

# Versatile Robust Clustering of Ad Hoc Cognitive Radio Network

Di Li, *Member, IEEE*, Erwin Fang, and James Gross, *Member, IEEE*

**Abstract**—Cluster structure in cognitive radio networks facilitates cooperative spectrum sensing, routing and other functionalities. The unlicensed channels, which are available for every member of a group of cognitive radio users, consolidate the group into a cluster, and the availability of unlicensed channels decides the robustness of that cluster against the licensed users' influence. This paper analyses the problem that how to form robust clusters in cognitive radio network, so that more cognitive radio users can get benefits from cluster structure even when the primary users' operation are intense. We provide a formal description of robust clustering problem, prove it to be NP-hard and propose a centralized solution, besides, a distributed solution is proposed to suit the dynamics in the ad hoc cognitive radio network. Congestion game model is adopted to analyse the process of cluster formation, which not only contributes designing the distributed clustering scheme directly, but also provides the guarantee of convergence into Nash Equilibrium and convergence speed. Our proposed clustering solution is versatile to fulfill some other requirements such as faster convergence and cluster size control. The proposed distributed clustering scheme outperforms the related work in terms of cluster robustness, convergence speed and overhead. The extensive simulation supports our claims.

**Index Terms**—cognitive radio, robust cluster, game theory, congestion game, distributed, centralised, cluster size control.

## 1 INTRODUCTION

COGNITIVE radio (CR) is a promising technology to solve the spectrum scarcity problem [1]. Licensed users access the spectrum allocated to them whenever there is information to be transmitted. In contrast, as one way, unlicensed users can access the spectrum via opportunistic spectrum access, i.e., they access the licensed spectrum only after validating the channel is unoccupied by licensed users, where spectrum sensing [2] plays an important role in this process. In this hierarchical spectrum access model [3], the licensed users are also called primary users (PU), while the unlicensed users are referred to as secondary users and constitute the cognitive radio networks (CRN). Regarding to the operation of CRN, efficient spectrum sensing is identified to be critical for a smooth operation of a cognitive radio network [4]. This can be achieved by cooperative spectrum sensing of multiple secondary users, which has been shown to cope effectively with noise uncertainty and channel fading, thus remarkably improving the sensing accuracy [5]. Collaborative sensing relies on the

consensus of CR users<sup>1</sup> within a certain area, in this regard, clustering is regarded as an effective method to realize cooperative spectrum sensing [6], [7]. Clustering is also efficient to coordinate the channel switch operation when primary users are detected by at least one CR node residing in the cluster. The cluster head (CH) can enable all the CR devices within the same cluster to stop payload transmission swiftly on the operating channel and to vacate the channel [8]. In addition to the collaborate sensing advantage, the use of clusters is beneficial as it reduces the interference between cognitive clusters [9]. Clustering algorithm has also been proposed to support routing in cognitive radio networks [10].

Forming clusters is conducted in the very beginning or periodically according to the dynamics of the CRN. To form a cluster which is composed by the CR users, there should be channels available for communication within the cluster. Usually there are multiple unlicensed channels available for all the CR nodes in the cluster, which are referred to in the following of this paper as *common control channels* (CCC). Out of the available CCCs, there are always one or multiple channels which are used for the payload communication. When one or several cluster members can not use one certain CCC for example because primary user activity has been detected on that channel, it will be excluded from the set of CCCs. If the channel is being used for payload communication, all the cluster members will switch to another channel in the set of available CCCs to achieve seamless transmission. As long as there is a CCC available, the corresponding cluster can continue to exchange payload data. In the context of CRN, as the activity of primary users is unknown to the secondary users, the availability of CCCs of the formed clusters is totally dependent on primary users' activity. Thus, the clusters with more CCCs are in general better as this anticipates a longer time span payload can be exchanged. In this paper the robustness of a cluster against primary users is synonymous with the affluence of CCCs which are possessed by that cluster.

There is a trade-off between CCCs in the formation process and the collaborative sensing performance, as less members in a cluster yield in general a higher number of CCCs while this reduces the sensing accuracy [13]. In addition, there are other reasons that motivate clusters with more members. For example, instead of less members, the proper cluster size results in smaller power consumption [11], [12]. Thus the cluster robustness dis-

D. Li was with RWTH Aachen university, Germany.

Erwin. Fang is with ETH, Switzerland.

J. Gross is with KTH Royal Institute of Technology, Sweden.

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1. The terms user and node appear interchangeably in this paper. In particular, user is adopted when its networking or cognitive ability are discussed or stressed, while we refer node typically in the context of the topology.

cussed in terms of number of CCCs carries little meaning when the sizes of formed clusters are not given consideration.

In this paper, a decentralized clustering approach ROSS (RObust Spectrum Sharing) is proposed to cover the issues of robustness and size control of clusters in CRN. ROSS is able to form clusters with desired sizes, and when compared with previous works, ROSS involves smaller signalling overhead, and the generated clusters are significantly more robust against the primary users which appear after the clusters are formed. We also propose the light weighted versions of ROSS, which involve less overheads and thus are more suitable for fast deployment. Throughout this paper, we refer the clustering schemes on the basis of ROSS as *variants of ROSS*, i.e., the fast versions, or that with size control feature.

The rest of paper is organized as follows. After reviewing related work in Section 2, we present the system model in Section 3. Then the formal description of robust clustering problem in CRN and the characteristics of the problem are given in Section 4. The centralized and distributed solutions are introduced in Section 5 and 6 respectively. Extensive performance evaluation is presented in Section 7. Finally, we conclude our work and point out the direction for the future research in Section 8.

## 2 RELATED WORK

Prior to the emergence of cognitive radio, clustering has been proposed as an important method to manage network in ad hoc networks [14], [15], [16], wireless mesh networks and sensor networks [10]. In ad hoc and mesh networks, the major focus of clustering is to preserve connectivity (under static channel conditions) or to improve routing. In sensor networks, the emphasis of clustering is on longevity and coverage. Overhead generated by clustering in ad hoc network is analysed in [17], [18].

As to cognitive radio networks, clustering schemes are also proposed, which target different aspects. Work [13] improves spectrum sensing ability by grouping the CR users with potentially best detection performance into the same cluster. Clustering scheme [11] obtains the best cluster size which minimizes power consumption caused by communication within and among clusters. [11] proposes clustering strategy in cognitive radio network, which looks into the relationship between cluster size and power consumption and accordingly controlling the cluster size to decrease power consumption. Cogmesh is proposed in [19] to construct clusters with the neighbouring nodes which share local common channels. This method pays attention to the communication among the formed clusters, but cluster robustness is not considered. [20] targets on the QoS poisoning and energy efficiency. This approach first decides on the relay nodes which minimize transmission power consumption, then the chosen nodes become cluster heads and clusters are formed in a dynamic coalition process. This work emphasis on power efficiency and doesn't take into account the channel availability and the issue of robustness of the formed clusters. In [7], [21], the channel available to the largest set of one-hop neighbours is selected as common channel which yields a partition of the CRN into clusters. This approach minimizes the set of distinct frequency bands (and hence, the set of clusters) used as common channels within the CRN. However, bigger cluster sizes generally lead to less options within one cluster to switch to if the common channel is reclaimed by a primary node. Hence, this scheme does not provide robustness to formed clusters. [22] deploys cluster

structure in order to implement common channel control, medium access with multiple channel and channel allocation. The node with the maximum number of common channels within its k-hop neighborhood is chosen as cluster head, but how to avoid one node appearing in multiple clusters is not given consideration. A event-driven clustering scheme is proposed for cognitive radio sensor network in [23]. The cluster heads are selected according to node degree, spectrum availability and the distance to the sink, and the clusters are no longer available after the event ends.

Clustering robustness is considered in [24], [25], [26]. The first two propose a distributed scheme where the metric is the product of cluster size and the number of common control channels. This scheme involves both cluster size and the number of CCCs, but it is inherently flawed. With the metric, cluster could be formed only due to one factor of the two, e.g. a spectrum rich node will exclude its neighbour to form a cluster by itself. Besides, this scheme leads to a high variance on the size of clusters, which is not desired in certain applications as discussed in [11], [22]. [26] presents a heuristic method to form clusters, although the authors claim robustness is one goal to achieve, they actually uphold the minimum number of formed clusters.

## 3 SYSTEM MODEL

We consider a set of cognitive radio users  $\mathcal{N}$  and a set of primary users distributed on a two-dimensional Euclidean plane. These users share a number of non-overlapping licensed channels according to the spectrum overlay model. The set of these licensed channels is denoted as  $\mathcal{K}$ . As secondary users, the CR users are allowed to transmit on a channel  $k \in \mathcal{K}$  only if no primary user is detected being accessing channel  $k$ . Further, we consider a *cognitive radio ad-hoc network* which consists of all secondary users and does not contain any primary user.

Secondary users conduct spectrum sensing independently and sequentially on all licensed channels. We assume that every node can detect the presence of primary user on each channel with certain accuracy.<sup>2</sup> We denote  $K_i \subseteq \mathcal{K}$  as the set of available channels for  $i$ . We adopt the unit disk model [27] for the transmission of both primary and CR users. Both primary users and CR users have fixed transmission ranges respectively, and all the channels are regarded to be identical in terms of signal propagation. If a CR node locates within the transmission range of primary user  $p$ , that CR node is not allowed to use the channel  $k(p)$ .

We assume that in addition to the licensed channels, there is one dedicated control channel. This control channel could be in ISM band or other reserved spectrum which is exclusively used for transmitting control messages. Actually, the control messages involved in the clustering process can also be transmitted on the available licensed channels through a rendezvous process by channel hopping [28], [29], i.e., two neighbouring nodes establish communication on the same channel. Over the control channel, a secondary user  $i$  can exchange its spectrum sensing result  $K_i$  to any  $i' \in \text{Nb}(i)$ . It is available for any secondary node  $i$  to exchange control messages with any other node in its neighborhood  $\text{Nb}(i)$  during the cluster formation phase.  $\text{Nb}(i)$  is simply defined as the set of nodes located within the transmission range of  $i$ .

