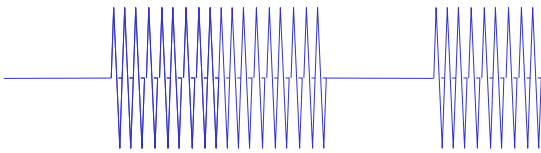


Bandpass Digital Modulation

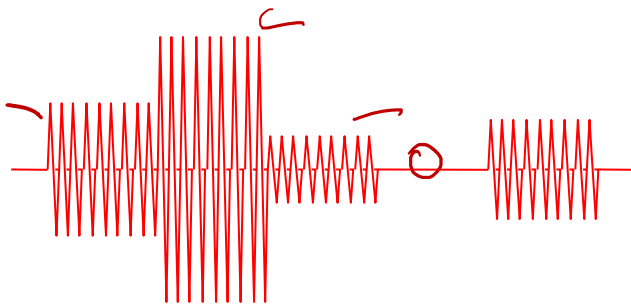
DiscreteS

modulating on to a carrier

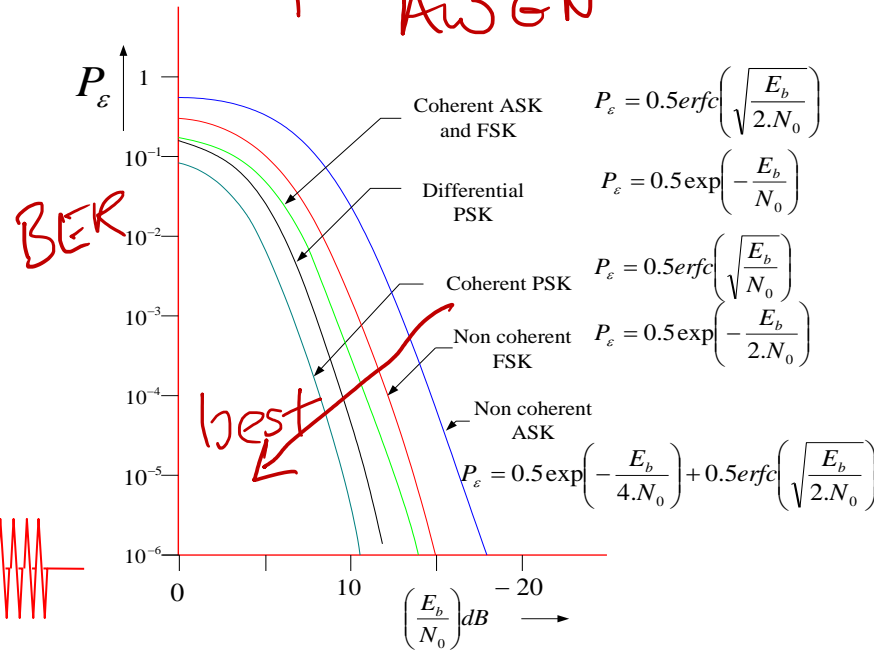
Amplitude shift keying



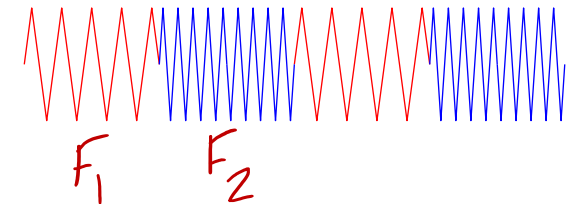
multi-level ASK



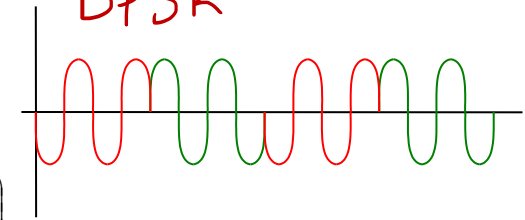
Performance in
AWGN



FSK



BPSK



Digital Modulation

Mathematical Background: Orthogonality

(1)

- Two signals $a_i(t)$ and $a_j(t)$ are said to be orthogonal if:

$$\left[\int_0^{T_s} a_i(t) \cdot a_j(t) \cdot dt = 0 \right]_{i \neq j}$$

- Examples of orthogonal signals are:

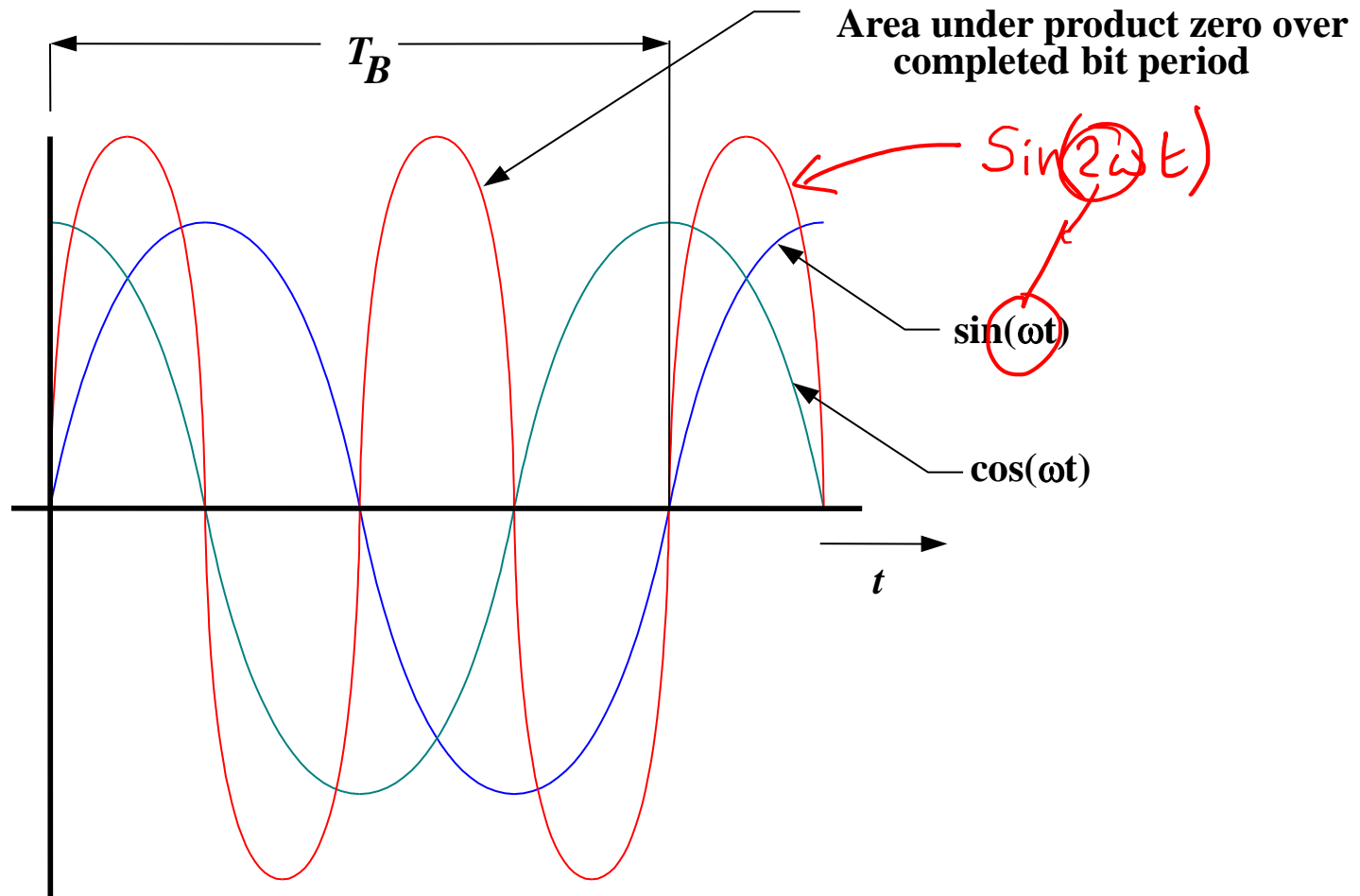
$$a_i(t) = \cos(2\pi f_i t) \text{ and } a_j(t) = \sin(2\pi f_j t)$$

$$a_i(t) = \cos(2\pi f_i t) \text{ and } a_j(t) = \cos(2\pi f_j t)$$

$$\text{where } f_i, f_j = \{1, 2, 3, \dots\}; f_i \neq f_j \quad \cos f_c \quad \cos 2f_c \quad \cos 3f_c$$



Mathematical Background: Orthogonality (2)



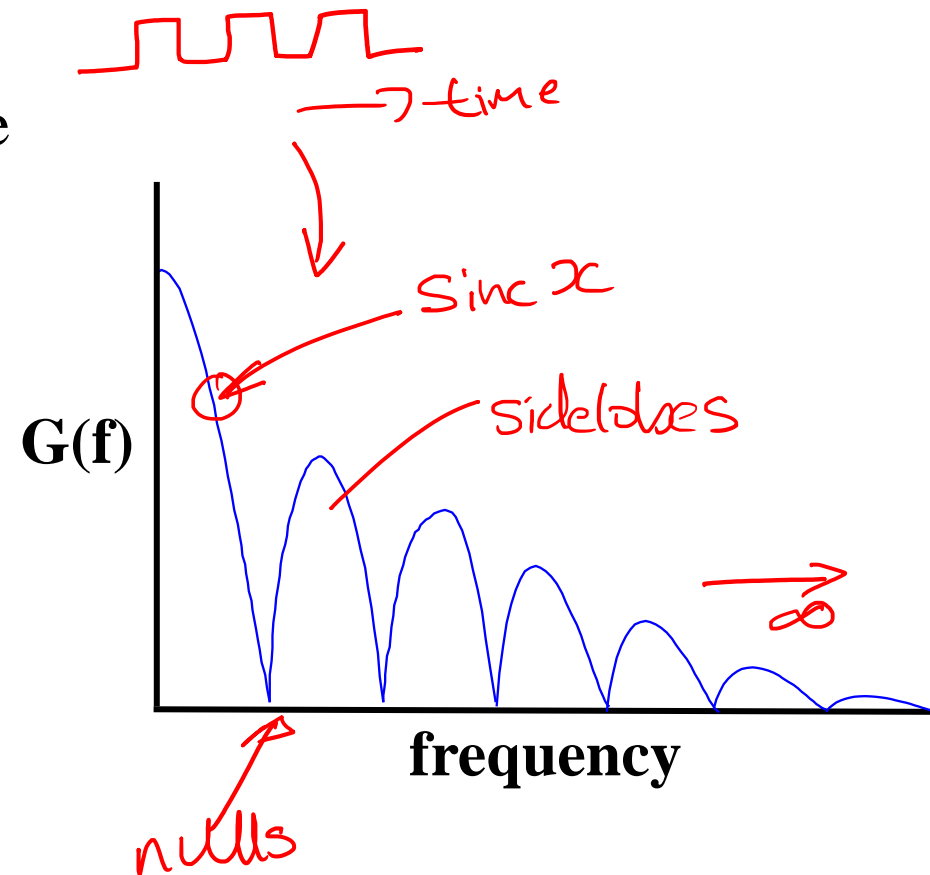
Mathematical Background:

