

## FINAL PROJECT

### Initialization of packages & forecast data:

```
library(forecast)
library(readxl)
library(ggplot2)
windows()
setwd("C:/Users/YAZGAN/Desktop/360 final proj")
data <- read_xls("C:/Users/hp/Desktop/Project/beer.xls")
```

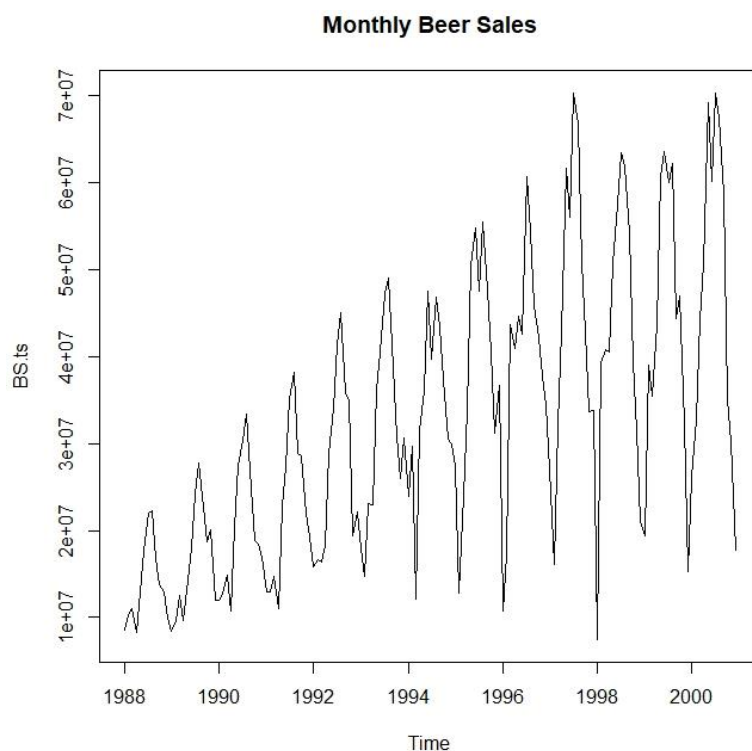
In the R code above, excel data is imported into R via “readxl” package and setup is completed. Windows function is being used for the sake of better graphics on plots.

*1. Plot the time series of “Beer Sales”. Comment on the shape of the time series. Specifically, do you think the time series is stationary with respect to its mean and variance?*

```
BS<-data[,2]
BS.ts<-ts(BS,freq=12,start=c(1988,1))
plot(BS.ts)
```

Since given data is aggregate and contains extra information and related factors with sales data, firstly sales data is extracted and followingly transformed into time series data on monthly basis.

### Plot of time series of Beer Sales:



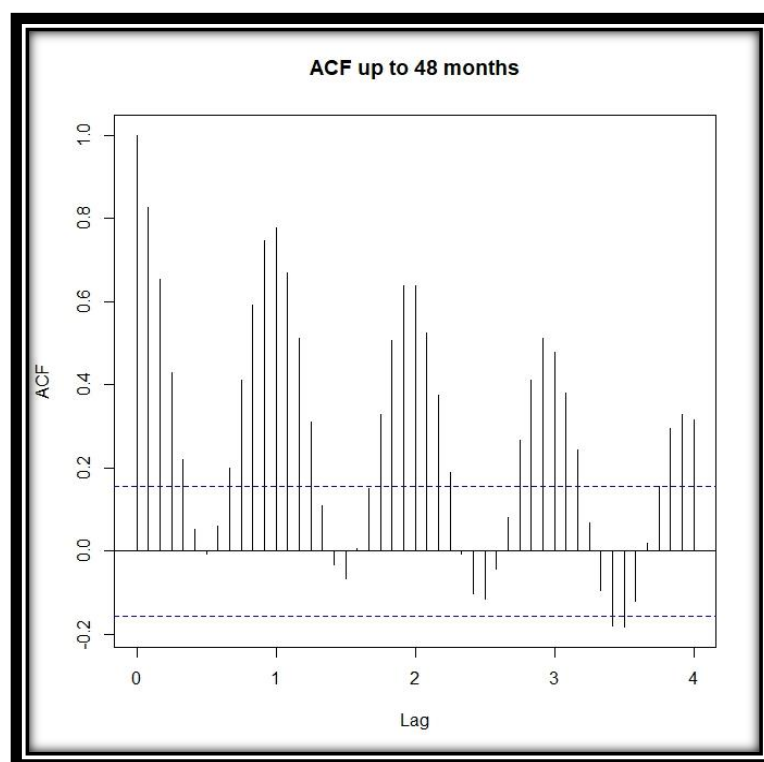
When the shape of Beer Sales plot is analyzed, one can see the obvious positive trend by year and yearly seasonality. The increase in variance of seasonal shifts should be noticed also.

For the stationary decision, we should check stationarity conditions, which are constant mean and constant variance. Violation of one of these conditions is enough to come up with the nonstationary decision. The plot above evidently reveals that the mean of the time series is increasing as the time and so does the variance. Therefore, it is concluded that the data is not stationary.

*2. Plot the autocorrelation function of the time series (get autocorrelations for at least 24 lags). What do you think the autocorrelation values at different lags indicate?*

The R code below is utilized for omitting NA's in the vectors and plotting auto correlation functions of the time series of beer sales.

```
BS.ts<-na.omit(BS.ts)
acf(BS.ts,lag.max = 48)
pacf(BS.ts,lag.max = 48)
```

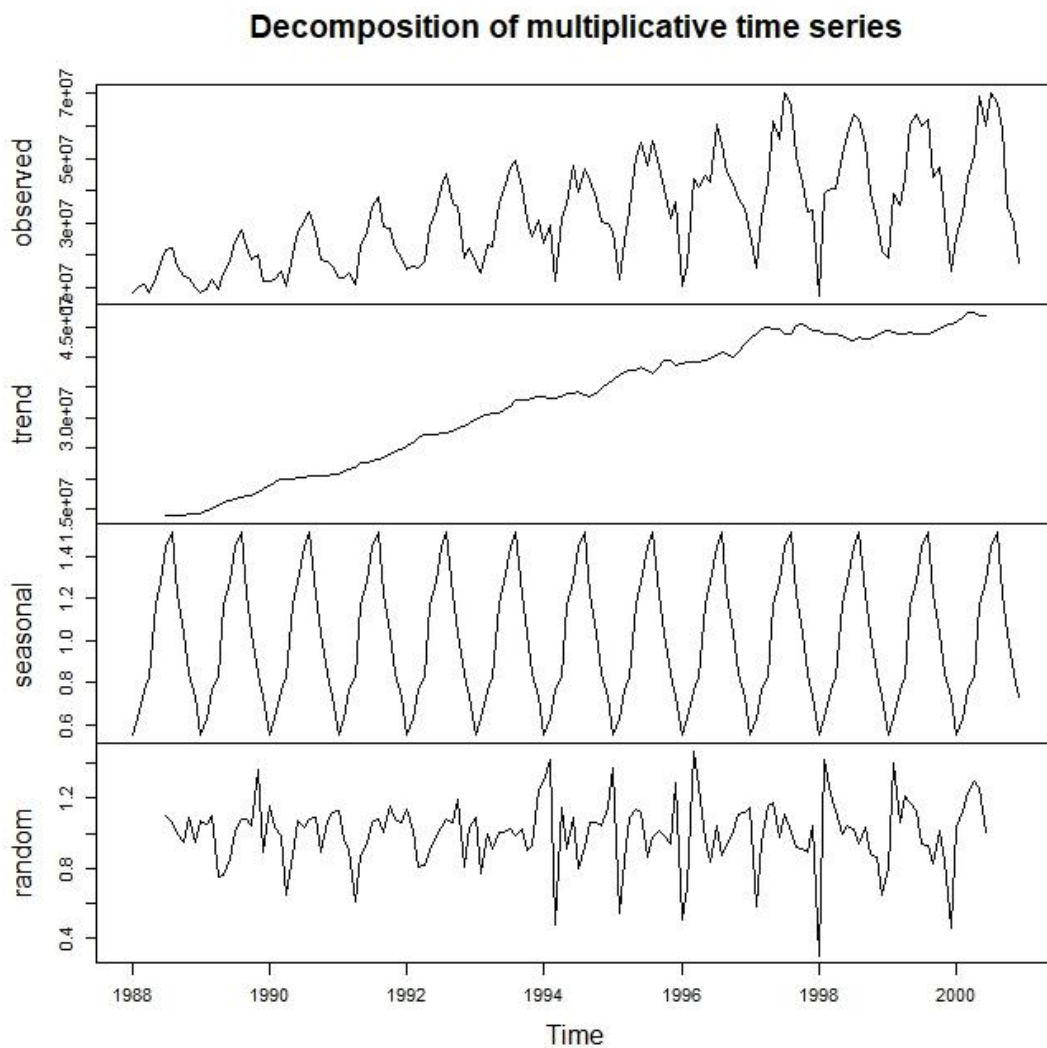


When the ACF plot is analyzed, significant spikes at 12,24,36... months can be seen and they are positive. This indicates positive seasonality on yearly basis with lag=12.