If a secondary user  $i$  is not in the transmission range of a primary user  $p$ ,  $i$  can certainly not detect the presence of  $p$ . As the transmission range of primary users is limited and secondary

2. The spectrum availability can be validated with a certain probability of detection. Spectrum sensing/validation is out of the scope of this paper.

users are located at different locations, different secondary users may have different views of the spectrum availability, i.e., for any  $i, i' \in \mathcal{N}$ ,  $K_i = K_{i'}$  does not necessarily hold. As the assumed 0/1 state of connectivity is solely based on the Euclidean distance between secondary users,

A cognitive radio network can be represented as an undirected graph  $G = (\mathcal{N}, E)$ , where  $E \subseteq \mathcal{N} \times \mathcal{N}$  such that  $\{i, i'\} \in E$  if, and only if, there exists a channel  $k \in \mathcal{K}$  with  $k \in K_i \cap K_{i'}$ . Note that we consider the channel availability only for one snapshot of time. For the rest of this paper the word channel is referred to licensed channel, if the control channel is not explicitly mentioned.

## 4 ROBUST CLUSTERING PROBLEM IN CRN

In this section, we describe the definition of cluster in the context of CRNs, and the problem of robust clustering.

### 4.1 Cluster in CRN

A cluster  $C \subseteq \mathcal{N}$  is a set of secondary nodes consisting of a cluster head  $h_C$  and a number of cluster members. The cluster head is able to communicate with any cluster member directly. In other terms, for any cluster member  $i \in C$ ,  $i \in \text{Nb}(h_C)$  holds.

Cluster is denoted as  $C(i)$  when its cluster head is  $i$ . Cluster size of  $C(i)$  is written as  $|C(i)|$ .  $K(C) = \cap_{i \in C} K_i$ ,  $K(C)$  denotes the set of common control channels in cluster  $C$ . Clustering is performed periodically, as secondary users are mobile and the channel availability on secondary users are changing as primary users change their operation state.

TABLE 1. Notations in robust clustering problem

Symbol	Description
$\mathcal{N}$	collection of CR users in a CRN
$N$	number of CR users in a CRN, $N =  \mathcal{N} $
$\mathcal{K}$	set of licensed channels
$k(i)$	the working channel of user $i$
$\text{Nb}(i)$	the neighborhood of CR node $i$
$C(i)$	a cluster whose cluster head is $i$
$K_i$	the set of available channels at CR node $i$
$K(C(i))$	the set of available CCCs of cluster $C(i)$
$h_C$	the cluster head of a cluster $C$
$\delta$	desired cluster size
$S_i$	a set of claiming clusters, each of which includes debatable node $i$ after phase I
$d_i$	individual connectivity degree of CR node $i$
$g_i$	social connectivity degree of CR node $i$
$C_i$	the $i$ th legitimate cluster (only appear in Sec. 5)

### 4.2 Robust Clustering Problem

In the introduction section, we have stated that cluster size should be given consideration to justify the concept of robustness of clusters, i.e., without specifying requirement on cluster sizes, small clusters will be generated to obtain more CCCs. Except for cooperative sensing, clusters need to conduct some other functionalities. When cluster size is large, there will be substantial burden on cluster heads to manage the cluster members, which is a challenge for resource limited cluster heads, thus the cluster size should fall in a desired range [30], [31].

The centralized clustering scheme aims to form clusters with desired sizes, meanwhile the total number of CCCs of all clusters is maximized. In the following, we refer this problem as *centralized clustering*, and give the formal problem definition.

#### DEFINITION 1: Robust clustering problem in CRN.

Given a cognitive radio network  $\mathcal{N}$  where nodes are indexed from 1 to  $N$  sequentially. Based on certain correlation, certain secondary users constitute one cluster  $C$ .  $1 \leq |C| \leq k$  where  $|C|$  is the size of cluster  $C$  and  $k$  is a positive integer. We name the collection of such clusters as  $\mathcal{S} = \{C_1, C_2, \dots, C_{|\mathcal{S}|}\}$ , where  $\mathcal{S}$  satisfies the following properties:  $\bigcup_{1 \leq i \leq |\mathcal{S}|} C_i = \mathcal{N}$  and  $K(C(i)) \neq \emptyset$  for any  $i$  which satisfies  $1 \leq i \leq |\mathcal{S}|$ .

We give a new definition of the number of CCCs, where the number of common control channels is  $|K(C)|$  if  $|C| > 1$ , and is zero when  $|C| = 1$ . We use  $f(C)$  to denote the number of CCCs of a cluster  $C$  in the new definition.

The centralized clustering problem is to find a subcollection  $\mathcal{S}' \subseteq \mathcal{S}$ , so that  $\bigcup_{C_j \in \mathcal{S}'} C_j = \mathcal{N}$ , and  $C_j \cap C_{j'} = \emptyset$  for  $C_j, C_{j'} \in \mathcal{S}'$  and  $j' \neq j$ , so that  $\sum_{C \in \mathcal{S}'} f(C)$  is maximized. The decision version of centralized clustering in CRN is to ask whether there exists a non-empty  $\mathcal{S}' \subseteq \mathcal{S}$ , so that  $\sum_{C \in \mathcal{S}'} f \geq \lambda$  where  $\lambda$  is a real number.

### 4.3 Complexity of the Robust Clustering Problem

In this section we investigate the complexity of robust clustering problem. Theorem 4.1 tells centralized clustering problem in CRN is one NP-hard problem.

**THEOREM 4.1:** CRN clustering problem is NP-hard, when the maximum size of clusters  $k \geq 3$ .

The proof is in Appendix 19. In the following sections, both centralized and distributed solutions will be introduced.

## 5 CENTRALIZED SOLUTION FOR ROBUST CLUSTERING

As the robust clustering problem in CRN is NP hard, there is no polynomial algorithm to solve the problem, i.e., maximizing the sum of CCCs in all non-singleton clusters. Thus, we formulate the problem into a binary linear programming problem, where the objective function and the constraints are heuristic, in particular, the objective is different from the object in the Definition 1.

Given a CRN  $\mathcal{N}$  and desired cluster size  $\delta$ , we obtain a collection of clusters  $\mathcal{G}$  which contains all the *legitimate* clusters, and the sizes of these clusters are  $1, 2, \dots, \delta$ . Legitimate clusters are the clusters which satisfy the conditions in Section 4.1. Note that the legitimate clusters include the *singleton* ones, i.e., the cluster which has only one CR node, so that we can guarantee the partition of any network is always feasible. With  $N = |\mathcal{N}|$ ,  $G = |\mathcal{G}|$ , we construct a constant  $G \times N$  matrix  $Q_{G \times N}$ . The element of matrix  $Q$  is  $q_{ij}$ , where the subscript  $i$  is the index of legitimate cluster, and  $j$  is the node ID of one CR node. There are  $i \in \{1, 2, \dots, G-1, G\}$ , and  $j \in \{1, 2, \dots, N-1, N\}$ . Element  $q_{ij} = |K(C_i)|$  if node  $j \in C_i$ , and  $q_{ij} = 0$  if  $j \notin C_i$ . In other words, each non-zero element  $q_{ij}$  denotes the number of CCCs of the cluster  $i$  where node  $j$  resides.

We build a  $G \times N$  binary variable matrix  $X$ , which illustrates the clustering solution. The element of matrix  $X$  is binary vari-

$$\begin{matrix}
& 1 & 2 & 3 & \dots & j & \dots & N-1 & N \\
\begin{matrix} 1 \\ 2 \\ \vdots \\ i \\ \vdots \\ \vdots \\ G \end{matrix} & \begin{pmatrix} |K(C_1)| & |K(C_1)| & 0 & \dots & \dots & \dots & 0 & 0 \\ |K(C_2)| & 0 & |K(C_2)| & \dots & \dots & \dots & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & |K(C_i)| & 0 & \dots & \dots & \dots & |K(C_i)| & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & 0 & 0 & \dots & \dots & \dots & |K(C'_i)| & 0 \\ |K(C_G)| & \dots & \vdots & \dots & \dots & \vdots & \vdots & \vdots \end{pmatrix}
\end{matrix}$$

Fig. 1: An example of Matrix  $Q$ , its rows correspond to all legitimate clusters, and columns correspond to the CR nodes in the CRN.

able  $x_{ij}, i = 1, \dots, G, j = 1, \dots, N$ . Now, we can formulate the optimization problem as follows,

$$\begin{aligned}
& \min_{x_{ij}} \quad \sum_{j=1}^N \sum_{i=1}^G (-x_{ij} q_{ij} + (1 - w_i) * p) \\
& \text{subject to} \quad \sum_{i=1}^G x_{ij} = 1, \text{ for } \forall j = 1, \dots, N \\
& \quad \quad \quad \sum_{j=1}^N x_{ij} = |C_i| * (1 - w_i), \text{ for } \forall i = 1, \dots, G \\
& \quad \quad \quad x_{ij} \text{ and } w_i \text{ are binary variables.} \\
& \quad \quad \quad i \in \{1, 2, \dots, G\}, \quad j \in \{1, 2, \dots, N\}
\end{aligned}$$

The objective is a sum of two components, the first component is the sum of products of cluster size and the corresponding number of CCCs, which is the sole metric adopted by the scheme SOC [24]. The second component is the *punishment* for choosing the clusters whose sizes are not  $\delta$ . In fact, the second part is particularly designed to eliminates the drawbacks of SOC, i.e., SOC produces a large number of singleton clusters and a few large clusters. In practical computation, we minimize the opposite of the first part, and the punishment is a positive value. The first constraint restricts each node  $j$  to reside in exactly one cluster. In the second constraint,  $w_i$  is an auxiliary binary variable which denotes whether cluster  $C_i$  is chosen by the solution, in particular,

$$w_i = \begin{cases} 0 & \text{if } i\text{th legitimate cluster } C_i \text{ is chosen} \\ 1 & \text{if } i\text{th legitimate cluster } C_i \text{ is not chosen} \end{cases}$$

The second constraint regulates that when the  $i$ th legitimate cluster  $C_i$  is chosen, the number of elements which equal to 1 in the  $i$ th row of the matrix  $X$  is  $|C_i|$ . Now we explain how does the mechanism of the punishment in the objective work. The parameter  $p$  is defined as follows,

$$p = \begin{cases} 0 & \text{if } |C_i| = \delta \\ \alpha_1 & \text{if } |C_i| = \delta - 1 \\ \alpha_2 & \text{if } |C_i| = \delta - 2 \\ \dots & \end{cases}$$

where  $\alpha_i > 0$  and increases when  $|C_i|$  diverges from  $\delta$ . Because of  $w_i$ , any chosen cluster ( $w = 0$ ) brings certain *punishment*. When the chosen cluster's size is desired size  $\delta$ , the punishment is zero. In contrary, when the chosen cluster's size diverges from  $\delta$ , the objective function suffers *loss*. In particular, when  $w_i = 0$  and  $|C_i| = 1$ , the punishment is the most severe. This design doesn't follow the definition of  $f(C)$  in Definition 1 strictly, where  $f(C_i) = 0$  when  $|C_i| = 1$ , but our design echoes the definition by exerting the most severe punishment on the singleton clusters in the clustering solution. Choice of  $\alpha_i$  affects the resultant clusters.

