

Data Structures and Algorithms

The List Abstract Data Type - Array-Based List

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Learning outcomes

After this lecture and the related practical students should...

- be able to implement an array based list
- understand the resizing strategies

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1 The List Abstract Data Type

2 Array-Based List Implementation

- Algorithmic Complexity

The List Abstract Data Type

Concept

- The List ADT models a sequence of **positions**
- Each position store a piece of data
- There is a before/after relation between positions
- This allows for efficient insertion into the middle of a list

The Position Abstract Data Type

Concept

Before we can fully understand the list abstract data type we need to look at the position abstract data type

- The Position abstract data type models the idea of a place within a data structure where a single piece of data is stored
- Positions provide a simple view of different ways of storing data
 - ▶ An element in an array
 - ▶ A Node in a linked list

The Position Abstract Data Type

Specification

- Operation:
 - ▶ **element()**: This returns the piece of data that is stored in this position

The Position Abstract Data Type

Interface

```
1 public interface Position{  
2     public int element();  
3 }
```

The List Abstract Data Type

Specification

Operations:

- **first()**: returns the first position in the list

The List Abstract Data Type

Specification

Operations:

- **first()**: returns the first position in the list
- **last()**: return the last position in the list

The List Abstract Data Type

Specification

Operations:

- **first()**: returns the first position in the list
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- **before(p)**: returns the position in the list before p

The List Abstract Data Type

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- **first()**: returns the first position in the list
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- **before(p)**: returns the position in the list before p
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The List Abstract Data Type

Specification

Operations:

- **first()**: returns the first position in the list
- **last()**: return the last position in the list
- **before(p)**: returns the position in the list before p
- **after(p)** : returns the position in the list after p
- **insertBefore(p, d)**: inserts the value d into the position in the list before p

The List Abstract Data Type

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- **first()**: returns the first position in the list
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- **insertAfter(p, d)**: inserts the value d into the position in the list after p
- **insertFirst(d)**: inserts the value d into the first position in the list
- **insertLast(d)**: inserts the value d into the last position in the list
- **remove(p)**: removes the position p from the list

The List Abstract Data Type

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- **insertFirst(d)**: inserts the value d into the first position in the list
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- **remove(p)**: removes the position p from the list
- **size()**: returns the number of elements stored in the list

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- **insertFirst(d)**: inserts the value d into the first position in the list
- **insertLast(d)**: inserts the value d into the last position in the list
- **remove(p)**: removes the position p from the list
- **size()**: returns the number of elements stored in the list
- **isEmpty()**: is the list empty?

The List Abstract Data Type

Interface

```
1 public interface List {  
2     public Position first();  
3     public Position last();  
4     public Position before(Position p);  
5     public Position after(Position p);  
6     public Position insertBefore(Position p,  
7         int d);  
8     public Position insertAfter(Position p, int  
9         d);  
10    public Position insertFirst(int d);  
11    public Position insertLast(int d);  
12    public int remove(Position p);  
13    public int size();  
14    public boolean isEmpty();  
15 }
```

The List Abstract Data Type

Implementation Strategies

- Array based implementation

The List Abstract Data Type

Implementation Strategies

- Array based implementation
 - ▶ An array of `Position` objects

The List Abstract Data Type

Implementation Strategies

- Array based implementation
 - ▶ An array of `Position` objects
 - ▶ Search through the array to find the correct position

The List Abstract Data Type

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 - ▶ An array of `Position` objects
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 - ▶ Not very efficient

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- Link based implementations

The List Abstract Data Type

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- Link based implementations
- There are two versions

The List Abstract Data Type

Implementation Strategies

- Array based implementation
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- There are two versions
 - ▶ Singly-Linked List

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- There are two versions
 - ▶ Singly-Linked List
 - ★ Each `Position` object keeps a reference to the next `Position` in the sequence

The List Abstract Data Type

Implementation Strategies

- Array based implementation
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- Link based implementations
- There are two versions
 - ▶ Singly-Linked List
 - ★ Each `Position` object keeps a reference to the next `Position` in the sequence
 - ▶ Doubly-Linked List

