## Distributivité

Niveau de difficulté : VIOLENT

## 1 Enoncé

Développer et réduire les expressions suivantes :

$A = (31t^3 + 7t)(7t^2 - 40t)$	$B = (-25y^6 + 43y)(19y^2 - 27)$
$C = (-2x^5 + 44x^4)(43 - 3x)$	$D = (40y^2 + 28y)(8y^4 - 12)$
$E = (-7x^4 + 15x)(-34x + 16)$	$F = (32x^3 + 15x^2)(-6x^5 + 32)$
$G = (16z^2 - 32)(-34z^3 + 39)$	$H = (35x^6 + 39x^5)(-37 + 13x)$
$I = (-5z^3 + 30)(15z^2 - 26)$	$J = (8y^3 + 50)(-17y^2 - 30)$
K = (37 + 7x)(-40x - 14)	$L = (44z^6 - 8z)(-44z + 15)$
$M = (29z^2 - 37z^5)(11z^5 - 17z)$	$N = (12 + 14x)(25x^6 + 36x)$
$O = (24y^6 + 19y^4)(-43y^2 + 16y)$	$P = (-10z^3 - 40z)(-38z^3 - 34)$
$Q = (-15y - 38y^5)(18y + 9)$	$R = (-19z + 16z^6)(-33z^6 - 15)$
$S = (-28t^6 - 38t^3)(-5t^6 - 14t)$	$T = (-19z^5 - 37)(-31z^3 + 1)$

## 2 Corrigé

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A = (31t^3 + 7t)(7t^2 - 40t)
                                                                                                                                                                                                           B = (-25y^6 + 43y)(19y^2 - 27)
A=31t^3 \times 7t^2 + 31t^3 \times (-40t) + 7t \times 7t^2 + 7t \times (-40t)
                                                                                                                                                                                                           B = -25y^6 \times 19y^2 - 25y^6 \times (-27) + 43y \times 19y^2 + 43y \times (-27)
A = 217t^5 - 1240t^4 + 49t^3 - 280t^2
                                                                                                                                                                                                           B = -475y^8 + 675y^6 + 817y^3 - 1161y
A = 217t^5 - 1240t^4 + 49t^3 - 280t^2
                                                                                                                                                                                                           B = -475y^8 + 675y^6 + 817y^3 - 1161y
C = (-2x^5 + 44x^4)(43 - 3x)
                                                                                                                                                                                                           D = (40y^2 + 28y)(8y^4 - 12)
C = -2x^5 \times 43 - 2x^5 \times (-3x) + 44x^4 \times 43 + 44x^4 \times (-3x)
                                                                                                                                                                                                           D=40y^2 \times 8y^4 + 40y^2 \times (-12) + 28y \times 8y^4 + 28y \times (-12)
C = -86x^5 + 6x^6 + 1892x^4 - 132x^5
                                                                                                                                                                                                           D=320y^6 - 480y^2 + 224y^5 - 336y
                                                                                                                                                                                                           D=320y^{6} + 224y^{5} - 480y^{2} - 336y

D=320y^{6} + 224y^{5} - 480y^{2} - 336y
C=6x^6-86x^5-132x^5+1892x^4
C=6x^6-218x^5+1892x^4
                                                                                                                                                                                                           F = (32x^3 + 15x^2)(-6x^5 + 32)
E = (-7x^4 + 15x)(-34x + 16)
                                                                                                                                                                                                           F=32x^3 \times (-6x^5) + 32x^3 \times 32 + 15x^2 \times (-6x^5) + 15x^2 \times 32
E = -7x^4 \times (-34x) - 7x^4 \times 16 + 15x \times (-34x) + 15x \times 16
                                                                                                                                                                                                           F = -192x^8 + 1024x^3 - 90x^7 + 480x^2
E=238x^5 - 112x^4 - 510x^2 + 240x
                                                                                                                                                                                                           \begin{aligned} \mathbf{F} &= -192x^8 - 90x^7 + 1024x^3 + 480x^2 \\ \mathbf{F} &= -192x^8 - 90x^7 + 1024x^3 + 480x^2 \end{aligned}
E=238x^5 - 112x^4 - 510x^2 + 240x
G=(16z^2-32)(-34z^3+39)
                                                                                                                                                                                                           H=(35x^6+39x^5)(-37+13x)
G=16z^2 \times (-34z^3) + 16z^2 \times 39 - 32 \times (-34z^3) - 32 \times 39
                                                                                                                                                                                                           H = 35x^6 \times (-37) + 35x^6 \times 13x + 39x^5 \times (-37) + 39x^5 \times 13x
G = -544z^5 + 624z^2 + 1088z^3 - 1248
                                                                                                                                                                                                           H = -1295x^6 + 455x^7 - 1443x^5 + 507x^6
                                                                                                                                                                                                           \begin{array}{l} \mathrm{H}{=}455x^{7}-1295x^{6}+507x^{6}-1443x^{5} \\ \mathrm{H}{=}455x^{7}-788x^{6}-1443x^{5} \end{array}
\mathbf{G} = -544z^5 + 1088z^3 + 624z^2 - 1248
G = -544z^5 + 1088z^3 + 624z^2 - 1248
I = (-5z^3 + 30)(15z^2 - 26)
                                                                                                                                                                                                           J = (8y^3 + 50)(-17y^2 - 30)
I = -5z^3 \times 15z^2 - 5z^3 \times (-26) + 30 \times 15z^2 + 30 \times (-26)
                                                                                                                                                                                                           J=8y^3 \times (-17y^2) + 8y^3 \times (-30) + 50 \times (-17y^2) + 50 \times (-30)
I = -75z^5 + 130z^3 + 450z^2 - 780
                                                                                                                                                                                                           J = -136y^5 - 240y^3 - 850y^2 - 1500
I = -75z^5 + 130z^3 + 450z^2 - 780
                                                                                                                                                                                                           J = -136y^5 - 240y^3 - 850y^2 - 1500
K=(37+7x)(-40x-14)
                                                                                                                                                                                                           L=(44z^6-8z)(-44z+15)
K=37 \times (-40x) + 37 \times (-14) + 7x \times (-40x) + 7x \times (-14)
                                                                                                                                                                                                           L=44z^6 \times (-44z) + 44z^6 \times 15 - 8z \times (-44z) - 8z \times 15
K = -1480x - 518 - 280x^2 - 98x
                                                                                                                                                                                                           L = -1936z^{7} + 660z^{6} + 352z^{2} - 120z
K = -280x^2 - 1480x - 98x - 518