## 6 DISTRIBUTED CLUSTERING ALGORITHM: ROSS

The cluster formation of one CRN can be obtained by solving the proposed optimization problem, but centralized scheme is inherently not suitable for the CRN which involves dynamics, e.g., the mobility of CR users and the variance of the available spectrum due to primary users' operation. In this section we introduce the distributed clustering scheme ROSS. ROSS consists of two cascaded phases: *cluster formation* and *membership clarification*. With ROSS, CR nodes form clusters based on the proximity of the available spectrum in their neighbourhood. Afterwards, CR nodes belong to one certain cluster.

### 6.1 Phase I - Cluster Formation

After conducting spectrum sensing and communication with neighbours, every CR node is aware of the available channels available for themselves as well as for all its neighbors. For each CR user  $i$ , two metrics are proposed to characterize the spectrum proximity between  $u$  and its neighborhood:

- *Individual connectivity degree*  $d_i$ :  $d_i = \sum_{j \in \text{Nb}(i)} |K_i \cap K_j|$ . It denotes the sum of the numbers of common controls channels between node  $i$  and every neighbour. It is an indicator of node  $i$ 's adhesive property to the CRN.
- *Social connectivity degree*  $g_i$ :  $g_i = |\bigcap_{j \in \text{Nb}(i) \cup i} K_j|$ . It is the number of common channels available to  $i$  and all its neighbors.  $g_i$  represents the ability of  $i$  to form a robust cluster with its neighbours.

Individual connectivity degree  $d_i$  and social connectivity degree  $g_i$  together form the *connectivity vector*. Figure 2 illustrates an example CRN where each node's connectivity vector is shown.

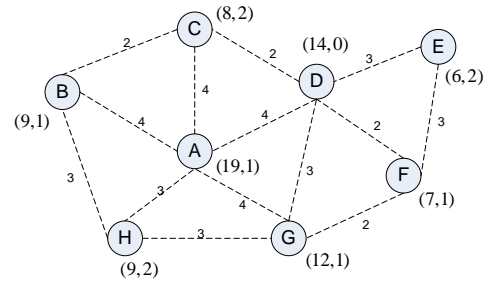


Fig. 2: Connectivity graph of the example CRN and the connectivity vector  $(d_i, g_i)$  for each node. The sets of the indices of the available channels sensed by each node are:  $K_A = \{1, 2, 3, 4, 5, 6, 10\}$ ,  $K_B = \{1, 2, 3, 5, 7\}$ ,  $K_C = \{1, 3, 4, 10\}$ ,  $K_D = \{1, 2, 3, 5\}$ ,  $K_E = \{2, 3, 5, 7\}$ ,  $K_F = \{2, 4, 5, 6, 7\}$ ,  $K_G = \{1, 2, 3, 4, 8\}$ ,  $K_H = \{1, 2, 5, 8\}$ . Dashed edge indicates the end nodes are within each other's transmission range.

After introducing the connectivity vector, we proceed to introduce the first phase of algorithm ROSS. To put it briefly, in this phase cluster heads are determined in the beginning. Then clusters are formed on the basis of the cluster heads' neighborhoods.

#### 6.1.1 Determining Cluster Heads and Form the Initial Clusters

In this phase, each CR node decides whether it is a cluster head by comparing its connectivity vector with its neighbors. When CR node  $i$  has lower individual connectivity degree than any neighbors except for those which have already become cluster heads (the appearance of cluster heads will be explained in Section 6.2), then node  $i$  becomes clusters head. If there is another CR node



$j$  in its neighborhood which has the same individual connectivity degree as  $i$ , i.e.,  $d_j = d_i$  and  $d_j < d_k, \forall k \in \text{Nb}(j) \setminus \{\text{CHs} \cup i\}$ , then the node out of  $\{i, j\}$  with higher social connectivity degree becomes cluster head. The other nodes become a member of that cluster. If  $g_i = g_j$  as well, the node ID is used to break the tie, i.e., the one with smaller node ID becomes the cluster's head. The node which becomes cluster head broadcasts a message of its eligibility of being cluster head to notify its neighbours, and claims its neighbourhood as its cluster. The pseudo code for the cluster head decision and the initial cluster formation is shown in Algorithm 1 in the appendix.

After receiving the notification from a cluster head, a CR node  $i$  is aware that it becomes a member of a cluster. Consequently,  $i$  sets its individual connectivity degree to a positive number  $M > |\mathcal{K}| \cdot N$ . Then  $i$  broadcasts its new individual connectivity degree to all its neighbors. We manipulate the individual connectivity degree of the CR nodes which are included in certain clusters. Hence, nodes located outside of the a formed cluster can possibly become cluster heads or can also be included into other clusters. When a CR node  $i$  is associated to multiple clusters, i.e.,  $i$  has received multiple notifications of cluster head eligibility from different CR nodes,  $d_i$  is still set to  $M$ . We have the following theorem to show that as long as a secondary user's individual connectivity degree is greater than zero, that secondary user will eventually be integrated into a certain cluster, or it eventually becomes a cluster head.

**THEOREM 6.1:** *Given a CRN, it takes at most  $N$  steps that every secondary user either becomes cluster head, or gets included into at least one cluster.*

Here, by *step* we mean one secondary user executing Algorithm 6.1 for one time. The Proof is in Appendix 19.

The procedure of the proof also illustrates the time needed to conduct Algorithm 6.1. Consider an extreme scenario, where all the secondary nodes sequentially execute Algorithm 1, i.e., they constitute one list as discussed in the example in the proof. If one step can be finished within certain time  $T$ , then the total time needed for the network to conduct Algorithm 6.1 is  $N * T$ . In other scenarios, as Algorithm 1 can be executed concurrently by secondary users which locate in different places, the needed time can be considerably reduced. Let us apply Algorithm 1 to the example shown in Figure 2. Node  $B$  and  $H$  have the same individual connectivity degree, i.e.,  $d_B = d_H$ . As  $g_H = 2 > g_B = 1$ , node  $H$  becomes the cluster head and cluster  $C_H$  is  $\{H, B, A, G\}$ .

### 6.1.2 Guarantee the Availability of Common Control Channel

After executing phase I of ROSS, it is possible that certain formed clusters don't own CCCs. As decreasing cluster size increases the number of CCCs within the cluster, for those clusters having no CCCs, certain nodes need to be eliminated to gain at least one CCC. The sequence of elimination is performed according to an ascending list of nodes which are sorted by the number of common channels between the nodes and the cluster head. In other words, the cluster member which has the least number of common channels with the cluster head is excluded first. If there are multiple nodes having the same number of common channels with the cluster head, the node whose elimination brings in more common channels will be excluded. If this criterion meets a tie, the tie will be broken by deleting the node with smaller node ID. It is possible that the cluster head excludes all its neighbours and resulting in a *singleton cluster* which is composed by itself. The pseudo code for cluster head to obtain at least one common

channel is shown in Algorithm 2. As to the nodes eliminated in this procedure, they restore their original individual connectivity degrees, and become either cluster heads or get included into other clusters afterwards according to Theorem 6.1.

### 6.1.3 Cluster Size Control in Dense CRN

In the following we illustrate the pressing necessity to control the cluster size when CRN becomes dense via both theoretical analysis and simulation. Assuming the CR users and PUs are evenly distributed and PUs occupy the licensed channels randomly, then both CR nodes density and channel availability in the CRN can be seen to be spatially homogeneous. The formed clusters are the neighbourhoods of cluster heads, and the neighbourhood is decided by the transmission range and network density. We consider a cluster  $C(i)$  where  $i$  is CH in a dense CRN. When we don't consider the CHs which could appear within  $i$ 's neighbourhood in the procedure of guaranteeing CCCs, according to Algorithm 1, the nearest cluster heads could locate just outside node  $i$ 's transmission range. An instance of this situation is shown in Figure 3. In the figure, black dots represent cluster heads, the circles denotes the transmission ranges of cluster heads. Cluster members are not shown in the figure. Let  $l$  be the length of side of

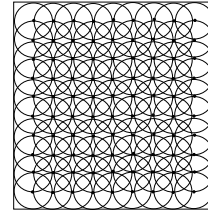


Fig. 3: Clusters formation in extremely dense CRN. Black dots are cluster heads, cluster members are not drawn.

simulation plan square, and  $r$  be CR's transmission radius. Based on the aforementioned analysis and geometry illustration as shown in Figure 3, we give an estimate on the maximum number of generated clusters, which is the product of the number of cluster heads in one row and that number in one line,  $l/r * l/r = l^2/r^2$ . Given  $r=10$  and  $l=50$ , the maximum number of clusters is 25. The number of clusters in the simulation is shown in Figure 4. Simulation is run for 50 times and the confidence interval is 95%. With the increase of CR users, network density (the average number of neighbours) increases linearly, and the number of clusters approaches to 25 which complies with the estimation.

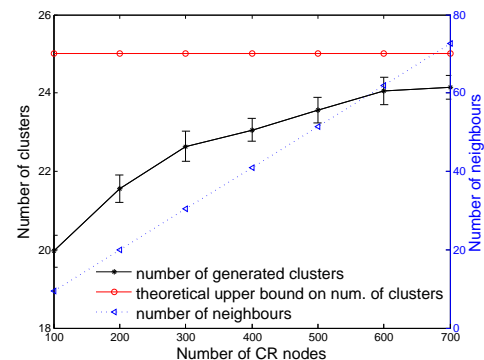


Fig. 4: The correlation between the number of formed clusters and network density.