The List Abstract Data Type

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- Array based implementation
 - ▶ An array of `Position` objects
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 - ▶ Not very efficient
- Link based implementations
- There are two versions
 - ▶ Singly-Linked List
 - ★ Each `Position` object keeps a reference to the next `Position` in the sequence
 - ▶ Doubly-Linked List
 - ★ Each `Position` object keeps a reference to the next and previous `Positions` in the sequence

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 - Algorithmic Complexity

Position Abstract Data Type

Array-Based Implementation

- We create a `ArrPos` class that implements the `Position` interface

Position Abstract Data Type

Array-Based Implementation

- We create a `ArrPos` class that implements the `Position` interface
- We add functionality to the class to store the index of the `ArrPos` in the array

Position Abstract Data Type

Array-Based Implementation

- We create a `ArrPos` class that implements the `Position` interface
- We add functionality to the class to store the index of the `ArrPos` in the array
- We also add some functionality to increment and decrement the index

Position Abstract Data Type

Array-Based Implementation

```
1 public class ArrPos implements Position {
2     private int index;
3     private int data;
4     public ArrPos(int i, int d){
5         index = i;
6         data = d;
7     }
8     public int element() { return data; }
9     public int getIndex(){ return index; }
10    public void incrementPosition() {
11        index++;
12    }
13    public void decrementPosition() {
14        index--;
15    }
16 }
```

Array-Based List Implementation

- We keep an array of `ArrPos` objects to store our data

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- We keep an array of `ArrPos` objects to store our data
- When inserting or removing data we have to update the `ArrPos` objects so they point to the correct index

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- A reference to the array of `ArrPos` objects

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Variables:

- A reference to the array of `ArrPos` objects

```
private ArrPos[] items;
```


Array-Based List Implementation

- We keep an array of `ArrPos` objects to store our data
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Variables:

- A reference to the array of `ArrPos` objects
`private ArrPos[] items;`
- A number to keep track of the size

Array-Based List Implementation

- We keep an array of `ArrPos` objects to store our data
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Variables:

- A reference to the array of `ArrPos` objects
`private ArrPos[] items;`
- A number to keep track of the size
`private int size;`

Array-Based List Implementation

- We keep an array of `ArrPos` objects to store our data
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- When we run out of space we must increase the size of the array of objects

Variables:

- A reference to the array of `ArrPos` objects
`private ArrPos[] items;`
- A number to keep track of the size
`private int size;`
- A number to keep track of the maximum number of elements we can hold

Array-Based List Implementation

- We keep an array of `ArrPos` objects to store our data
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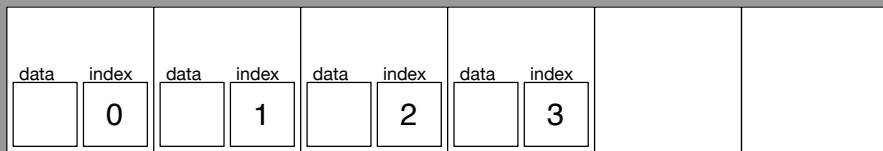
Variables:

- A reference to the array of `ArrPos` objects
`private ArrPos[] items;`
- A number to keep track of the size
`private int size;`
- A number to keep track of the maximum number of elements we can hold
`private int maxSize;`

Representation of an ArrPos Object



Representation of a List



Array-Based List Operations

- `first()`

Array-Based List Operations

- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`

Array-Based List Operations

- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`
- `last()`

Array-Based List Operations

- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`
- `last()`
 - ▶ Return the reference that is stored in index `size - 1` of the array `items`

Array-Based List Operations

- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`
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 - ▶ Return the reference that is stored in index `size - 1` of the array `items`
- `size()`

Array-Based List Operations

- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`
- `last()`
 - ▶ Return the reference that is stored in index `size - 1` of the array `items`
- `size()`
 - ▶ Return the value of the `size` variable

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- `first()`
 - ▶ Return the reference that is stored in index 0 of the array `items`
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 - ▶ Return the reference that is stored in index `size - 1` of the array `items`
- `size()`
 - ▶ Return the value of the `size` variable
- `isEmpty()`

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 - ▶ Return the reference that is stored in index 0 of the array `items`
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- `isEmpty()`
 - ▶ Return the result of the expression `size == 0`

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 - ▶ Return the reference that is stored in index 0 of the array `items`
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- `after(p)`

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- `after(p)`
 - ▶ Convert `p` to a `ArrPos` object