### Additional analysis:

```
bs.dec <- decompose(BS.ts, type="multiplicative")  
plot(bs.dec)
```

Since the amplitude of the seasonal effect seems to increase as  $t$  increases, assuming seasonal effect acts proportionally rather than constant difference per year might be more useful in correct analysis approach. That's why multiplicative model type is used in decomposing.



As decomposed model graphs show, obvious trend and significant seasonal effect are proven by decomposition model. Linear/time-varying increase in trend should be reduced with differencing method and the multiplicative progress can be eliminated with logarithmic transformation.

# Method A: FORECASTING WITH REGRESSION

## 1. Preliminary Transformation

Since the model is multiplicative, logarithmic function is used to turn the model to an additive process.

## 2. Definition of new variables

There are two way to include variables for seasonality and trend:

1. One way is using lagged variables for trend and seasonality. For trend  $Y_{t-1}$  variable and for seasonality  $Y_{t-12}$  and  $Y_{t-13}$  variables are created.

```
Sales lag1<-log(data[c(13:155),2])
Sales lag12<-log(data[c(2:144),2])
Sales lag13<-log(data[c(1:143),2])
```

2. Other way is creating different vectors for trend and seasonality:

```
trend=c(1:143)
s2<-as.numeric(trend%%12==2)
s3<-as.numeric(trend%%12==3)
s4<-as.numeric(trend%%12==4)
s5<-as.numeric(trend%%12==5)
s6<-as.numeric(trend%%12==6)
s7<-as.numeric(trend%%12==7)
s8<-as.numeric(trend%%12==8)
s9<-as.numeric(trend%%12==9)
s10<-as.numeric(trend%%12==10)
s11<-as.numeric(trend%%12==11)
s12<-as.numeric(trend%%12==0)
```

The length of the vector is 143, because:

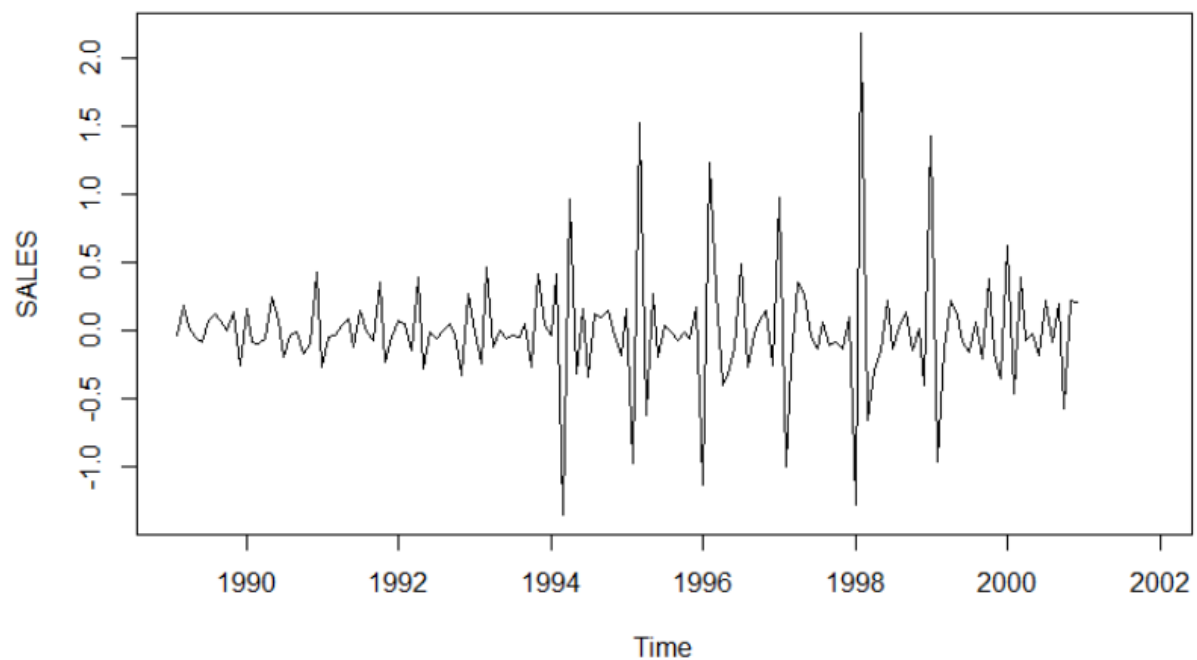
- The models will be compared and because of  $Y_{t-13}$  variable the regression starts from 14<sup>th</sup> variable.
- The data set contains 156 observations of sales value.

## 3. Detection of elements to be extracted

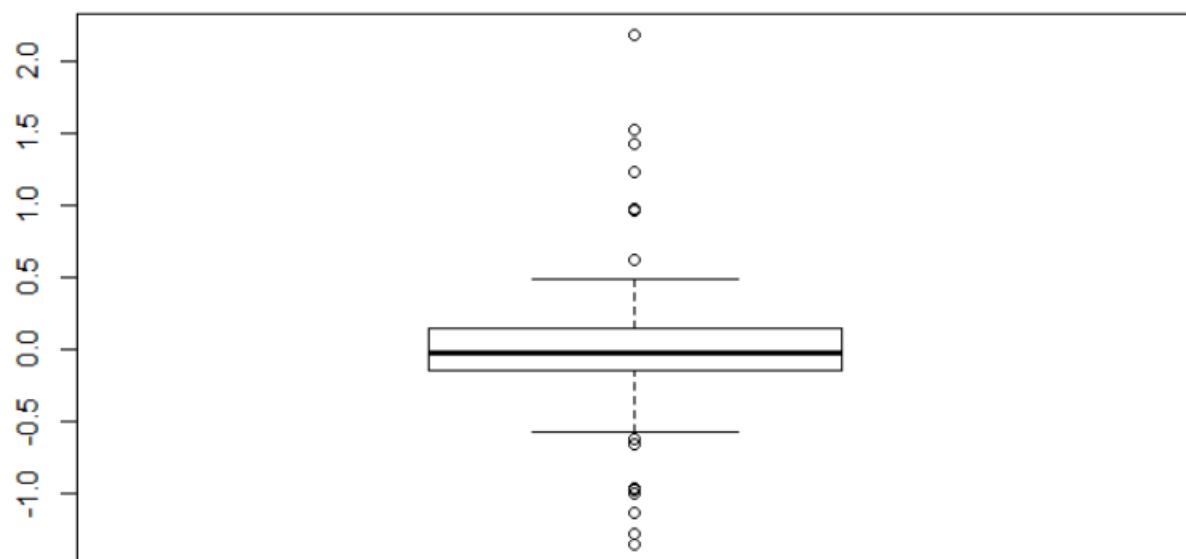
Since the data is multiplicative and consists trend and seasonality, there is need for logarithmic for turning it to a additive process and differentials for removing trend and seasonality. After these processes outlier analysis can be made.

```
data <- read_xls("C:/Users/marji/Desktop/Bogazici/IE360/Project/EP-IE360-Project 2019.xls")
BS<-data[,2]
BS.ts<-ts(BS,freq=12,start=c(1988,1))
Bs.ts.residuals<-diff(diff(log(BS.ts)),lag=12)
plot(Bs.ts.residuals)
boxplot(Bs.ts.residuals)
boxplot.stats(Bs.ts.residuals)
```

Additive time series with trend and seasonality removed: Some outliers seems to exist:



Box plot of the data:



Statistical approach to outliers.

```
> boxplot.stats(Bs.ts.residuals)
$stats
[1] -0.57445318 -0.14746895 -0.01869725  0.14282607  0.49496650

$n
[1] 143

$conf
[1] -0.05705283  0.01965834

$out
[1] -1.3530896  0.9683141 -0.9760562  1.5336822 -0.6212097 -1.1321026  1.2315122  0.9839660 -0.9953860
[10] -1.2765046  2.1893484 -0.6540577  1.4332498 -0.9673505  0.6190688
```

These outlier elements can be extracted from the data.

```
> which(Bs.ts.residuals %in% boxplot.stats(Bs.ts.residuals)$out)
[1] 62 63 73 74 75 84 85 96 97 108 109 110 120 121 132
```

## 4. Model

Sales are fitted into model as logarithms and all the explanatory variables are used.

```
Sales<-log(data[c(14:156),2])
dataforsales<-data[c(14:156),c(3:8)]
```

Lagged variables for trend and seasonality:

```
> dataforsalesreg2<-data.frame(SALES=Sales, dataforsales, trend=Saleslag1,
  lag12=Saleslag12, lag13=Saleslag13)
> new.reg.sales<-lm(SALES~.,data=dataforsalesreg2)
> summary(new.reg.sales)
```

```
Call:
lm(formula = SALES ~ ., data = dataforsalesreg2)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-0.83518 -0.10548 -0.00222  0.10304  0.58839
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)   9.2432295   1.7559783    5.264 5.51e-07 ***
CORRECTED.PRICE -0.0005455   0.0002003   -2.723  0.00734 **
TOURISM        0.4941184   0.0944949    5.229 6.44e-07 ***
RAMADAN       -0.0200352   0.0030301   -6.612 8.42e-10 ***
TU.EP.PARITY  -0.6179475   0.9339758   -0.662  0.50935
RAKI.EP.PARITY -0.0019592   0.0120375   -0.163  0.87096
Cola.EP.Parity  0.3364734   0.1567561    2.146  0.03365 *
SALES.1       -0.1115683   0.0799533   -1.395  0.16521
SALES.2        0.4065665   0.0758313    5.361 3.54e-07 ***
SALES.3        0.1997635   0.0675340    2.958  0.00367 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.2065 on 133 degrees of freedom
Multiple R-squared:  0.8528,    Adjusted R-squared:  0.8428
F-statistic: 85.62 on 9 and 133 DF, p-value: < 2.2e-16
```

Vectors for trend and seasonality:

```
> dataforsalesreg1<-data.frame(SALES=Sales, dataforsales, trend=trend, S2=s2,
S3=s3, S4=s4, S5=s5, S6=s6, S7=s7, S8=s8, S9=s9, S10=s10, S11=s11, S12=s12)
> reg.sales<-lm(SALES~., data=dataforsalesreg1)
> summary(reg.sales)
```

Call:

```
lm(formula = SALES ~ ., data = dataforsalesreg1)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-0.55373	-0.08347	0.00928	0.09216	0.60051

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	15.7448124	1.1719239	13.435	< 2e-16	***
CORRECTED.PRICE	-0.0009189	0.0001765	-5.208	7.71e-07	***
TOURISM	0.0455547	0.1253841	0.363	0.716984	.
RAMADAN	-0.0264182	0.0024687	-10.701	< 2e-16	***
TU.EP.PARITY	0.8771478	1.0474122	0.837	0.403955	
RAKI.EP.PARITY	0.0200606	0.0109587	1.831	0.069566	.
Cola.EP.Parity	0.1826572	0.1382385	1.321	0.188828	
trend	0.0071267	0.0007465	9.547	< 2e-16	***
S2	0.2500666	0.0727103	3.439	0.000795	***
S3	0.2901467	0.0786457	3.689	0.000335	***
S4	0.5284039	0.0971812	5.437	2.76e-07	***
S5	0.5993458	0.0977075	6.134	1.06e-08	***
S6	0.7600834	0.1039038	7.315	2.80e-11	***
S7	0.7893207	0.1068559	7.387	1.93e-11	***
S8	0.5440444	0.1032362	5.270	5.85e-07	***
S9	0.3622490	0.0935867	3.871	0.000174	***
S10	0.1583492	0.0730430	2.168	0.032077	*
S11	0.0997400	0.0716138	1.393	0.166188	
S12	-0.1142736	0.0728983	-1.568	0.119529	

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1737 on 124 degrees of freedom

Multiple R-squared: 0.903, Adjusted R-squared: 0.8889

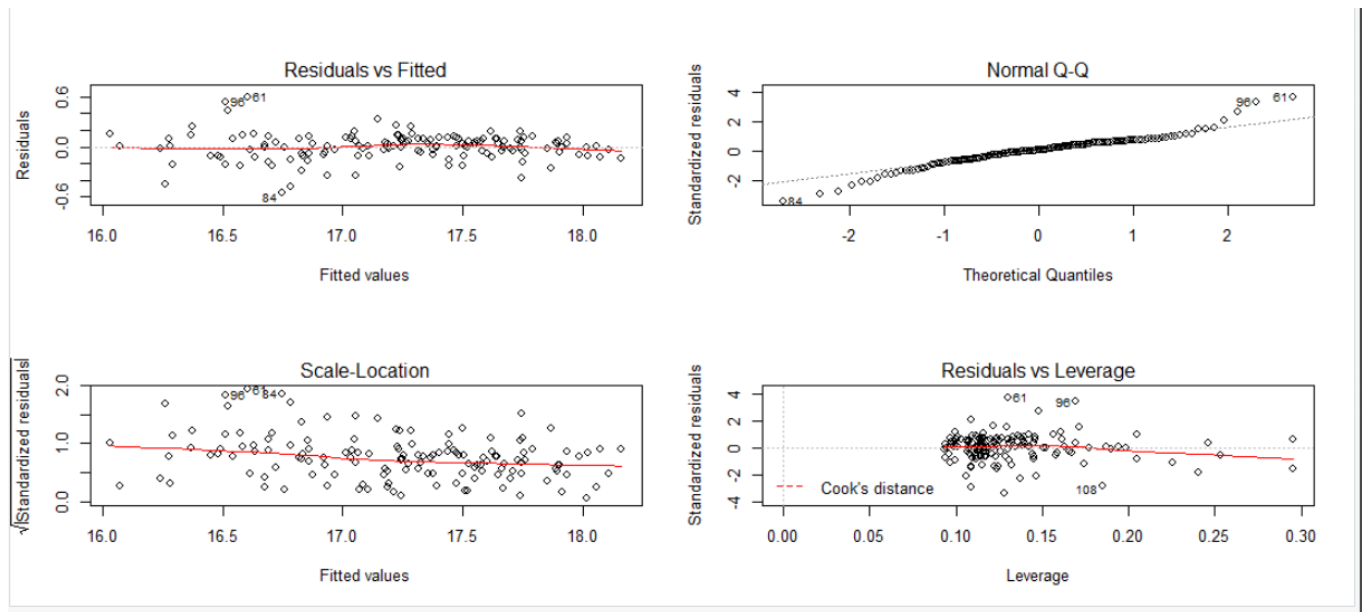
F-statistic: 64.12 on 18 and 124 DF, p-value: < 2.2e-16

By looking at the model summary, the R-squared values are good. The F-value is significant that the variables explain the "SALES" variable. There is a trade-off between the F-statistic value and the R-squared value. Since the error explained by the model is higher with vectors used for trend and seasonality, second model will be used.

Investigating the regression coefficients, it can be seen that "TOURISM", "RAKI.EP.PARITY", and "Cola.EP.Parity" are not significant to explain the "SALES" variable.