Both analysis and simulation show that when applying ROSS, after the number of clusters saturates with the increase of network density, the cluster size increases linearly with the network density, thus certain measures are needed to curb this problem.

This task falls to the cluster heads. To control the cluster size, cluster heads prune their cluster members to achieve the desired cluster size. The desired size  $\delta$  is decided based on the capability of the CR users and the tasks to be conveyed. Given the desired size  $\delta$ , a cluster head excludes members sequentially according to the following principle, the absence of one cluster member leads to the maximum increase of common channels within the cluster. This process ends when the size of resultant cluster is  $\delta$  and at least one CCC is available. This procedure is similar with that to guarantee CCCs in cluster, thus the algorithm can reuse Algorithm 2.

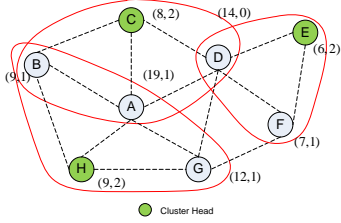


Fig. 5: Clusters formation after the phase I of ROSS. Some nodes are debatable nodes, i.e., belonging to more than one cluster.

## 6.2 Phase II - Membership Clarification

After applying phase I of ROSS to the example in Figure 2, the resulted clusters are shown in Figure 5. We notice nodes A, B, D are included in more than one cluster. We refer these nodes as *debatable nodes* as their cluster affiliations are not clear, and the clusters which include the debatable node  $i$  are called *claiming clusters* of node  $i$ , and are denoted as  $S_i$ . Actually, debatable nodes extensively exist in CRN with larger scale. Debatable nodes should be exclusively associated with only one cluster and be removed from the other claiming clusters, this procedure is called *cluster membership clarification*. We will introduce the solution for cluster membership clarification in the following.

### 6.2.1 Distributed Greedy Algorithm (DGA)

After Phase I, debatable nodes, e.g.,  $i$  needs to decide one cluster  $C \in S_i$  to stay, and thereafter leaves the rest others in  $S_i$ . The principle for debatable node  $i$  to choose one claiming cluster is that its decision can result in the greatest increase of common channels in all its claiming clusters. Since node  $i$  is a neighbour of all the cluster heads in  $S_i$ , node  $i$  is aware of the channel availability on these claiming cluster heads, and the common control channels in these claiming clusters. With these information, node  $i$  is able to calculate how many more CCCs will be produced in one claiming cluster if  $i$  leaves that cluster. If there exists one cluster  $C \in S_i$ , when  $i$  leaves this cluster brings the least increased CCCs than leaving any other claiming clusters, then  $i$  chooses to stay in cluster  $C$ . When there comes a tie, among the relevant claiming clusters,  $i$  chooses to stay in the cluster whose cluster head shares the most CCCs with  $i$ . In case there are multiple claiming clusters demonstrating the same on the aforementioned criteria, node  $i$  chooses to stay in the claiming cluster which has the smallest size. Node IDs of cluster heads will be used to break tie if the previous rules could not decide on the unique claiming cluster to stay.

The pseudo code of this algorithm is described as Algorithm 3. After deciding its membership, debatable node  $i$  notifies all its claiming clusters, and retrieves the updated information of the claiming clusters, e.g.,  $K(C)$ ,  $K_{hc}$ ,  $|C|$ , where  $C \in S_i$ . In the following we show that the process of membership clarification can be formulated into a game, and an equilibrium is reached after a finite number of best response updates made by the debatable nodes.

### 6.2.2 Bridging ROSS-DGA with Congestion Game

Game theory is a powerful mathematical tool for studying, modelling and analysing the interactions among individuals. A game consists of three elements: a set of players, a selfish utility for each player, and a set of feasible strategy space for each player. In a game, the players are rational and intelligent decision makers, which are related with one explicit formalized incentive expression (the utility or cost). Game theory provides standard procedures to study its equilibriums [32]. In the past few years, game theory has been extensively applied to problems in communication and networking [33], [34]. Congestion game is an attractive game model which describes the problem where participants compete for limited resources in a non-cooperative manner, it has good property that Nash equilibrium can be achieved after finite steps of best response dynamic, i.e., each player choose strategy to maximizes/minimizes its utility/cost with respect to the other players' strategies. Congestion game has been used to model certain problems in internet-centric applications or cloud computing, where self-interested clients compete for the centralized resources and meanwhile interact with each other. For example, server selection is involved in distributed computing platforms [35], or users downloading files from cloud, etc.

To formulate the debatable nodes' membership clarification into the desired congestion game, we observe this process from a different (or opposite) perspective. From the new perspective, the debatable nodes are regarded to be isolated and don't belong to any cluster, in other words, their claiming clusters become clusters which are beside them. Now for the debatable nodes, the previous problem of deciding which clusters to leave becomes a new problem that which cluster to join. In the new problem, debatable node  $i$  chooses one cluster  $C$  out of  $S_i$  to join if the decrease of CCCs in cluster  $C$  is the smallest in  $S_i$ , and the decrease of CCCs in cluster  $C$  is  $\sum_{C \in S_i} \Delta |K(C)| = \sum_{C \in S_i} (|K(C)| - |K(C \cup i)|)$ . The interaction between the debatable nodes and the claiming clusters is shown in Figure 6.

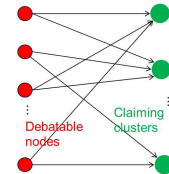


Fig. 6: Debatable nodes and claiming clusters

In the following, we show that the decision of debatable nodes to clarify their membership can be mapped to the behaviour of the players in a *player-specific singleton congestion game* when proper cost function is given. The game to be constructed is represented with a 4-tuple  $\Gamma = (\mathcal{P}, \mathcal{R}, \sum_{i \in \mathcal{P}}, f)$ , and the elements in  $\Gamma$  are explained below,

- $\mathcal{P}$ , the set of players in the game, which are the debatable nodes in our problem.

- $\mathcal{R} = \cup_{S_i, i \in \mathcal{P}}$ , denotes the set of resources for players to choose, in our problem,  $S_i$  is the set of claiming clusters of node  $i$ , and  $\mathcal{R}$  is the set of all claiming clusters.
- Strategy space  $\sum_i, i \in \mathcal{P}$  is the set of claiming clusters  $S_i$ . As debatable node  $i$  is supposed to choose only one claiming cluster, then only one piece of resource will be allocated to  $i$ .
- The utility (cost) function  $f(C)$  as to a resource  $C$ .  $f(C) = \Delta|K^i(C)|$ ,  $C \in S_i$ , which represents the decrease of CCCs in cluster  $C$  when debatable node  $i$  joins  $C$ . As to cluster  $C \in S_i$ , the decrease of CCCs caused by the enrolment of debatable nodes is  $\sum_{i: C \in S_i, i \rightarrow C} \Delta|K^i(C)|$ .  $i \rightarrow C$  means  $i$  joins cluster  $C$ . Obviously this function is non-decreasing with respect to the number of nodes joining cluster  $C$ .

The utility function  $f$  is not purely decided by the number of players accessing the resource (debatable nodes join claiming clusters), which happens in a canonical congestion game. The reason is in this game the channel availability on debatable nodes is different. Given two same groups of debatable nodes and their sizes are the same, when the nodes are not completely the same (neither are the channel availabilities on these nodes), the cost happened on one claiming cluster could be different if the two groups of debatable nodes join that cluster respectively. Hence, this congestion game is player specific [36]. In this game, every player greedily updates its strategy (choosing one claiming cluster to join) if joining a different claiming cluster minimizes the decrease of CCCs  $\sum_{i: C \in S_i} \Delta|K^i(C)|$ , and a player's strategy in the game is exactly the same with the behaviour of a debatable node in the membership clarification phas.

As to singleton congestion game, there exists a pure equilibria which can be reached with the best response update, and the upper bound for the number of steps before convergence is  $n^2 * m$  [36], where  $n$  is the number of players, and  $m$  is the number of resources. In our problem, the players are the debatable nodes, and the resources are the claiming clusters. Thus the upper bound of the number of steps can be expressed as  $O(N^3)$ .

In fact, the number of steps which are actually involved in this process is much smaller than  $N^3$ , as both  $n$  and  $m$  are considerably smaller than  $N$ . The percentage of debatable nodes in  $\mathcal{N}$  is illustrated in Figure 14, which is between 10% to 60% of the total number of CR nodes in the network. The number of clusters heads, as discussed in Section 6.1, is dependent on the network density and the CR node's transmission range. As shown in Figure 4, the cluster heads take up only 3.4% to 20% of the total number of CR nodes.

### 6.2.3 Distributed Fast Algorithm (DFA)

We propose a faster version of ROSS, ROSS-DFA, which differs from ROSS-DGA in the second phase. With ROSS-DFA, debatable nodes decide their respective cluster heads once. The debatable nodes consider their claiming clusters to include all their debatable nodes, thus the membership of claiming clusters is static and all the debatable nodes can make decision simultaneously without considering the change of membership of their claiming clusters. As ROSS-DFA is quicker than ROSS-DGA, the former is especially suitable for the CRN where the channel availability changes dynamically and re-clustering is necessary. To run ROSS-DFA, debatable node executes only one loop in Algorithm 3.

Now we apply both ROSS-DGA and ROSS-DFA to the toy network in Figure 5 which has been applied the phase I of ROSS. In the network, node A's claiming clusters are cluster  $C(C)$ ,  $C(H) \in S_A$ , their members are  $\{A, B, C, D\}$  and  $\{A, B, H, G\}$

respectively. The two possible strategies of node A is illustrated in Figure 7. In Figure 7(a), node A staying in  $C(C)$  and leaving  $C(H)$  brings 2 more CCCs to  $S_A$ , which is more than that brought by another strategy showed in 7(b). After the decisions made similarly by the other debatable nodes B and D, the final clusters are formed as shown in Figure 8.