Spectrum of a Baseband Square Wave

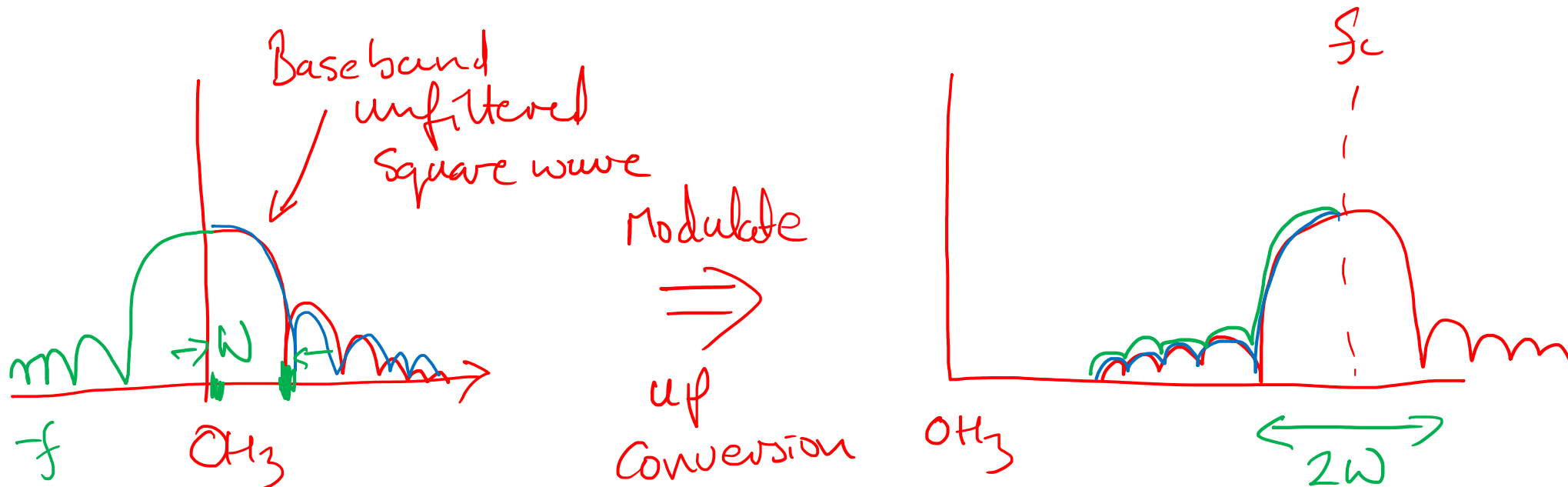
- It can be shown by fourier analysis that the spectrum of a (baseband) square wave signal is described by a sinc or $\sin(x)/x$ function:

$$G(f) = T.A. \left[\frac{\sin(\pi.f.T)}{\pi.f.T} \right]$$

- This spectrum extends to infinity. It is often necessary to apply a pulse shaping (band limiting) filter to this signal.



Baseband to Bandpass Spectrum



Bandpass and Baseband Signalling

- With baseband signalling the channel is assumed to extend from 0Hz upwards.
- Transmitting this type of data over conventional media, such as radio channels, requires a shift in frequency.
 - This process is called ‘carrier modulation’ or just ‘modulation’.
- Often the process of modulation takes a band of signals based on zero Hz and shifts them to occupy twice the bandwidth centred on a carrier frequency.
- A corresponding ‘demodulation’ or ‘detection’ process is required to recover the data.



Carrier Modulation (1)

- The carrier signal is typically a sine wave. The transmitted signal can be described by:

$$s(t) = A \cos(\omega t + \theta)$$

- This signal has three properties which we can modulate.
 - Amplitude, A .
 - Frequency, ω .
 - Phase, θ .
- Initially we will consider modulation schemes which modulates only one of these three properties.
- Also, we will first consider binary modulation schemes. M-ary modulation will be covered later.

Carrier Modulation (2)

- If we modulate just one property of the signal, we can modulate our data signal onto this carrier signal in one of three ways:
 - By modulating the amplitude of the carrier wave. Thus, A is a function of the modulating signal. This is known as Amplitude Shift Keying (ASK).
 - By modulating the frequency of the carrier wave. Thus, ω , is a functions of the modulating signal. This is known as Frequency Shift Keying (FSK)
 - By modulating the phase of the carrier wave. Thus, θ , is a function of the modulating signal. This is known as Phase Shift Keying (PSK)

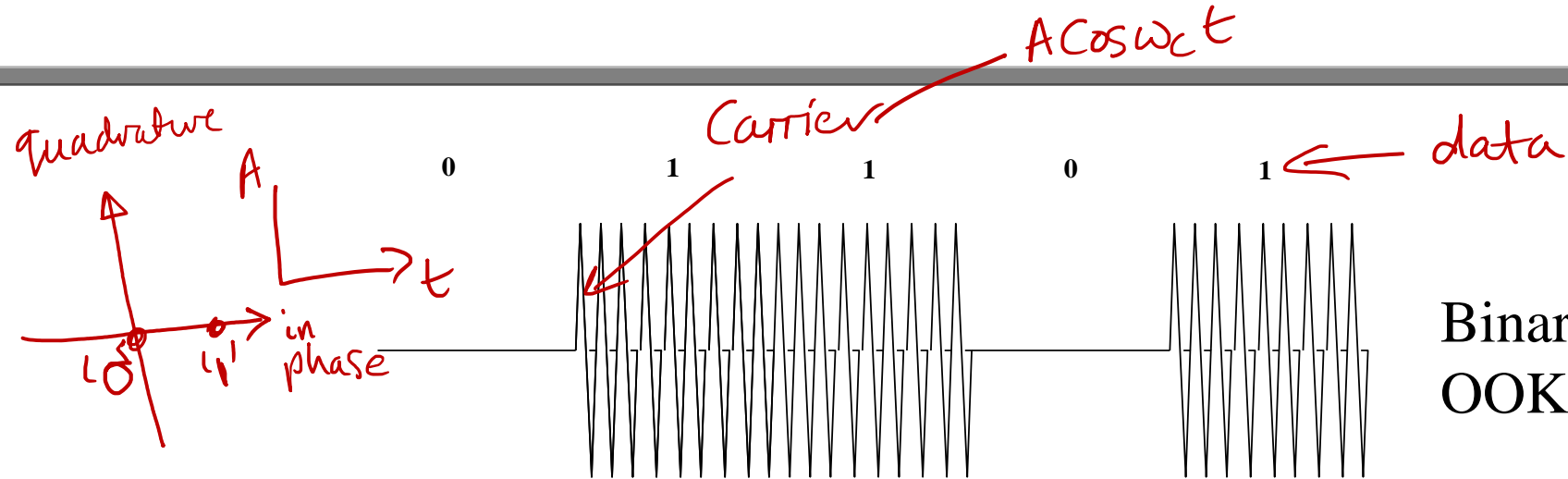
Amplitude Shift Keying (ASK) Generation

Amplitude Shift Keying (ASK)

