# Spatial Domain Filtering

### Topics to be covered

- Neighborhood Processing
- 2D Convolution
- Applications of 2D Convolution
- Mean Filter
- Gaussian Filter

- Median Filter
- Laplacian
- High Boost Filtering
- Sobel Filtering
- Canny Edge Detection

### Concept of Neighborhood

Number of pixels surrounding a given pixel in an image form its neighborhood. This neighborhood is usually a small matrix containing given pixel at its center.

The size of neighborhood matrix is usually  $3 \times 3$ ,  $5 \times 5$  OR  $7 \times 7$  i.e an odd number so that a given pixel can reside easily at the center of neighborhood matrix.

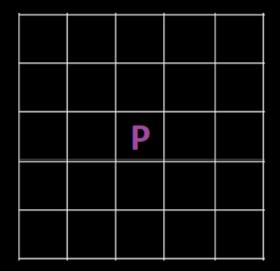
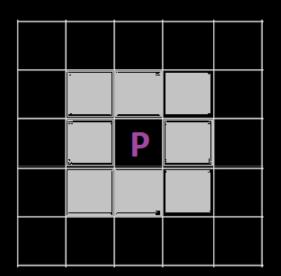
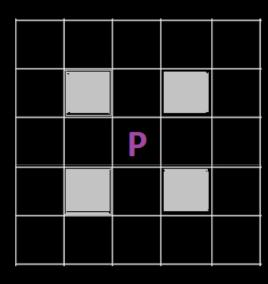


Image With Given pixel " P "



8 - Neighborhood



**Diognal Neighborhood** 

### Neighborhood Processing

Neighborhood processing involves those algorithms in image processing where the resulting value for a pixel at the reference pixel depends upon the original pixel value at that point as well as the original pixel value of some of its surrounding or neighboring points.

### Steps of Neighborhood Processing

- Select a reference pixel in an input image. Lets call it  $I(x_r, y_r)$ .
- Perform neighborhood processing operation which involves the pixels within a neighborhood around the reference pixel in the input image.
- Apply the result of the neighborhood processing operation to the pixel of same coordinates in the output image  $J(x_r, y_r)$ .
- Repeat the above neighborhood processing operation for every pixel in the input image.

# 2D Convolution

### Steps in 2D Convolution

- Flipping
- Shifting / Sliding
- Multiplication
- Addition

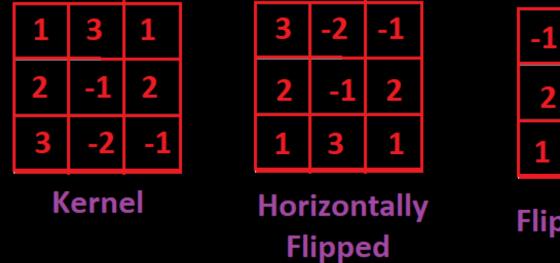
# Numerical Example in 2D Convolution

6	3	7	9	1
7	0	3	1	3
8	1	5	3	6
3	9	4	3	5
7	8	2	3	0

1	3	1
2	-1	2
3	-2	-1

Kernel

## Flipping the Kernel



**Flipped Kernel** 

6	3	7	9	1
7	0	3	1	3
8	1	5	3	6
3	9	4	3	5
7	8	2	3	0

**Image** 

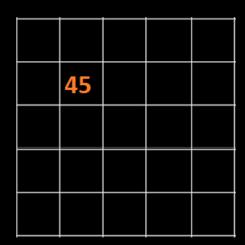
-1	-2	3
2	-1	2
1	3	1

Flipped Kernel

6	3	7	9	1
7	0	3	1	3
8	1	5	3	6
3	9	4	3	5
7	8	2	3	0

-1	-2	3
2	-1	2
1	3	1

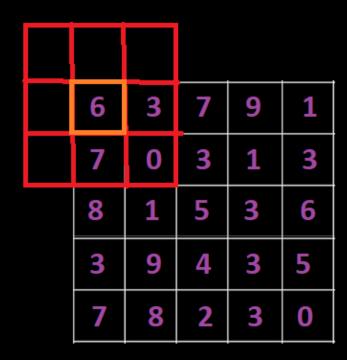
#### **Image**



**Convolution** 

#### Multiplication and Addition

$$(6 \times -1) + (3 \times -2) + (7 \times 3)$$
  
 $(7 \times 2) + (0 \times -1) + (3 \times 2)$   
 $(8 \times 1) + (1 \times 3) + (5 \times 1)$   
 $= -6 - 6 + 21 + 14 + 0 + 6 + 8 + 3 + 5$   
 $= 45$ 