```
par(mfrow=c(2,2))
```

```
plot(reg.sales)
```



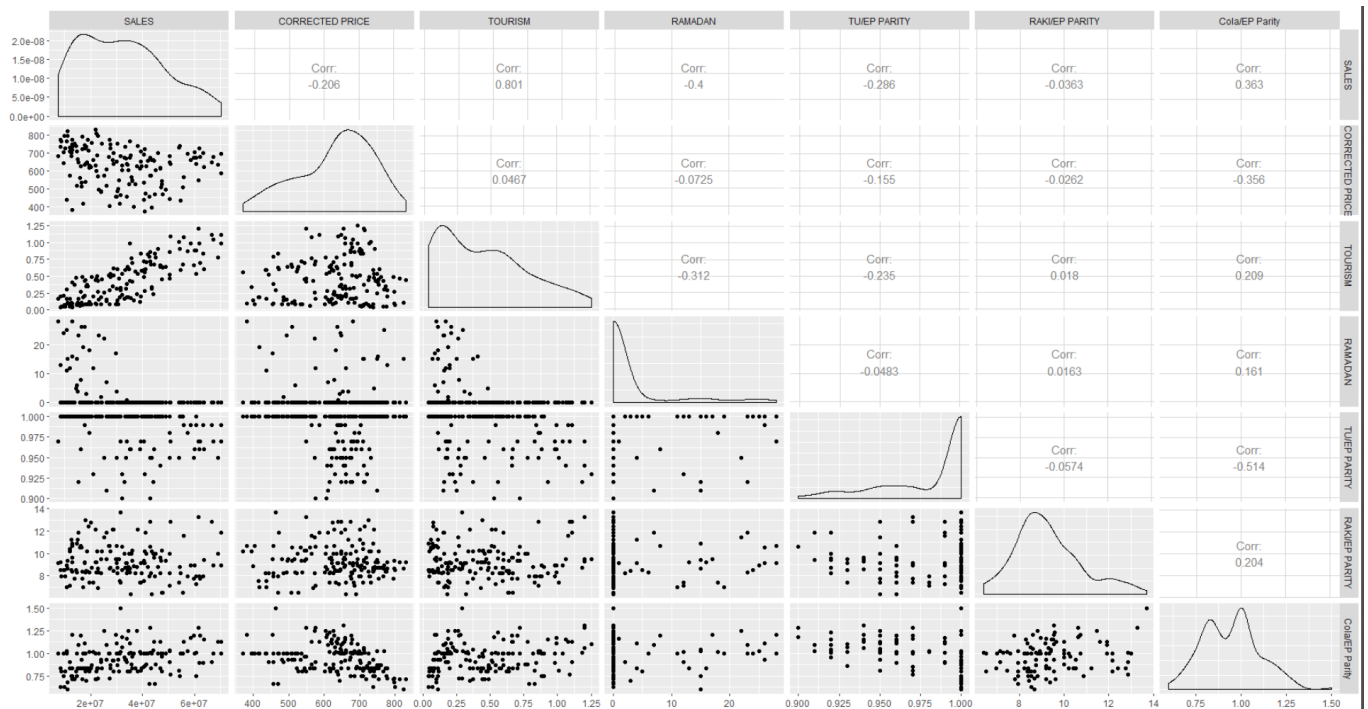
Diagnostic plot shows that the assumptions are satisfied. Correlations between the regression coefficients should be investigated.

```
> dataset<-data[,c(-1)]
> cor(dataset,method="pearson")
```

	SALES	CORRECTED PRICE	TOURISM	RAMADAN	TU/EP PARITY	RAKI/EP PARITY	Cola/EP Parity
SALES	1	NA	NA	NA	NA	NA	NA
CORRECTED PRICE	NA	1.00000000	0.04673927	-0.07249671	-0.15494726	-0.02616131	-0.3561985
TOURISM	NA	0.04673927	1.00000000	-0.31234849	-0.23457872	0.01799197	0.2088743
RAMADAN	NA	-0.07249671	-0.31234849	1.00000000	-0.04827465	0.01625614	0.1605598
TU/EP PARITY	NA	-0.15494726	-0.23457872	-0.04827465	1.00000000	-0.05738101	-0.5135383
RAKI/EP PARITY	NA	-0.02616131	0.01799197	0.01625614	-0.05738101	1.00000000	0.2043873
Cola/EP Parity	NA	-0.35619854	0.20887425	0.16055983	-0.51353826	0.20438725	1.0000000

```
library(GGally)
dataset<-data[,c(-1)]
ggpairs(dataset)
```





The correlation matrix shows that the correlation between the Cola/EP variable and other variables are too high. Therefore, this explanatory variable should be excluded from the model. This high correlation may cause malfunction of the model:

```
> dataforsales<-data[c(14:156),c(3:7)]
> dataforsalesreg3<-data.frame(SALES=Sales,dataforsales, trend=trend, S2=s2,
S3=s3,S4=s4,S5=s5,S6=s6,S7=s7,S8=s8,S9=s9,S10=s10,S11=s11,S12=s12)
> reg.sales.3<-lm(SALES~.,data=dataforsalesreg3)
> summary(reg.sales.3)
```

Call:  
lm(formula = SALES ~ ., data = dataforsalesreg3)

Residuals:

Min	1Q	Median	3Q	Max
-0.54572	-0.08215	0.00809	0.08624	0.62739

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	16.1014558	1.1438148	14.077	< 2e-16	***
CORRECTED.PRICE	-0.0009919	0.0001681	-5.902	3.16e-08	***
TOURISM	0.0341241	0.1254580	0.272	0.786074	
RAMADAN	-0.0257334	0.0024209	-10.630	< 2e-16	***
TU.EP.PARITY	0.6707265	1.0387816	0.646	0.519666	
RAKI.EP.PARITY	0.0249287	0.0103515	2.408	0.017491	*
trend	0.0074264	0.0007133	10.411	< 2e-16	***
S2	0.2404610	0.0725615	3.314	0.001204	**
S3	0.2943821	0.0788144	3.735	0.000284	***
S4	0.5312395	0.0974470	5.452	2.56e-07	***
S5	0.6054666	0.0978884	6.185	8.12e-09	***
S6	0.7669661	0.1040823	7.369	2.05e-11	***
S7	0.7947101	0.1070961	7.421	1.57e-11	***
S8	0.5486204	0.1034855	5.301	5.03e-07	***
S9	0.3644651	0.0938505	3.883	0.000166	***
S10	0.1625987	0.0731896	2.222	0.028109	*
S11	0.0992055	0.0718260	1.381	0.169684	
S12	-0.1228252	0.0728268	-1.687	0.094186	.

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.1742 on 125 degrees of freedom  
Multiple R-squared: 0.9016, Adjusted R-squared: 0.8882  
F-statistic: 67.39 on 17 and 125 DF, p-value: < 2.2e-16

F-statistic improved where R-squared is still 90%. In contrast there are still regression coefficients with large p values. Therefore another model is suggested:

```
reg.sales.4=step(reg.sales.3,direction=c("backward"))
summary(reg.sales.4)
```

```
Call:
lm(formula = SALES ~ CORRECTED.PRICE + RAMADAN + RAKI.EP.PARITY +
    trend + S2 + S3 + S4 + S5 + S6 + S7 + S8 + S9 + S10 + S11 +
    S12, data = dataforsalesreg3)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-0.54218 -0.09622  0.00349  0.09724  0.62769
```