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 - ▶ Access the index stored in `p`

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- `after(p)`
 - ▶ Convert `p` to a `ArrPos` object
 - ▶ Access the index stored in `p`
 - ▶ Return the `ArrPos` object stored in index $+ 1$ in the array `items`

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 - ▶ Convert `p` to a `ArrPos` object
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- `before(p)`

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- `after(p)`
 - ▶ Convert `p` to a `ArrPos` object
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 - ▶ Access the index stored in `p`
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- `before(p)`
 - ▶ Convert `p` to a `ArrPos` object
 - ▶ Access the index stored in `p`
 - ▶ Return the `ArrPos` object stored in index `- 1` in the array `items`

Array-Based List

Array Size

- When we implemented this using the links, the list had an infinite capacity

Array-Based List

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 - ▶ Every time we try to insert and there is no space we create a new array which is double the size

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Array Size

- When we implemented this using the links, the list had an infinite capacity
- However, arrays cannot grow infinitely
- Therefore we must replace the array every time that it runs out of room
- There are many strategies for resizing the array, we will use this one
 - ▶ Every time we try to insert and there is no space we create a new array which is double the size
 - ▶ Every time we remove a value, if we are using less than 25% of the array we create a new array which is half the size

Array-Based List

Increasing Array Size

- Once an array is created, it is impossible for the size to be changed

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Increasing Array Size

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- However, we can create a new array and change the references, so that we point to this instead

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- This means that we only need to copy the data contained in the array and we are finished

Array-Based List

Increasing Array Size

- Once an array is created, it is impossible for the size to be changed
- However, we can create a new array and change the references, so that we point to this instead
- This means that we only need to copy the data contained in the array and we are finished
- We might want to use this in multiple locations, so we will implement it as a private method in the class

Array-Based List

Grow Method

- The steps we must follow are:

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Grow Method

- The steps we must follow are:
 - ▶ Create a new array that is twice the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Multiply the value of `maxSize` by 2

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Grow Method

- The steps we must follow are:
 - ▶ Create a new array that is twice the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Multiply the value of `maxSize` by 2
 - ▶ Copy the reference of the new array into the variable `items`

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- The steps we must follow are:
 - ▶ Create a new array that is twice the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Multiply the value of `maxSize` by 2
 - ▶ Copy the reference of the new array into the variable `items`

```
1 private void grow(){
2     ArrPos[] a = new ArrPos[maxSize*2];
3     for (int i = 0; i < items.length; i++) {
4         a[i] = items[i];
5     }
6     maxSize = maxSize * 2;
7     items = a;
8 }
```

Array-Based List

Shrink Method

- Similar to the grow method we will also write one for shrinking, it has the following steps

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- Similar to the grow method we will also write one for shrinking, it has the following steps
 - ▶ Create a new array that is half the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Divide the value of `maxSize` by 2

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Shrink Method

- Similar to the grow method we will also write one for shrinking, it has the following steps
 - ▶ Create a new array that is half the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Divide the value of `maxSize` by 2
 - ▶ Copy the reference of the new array into the variable `items`

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 - ▶ Create a new array that is half the previous maximum size
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Shrink Method

- Similar to the grow method we will also write one for shrinking, it has the following steps
 - ▶ Create a new array that is half the previous maximum size
 - ▶ Copy the references of all objects to the new array
 - ▶ Divide the value of `maxSize` by 2
 - ▶ Copy the reference of the new array into the variable `items`

```
1 private void shrink(){
2     ArrPos[] a = new ArrPos[maxSize/2];
3     for (int i = 0; i < size; i++) {
4         a[i] = items[i];
5     }
6     maxSize = maxSize / 2;
7     items = a;
8 }
```

Array-Based List Operations

`insertFirst(d)`

- Insert the value into the first position

Array-Based List Operations

`insertFirst(d)`

- Insert the value into the first position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index 0

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`insertFirst(d)`

- Insert the value into the first position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index 0
 - ▶ Copy all `ArrPos` objects into the position next in the array and increment the index in each

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`insertFirst(d)`

- Insert the value into the first position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index 0
 - ▶ Copy all `ArrPos` objects into the position next in the array and increment the index in each
 - ▶ Copy the reference of `n` to index 0 in the array

