

HEIGHT - BALANCE PROPERTY

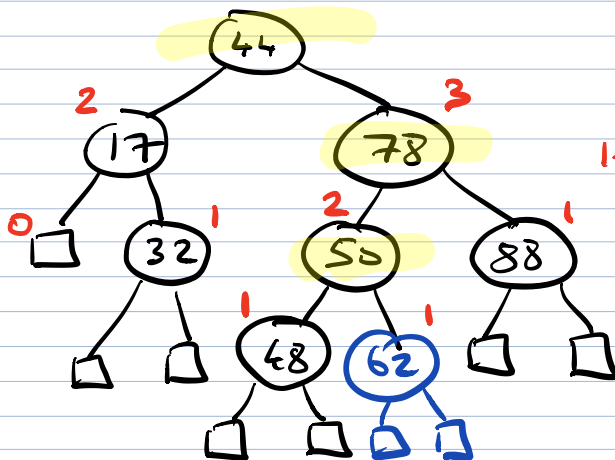
FOR EVERY INTERNAL NODE THE HEIGHTS OF ITS CHILDREN CAN DIFFER BY AT MOST 1

AFTER INSERT, CHECK THE HEIGHT BALANCE OF THE ANCESTORS OF THE NEWLY EXPANDED NODE, WORKING UPWARDS FROM THE BOTTOM OF THE TREE.

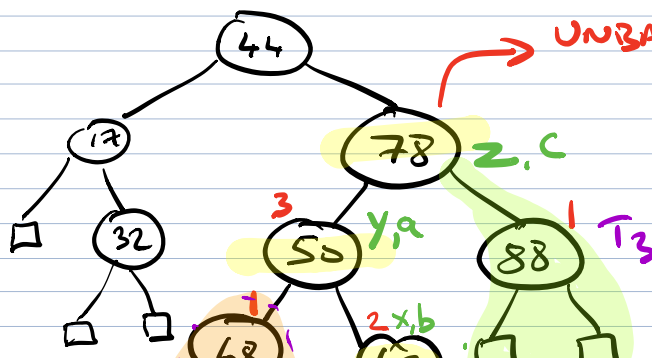
IF AN UNBALANCED NODE IS FOUND **RESTRUCTURE** TO RESTORE THE BALANCE

AFTER INSERT, RESTRUCTURING ONCE WILL BALANCE THE TREE

TRY: INSERT 62
INSERT 54

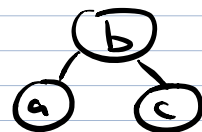


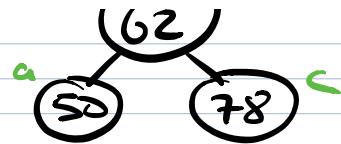
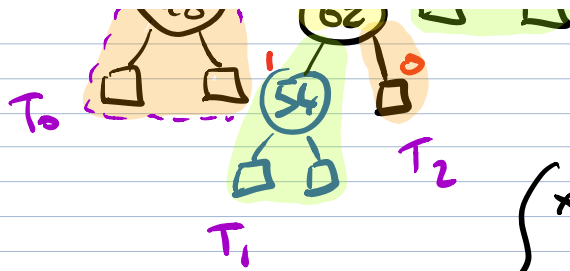
$$\begin{aligned} \text{height}(78) &= 1 + \max(\text{height}(50), \text{height}(88)) \\ &= 1 + \max(2, 1) \\ &= 1 + 2 = 3 \end{aligned}$$



UNBALANCED

Outcome of restructure





x, y, z say which nodes to restructure.
 a, b, c say where these nodes finish

Double rotation