```
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)   16.8257397   0.1408845  119.429 < 2e-16 ***
CORRECTED.PRICE -0.0010486   0.0001448   -7.241 3.78e-11 ***
RAMADAN       -0.0256733   0.0023849  -10.765 < 2e-16 ***
RAKI.EP.PARITY  0.0235382   0.0093747   2.511 0.013300 *
trend          0.0072161   0.0003625   19.908 < 2e-16 ***
S2             0.2385147   0.0707594    3.371 0.000993 ***
S3             0.3025760   0.0708927    4.268 3.82e-05 ***
S4             0.5558265   0.0725261    7.664 4.07e-12 ***
S5             0.6313128   0.0725838    8.698 1.48e-14 ***
S6             0.7967868   0.0734409   10.849 < 2e-16 ***
S7             0.8263961   0.0732352   11.284 < 2e-16 ***
S8             0.5776868   0.0727700    7.939 9.33e-13 ***
S9             0.3861397   0.0726507    5.315 4.64e-07 ***
S10            0.1674269   0.0724268    2.312 0.022406 *
S11            0.1031710   0.0709725    1.454 0.148503
S12           -0.1230572   0.0723663   -1.700 0.091489 .
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 0.1732 on 127 degrees of freedom
Multiple R-squared:  0.9012,    Adjusted R-squared:  0.8895
F-statistic: 77.24 on 15 and 127 DF,  p-value: < 2.2e-16
```

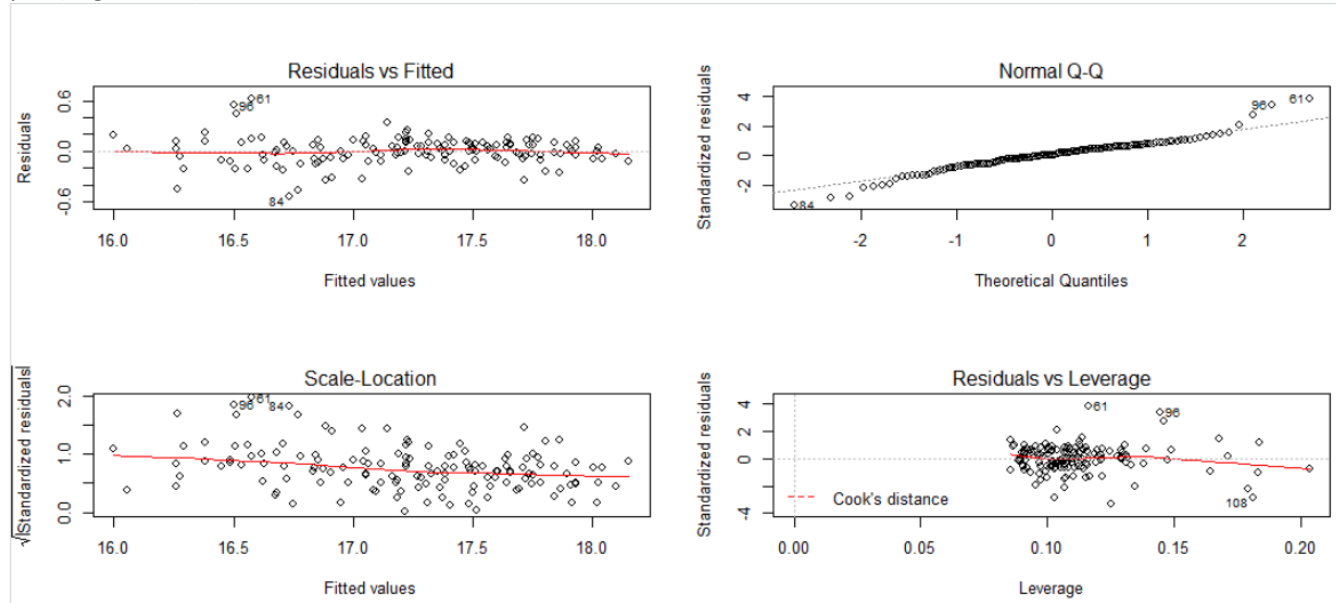
## 5. Validity of Analysis

P value of F-statistic is low, therefore the regression variables together are significant to explain the "SALES" variable. The p value of T-distribution of all the variables are low and that means  $H_0: \beta_i = 0$  is rejected.

```
> library(car)
> vif(reg.sales.4)
CORRECTED.PRICE      RAMADAN  RAKI.EP.PARITY      trend
      1.073717      1.268168      1.066783      1.067866
      S2          S3          S4          S5
      1.835847      1.842771      1.928667      1.931736
      S6          S7          S8          S9
      1.977624      1.966564      1.941658      1.935295
      S10         S11         S12
      1.923385      1.846920      1.773597
```

There is no large vif values, that means there is no multicollinearity between them.

```
par(mfrow=c(2,2))
plot(reg.sales.4)
```



Residuals do not follow a pattern, normality assumption is satisfied, the diagnostic plot supports the validity of the model.

```
> dwtest(reg.sales.4)
```

Durbin-Watson test

```
data: reg.sales.4
DW = 1.9326, p-value = 0.2965
alternative hypothesis: true autocorrelation is greater than 0
```

DW test shows that the hypothesis "The autocorrelation between residuals is greater than 0" is not significant.

## 6. Prediction of Beer Sales for 2001

The prediction data set for the next year is created. Since the model output is a logarithm value, the exponential of the value is the forecast for the corresponding month next year.

```
trend.pred=c(144:155)
s2.pred<-as.numeric(trend.pred%%12==2)
s3.pred<-as.numeric(trend.pred%%12==3)
s4.pred<-as.numeric(trend.pred%%12==4)
s5.pred<-as.numeric(trend.pred%%12==5)
s6.pred<-as.numeric(trend.pred%%12==6)
s7.pred<-as.numeric(trend.pred%%12==7)
s8.pred<-as.numeric(trend.pred%%12==8)
s9.pred<-as.numeric(trend.pred%%12==9)
s10.pred<-as.numeric(trend.pred%%12==10)
s11.pred<-as.numeric(trend.pred%%12==11)
s12.pred<-as.numeric(trend.pred%%12==0)
dataforsales.pred<-data[c(157:168),c(3:7)]

prediction=data.frame(dataforsales.pred, trend=trend.pred,
                      S2=s2.pred,S3=s3.pred,S4=s4.pred,S5=s5.pred,
                      S6=s6.pred,S7=s7.pred,S8=s8.pred,S9=s9.pred,
                      S10=s10.pred,S11=s11.pred,S12=s12.pred)
```

```
> exp(predict(reg.sales.4,prediction))
      157      158      159      160      161      162      163      164
32829931 35911375 47739100 52171564 61320467 70006786 77184173 83329950
      165      166      167      168
68158986 53136342 29341960 26663512
```

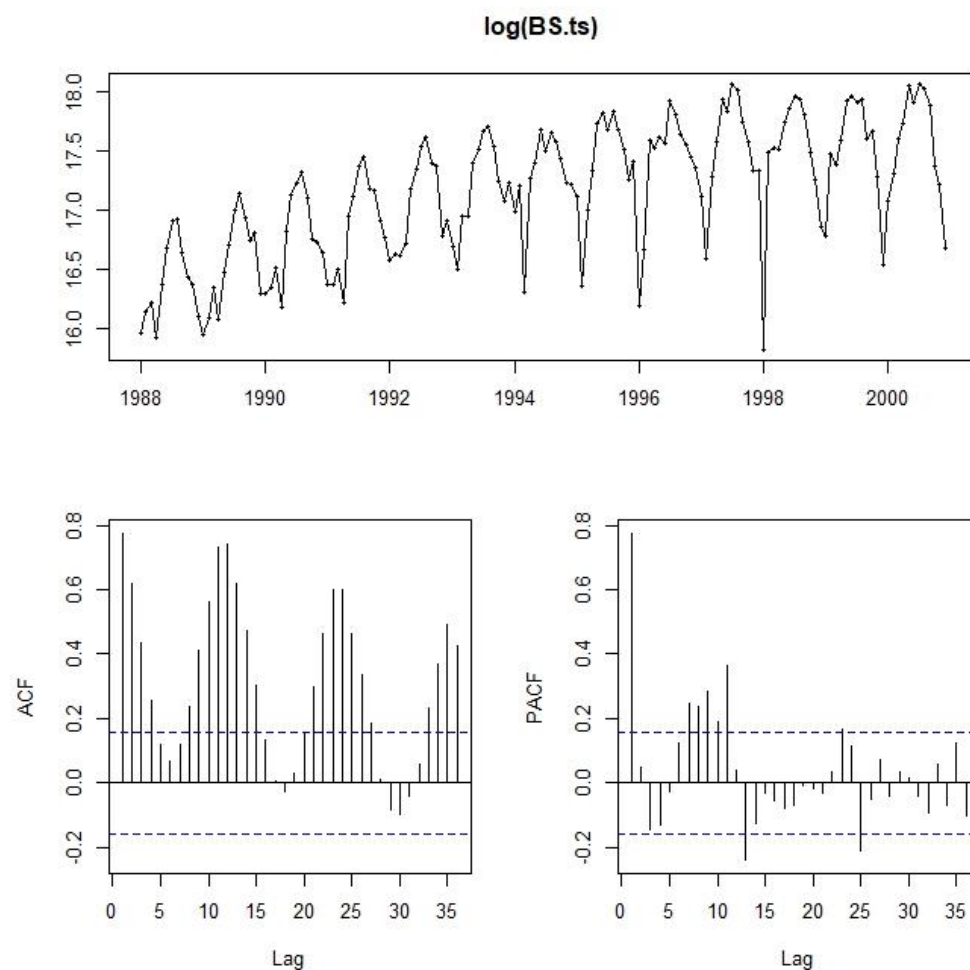
## Method B: FORECASTING WITH TIME SERIES ANALYSIS

### 1- Preliminary transformation decision:

To induce stationarity, it is decided that preliminary transformation is needed. Logarithmic transformation should be applied to stabilise the variance of time series.

```
tsdisplay(log(BS.ts))
```

### 2- Utilization of time series plots with ACF and PACF



When the shapes of auto correlation functions of the time series of logarithmic Beer Sales is examined, it is clearly observed that there is a sinusoidal relationship with 12 lags which implies that there is seasonality at lag 12. The auto correlation values at the other lags are also significant so there is a both trend and seasonality . Since the series has a strong and consistent seasonal pattern, then we should use an order of seasonal differencing.