**Image** 

-1	-2	3
2	-1	2
1	3	1

0	0	0			
0	6	3	7	9	1
0	7	0	3	1	3
	8	1	5	3	6
	3	9	4	3	5
	7	8	2	3	0

**Image** 

-1	-2	3
2	-1	2
1	3	1

#### Multiplication and Addition

$$= -6 + 6 + 21 + 0$$
  
 $= 21$ 

### Convolution Results

21	33	27	16	27
<b>15</b>	45	28	9	9
0	61	24	41	11
31	43	35	33	0
10	1	12	6	0

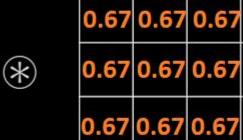
Convolution

## Applications of 2D Convolution

# Image Blurring



Image



Kernel



Blurred Image

# Image Sharpening







Kernel

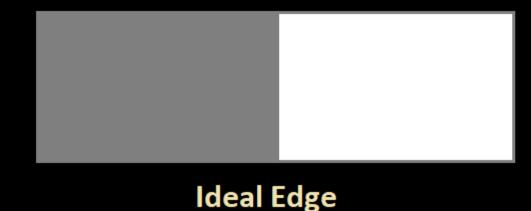


Sharped Image

### Edge Detection

#### Concept of Edge

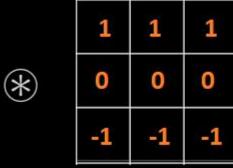
An edge is a boundary between two image regions having sharp variations in their intensities.



## Edge Detection



Image



Kernel



Edge Detected Image

#### Mean Filter

Mean filter is a neighborhood averaging filter which is used to smooth the image. It is used to create blurring in the image and to remove high frequency contents such as noise from the image.

This filter uses convolution with  $m \times m$  kernel or mask. All the coefficients in the kernel are 1 divided by the number of elements in kernel.