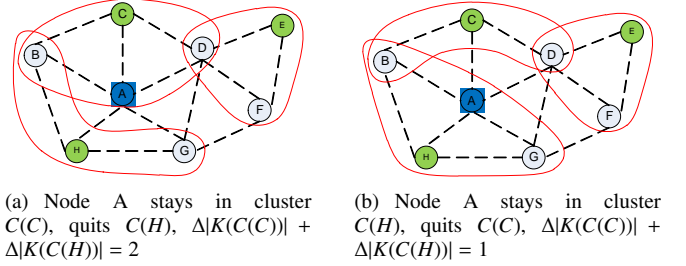


Fig. 7: Membership clarification: possible cluster formations caused by node A's different choices

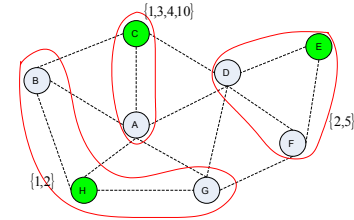


Fig. 8: Final formation of clusters.  $K(C(C))$ ,  $K(C(E))$ ,  $K(C(H))$  are shown beside corresponding clusters.

### 6.3 Apply the Centralized and Comparison Distributed Schemes in the Example CRN

After introducing the resulted clusters from ROSS in Fig. 8, we apply the other robust clustering schemes in the same example CRN in Figure 2. As to the centralized robust clustering scheme, we let the desired cluster size  $\delta$  be 3. A collection of clusters  $\mathcal{G}$  is obtained, which contains all the clusters satisfying the conditions of cluster in Section 4.1 and the sizes of clusters are 1, 2 or 3.  $\mathcal{G} = \{\{A\}, \{B\}, \dots, \{B, C\}, \{B, A\}, \{B, H\}, \dots, \{B, A, C\}, \{B, H, C\}, \{A, D, C\}, \dots\}$ , and  $G = |\mathcal{G}| = 38$ . When  $\alpha_1$  and  $\alpha_1$  are set as 0.2 and 0.8, the formed clusters are shown in Fig. 9(b). The resulted clustering solutions from SOC is shown in Fig. 9(a).

As to the average number of CCCs, the results of ROSS (including both ROSS-DGA and ROSS-DFA), centralized and SOC are 2.66, 2.66, and 3 respectively. Note there is one singleton cluster  $C(H)$  generated by SOC, which is not preferred. When we take no account of the singleton clusters, then the average number of common channels of SOC drops to 2.5.

## 7 PERFORMANCE EVALUATION

The schemes involved in the simulation are listed as follows,

- ROSS without size control, i.e., ROSS-DGA and ROSS-DFA.
- ROSS- $\delta$ -DGA and ROSS- $\delta$ -DFA, which are the variants of ROSS with the size control feature.  $\delta$  is the desired cluster size.
- SOC [24], one distributed clustering scheme pursuing cluster robustness. To the best of our knowledge, SOC is the only work



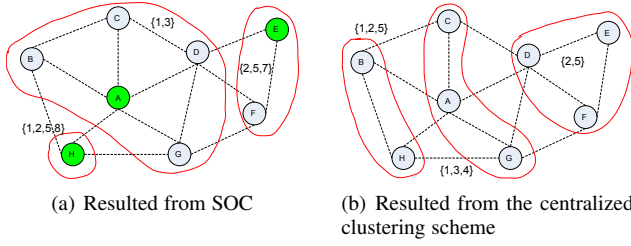


Fig. 9: Final clusters formed in the example network when being applied with SOC and the centralized clustering scheme.

emphasizing on the robustness of clustering structure among the related works.

- **Centralized robust clustering scheme.** The formulated optimization is an integer linear optimization problem, which is solved by the function *bintprog* provided in MATLAB.

The authors of [24] compared SOC with other schemes in terms of the average number of CCCs of the formed cluster, on which SOC outperforms other schemes by 50%-100%. SOC's comparison schemes are designed either for ad hoc network without consideration of channel availability [16], or for CRN but just considering connection among CR nodes [7]. Thus SOC is chosen to be the only distributed scheme as comparison, besides, we also compare ROSS with the centralized scheme. We investigate the schemes with the following metrics.

- **Average number of CCCs per non-singleton cluster.** Non-singleton cluster refers the cluster whose cluster size is larger than 1. Comparing with the metric adopted by SOC [24], which is the average number of CCCs per cluster without excluding the singleton clusters, this metric provides an more accurate description of the robustness of the non-singleton cluster. The larger number of CCCs per non-singleton clusters means these clusters have higher probability to survive when the primary users' operation becomes more intense. Although this metric doesn't disclose the information about the CR nodes which are not included in any non-singleton clusters, we still examine this metric as the number of CCCs is involved in the utility which is adopted by all robust clustering schemes.
- **Cluster sizes.** The distribution of CRs residing in the formed clusters with different sizes is presented.
- **Robustness of the clusters against newly added PUs.** We increase the number of PUs to challenge the clusters, and count the number of *unclustered* CR nodes which are the CR nodes which are not included in any non-singleton clusters. This metric indicates the robustness of clusters from a more practical point of view, i.e., as to the clusters formed for a given CRN and spectrum availability, how many CR nodes can still make use of the clusters when the spectrum availability decreases.
- **Amount of control messages involved.** We investigate the number of control messages involved in the clustering process.

Simulation consists of two parts, in the first part, we investigate the performance of centralized scheme, and the gap between the distributed schemes and the centralized scheme. This part is conducted in a small network, as there is no polynomial time solution available to solve the centralized problem. In the second part, we investigate the performance of the proposed distributed schemes in the CRN with different scales and densities.

We give a brief introduction to the settings which are common for both simulation parts. CRs and PUs are deployed on a two-dimensional Euclidean plane. The number of licensed channels is 10, each PU is operating on each channel with probability of 50%. CR users are assumed to be able to sense the existence of primary users and identify available channels. All primary and CR users are assumed to be static during the process of clustering. The simulation is written in C++, and the performance results are averaged over 50 randomly generated topologies, and the confidence interval corresponds to 95% confidence level.

## 7.1 Centralized Schemes vs. Decentralized Schemes

There are 10 primary users and 20 CR users are dropped randomly (with uniform distribution) within a square area of size  $A^2$ , where we set the transmission ranges of primary and CR users to  $A/3$ . When clustering scheme is executed, around 7 channels are available on each CR node. The desired cluster size  $\delta$  is 3, the parameters used in the *punishment* for choosing the clusters with undesired sizes are set as follows,  $\alpha_1 = 0.4$ ,  $\alpha_2 = 0.6$ .

### 7.1.1 Number of CCCs in Non-singleton Clusters

From Figure 10, we can see the centralized schemes outperform the distributed schemes. As to the distributed schemes, SOC achieves the best than all the variants of ROSS. The reason is, SOC is liable to group the neighbouring CRs which share the most abundant spectrum together, no matter how many of them are, thus the number of CCC of the formed clusters is higher. We have discussed the flaw of this metric as it doesn't convey the number of unclustered CR nodes, in fact, SOC generates the most unclustered CRs, which can be seen when we discuss the performance on the number of unclustered CR nodes. As to the variants of ROSS, we notice that the greedy mechanism increases CCCs in non-singleton clusters significantly.

### 7.1.2 Cluster Size Control

Figure 11 depicts the empirical cumulative distribution of the CRs residing in certain sized clusters, from which we have two conclusions. The first, SOC generates more unclustered CR nodes than other schemes. The centralized schemes produce no unclustered CR nodes, ROSS-DGA/DFA generate 3% unclustered nodes, as comparison, 10% of nodes are unclustered when applying SOC. ROSS-DGA and ROSS-DFA with size control feature generate 5%-8% unclustered CR nodes, which is due to the cluster pruning procedure (discussed in section 6.1.3). Second, the centralized schemes and cluster size control mechanism of RPSS generate clusters which satisfy the requirement on cluster size strictly. As to ROSS-DGA and ROSS-DFA with size control feature, CR nodes reside averagely in clusters whose sizes are 2, 3 and 4. The sizes of clusters resulted from ROSS-DGA and ROSS-DFA are disperse, but appear to be better than SOC, i.e., the 50% percentiles for ROSS-DGA, ROSS-DFA and SOC are 4.5, 5, and 5.5, and the 90% percentiles for the three schemes are 8, 8, and 9.

### 7.1.3 Robustness of the clusters against newly added PUs

We add PUs in the CRN to decrease the available spectrum, and observe the number of unclustered CR nodes. Clusters are formed with the presence of 10 PUs in the beginning, then extra 20 batches of PUs are added sequentially, where each batch includes 5 PUs.

Figure 12 shows with the increase of PUs, certain clusters disappear and the number of unclustered CR nodes increases.





Fig. 10: Number of common channels of non-singleton clusters



Fig. 11: Cumulative distribution of CRs residing in clusters with different sizes



Fig. 12: Number of unclustered CRs with decreasing spectrum availability

Fig. 13: Comparison between the distributed and centralized clustering schemes ( $N = 20$ )

Among the robust clustering schemes, the centralized scheme with desired size of two generates the most robust clusters, meanwhile, SOC results in the most vulnerable clusters. The centralized scheme with desired size of three doesn't outperform the variants of ROSS, because the centralized scheme peruses clusters with size of 3 at the expenses of sanctifying CCCs. In contrary, the variants of ROSS generate some smaller clusters which are more likely to survive when PUs' activities become intense.

#### 7.1.4 Control Signalling Overhead

In this section we compare the overhead of signalling involved in different clustering schemes. We omit the control messaged involved in neighbourhood discovery, which is the premise for any clustering scheme. According to [37], the message complexity is defined as the number of messages used by all nodes. To have the same criterion to compare, we count *the number of transmissions of control messages*, without distinguishing they are sent with broadcast or unicast. This metric is synonymous with *the number of updates* discussed in Section 6.

As to ROSS, the control messages are generated in both phases. In the first phase, when a CR node decides itself to be the cluster head, it broadcasts a message containing its ID, cluster members and the set of CCCs in its cluster. In the second phase, a debatable node broadcasts its affiliation to inform its claiming clusters, then the CHs of the claiming clusters broadcast message about the new cluster members if they are changed due to the debatable node's decision. The total number of the decisions involved in cluster formation has been analysed in Theorem 6.1 and Section 6.2.2 respectively.