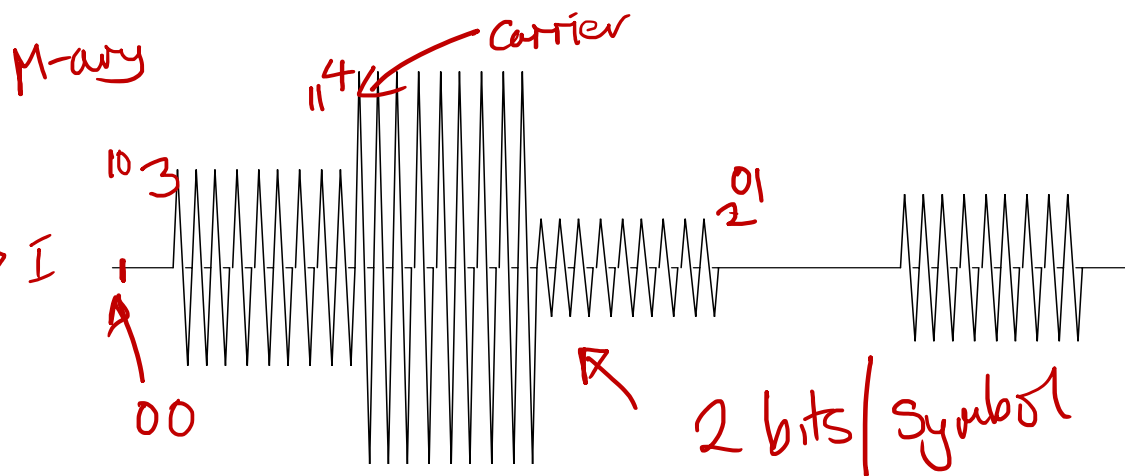
- The simplest form of bandpass modulation is Amplitude Shift Keying (ASK). With this modulation the data is represented as various (discrete) amplitude levels of a fixed frequency carrier.
- The simplest form of ASK is to switch a fixed frequency oscillator ON for a 'one', and OFF for a 'zero'. This is known as ON-OFF KEYING (OOK).
- If more than two symbol states are used, then M-ary ASK is generated.



Amplitude Shift Keying (ASK)