A typical  $3 \times 3$  kernel is given by

$$k(x,y) = \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

A  $5 \times 5$  kernel is given by

# Applications of Mean Filter

## Image Blurring



 $\frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} =$ 

**Mean Filter** 

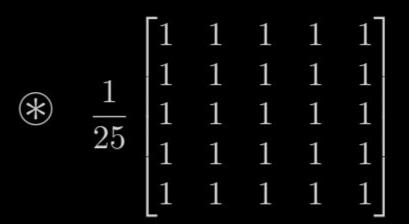


**Blurred Image** 

**Image** 

### Image Blurring

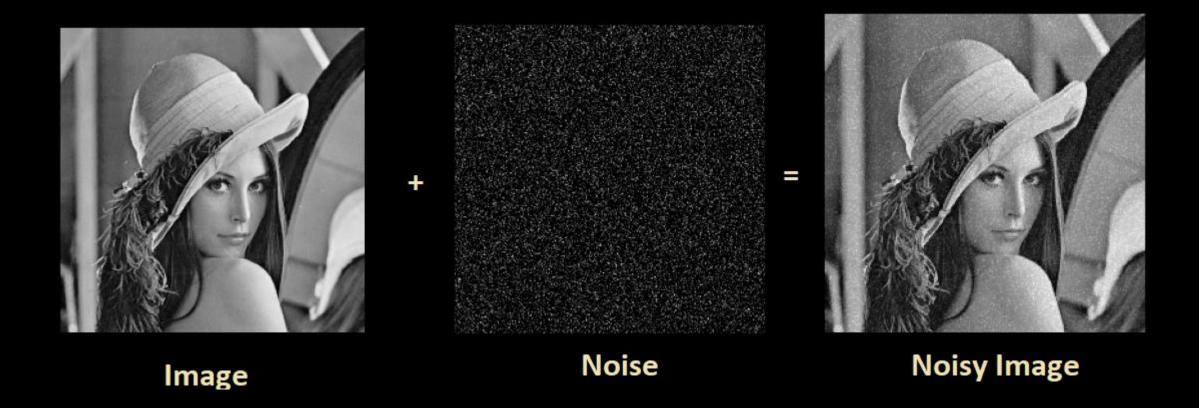




**Mean Filter** 

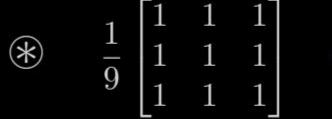


**Blurred Image** 





**Noisy Image** 



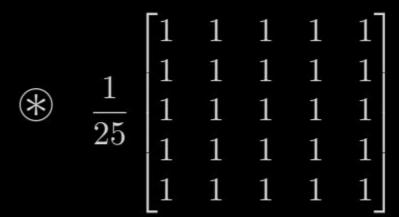
**Mean Filter** 



**Denoised Image** 



**Noisy Image** 



**Mean Filter** 



**Denoised Image** 

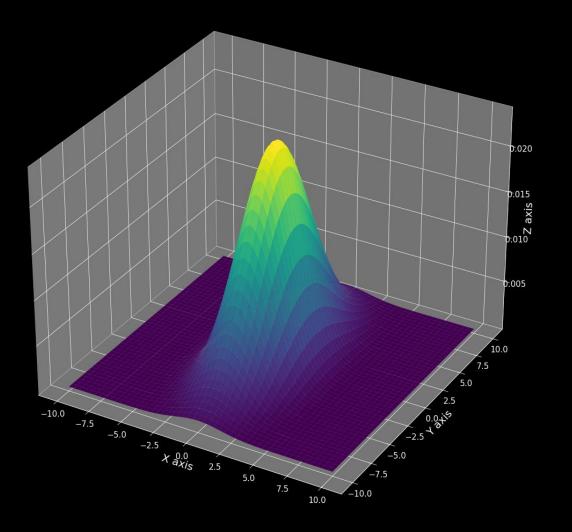
#### Gaussian Smooth Filter

Instead if using simple mean, Gaussian smoothing filter uses a weighted mean, where neighborhood pixels that are closer to the central pixel contribute more weight to the average.

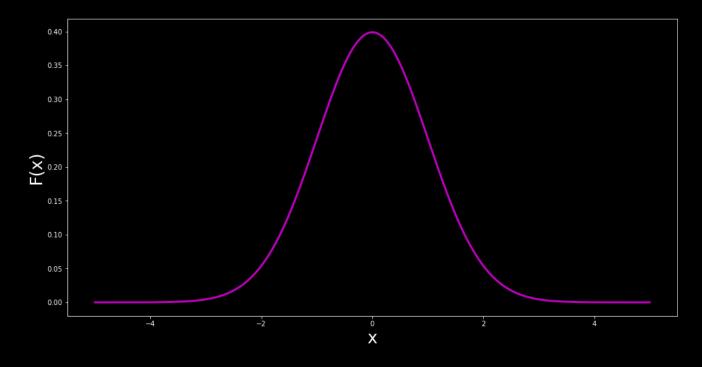
More natural smoothing or blurring is obtained with Gaussian filter as compared to Mean filter and more edges or details are preserved with Gaussian filter.