Comparison scheme SOC involves three rounds of execution. In the first two rounds, every CR node maintains its own cluster and seek to integrate neighbouring clusters, or joins one of them. The final clusters are obtained in the third round. In each round, every CR node is involved in comparisons and cluster mergers.

The centralized scheme is conducted at the centralized control device, but it involves two phases of control message transmission. The first phase is information aggregation, in which every CR node's channel availability and neighborhood is transmitted to the centralized controller. The second phase is broadcasting, where the clustering solution is disseminated to every CR node. We adopt the algorithm proposed in [38] to broadcast and gather information as the algorithm is simple and self-stabilizing. This scheme needs

building a backbone structure to support the communication, and we apply ROSS to generate cluster heads which serve as the backbone, besides, the debatable nodes as used as the gateway nodes between the backbone nodes. As the backbone is built once and support transmission for multiple times, the messages involved in the clustering process are not counted. As to the process of information gathering, we assume that every cluster member sends the spectrum availability and its ID to its cluster head, which further forwards the message to the controller, thus the number of transmission is  $N$ . As to the process of dissemination, in an extreme situation where all the gateway and the backbone nodes broadcast, the number of transmission is  $h + m$ , where  $h$  is the number of cluster heads and  $m$  is number of debatable nodes.

The number of control messages which are involved in both ROSS and the centralized scheme is related with the number of debatable nodes. Figure 14 shows the percentage of debatable nodes when the CRN network becomes denser, from which we can obtain the value of  $m$ . The message complexity, quantitative

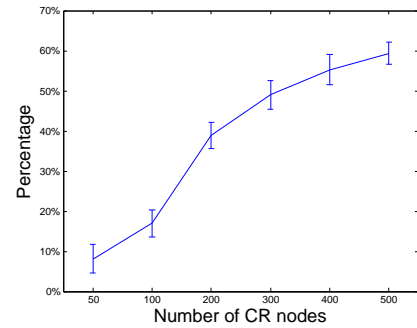


Fig. 14: The percentage of debatable nodes after phase I of ROSS.

analysis of the number of control messages involved in clustering, and the size of control messages are shown in Table 2. Figure 15 shows the number of transmissions of SOC, the upper bound of the number of transmissions for ROSS, and the analytical number of transmissions of the centralised scheme.

TABLE 2. Signalling overhead

Scheme	Message Complexity	Quantitative number of messages	Content of message (size of message)
ROSS-DGA, ROSS- $\delta$ -DGA	$O(N^3)$ (worst case)	$h + 2 * m^2 d$ (upper bound)	Phase I: notification from cluster head (1 byte), new individual connectivity degree (1 byte); Phase II: update of debatable nodes' affiliation (1 byte), claiming cluster $i$ ' new membership ( $ C(i) $ bytes)
ROSS-DFA, ROSS- $\delta$ -DFA	$O(N)$ (worst case)	$h + 2m$ (upper bound)	
SOC	$O(N)$	$3 * N$	$C(i)$ ( $ C(i) $ bytes), $K(C(i))$ ( $ P $ bytes), $i \in N$
Centralized	$O(N)$	$h + m + N$ (upper bound) [38]	$\{C\}$ ( $ C_i  * N$ bytes)

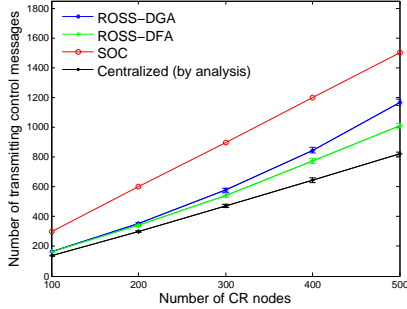


Fig. 15: Number of control messages. Note the curves of ROSS-DGA and ROSS-DFA are the upper bounds

## 7.2 Comparison between Distributed Schemes

In this section we investigate the performances of distributed clustering schemes in CRN with different network scales and densities. The transmission range of CR is  $A/5$ , PR's transmission range is  $2A/5$ . The initial number of PU is 30. The desired sizes adopted are listed in the Table 3, which is about 60% of the average number of neighbours.

TABLE 3

Number of CRs	100	200	300
Average num. of neighbours	9.5	20	31
Desired size $\delta$	6	12	20

### 7.2.1 Number of CCCs per Non-singleton Clusters

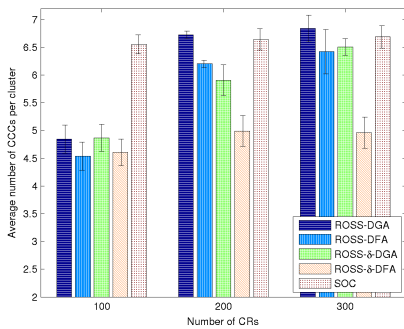


Fig. 16: Number of common channels of non-singleton clusters.

Figure 16 shows the average number of CCCs of the non-singleton clusters. We notice that SOC achieves the most CCCs per non-singleton cluster, although the lead over the variants of ROSS shrinks significantly when  $N$  increases.

### 7.2.2 Robustness of the clusters against newly added PUs

We add extra 20 batches of PUs sequentially in the CRN, where each batch includes 10 PUs. Figure 17 and 18 show that when  $N = 100$  and 200, more unclustered CR nodes appear in the CRN where SOC is applied. When the network becomes denser, ROSS-DGA/DFA generate slightly more unclustered CR nodes than SOC when new PUs are not many, but SOC's performance deteriorates quickly when the number of PUs becomes larger. We only show the average values of the variants of ROSS as their confidence intervals overlap. When applying ROSS with size control mechanism, significantly less unclustered CR nodes are generated. Besides, the greedy mechanism moderately strengthens the robustness of the clusters.

### 7.2.3 Cluster Size Control

Figure 25 shows when the network density scales up, the number of formed clusters by ROSS increases by smaller margin, and that generated by SOC increases linearly. This result coincides with the analysis in Section 6.1.3. To better understand the distribution of the sizes of formed clusters, we depict the empirical cumulative distribution of CR nodes which reside in clusters with certain sizes in CRNs in Figures 21 22 23.

The sizes of clusters generated by ROSS-DGA and ROSS-DFA span a wider range than ROSS with size control feature. Most of the generated clusters are smaller than the average number of neighbours, which is roughly equal with the 95% percentile of the ROSS-DGA curve. The 50% percentile of the ROSS-DGA curve is roughly the desired size  $\delta$ . When the variants of ROSS with size control feature are applied, the sizes of the most generated clusters are smaller than  $\delta$ . As to the curves of SOC, the 95% percentiles are 36, 30, and 40 in respective networks.

Overviewing Figure 24, we conclude that the sizes of the clusters generated by ROSS are limited by the network density, the sizes of the clusters formed by ROSS with size control feature are restricted by the desired size. In contrary, the clusters generated from SOC demonstrate strong divergence on cluster sizes.

## 7.3 Insights from the Simulation

The centralized clustering scheme can form the clusters which satisfy the requirement on cluster size strictly, and the clusters are robust against the newly added PUs, besides, it generates the smallest control overhead in the process of cluster formation.

As distributed schemes, ROSS outperform the comparison scheme SOC considerably on three metrics. ROSS generates much less singleton clusters than SOC, and the resulted clusters are robust against the newly added PUs. The signalling overhead involved in ROSS is about half of that needed for SOC, and the signalling messages are much shorter than the latter. The sizes of the clusters which are generated by ROSS are restricted



Fig. 17: 100 CRs



Fig. 18: 200 CRs



Fig. 19: 300 CRs

Fig. 20: Percentage of CR nodes which are not included in any non-singleton clusters



Fig. 21: 100 CRs, 30 PUs in network



Fig. 22: 200 CRs, 30 PUs in network



Fig. 23: 300 CRs, 30 PUs in network

Fig. 24: Cumulative distribution of CRs residing in clusters with different sizes



Fig. 25: The number of formed clusters.

by the network density, which demonstrate smaller discrepancy than that of SOC. Besides, ROSS achieves similar performance to the centralized scheme, i.e., the cluster sizes obtained by ROSS with size control feature are limited by the desired size, and the cluster robustness is similar when applying the variants of ROSS and the centralized scheme respectively. As to the variants of ROSS, the greedy mechanism in ROSS-DGA helps to improve the performance on cluster size and cluster robustness at the cost of mildly increased signalling overhead.

We also notice that the metric that the number of CCCs per non-singleton cluster doesn't indicate the robustness of clusters as

shown in Figure 12 and 20, although it is adopted as the metric in the formation of clusters.

## 8 CONCLUSION

In this paper we investigate the robust clustering problem in CRN extensively, in order to generate robust clusters against primary users' influence, so that more CR users can benefit from operative decision making provided by the clusters. We provide the mathematical description of the problem, and propose both centralized and distributed schemes. We prove the NP hardness of this problem, and the congestion game model in game theory is used to design the distributed scheme. A Light weighted clustering scheme ROSS is also proposed. Through simulation and theoretical analysis, we find that distributed schemes achieve similar performance with centralized optimization in terms of cluster robustness, signalling overhead and cluster sizes, and outperform the comparison distributed scheme on the above mentioned metrics.

The shortage of ROSS scheme is it doesn't generate big clusters whose sizes exceed the cluster head's neighbourhood. This problem is attributed to fact that ROSS forms clusters on the basis of cluster head's neighbourhood, and doesn't involve interaction with the nodes outside its neighbourhood. In the other way around, forming big cluster which extends a cluster head's neighbourhood has limited applications, as multiple hop communication and coordination are required within such clusters.