```
#ndiffs(log(BS.ts))  
[1] 1  
#nsdiffs(log(BS.ts))  
[1] 1
```

Additional proof to use seasonal and regular difference as appropriate number of differences are shown by KPSS test. These functions suggests that we should do both a seasonal difference and one regular difference on logarithmic beer sales data.

```
diff1 <- diff(log(BS.ts), 12)
```

```
acf(diff1)
```

```
pacf(diff1)
```

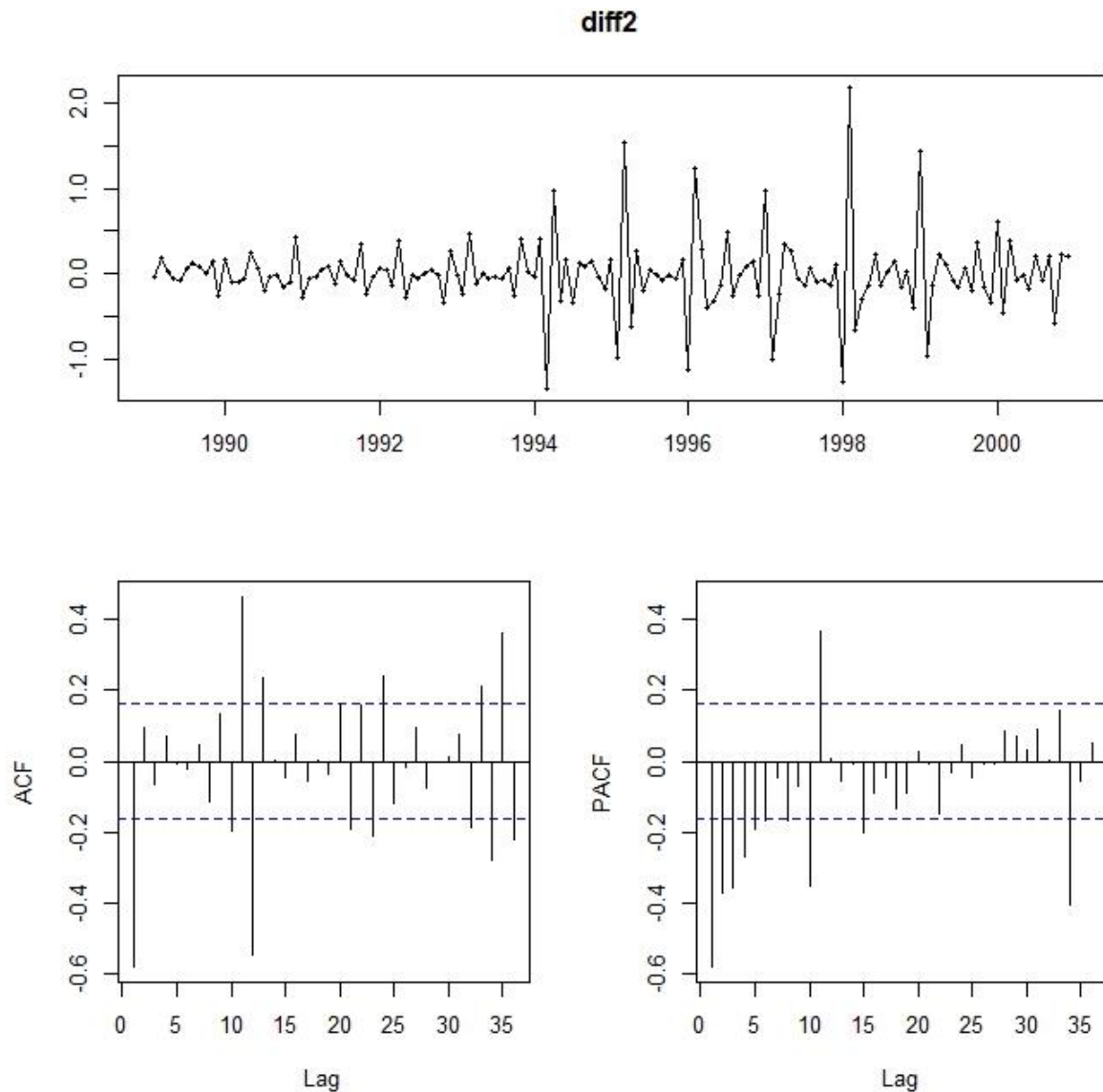
```
diff2 <- diff(diff1, 1)
```

```
plot(diff2)
```

```
acf(diff2, lag.max = 36)
```

```
pacf(diff2, lag.max = 36)
```

```
tsdisplay(diff2)
```



ACF cut off at lag=1 which is a sudden fall from significant level can be seen and PACF dies out slowly, in other words exponentially decaying. MA(1) might be suggested in regular terms. In seasonal terms, significant levels are seen on ACF plot which suggests seasonal AR(1). Since acf function has oscillation movements in significant exceedings while pacf has not, AR(1) is used instead of MA.

### 3- Initial ARIMA model

```

arimaBS<-Arima(log(BS.ts), order=c(1,1,0), seasonal=c(0,1,1))
arimaBS
plot(forecast(arimaBS,h=12))

```

The R code above is used for making ARIMA model with the reasons mentioned above. This is the initial ARIMA model based on the inspection on ACF and PACF plot.

```

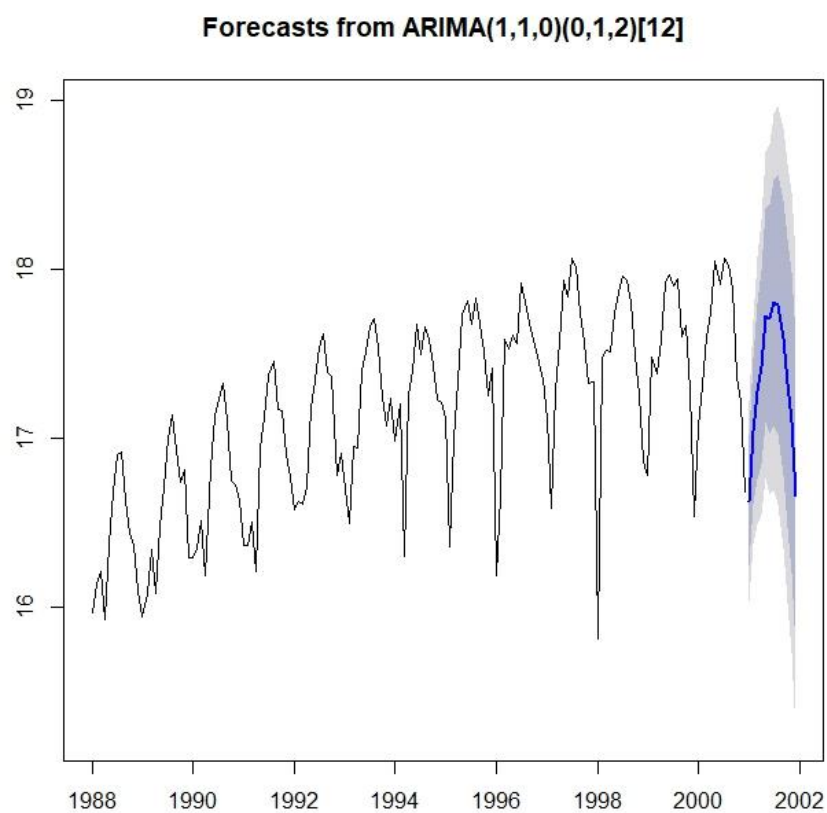
Series: log(BS.ts)
ARIMA(1,1,0)(0,1,2)[12]

Coefficients:
      ar1      sma1      sma2
    -0.5066  -0.610  -0.0065
s.e.   0.0746   0.098   0.1003

sigma^2 estimated as 0.09111:  log likelihood=-33.07
AIC=74.14  AICc=74.43  BIC=85.99

```

The output above gives the AIC, AICc and BIC values of the initial ARIMA model. The plot below gives the data with forecast values of the initial ARIMA model.



## 4- Neighborhood search of the initial model

```

candidate1 <- auto.arima(log(BS.ts) , allowdrift = TRUE)
candidate1
tsdisplay(candidate1$residuals)

```