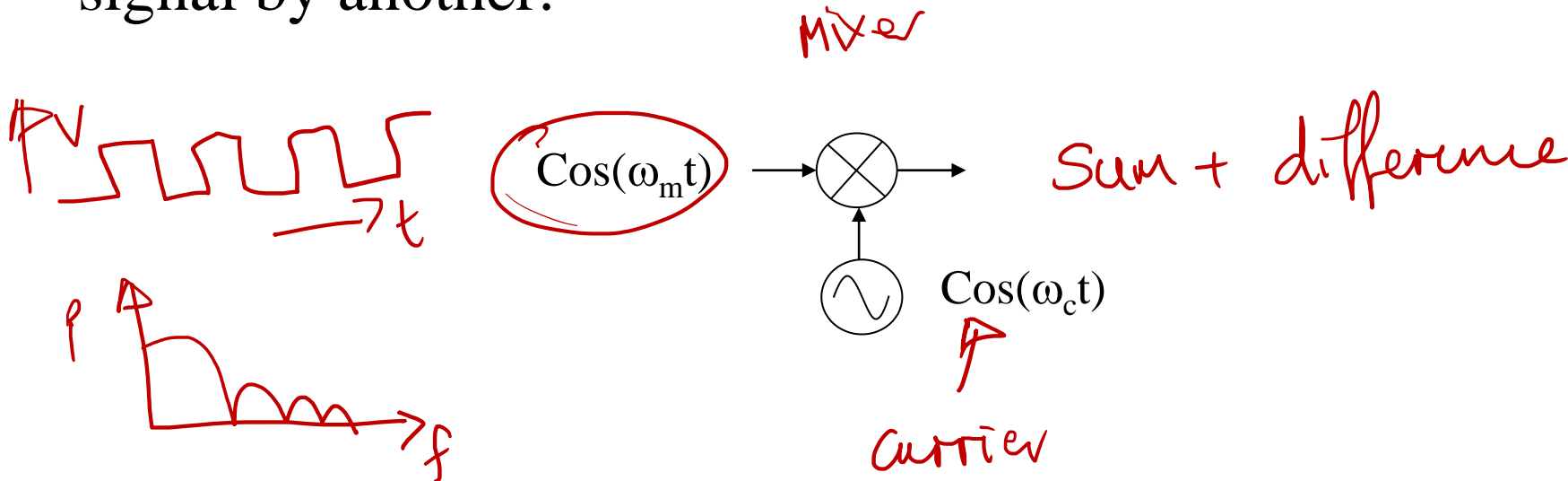
Binary ASK or
OOK



M-ary
ASK

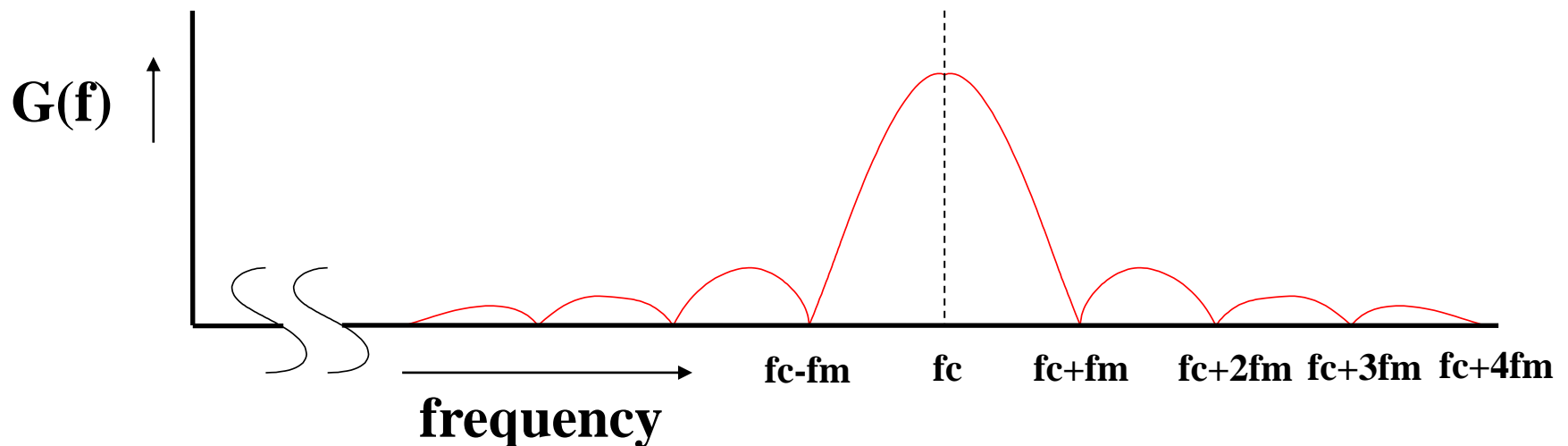
ASK Spectrum (1)

- The spectrum of an ASK signal can be calculated using trig identities.
- Amplitude modulation is essentially the multiplication of one signal by another.



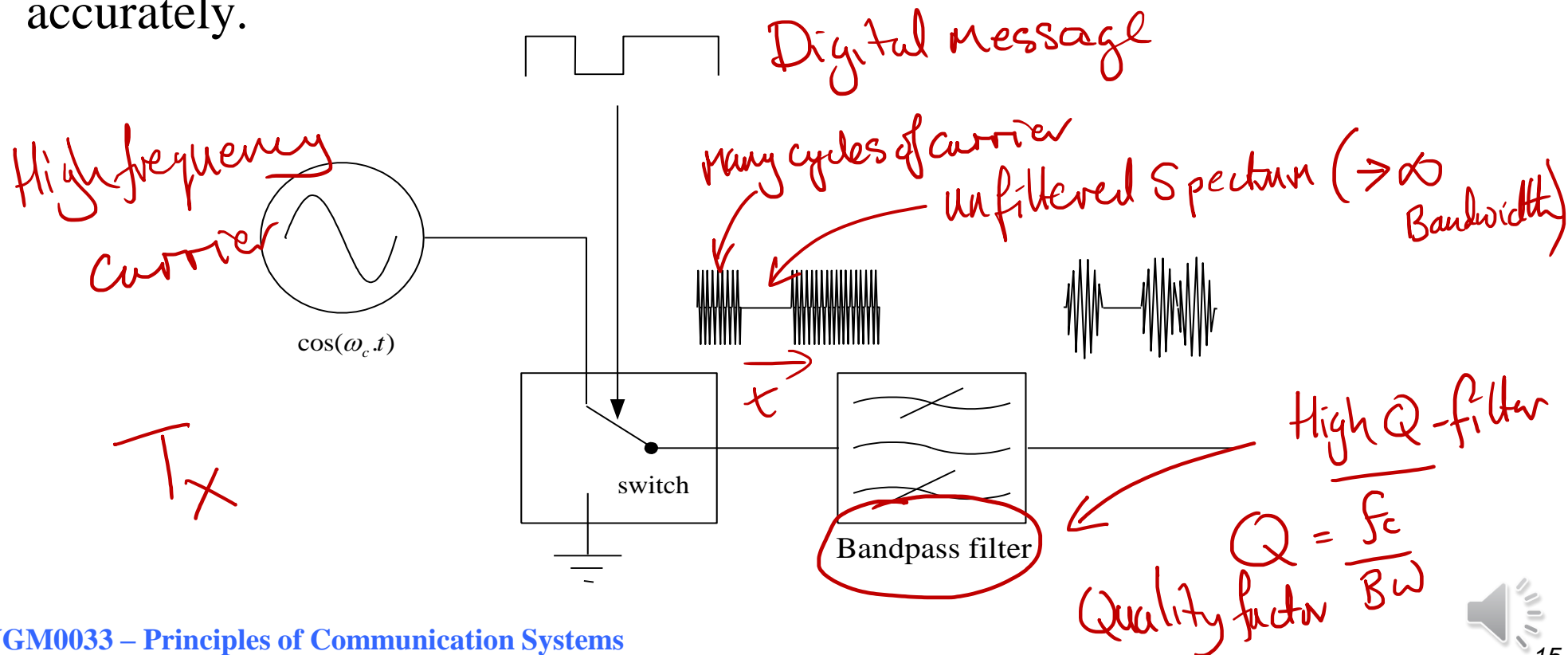
ASK spectrum (2)

- Note that the spectrum is two sided, and therefore the bandwidth required to transmit it is $2 \cdot \omega_m$. That is, **twice the baseband bandwidth**. Spectral efficiency is limited to **1 bit/s/Hz**.
- For square wave modulated ASK the spectrum takes the form:



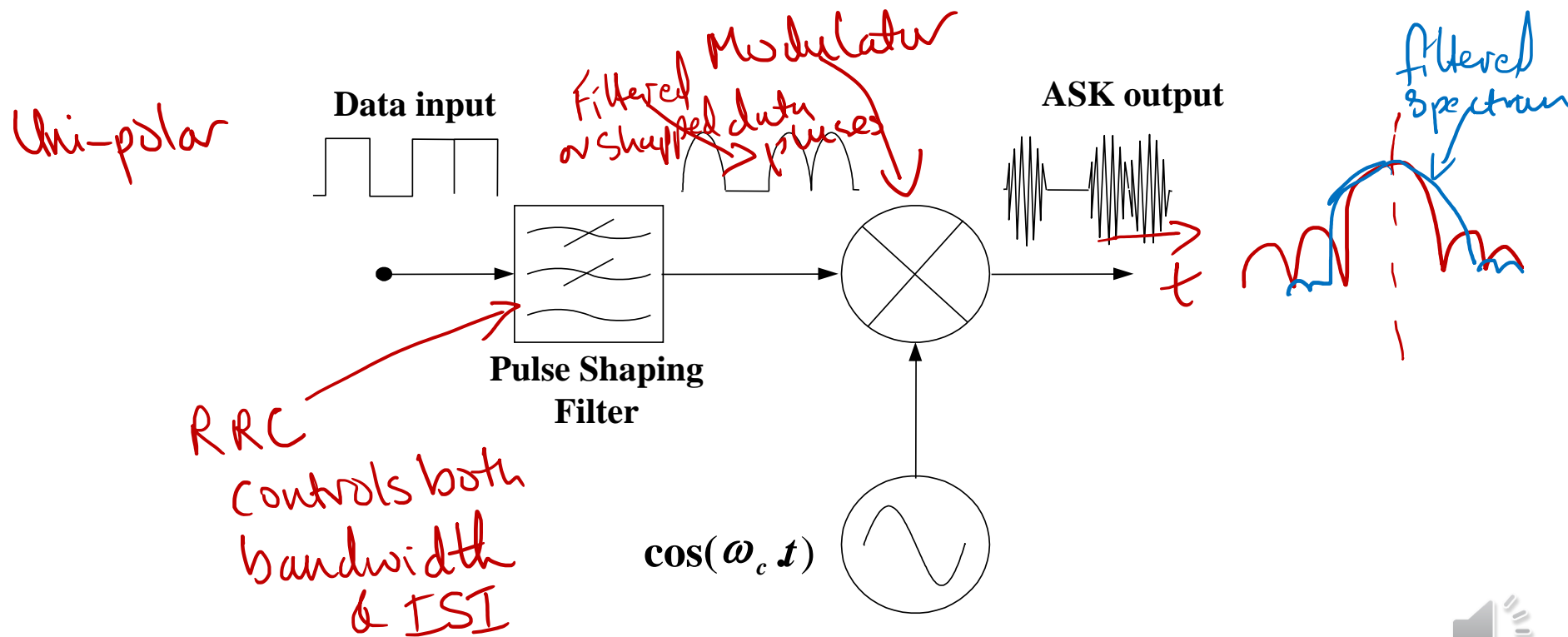
Generation of ASK (1)

- This diagram illustrates one way in which an ASK signal may be generated. However, bandpass filtering at RF is very difficult to achieve accurately.



Generation of ASK (2)

- Another method (one we have already discussed), is to multiply a carrier signal by the baseband signal stream. The multiplier is known as a mixer.



Amplitude Shift Keying (ASK) Detection

Detection of ASK

- Two methods are available for recovering the base band data stream from ASK.
- The process of recovering the baseband signal is known as demodulation.
- Alternatively it is known as detection.
- The methods fall under the headings ‘coherent’ and ‘non coherent’ detection.

↳ envelope detector

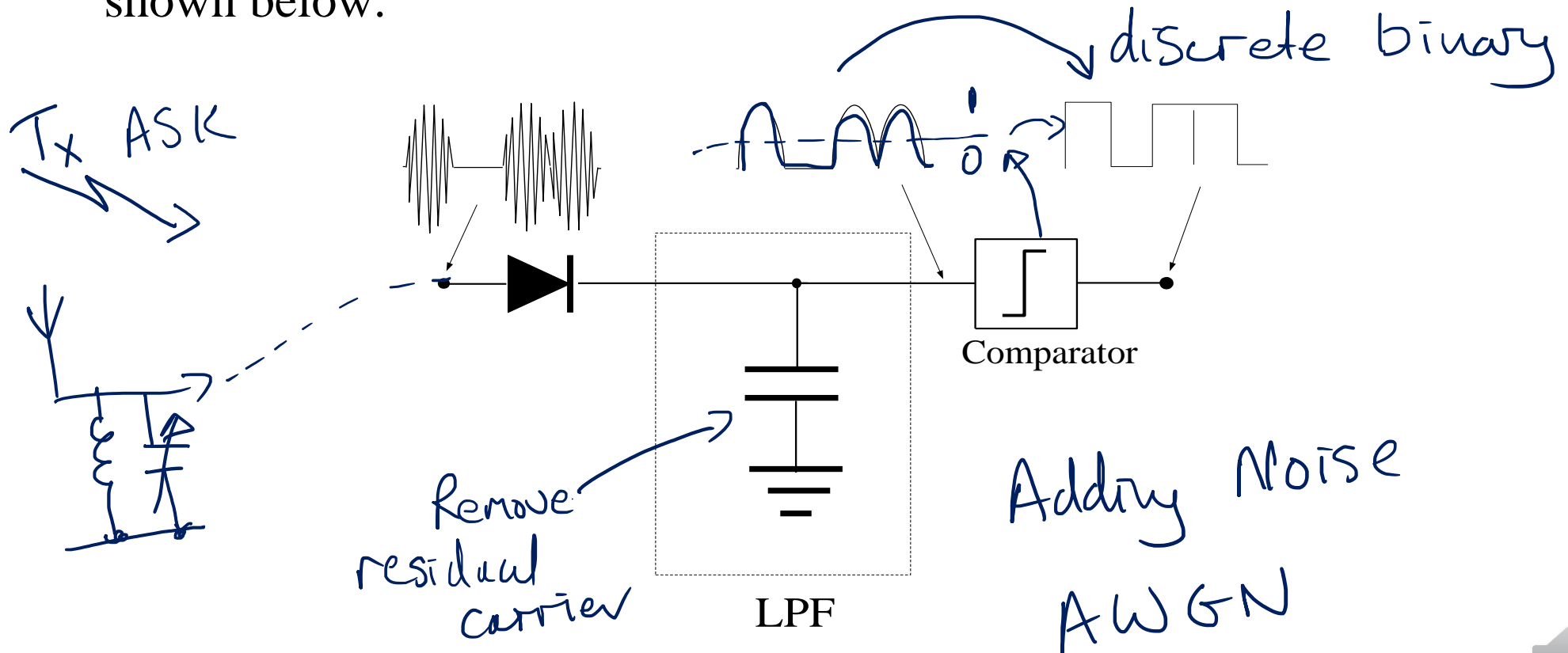
↗ Needs a local oscillator (LO)