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**Algorithm 1:** ROSS phase I: cluster head determination and initial cluster formation for Unclustered CR node  $i$

---

**Input:**  $d_j, g_j, j \in \text{Nb}_i \setminus \text{CHs}$ . Empty sets  $\tau_1, \tau_2$   
**Result:** Returning 1 means  $i$  is cluster head, then  $d_j$  is set to 0,  $j \in \text{Nb}_i \setminus \text{CHs}$ . returning 0 means  $i$  is not CH.

```

1 if  $\nexists j \in \text{Nb}_i \setminus \text{CHs}$ , such that  $d_i \geq d_j$  then
2   return 1;
3 end
4 if  $\exists j \in \text{Nb}_i \setminus \text{CHs}$ , such that  $d_i > d_j$  then
5   return 0;
6 else
7   if  $\nexists j \in \text{Nb}_i \setminus \text{CHs}$ , such that  $d_j == d_i$  then
8      $\tau_1 \leftarrow j$ 
9   end
10 end
11 if  $\nexists j \in \tau_1$ , such that  $g_i \leq g_j$  then
12   return 1;
13 end
14 if  $\exists j \in \tau_1$ , such that  $g_i < g_j$  then
15   return 0;
16 else
17   if  $\nexists j \in \tau_1$ , such that  $g_j == g_i$  then
18      $\tau_2 \leftarrow j$ 
19   end
20 end
21 if  $ID_i$  is smaller than any  $ID_j, j \in \tau_2 \setminus i$  then
22   return 1;
23 end
24 return 0;
```

---

### PROOF OF THEOREM 6.1

**Proof.** We consider a CRN which can be represented as a connected graph. To simplify the discussion, we assume the secondary users have unique individual connectivity degrees. Each user has an identical ID and a social connectivity degree. This assumption is fair as the social connectivity degrees and node ID are used to break ties in Algorithm 1, when the individual connectivity degrees are unique, it is not necessary to use the former two metrics.

For the sake of contradiction, let us assume there exist some secondary user  $\alpha$  which is not included into any cluster. Then there is at least one node  $\beta \in \text{Nb}_\alpha$  such that  $d_\alpha > d_\beta$ . According to Algorithm 1,  $\delta$  is not included in any clusters, because otherwise  $d_\beta = M$ , a large positive integer. Now, we distinguish between two cases: If  $\beta$  becomes cluster head, node  $\alpha$  is included, the assumption is not true. If  $\beta$  is not a cluster head, then  $\beta$  is not in any cluster, we can repeat the previous analysis made on node  $\alpha$ , and deduce that node  $\beta$  has at least one neighbouring node  $\gamma$  with  $d_\gamma < d_\beta$ . Till now, when there is no cluster head identified, the unclustered nodes, i.e.,  $\alpha, \beta$  form a linked list, where their connectivity degrees monotonically decrease. But this list will not continue to grow, because the minimum individual connectivity degree is zero, and the length of this list is upper bounded by the total number of nodes in the CRN. An example of the formed node series is shown as Figure 26.

---

**Algorithm 2:** ROSS phase I: cluster head guarantees the availability of CCC (start from line 1) / cluster size control (start from line 2)

---

**Input:** Cluster  $C$ , empty sets  $\tau_1, \tau_2$   
**Output:** Cluster  $C$  has at least one CCC, or satisfies the requirement on cluster size

```

1 while  $K_C = \emptyset$  do
2   while  $|C| > \delta$  do
3     if  $\exists$  only one  $i \in C \setminus H_C, i = \arg \min(|K_{H_C} \cap K_i|)$ 
4       then
5          $C = C \setminus i$ ;
6       else
7          $\exists$  multiple  $i$  which satisfies
8            $i = \arg \min(|K_{H_C} \cap K_i|)$ ;
9          $\tau_1 \leftarrow i$ ;
10        end
11        if  $\exists$  only one  $i \in \tau_1$ ,
12           $i = \arg \max(|\cap_{j \in C \setminus i} K_j| - |\cap_{j \in C} K_j|)$  then
13             $C = C \setminus i$ ;
14          else
15             $C = C \setminus i$ , where  $i = \arg \min_{i \in \tau_1} ID_i$ 
16          end
17        end
18      end
19    end
```

---



---

**Algorithm 3:** Debatable node  $i$  decides its affiliation in phase II of ROSS

---

**Input:** all claiming clusters  $C \in S_i$   
**Output:** one cluster  $C \in S_i$ , node  $i$  notifies all its claiming clusters in  $S_i$  about its affiliation decision.

```

1 while  $i$  has not chosen the cluster, or  $i$  has joined cluster  $\tilde{C}$ ,
  but  $\exists C' \in S_i, C' \neq \tilde{C}$ , which has
   $|K(C' \setminus i)| - |K(C')| < |K(C \setminus i)| - |K(C)|$  do
2   if  $\exists$  only one  $C \in S_i, C = \arg \min(|K(C \setminus i)| - |K(C)|)$ 
3     then
4       return  $C$ ;
5   else
6      $\exists$  multiple  $C \in S_i$  which satisfies
7        $C = \arg \min(|K(C \setminus i)| - |K(C)|)$ ;
8      $\tau_1 \leftarrow C$ ;
9   end
10  if  $\exists$  only one  $C \in \tau_1, C = \arg \max(K_{h_C} \cap K_i)$  then
11    return  $C$ ;
12  else
13     $\exists$  multiple  $C \in S_i$  which satisfies
14       $C = \arg \max(K_{h_C} \cap K_i)$ ;
15     $\tau_2 \leftarrow C$ ;
16  end
17  if  $\exists$  only one  $C \in \tau_2, C = \arg \min |C|$  then
18    return  $C$ ;
19  else
20    return  $\arg \min_{C \in \tau_2} h_C$ ;
21  end
22 end
```

---



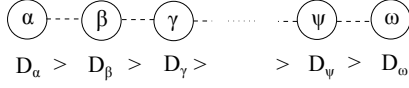


Fig. 26: The node series discussed in the proof of Theorem 6.1, the deduction begins from node  $\alpha$

In this example, node  $\omega$  is at the tail of the list. As  $\omega$  does not have neighboring nodes with lower individual connectivity degree,  $\omega$  becomes a cluster head. Then  $\omega$  incorporates all its one-hop neighbours (here we assume that every newly formed cluster has common channels), including the nodes which precede  $\omega$  in the list. The nodes which join a cluster set their individual connection degrees to  $M$ , which enables the node immediately precede in the list to become a cluster head. In this way, cluster heads are generated from the tail of list to the head of the list, and all the nodes in the list are in at least one cluster, which contradicts the assumption that  $\alpha$  is not included in any cluster.

If we see a secondary user *becoming a cluster head*, or *becoming a cluster member* as one step, as the length of the list of secondary users is not larger than  $N$ , there are  $N$  steps for this scenario to form the initial clusters.

□

### PROOF OF THEOREM 4.1

**Proof.** We put the definition of weighted k-set packing problem here as it to be used in the analysis on the complexity of the centralised clustering problem.

**DEFINITION 2:** *Weighted k-set packing.*

Given a finite set  $\mathcal{G} = \{g_1, \dots, g_N\} \subseteq \mathbb{N}$  of non-negative integers and a collection of sets  $\mathcal{Q} = \{S_1, S_2, \dots, S_m\}$  such that  $S_i \subseteq \mathcal{G}$  for every  $1 \leq i \leq m$ . Each set  $S \in \mathcal{Q}$  is associated with a weight  $\omega(S) \in \mathbb{R}$ . Further, we are given a threshold value  $\lambda \in \mathbb{N}$ .

The question is whether there exists a collection  $\mathcal{S} \subseteq \mathcal{Q}$  such that  $\mathcal{S}$  contains only pairwise disjoint sets, i.e., for all  $S, S' \in \mathcal{S}$  with  $S \neq S'$  it holds that  $S \cap S' = \emptyset$ , and the total weight of the sets in  $\mathcal{S}$  is greater than  $\lambda$ , i.e.,  $\sum_{S \in \mathcal{S}} \omega(S) > \lambda$ .

Weighted k-set packing is NP-hard when  $k \geq 3$ . [39]

To prove that the centralized clustering problem is NP-hard, we reduce the NP-hard problem *weighted k-set packing* to it to prove the former is at least as hard as the latter. We show the existence of a polynomial-time algorithm  $\sigma$  that transforms any instance  $\mathcal{I}$  of a weighted k-set packing into an instance  $\sigma(\mathcal{I})$  of centralized clustering problem.

W.l.o.g. let set  $\mathcal{G} = \{1, \dots, N\}$ . The polynomial algorithm  $\sigma$  consists of three steps.

- In the first step, we transform the instance  $\mathcal{I}$  to  $\mathcal{I}'$  by adding dummy elements into each set in  $\mathcal{I}$ . Formally, for each set  $s_i \in \mathcal{I}$ , we create  $s'_i = s_i \times \{1, 2\}$ . Then we change the dummy elements by adding  $N$  on them. The purpose of this transformation is to eliminate the set in  $\mathcal{I}$ , which has single element. The weight of these sets remain unchanged, i.e.,  $\omega(s'_i) = \omega(s_i)$ .
- Mapping the elements in  $\mathcal{I}'$  to CR nodes on a two-dimensional Euclidean plane, and mapping the sets in  $\mathcal{I}'$  to clusters. There is a bijection between the union of sets in  $\mathcal{I}'$  to the CRN which consists of the CR nodes, in particular, each element one-to-one corresponds to the CR node whose node ID equals to the element. We further regulate that, each set in  $\mathcal{I}'$  has a corresponding cluster, i.e., there is a bijection between a set in  $\mathcal{I}'$  and a set of

node IDs in a cluster, besides, the number of CCCs is equal to the weight of the corresponding set.

- In this step, we transform the instance  $\mathcal{I}'$  to a clustering proposal for CRN. We adjust the locations of the CR nodes which are mapped from the dummy elements in the instance  $\mathcal{I}'$ , and let them beside the CR nodes whose ID is exact  $N$  smaller. Because of the dummy nodes, the clustering solution which corresponds to  $\mathcal{I}'$  doesn't have singleton cluster. This transformation requires  $2 \cdot \sum_{s_i \in \mathcal{I}'} |s_i|$  steps. Now we look back to the elements in  $\mathcal{Q}$ , which don't appear in  $\mathcal{I}'$ . We one-to-one map these elements to CR nodes, and arbitrarily put these CR nodes in the plane, and these CR nodes become single node clusters. According to the definition of clustering problem in CRN, the number of CCCs in these single node clusters is 0. These singleton clusters and the clusters mapped from  $\mathcal{I}'$  constitute a clustering proposal, and finding these singleton clusters requires at most  $N$  steps. An example is shown in Table 4.

