristics (or attributes) of neuronal

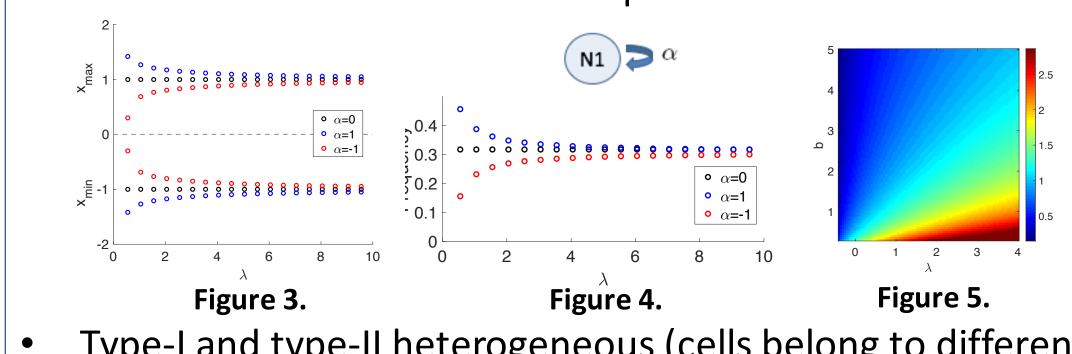
mechanism maintain m independent

LSs on 1,2,3 or 4-dimensional parameter spaces).

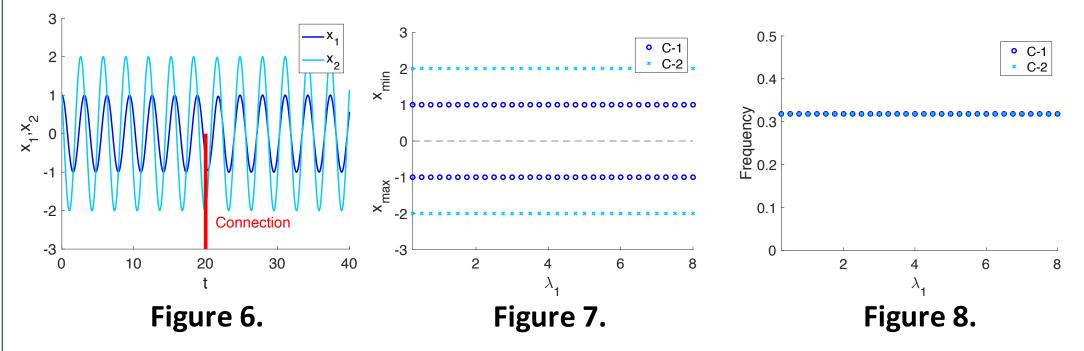
Results

Attribute Level Set Preservation

The self-connected cell do not preserve LSs.



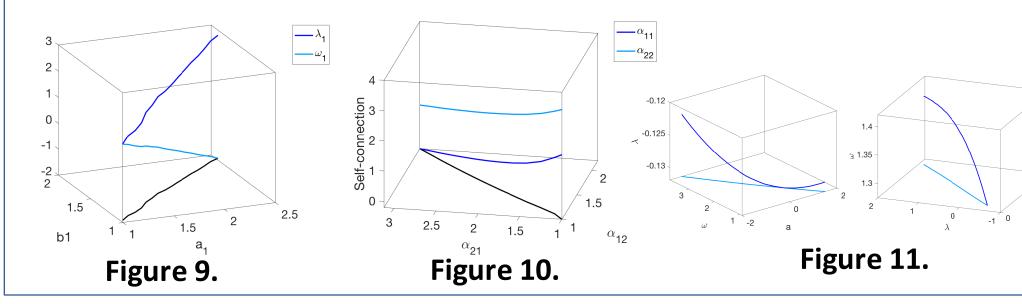
Type-I and type-II heterogeneous (cells belong to different individual amplitude LSs) two-cell networks preserve individual LSs on two-dimmensional manifolds on parameter space.



Gap junctions preserve LSs in type-I heterogeneous networks (cells belong to the same amplitude and frequency LS)

Newly Emerged Network Level Sets

- The self-connected cell $(N1) > \alpha$
- ✓ 2-dimensional total-degenerated LSs on the intrinsic parameter space (Figure 11)
- Homogeneous Networks
- ✓ 2-dimensional total-degenerated LSs on connectivity parameter space.
- Type-I Heterogeneous Networks
- √ 1-dimensional total-degenerated LSs on connectivity parameter space (Figure 10)
- Type-II Heterogeneous Networks
- - ✓ 1-dimensional total-degenerated LSs on each cell's intrinsic parameter space.
 - √ 1-dimensional total-degenerated LSs on the connectivity parameter space. (Figure 10)



Future Work

activity, then at least m parameters must be

changed as a response to a perturbation in one

How related are model symmetries with the preservation of LSs? How closely related are homeostatic mechanisms (LSs) at the neuron and network level? What do we exactly mean by a network LS? How could one develop methods for the disambiguation of degeneracy?

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