```

Series: log(BS.ts)
ARIMA(2,1,2)(0,1,2)[12]

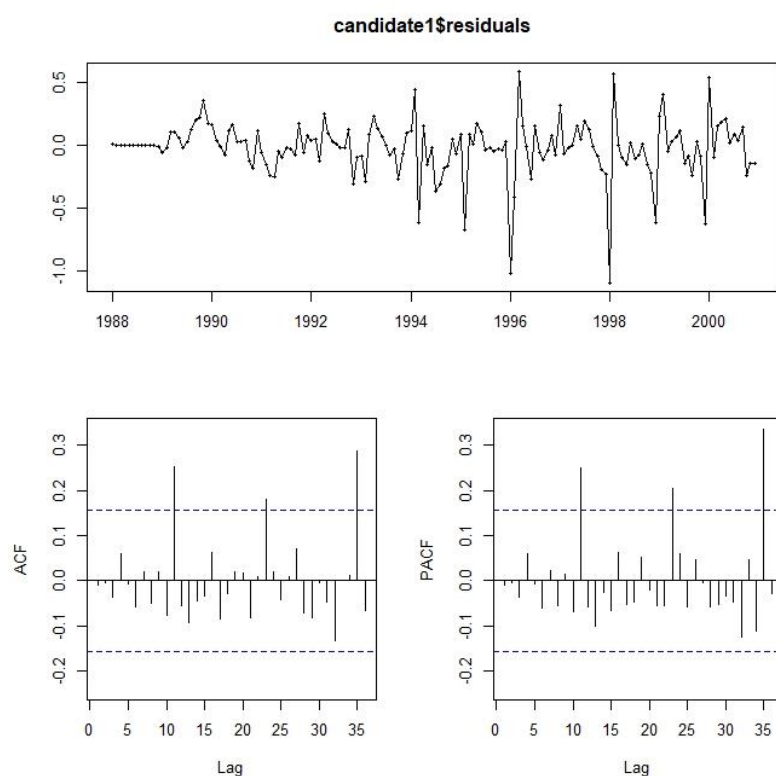
Coefficients:
          ar1      ar2      ma1      ma2      sma1      sma2
s.e.    0.3535  -0.0443  -1.5244   0.5623   -0.512   0.1958
        0.4814   0.1623   0.4680   0.4374    0.089   0.0910

sigma^2 estimated as 0.05701:  log likelihood=1.77
AIC=10.46  AICc=11.29  BIC=31.2

```

First candidate – which is determined by optimization process of auto.arima function and supposed to yield one of the best possible choice of variable selection in ARIMA model- has 1 regular and 1 seasonal difference just as our model and additionally regular AR(2)+MA(2) and a seasonal MA(2). AIC value is 10.46 which is far better than our AIC since lower values on AIC and BIC is preferred.

ACF and PACF of candidate 1 is shown below:



## Candidate 2:

```

candidate2 <- Arima(log(BS.ts), order=c(1,1,1), seasonal=c(0,1,1))
candidate2
tsdisplay(candidate2$residuals)

```



```

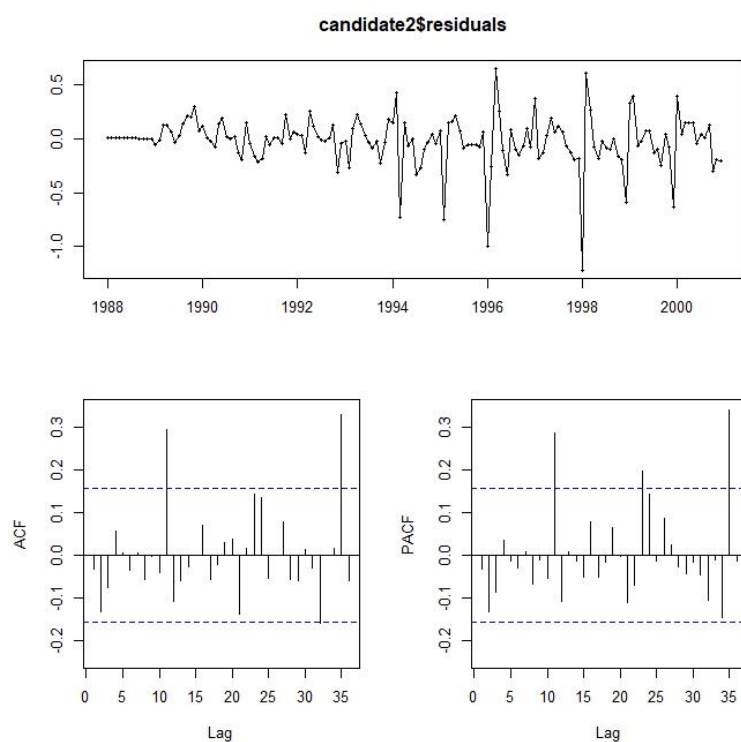
Series: log(BS.ts)
ARIMA(1,1,1)(0,1,1)[12]

Coefficients:
          ar1          ma1          sma1
        -0.1555    -0.9311    -0.4788
s.e.      0.0877     0.0257     0.0789

sigma^2 estimated as 0.05917:  log likelihood=-2.15
AIC=12.31   AICc=12.6   BIC=24.16

```

ACF&PACF plot:



**Candidate 3:**

```

candidate3 <- Arima(log(BS.ts), order=c(1,1,1), seasonal=c(0,1,2))

candidate3

tsdisplay(candidate3$residuals)

```

```

Series: log(BS.ts)
ARIMA(1,1,1)(0,1,2)[12]

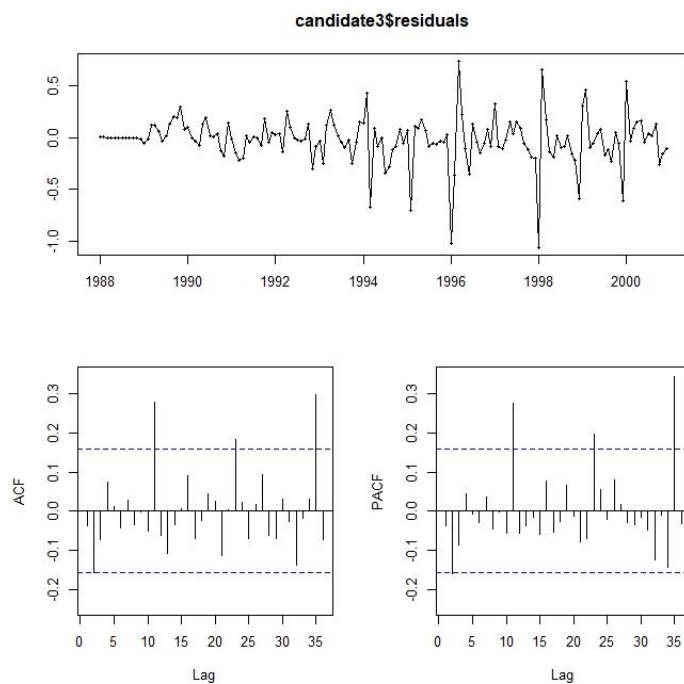
Coefficients:
          ar1          ma1          sma1          sma2
        -0.1856    -0.9396    -0.4883     0.1724
s.e.      0.0877     0.0242     0.0861     0.0929

sigma^2 estimated as 0.05818:  log likelihood=-0.45

```

AIC=10.9    AICc=11.34    BIC=25.72

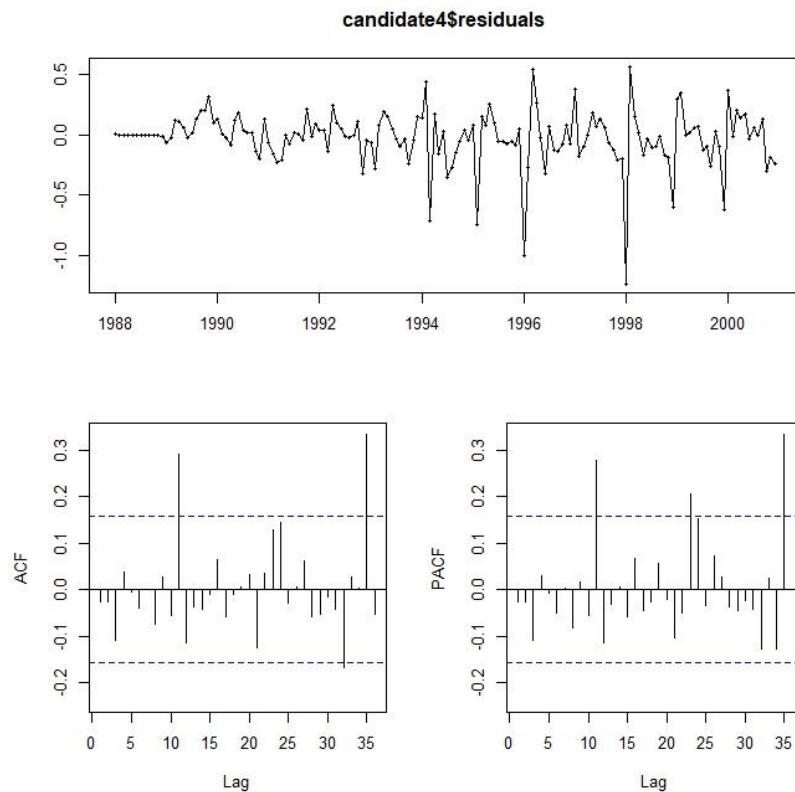
ACF&PACF plot:



**Candidate 4:**