Array-Based List Operations

insertFirst(d)

- Insert the value into the first position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index 0
 - ▶ Copy all `ArrPos` objects into the position next in the array and increment the index in each
 - ▶ Copy the reference of `n` to index 0 in the array
 - ▶ Increment the size

Array-Based List Operations

insertFirst(d)

data		index		data		index		data		index		data		index					
A		0		B		1		C		2		D		3					

Array-Based List Operations

insertFirst(d)

data	index	data	index	data	index	data	index	data	index		
A	0	B	1	C	2	D	4	D	4		

Array-Based List Operations

insertFirst(d)

data		index		data		index		data		index		data		index			
A		0		B		1		C		3		C		3		D	
																4	

Array-Based List Operations

insertFirst(d)

data		index		data		index		data		index		data		index			
A		0		B		2		B		2		C		3		D	

Array-Based List Operations

insertFirst(d)

data		index		data		index		data		index		data		index		data		index			
A		1		A		1		B		2		C		3		D		4			

Array-Based List Operations

insertFirst(d)

data		index		data		index		data		index		data		index		data		index			
X		0		A		1		B		2		C		3		D		4			

Array-Based List Operations

insertFirst(d)

```
1 Algorithm insertFirst (v):  
2   Input: The value to be inserted  
3   Output: The position it was inserted in  
4  
5   if size = maxSize then  
6     grow()  
7   Create ArrPos n containing v with index 0  
8   for every integer value i in the range size  
9     to 1 (inclusive) do  
10     items[i] ← items[i - 1]  
11     items[i].incrementIndex()  
12   items[0] ← n  
13   size ← size + 1  
14   return n
```

Array-Based List Operations

`insertLast(d)`

- Insert the value into the last position

Array-Based List Operations

`insertLast(d)`

- Insert the value into the last position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index size

Array-Based List Operations

`insertLast(d)`

- Insert the value into the last position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index size
 - ▶ Copy the reference of `n` to index size in the array

Array-Based List Operations

`insertLast(d)`

- Insert the value into the last position
 - ▶ Construct a new `ArrPos` object, called `n`, containing the value and the index size
 - ▶ Copy the reference of `n` to index size in the array
 - ▶ Increment the size

Array-Based List Operations

insertLast(d)

data		index		data		index		data		index		data		index					
A		0		B		1		C		2		D		3					

Array-Based List Operations

insertLast(d)

data		index		data		index		data		index		data		index		data		index			
A		0		B		1		C		2		D		3		X		4			

Array-Based List Operations

insertLast(d)

```
1 Algorithm insertLast (v):  
2   Input: The value to be inserted  
3   Output: The position it was inserted in  
4  
5   if size = maxSize then  
6     grow()  
7   Create ArrPos n containing v with index size  
8   items[size] ← n  
9   size ← size + 1  
10  return n
```

Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p

Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p
 - ▶ Convert p to an `ArrPos` object

Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy the index from `p` to a variable called `n`

Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p
 - ▶ Convert p to an `ArrPos` object
 - ▶ Copy the index from p to a variable called n
 - ▶ Copy all `ArrPos` objects in the array after p one index down and increment their index

Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy the index from `p` to a variable called `n`
 - ▶ Copy all `ArrPos` objects in the array after `p` one index down and increment their index
 - ▶ Create a new `ArrPos` object containing the data and the index `n + 1`

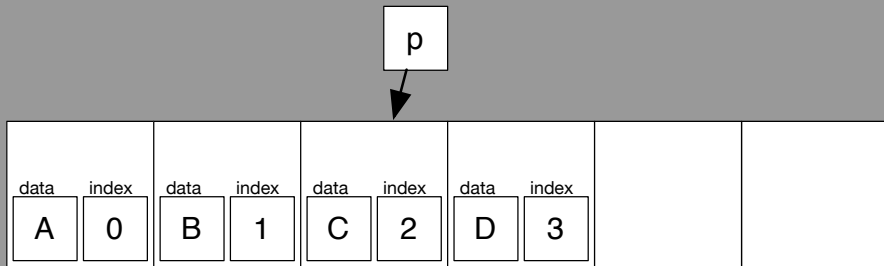
Array-Based List Operations

`insertAfter(p, d)`

- Insert the value into the position after p
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy the index from `p` to a variable called `n`
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 - ▶ Create a new `ArrPos` object containing the data and the index `n + 1`
 - ▶ Increment the size