$$k(x,y) = exp[\frac{-(x^2 + y^2)}{2\sigma^2}]$$

### 2D Gaussian

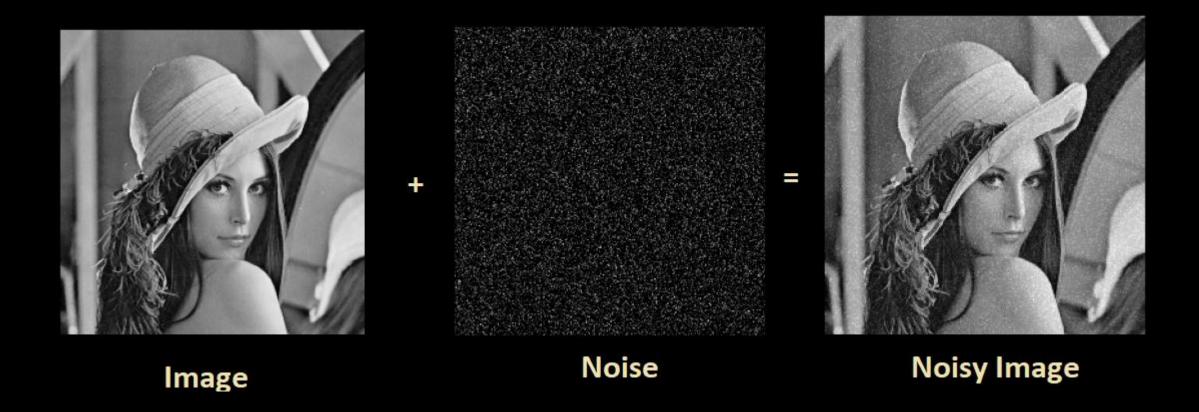


### 1D Gaussian



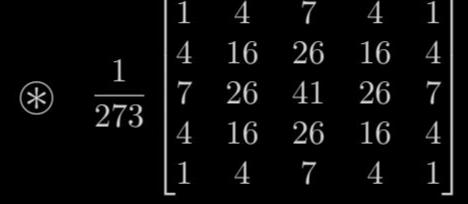
A typical  $5 \times 5$  kernel is given by

$$k(x,y) = \frac{1}{273} \begin{bmatrix} 1 & 4 & 7 & 4 & 1 \\ 4 & 16 & 26 & 16 & 4 \\ 7 & 26 & 41 & 26 & 7 \\ 4 & 16 & 26 & 16 & 4 \\ 1 & 4 & 7 & 4 & 1 \end{bmatrix}$$









**Gaussian Kernel** 



**Denoised Image** 



Denoised Image (Gaussian)

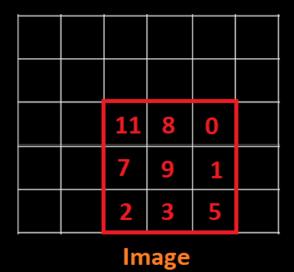


Denoised Image ( Mean Filter )

#### Median Filter

The median filter works by sorting the pixel values within a neighborhood, finding the median value, and replacing the original pixel value with the median of that neighborhood.

Median filter is used to remove salt and pepper noise from the image which is not well denoised by Gaussian or Mean Filter.



11 8 0 7 9 1 2 3 5
Sorting
0 1 2 3 5 7 8 9 11

Median

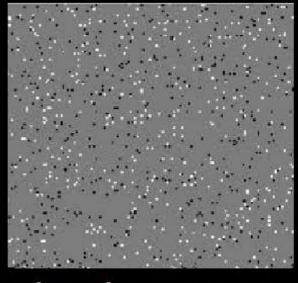


Image After Median Filtering

## Image Denoising by Median Filter



**Image** 



Salt and pepper noise



**Noisy Image** 



**Noisy Image** 



Denoised by Gaussian Filter



Denoised by Median Filter

### The Laplacian

The Laplacian of an image I(x,y) is given by

$$\nabla^{2}(x,y) = \frac{\partial^{2}(x,y)}{\partial x^{2}} + \frac{\partial^{2}(x,y)}{\partial y^{2}}$$

Laplacian is a second order derivative of the image pixels. It acts as a high pass filter by preserving the high frequency components such as fine details, edges, lines and also perform image sharpening.

A typical  $3 \times 3$  Laplacian kernel is given by

$$k(x,y) = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$

OR

$$k(x,y) = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

We can observe that signs of central element of kernel is reverse as compared to other elements.

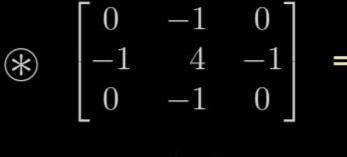
### Edge Detection by Laplacian



#### Edge Detection by Laplacian



**Smooth Image** 

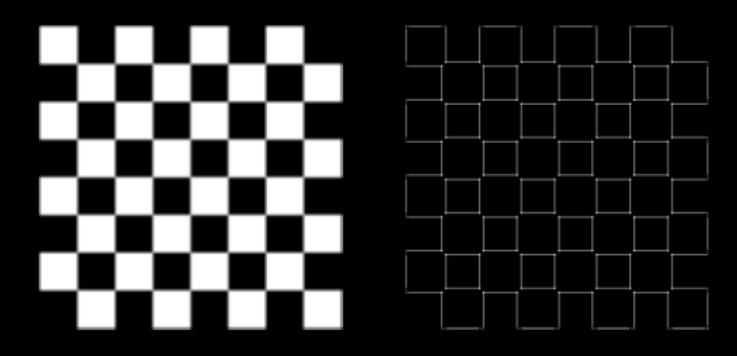


Laplacian



**Edge Detection** 

### Edge Detection by Laplacian



Smooth Image

Edge Detection by Laplacian

# High Boost Filtering

High boost filtering is a high pass filter version and is uesd to extract fine details from the image.