$\mathcal{N}$	{0, 1, 2, 3, 4, 5, 6, 7, 8, 9}
$\mathcal{Q}$	{{1}, {1, 5}, {1, 2, 4}, {2, 3}, {4}}
Instance for Weighted k-set packing	{{1}, {2, 3}, {4}}
Instance with dummy elements	{{1, 11}, {2, 12, 3, 13}, {4, 14}}
Instance for clustering solution (dashed circles are dummy nodes)	

TABLE 4

We have crossed the hurdle of finding one polynomial algorithm  $\sigma$  which transforms an instance of weighted k-set packing to an instance of the clustering problem in CRN. When  $\mathcal{I}$  is not an instance for weighted k-set packing problem due to the existence of joint sets, the corresponding cluster strategy is not a solution for the centralized clustering problem, as there are overlapped clusters.

When there are only disjoint sets in an instance  $\mathcal{I}$  for weighted k-set packing, the sum weight is identical to the sum number of CCCs in the CRN mapped from  $\mathcal{I}'$ , even  $\mathcal{I}$  contains sets which only have one element. Thus, when a instance  $\mathcal{I}$  for k-set packing problem is true, i.e., the sum of weights is greater than  $\lambda$ , then in the CRN which is mapped from  $\mathcal{I}'$ , the summed number of CCCs of the clusters is greater than  $\lambda$ . In the other way around, when an instance is false for weighted k-set packing problem, the summed number of CCCs of the clusters in the mapped CRN is smaller than  $\lambda$ , and there is no clustering solution satisfying the centralized clustering problem.

Thus, weighted k-set packing can be reduced to clustering problem in CRN, then the latter problem is of NP-hard. □

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### REFERENCES

- [1] I. Mitola, J. and J. Maguire, G.Q., "Cognitive radio: making software radios more personal," *Personal Communications, IEEE*, vol. 6, no. 4, pp. 13–18, aug. 1999.

- [2] T. Yucek and H. Arslan, "A survey of spectrum sensing algorithms for cognitive radio applications," *IEEE Communications Surveys Tutorials*, vol. 11, no. 1, pp. 116–130, First 2009.
- [3] Q. Zhao and B. Sadler, "A survey of dynamic spectrum access," *Signal Processing Magazine, IEEE*, vol. 24, no. 3, pp. 79–89, May 2007.
- [4] A. Sahai, R. Tandra, S. M. Mishra, and N. Hoven, "Fundamental design tradeoffs in cognitive radio systems," in *Proc. of the 1st Intl. workshop on technology and policy for accessing spectrum*, ser. ACM TAPAS '06.
- [5] I. F. Akyildiz, B. F. Lo, and R. Balakrishnan, "Cooperative spectrum sensing in cognitive radio networks: A survey," *Phys. Commun.*, vol. 4, no. 1, pp. 40–62, Mar. 2011.
- [6] C. Sun, W. Zhang, and K. B. Letaief, "Cluster-based cooperative spectrum sensing in cognitive radio systems," in *proc. of IEEE ICC*, 2007.
- [7] J. Zhao, H. Zheng, and G.-H. Yang, "Spectrum sharing through distributed coordination in dynamic spectrum access networks," *Wireless Com. and Mobile Computing*, vol. 7, no. 9, pp. 1061–1075, 2007.
- [8] D. Willkomm, M. Bohge, D. Hollós, J. Gross, and A. Wolisz, "Double hopping: A new approach for dynamic frequency hopping in cognitive radio networks," in *Proc. of PIMRC 2008*.
- [9] C. Passiatore and P. Camarda, "A centralized inter-network resource sharing (CIRS) scheme in IEEE 802.22 cognitive networks," in *Proc. of IFIP Annual Mediterranean Ad Hoc Networking Workshop 2011*, 2011.
- [10] A. A. Abbasi and M. Younis, "A survey on clustering algorithms for wireless sensor networks," *Comput. Commun.*, vol. 30, no. 14–15, pp. 2826–2841, 2007.
- [11] H. D. R. Y. Huazi Zhang, Zhaoyang Zhang<sup>1</sup> and X. Chen, "Distributed spectrum-aware clustering in cognitive radio sensor networks," in *Proc. of GLOBECOM 2011*.
- [12] B. E. Ali Jorio, Sanaa El Fkihi and D. Aboutajdine, "An energy-efficient clustering routing algorithm based on geographic position and residual energy for wireless sensor network," *Journal of Computer Networks and Communications*, vol. 2015, April 2015.
- [13] Q. Wu, G. Ding, J. Wang, X. Li, and Y. Huang, "Consensus-based decentralized clustering for cooperative spectrum sensing in cognitive radio networks," *Chinese Science Bulletin*, vol. 57, no. 28–29, 2012.
- [14] V. Kawadia and P. R. Kumar, "Power control and clustering in ad hoc networks," in *Proc. of INFOCOM '03*, 2003, pp. 459–469.
- [15] C. R. Lin and M. Gerla, "Adaptive clustering for mobile wireless networks," *IEEE Journal on Selected Areas in Communications*, vol. 15, pp. 1265–1275, 1997.
- [16] S. Basagni, "Distributed clustering for ad hoc networks," *Proc. of I-SPAN '99*, pp. 310–315, 1999.
- [17] J. Sucec and I. Marsic, "Clustering overhead for hierarchical routing in mobile ad hoc networks," in *Proc. of IEEE INFOCOM 2002*, vol. 3, 2002, pp. 1698–1706 vol.3.
- [18] H. Wu and A. Abouzeid, "Cluster-based routing overhead in networks with unreliable nodes," in *Proceedings of IEEE WCNC 2004*, vol. 4, march 2004, pp. 2557–2562 Vol.4.
- [19] T. Chen, H. Zhang, G. Maggio, and I. Chlamtac, "Cogmesh: A cluster-based cognitive radio network," *Proc. of DySPAN '07*.
- [20] D. Wu, Y. Cai, L. Zhou, and J. Wang, "A cooperative communication scheme based on coalition formation game in clustered wireless sensor networks," *IEEE Transactions on Wireless Communications*, vol. 11, no. 3, pp. 1190–1200, march 2012.
- [21] K. Baddour, O. Ureten, and T. Willink, "Efficient clustering of cognitive radio networks using affinity propagation," in *Proc. of ICCCN 2009*.
- [22] A. Asterjadhi, N. Baldo, and M. Zorzi, "A cluster formation protocol for cognitive radio ad hoc networks," in *Proc. of European Wireless Conference 2010*, pp. 955–961.
- [23] M. Ozger and O. B. Akan, "Event-driven spectrum-aware clustering in cognitive radio sensor networks," in *Proc. of IEEE INFOCOM 2013*.
- [24] L. Lazos, S. Liu, and M. Krunz, "Spectrum opportunity-based control channel assignment in cognitive radio networks," *Proc. of SECON '09*, pp. 1–9, jun. 2009.
- [25] S. Liu, L. Lazos, and M. Krunz, "Cluster-based control channel allocation in opportunistic cognitive radio networks," *IEEE Trans. Mob. Comput.*, vol. 11, no. 10, pp. 1436–1449, 2012.
- [26] N. Mansoor, A. Islam, M. Zareei, S. Baharun, and S. Komaki, "Construction of a robust clustering algorithm for cognitive radio ad-hoc network," in *Proc. of CROWNCOM 2015*.
- [27] B. Clark, C. Colbourn, and D. Johnson, "Unit disk graphs," *Annals of Discrete Mathematics*, vol. 48, no. C, pp. 165–177, 1991.
- [28] Y. Zhang, G. Yu, Q. Li, H. Wang, X. Zhu, and B. Wang, "Channel-hopping-based communication rendezvous in cognitive radio networks," *IEEE/ACM Transactions on Networking*, vol. 22, no. 3, June 2014.
- [29] Z. Gu, Q.-S. Hua, and W. Dai, "Fully distributed algorithms for blind rendezvous in cognitive radio networks," in *Proceedings of the 2014 ACM MobiHoc*, ser. MobiHoc '14.
- [30] Y. P. Chen, A. L. Liestman, and J. Liu, "Clustering algorithms for ad hoc wireless networks," in *Ad Hoc and Sensor Networks*. Nova Science Publishers, 2004.
- [31] E. Perevalov, R. S. Blum, and D. Safi, "Capacity of clustered ad hoc networks: how large is "large"?" *IEEE Transactions on Communications*, vol. 54, no. 9, pp. 1672–1681, Sept 2006.
- [32] A. MacKenzie and S. Wicker, "Game theory in communications: motivation, explanation, and application to power control," in *Proc. of IEEE GLOBECOM 2001*.
- [33] J. O. Neel, "Analysis and design of cognitive radio networks and distributed radio resource management algorithms," Ph.D. dissertation, Blacksburg, VA, USA, 2006, aAI3249450.
- [34] B. Wang, Y. Wu, and K. R. Liu, "Game theory for cognitive radio networks: An overview," *Comput. Netw.*, vol. 54, no. 14, Oct. 2010.
- [35] B. J. S. Chee and C. Franklin, Jr., *Cloud Computing: Technologies and Strategies of the Ubiquitous Data Center*, 1st ed. CRC Press, Inc., 2010.
- [36] H. Ackermann, H. Räußlin, and B. Vöcking, "Pure Nash equilibria in player-specific and weighted congestion games," *Theoretical Computer Science*, vol. Vol. 410, no. 17, pp. 1552–1563, 2009.
- [37] X.-Y. Li, Y. Wang, and Y. Wang, "Complexity of data collection, aggregation, and selection for wireless sensor networks," *IEEE Transactions on Computers*, vol. 60, no. 3, pp. 386–399, 2011.
- [38] M. Onus, A. Richa, K. Kothapalli, and C. Scheideler, "Efficient broadcasting and gathering in wireless ad-hoc networks," in *Proc. of ISPAN 2005*.
- [39] M. R. Garey and D. S. Johnson, *Computers and Intractability: A Guide to the Theory of NP-Completeness*. W. H. Freeman, 1979.

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**Di Li** received BE and MS degrees in control engineering from Zhejiang University and Shaanxi University of Science and Technology respectively in China. He worked with James Gross for his PhD in RWTH Aachen University since 2010.

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