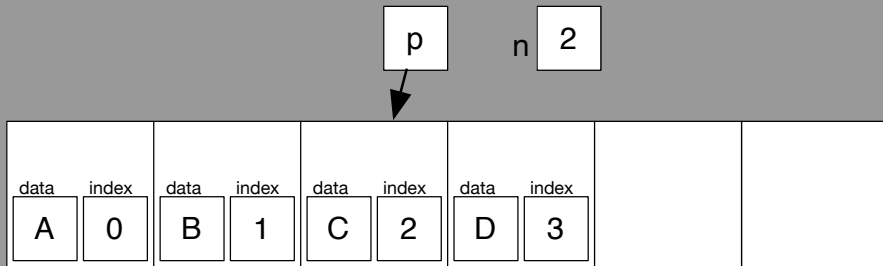
Array-Based List Operations

`insertAfter(p, d)`



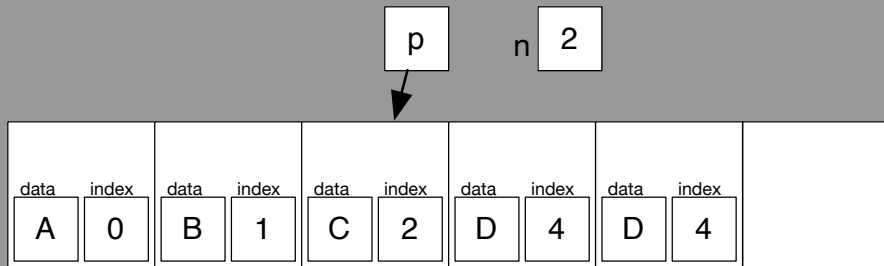
Array-Based List Operations

insertAfter(p, d)



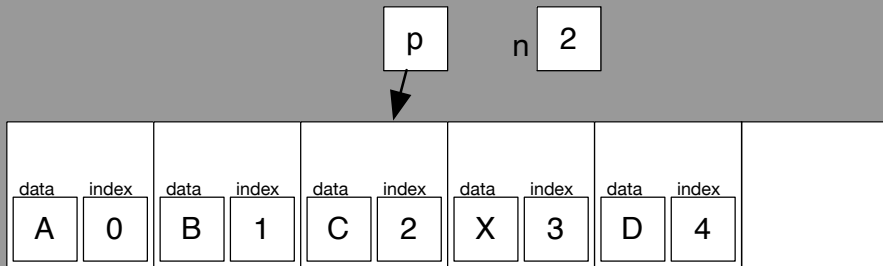
Array-Based List Operations

insertAfter(p, d)



Array-Based List Operations

insertAfter(p, d)



Array-Based List Operations

insertAfter(p, d)