A typical  $3 \times 3$  High boost filter is given by

$$k(x,y) = \begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

# High Boost Filtering



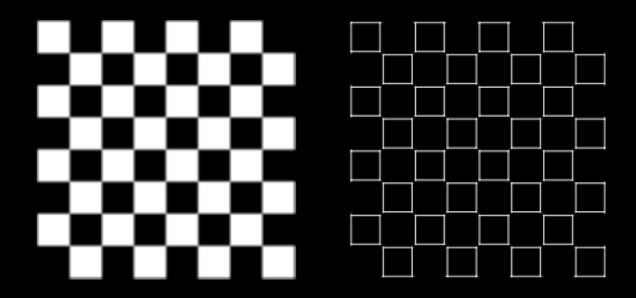
**Smooth Image** 

**High Boost Filter** 



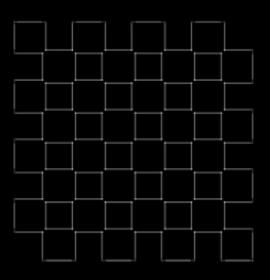
**Edge Detection** 

# High Boost Filtering



Smooth Image

Edge Detection
By High Boost Filter



Edge Detection by Laplacian

#### Sobel Filters

The Sobel filters are edge detectors. They detect the edges by estimating the first derivative of an image by doing a convolution between an image and the two kernels, one to detect vertical edges and one to detect horizontal edges.

Vertical edges are detected by using a horizontal gradient operator.

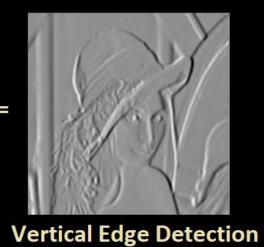
A typical  $3 \times 3$  sobel filter for vertical edge detection is given by

$$k_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

A typical  $3 \times 3$  sobel filter for horizontal edge detection is given by

$$k_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$





Sobel X

**Image** 



$$\begin{array}{c|cccc}
 & -1 & -2 & -1 \\
0 & 0 & 0 \\
1 & 2 & 1
\end{array}
=$$

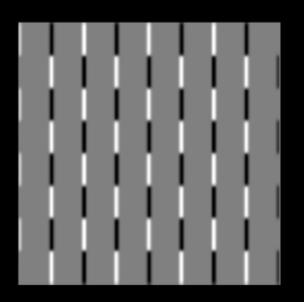
Sobel Y



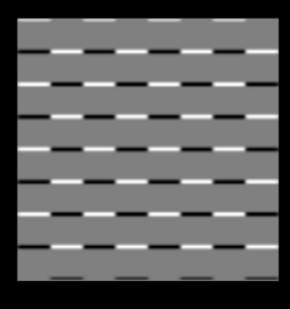
**Horizontal Edge Detection** 



Image



Vertical Edge Detection By Sobel X



Horizontal Edge Detection By Sobel Y

#### Canny Edge Detection

Canny edge detection works in following steps

- The input image is smoothed using a Gaussian low-pass filter.
- The gradient is calculated for each pixel in the smoothed image.
- The pixels are then thresholded using two threshold values i.e low threshold and high threshold. Pixels with values greater than high threshold are considered strong edge pixels whereas the pixels with values between Low threshold and high threshold are said to be weak pixels. This process is known as hysteresis thresholding.
- Pixels having intensity between both thresholds are weak. The algorithm performs edge linking that help us identify the ones that could be considered as strong edges.



**Image** 



**Thresholds = 10, 200** 



**Thresholds = 50, 120** 



Thresholds = 200, 240



**Image** 



**Thresholds = 50, 120** 



Thresholds = 10, 200



Thresholds = 200, 240