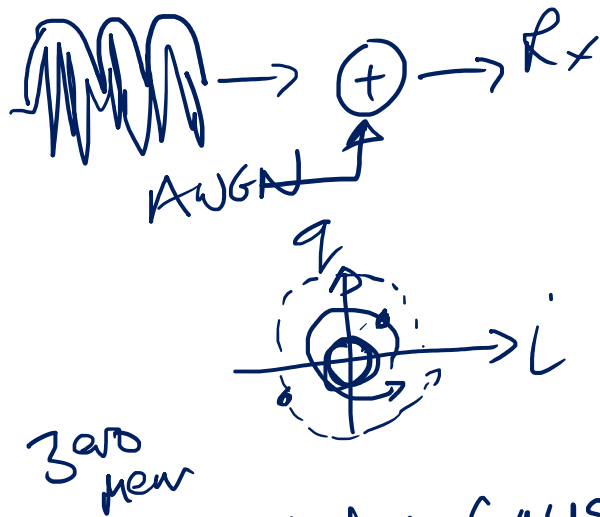
Non Coherent Detection of ASK (1)

R_x

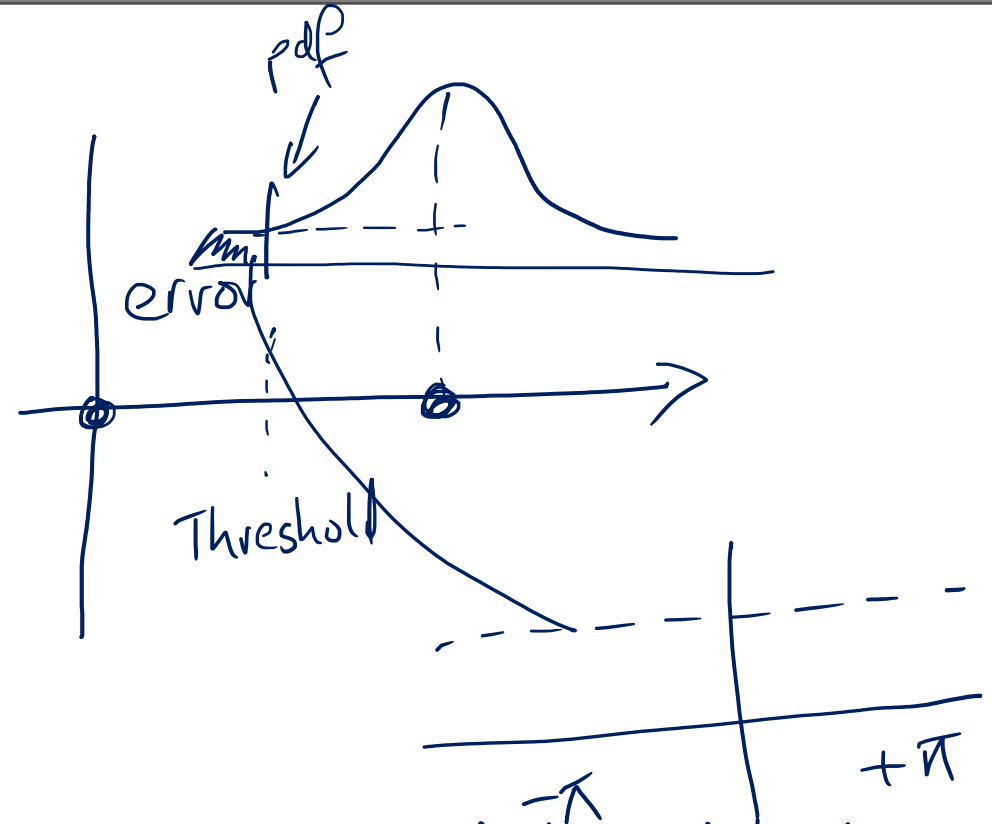
- Non coherent detection of ASK is straight forward. A circuit to do this is shown below.



AWGN in Non Coherent Detection of ASK



Amplitude is Gaussian
phase is uniform random
0 to 2π
exists in both in-phase & quadrature



Diode will detect both
inphase & quadrature noise
with respect to the carrier



Non-Coherent Detection of ASK (2)

- The simplicity of this approach is often outweighed by the inability of a non-coherent detector to extract signal from noise.
- A coherent detector can do this and can achieve a lower Bit Error Rate (BER) over the same channel, with the same S/N ratio.