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1 Algorithm insertAfter (p, v):
2   Input: The value to be inserted and the
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4   if size = maxSize then
5     grow()
6   n ← p.getIndex()
7   for every integer value i in the range size
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8     items[i] ← items[i - 1]
9     items[i].incrementIndex()
10  Create new ArrPos object, called a,
      containing data and index n+1
11  items[n+1] ← a
12  size ← size + 1
13  return a
```

Array-Based List Operations

`insertBefore(p, d)`

- Insert the value into the position before p

Array-Based List Operations

`insertBefore(p, d)`

- Insert the value into the position before p
 - ▶ Convert `p` to an `ArrPos` object

Array-Based List Operations

`insertBefore(p, d)`

- Insert the value into the position before p
 - ▶ Convert p to an `ArrPos` object
 - ▶ Copy the index from p to a variable called n

Array-Based List Operations

`insertBefore(p, d)`

- Insert the value into the position before p
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy the index from `p` to a variable called `n`
 - ▶ Copy all `ArrPos` objects in the array after and including `p` one index down and increment their index

Array-Based List Operations

`insertBefore(p, d)`

- Insert the value into the position before p
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy the index from `p` to a variable called `n`
 - ▶ Copy all `ArrPos` objects in the array after and including `p` one index down and increment their index
 - ▶ Create a new `ArrPos` object containing the data and the index `n`

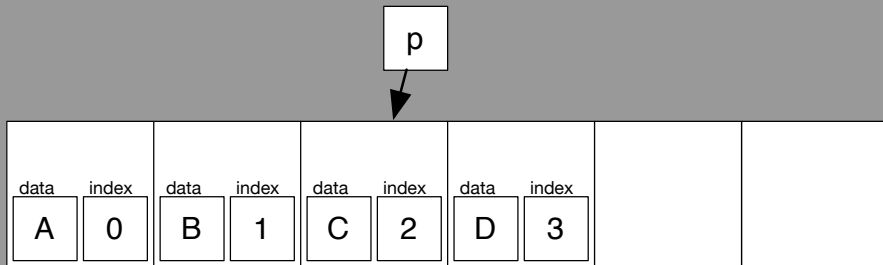
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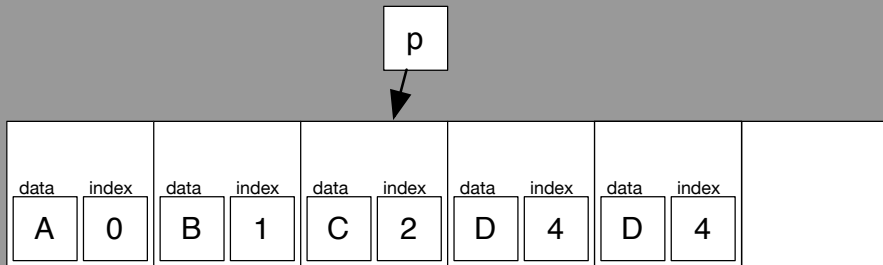
Array-Based List Operations

insertBefore(p, d)



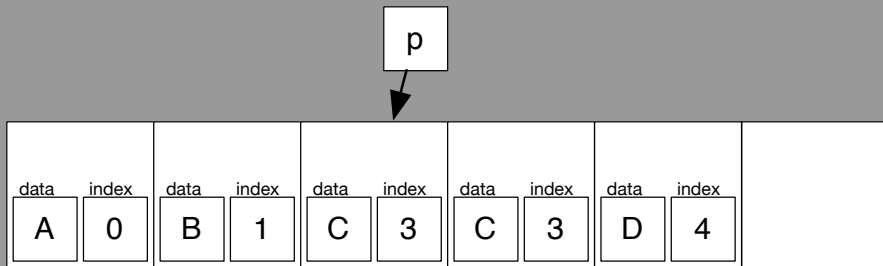
Array-Based List Operations

insertBefore(p, d)



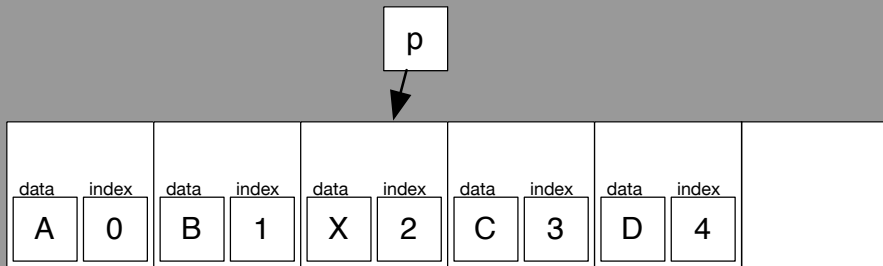
Array-Based List Operations

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Array-Based List Operations

insertBefore(p, d)



Array-Based List Operations

insertBefore(p, d)

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4   if size = maxSize then
5     grow()
6   n ← p.getIndex()
7   for every integer value i in the range size
      to n do
8     items[i] ← items[i - 1]
9     items[i].incrementIndex()
10  Create new ArrPos object, called a,
      containing data and index n
11  items[n] ← a
12  size ← size + 1
13  return a
```

Array-Based List Operations

`remove(p)`

- Remove the value from the list

Array-Based List Operations

`remove(p)`

- Remove the value from the list
 - ▶ Convert `p` to an `ArrPos` object

Array-Based List Operations

`remove(p)`

- Remove the value from the list
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy value from `p`

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`remove(p)`

- Remove the value from the list
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy value from `p`
 - ▶ Copy the index from `p` to a variable called `n`