K = -280x^2 - 1578x - 518
                                                                                                                                                                                                           L=-1936z^7+660z^6+352z^2-120z
M = (29z^2 - 37z^5)(11z^5 - 17z)
                                                                                                                                                                                                           N=(12+14x)(25x^6+36x)
\mathbf{M} = 29z^2 \times 11z^5 + 29z^2 \times (-17z) - 37z^5 \times 11z^5 - 37z^5 \times (-17z) \\ \mathbf{N} = 12 \times 25x^6 + 12 \times 36x + 14x \times 25x^6 + 14x + 14
M = 319z^7 - 493z^3 - 407z^10 + 629z^6
                                                                                                                                                                                                           N = 300x^6 + 432x + 350x^7 + 504x^2
M = -407z^{1}0 + 319z^{7} + 629z^{6} - 493z^{3}
                                                                                                                                                                                                           N = 350x^7 + 300x^6 + 504x^2 + 432x
M = -407z^{1}0 + 319z^{7} + 629z^{6} - 493z^{3}
                                                                                                                                                                                                           N=350x^7+300x^6+504x^2+432x
                                                                                                                                                                                                           \begin{array}{l} \mathrm{P}{=}(-10z^3-40z)(-38z^3-34) \\ \mathrm{P}{=}{-}10z^3{\times}(-38z^3){-}10z^3{\times}(-34){-}40z{\times}(-38z^3){-}40z{\times}(-34) \end{array}
O = (24y^6 + 19y^4)(-43y^2 + 16y)
O = (24y^{6} + 16y^{7})(16y^{4} + 16y^{7}) + 24y^{6} \times 16y + 19y^{4} \times (-43y^{2}) + 19y^{4} \times 16y^{4} + 16y^{2} + 10z^{2} \times (-30z^{7}) 
 O = -1032y^8 + 384y^7 - 817y^6 + 304y^5
                                                                                                                                                                                                           P=380z^6 + 1520z^4 + 340z^3 + 1360z
O = -1032y^8 + 384y^7 - 817y^6 + 304y^5
                                                                                                                                                                                                           P=380z^6+1520z^4+340z^3+1360z
                                                                                                                                                                                                            R = (-19z + 16z^6)(-33z^6 - 15)
Q = (-15y - 38y^5)(18y + 9)
                                                                                                                                                                                                           \mathbf{R} = -19z \times (-33z^6) - 19z \times (-15) + 16z^6 \times (-33z^6) + 16z^6 \times (-15)
 Q = -15y \times 18y - 15y \times 9 - 38y^5 \times 18y - 38y^5 \times 9
                                                                                                                                                                                                           R = 627z^7 + 285z - 528z^12 - 240z^6
 Q = -270y^2 - 135y - 684y^6 - 342y^5
 Q = -684y^6 - 342y^5 - 270y^2 - 135y
                                                                                                                                                                                                           R = -528z^12 + 627z^7 - 240z^6 + 285z
Q = -684y^6 - 342y^5 - 270y^2 - 135y
                                                                                                                                                                                                           R = -528z^{1}2 + 627z^{7} - 240z^{6} + 285z
S = (-28t^6 - 38t^3)(-5t^6 - 14t)
S = (-28t^{6} \times (-5t^{6}) - 28t^{6} \times (-14t) - 38t^{3} \times (-5t^{6}) - 38t^{3} \times (-14t) + (-19t^{6} \times (-31t^{3}) - 19t^{5} \times (-31t^{3}) - 19t^{5} \times (-31t^{3}) - 37 \times (-31t^{3}) - 37 \times (-31t^{3}) - 37 \times (-31t^{3}) - (-31t^{3}) + (-31t^{3}) 
S=140t^12 + 392t^7 + 190t^9 + 532t^4
                                                                                                                                                                                                           T=589z^8-19z^5+1147z^3-37
S=140t^12+190t^9+392t^7+532t^4
                                                                                                                                                                                                           T=589z^8-19z^5+1147z^3-37
S=140t^12+190t^9+392t^7+532t^4
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