↖ E_b/N_0

Coherent Detection (1)

ASK

- Coherent detection requires the local generation of a replica of the carrier signal. LO

- If a **local carrier** is available, then the reverse process to modulation can be performed at the receiver. LO

- Essentially the **locally generated carrier** is multiplied by the **incoming signal**. Thus:

$$\overset{\text{rx signal}}{A(t)\cos(\omega_c t)} \bullet \overset{\text{LO}}{\cos(\omega_c t + \theta)} = \underset{\text{DC}}{0.5A(t)\cos(\theta)} + \underset{\text{SUM}}{0.5A(t)\cos(2\omega_c t + \theta)}$$

phase offset between Tx & Rx (pointing to θ)

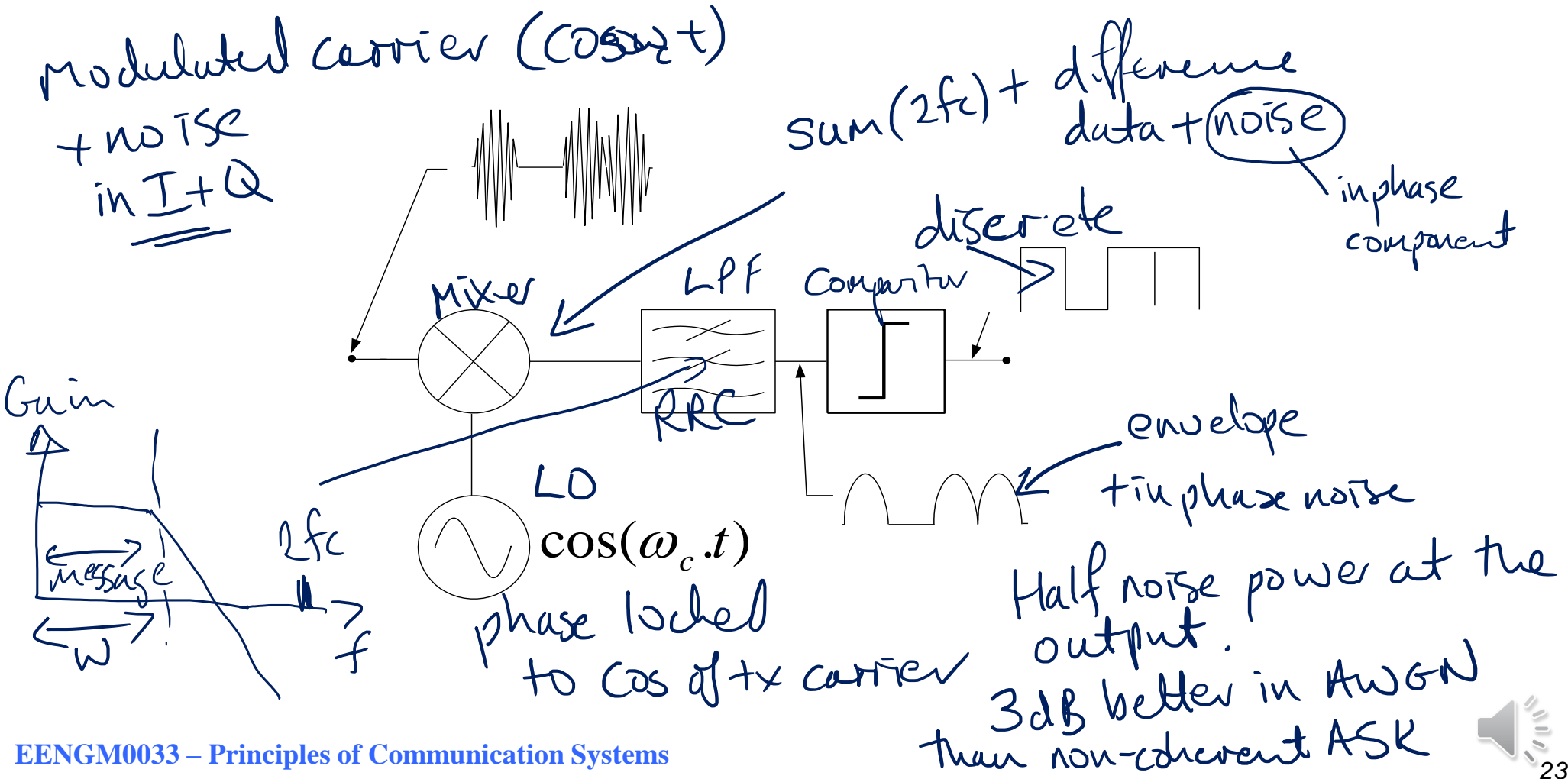
twice carrier frequency (pointing to $2\omega_c t$)

- The process results in two output components. One is the **baseband message signal** (multiplied by a $\cos(\theta)$ term) and the other is the **baseband message signal shifted to twice the carrier frequency**.

phase error

Coherent Detection (3)

ASK (R_x)



Coherent Detection (2)

- By passing these two products through a low pass filter, the higher frequency component can be removed. Thus only $A(t)\cos(\theta)$ is left. PLL
- θ defines the phase error between the locally generated carrier and the received carrier. Any non-zero value of θ (i.e. any phase error) causes a loss in performance since $\cos(\theta) < 1$.
- Thus, it is crucial for coherent detection to be able to accurately generate the local carrier signal.
- One way to do this is to use a Phase Lock Loop (PLL).

AWGN and Coherent Detection of ASK

$$\left[A_n \cos \omega_c t + A_n \sin \omega_c t \right] \cdot \cos \omega_c t$$

$$\rightarrow = A_n \cos \omega_c t \cdot \cos \omega_c t + A_n \sin \omega_c t \cdot \cos \omega_c t$$

$$\frac{A_n}{2} \left[\underbrace{\cos(\omega_c t - \omega_c t)}_{\substack{\cos 0 \\ = 1}} + \underbrace{\cos(\omega_c t + \omega_c t)}_{\substack{2\omega_c t \text{ LPF}}} + \underbrace{\sin(\omega_c t - \omega_c t)}_{\substack{\sin 0 \\ = 0}} + \underbrace{\sin(\omega_c t + \omega_c t)}_{\substack{2\omega_c t \text{ LPF}}} \right]$$

only detects "in-phase"
noise component.

No Quadrature
noise after
coherent mixer

