

We are given $f[0..M)$, $g[0..N)$ of int . We are told that f is ascending and g is descending. We are asked to construct a program to compute the number of pairs $f.i$ and $g.j$ whose sum exceeds 37.

$$r = \langle + i, j : 0 \leq i < M \wedge 0 \leq j < N : h.(f.i).(g.j) \rangle$$

where

$$* (0) h.x.y = 1 \iff x + y > 37$$

$$* (1) h.x.y = 0 \iff x + y \leq 37$$

We began by modelling our domain.

$$* (2) C.m.n = \langle + i, j : m \leq i < M \wedge n \leq j < N : h.(f.i).(g.j) \rangle$$

In Chapter 27 we saw how do construct a model based upon this definition (2) and then used the model to construct an algorithm.

Now I want you as an exercise to see what would have happened if we had chosen a different way to define $C.m.n$. In all there are 3 other ways we could have gone. They are as follows..

$$* (2) C.m.n = \langle + i, j : m \leq i < M \wedge 0 \leq j < n : h.(f.i).(g.j) \rangle$$

$$* (2) C.m.n = \langle + i, j : 0 \leq i < m \wedge 0 \leq j < n : h.(f.i).(g.j) \rangle$$

$$* (2) C.m.n = \langle + i, j : 0 \leq i < m \wedge n \leq j < N : h.(f.i).(g.j) \rangle$$

Starting from each of these definitions calculate and see what happens.