

Exercises.

Determine whether the following Hoare triples are valid.

$$\{y > 16\} \ x := x + 2 \ \{y > 15\}$$

$$\{x = 4\} \ x := x + 1 \ \{x > 4\}$$

$$\{y = z\} \ z := z + 1 \ \{y - 1 > z\}$$

$$\{17 = 18\} \ x := x + 1 \ \{x > z\}$$

$$\{x = 4\} \ x := 4 \ \{x = 4\}$$

$$\{x = 4\} \ x := x + 1 \ \{x = 4\}$$

Determine the Weakest Preconditions of the following.

$$x := x + 1 \ \{x = 12\}$$

$$x := y + 2 \ \{x > 17\}$$

$$y := 4 \ \{x = y + 2\}$$

$$x := y \ \{x \leq 0\}$$

$$x := 74 \ \{x = 73\}$$

What assignments would make the following into valid Hoare triples?

$$\{x = y + z\} \qquad \{x = z\}$$

$$\{y * 2 = 12\} \qquad \{y = 24\}$$

$$\{\text{true}\} \qquad \{y = 12\}$$

$$\{x > y\} \qquad \{x < y\}$$

$$\{x = X \wedge y = Y\} \qquad \{x = Y \wedge y = X\}$$

Note, in the last problem x and y are variables and X and Y are the values they contain at the start.