Array-Based List Operations

`remove(p)`

- Remove the value from the list
 - ▶ Convert `p` to an `ArrPos` object
 - ▶ Copy value from `p`
 - ▶ Copy the index from `p` to a variable called `n`
 - ▶ Copy all `ArrPos` objects in the array after `p` one index lower and decrement their index

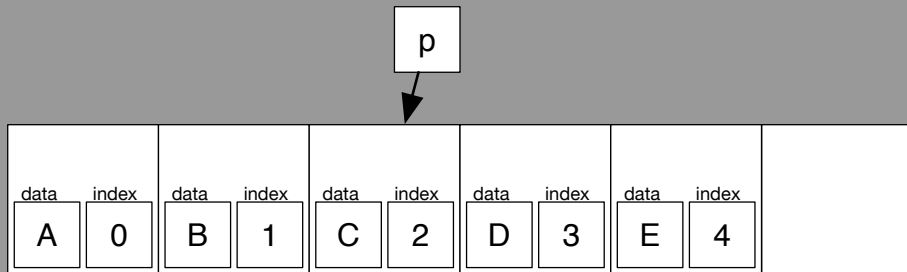
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 - ▶ Decrement the size

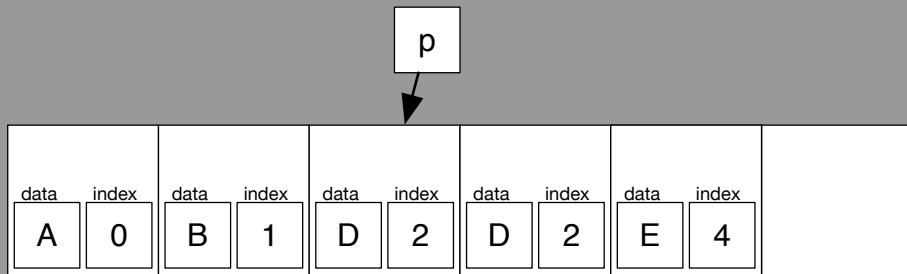
Array-Based List Operations

remove(p)



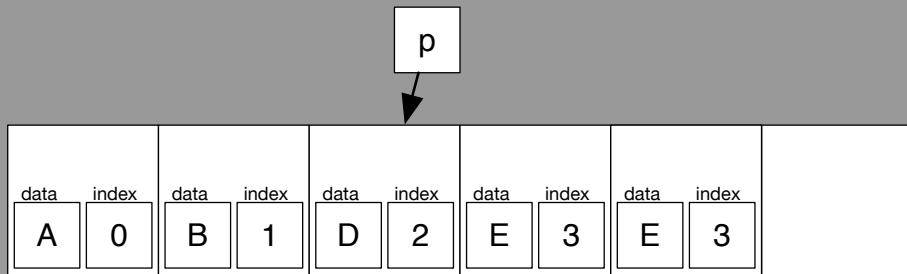
Array-Based List Operations

remove(p)



Array-Based List Operations

remove(p)



Array-Based List Operations

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1 Algorithm remove (p):
2   Input: The position to be removed from the
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5   n ← p.getIndex()
6   a ← p.element()
7   for every integer value i in the range n to
      size do
8       items[i] ← items[i + 1]
9       items[i].decrementIndex()
10  size ← size - 1
11  if size < maxSize/4 then
12      shrink()
13  return a
```

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insertFirst(d)

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5   if size = maxSize then  
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7   Create ArrPos n containing v with index 0  
8   for every integer value i in the range size  
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- Complexity is $O(1)$

Algorithmic Complexity

insertAfter(p, d)

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1 Algorithm insertAfter (p, v):  
2   Input: The value to be inserted and the position it  
   should be inserted after  
3   Output: The position it was inserted in  
4   if size = maxSize then  
5     grow()  
6   n ← p.getIndex()  
7   for every integer value i in the range size to n + 1 do  
8     items[i] ← items[i - 1]  
9     items[i].incrementIndex()  
10  Create new ArrPos object, called a, containing data and  
   index n+1  
11  items[n+1] ← a  
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Algorithmic Complexity

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2   Input: The position to be removed from the list  
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7   for every integer value i in the range n to size do  
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9     items[i].decrementIndex()  
10  size ← size - 1  
11  if size < maxSize/4 then  
12    shrink()  
13  return a
```

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