```
candidate4 <- Arima(log(BS.ts), order=c(2,1,1), seasonal=c(0,1,1))  
candidate4  
tsdisplay(candidate4$residuals)
```

```
Series: log(BS.ts)  
ARIMA(2,1,1)(0,1,1)[12]  
  
Coefficients:  
      ar1      ar2      ma1      sma1  
    -0.1828 -0.1156 -0.9217 -0.4784  
s.e.   0.0898   0.0859   0.0294   0.0773  
  
sigma^2 estimated as 0.05884: log likelihood=-1.26  
AIC=12.52  AICc=12.96  BIC=27.33  
ACF&PACF plot:
```



### Candidate 5:

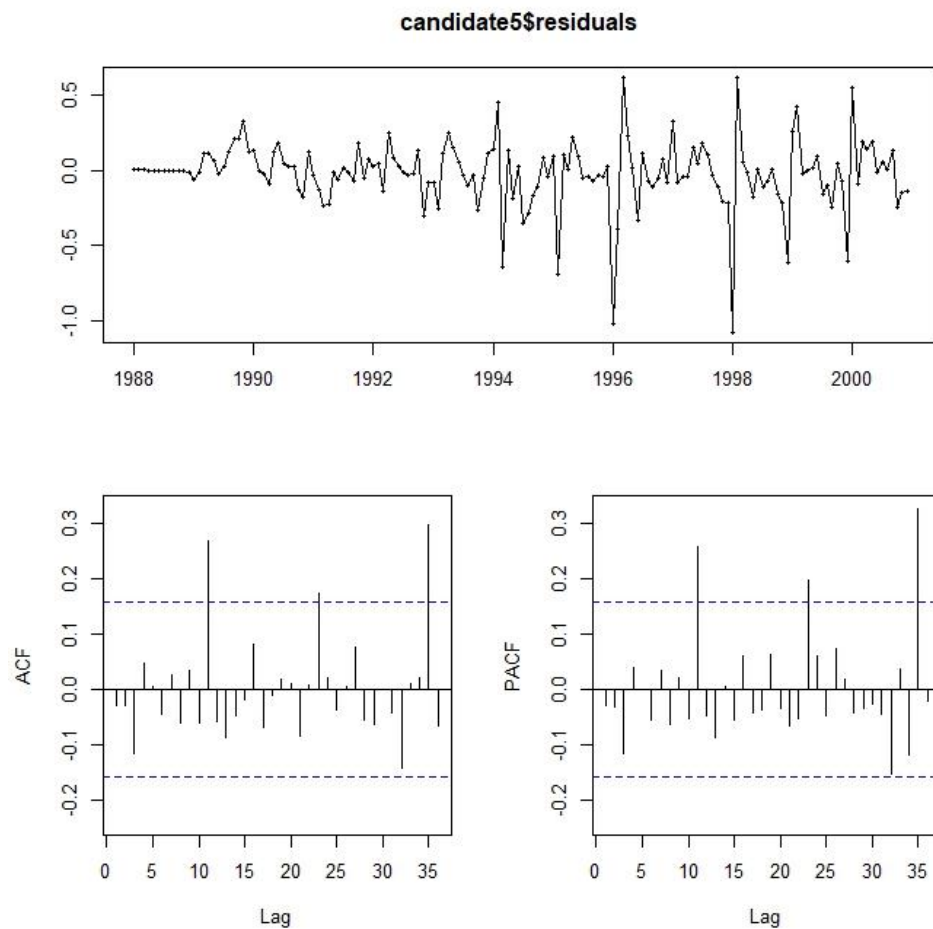
```
candidate5 <- Arima(log(BS.ts), order=c(2,1,1), seasonal=c(0,1,2))
candidate5
tsdisplay(candidate5$residuals)
```

```
Series: log(BS.ts)
ARIMA(2,1,1)(0,1,2)[12]

Coefficients:
      ar1      ar2      ma1      sma1      sma2
    -0.2228 -0.1436 -0.9290 -0.5019  0.1902
s.e.   0.0900  0.0859  0.0281  0.0867  0.0896

sigma^2 estimated as 0.05736: log likelihood=0.92
AIC=10.16  AICC=10.78  BIC=27.94
```

ACF&PACF plot:



### Candidate 6:

```
candidate6 <- Arima(log(BS.ts), order=c(3,1,1), seasonal=c(0,1,2))
```

```
candidate6
```

```
tsdisplay(candidate6$residuals)
```

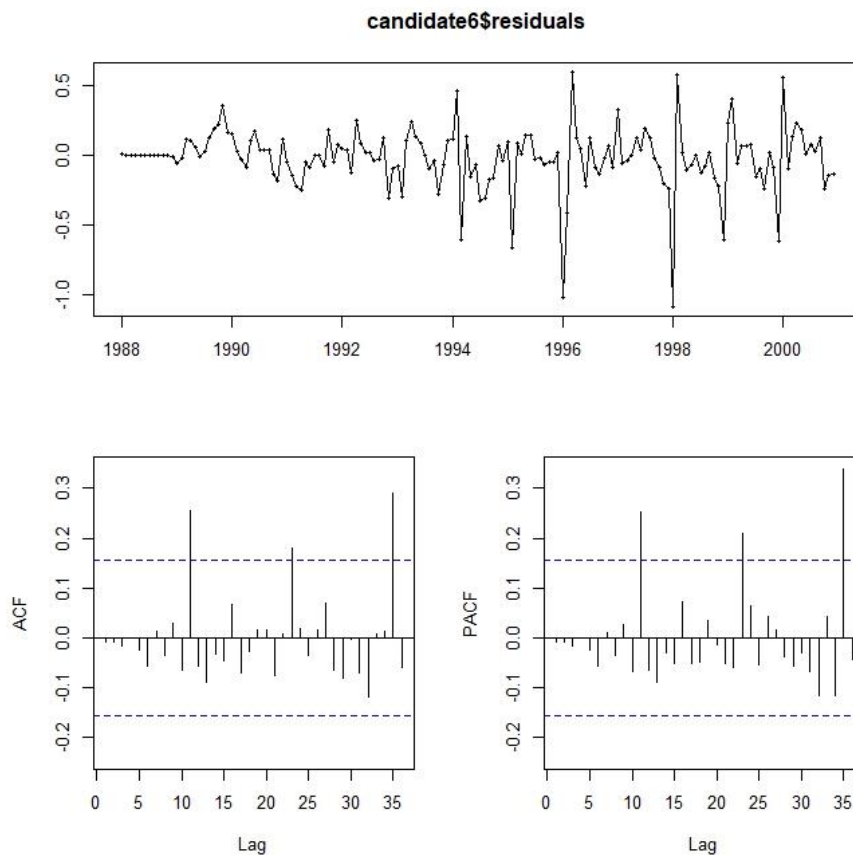
```
Series: log(BS.ts)  
ARIMA(3,1,1)(0,1,2)[12]
```

```
Coefficients:
```

	ar1	ar2	ar3	ma1	sma1	sma2
	-0.2577	-0.1878	-0.1326	-0.9160	-0.5036	0.2024
s.e.	0.0921	0.0902	0.0868	0.0346	0.0861	0.0908

```
sigma^2 estimated as 0.05679: log likelihood=2.07  
AIC=9.86 AICc=10.69 BIC=30.6
```

Acf&pacf plot:



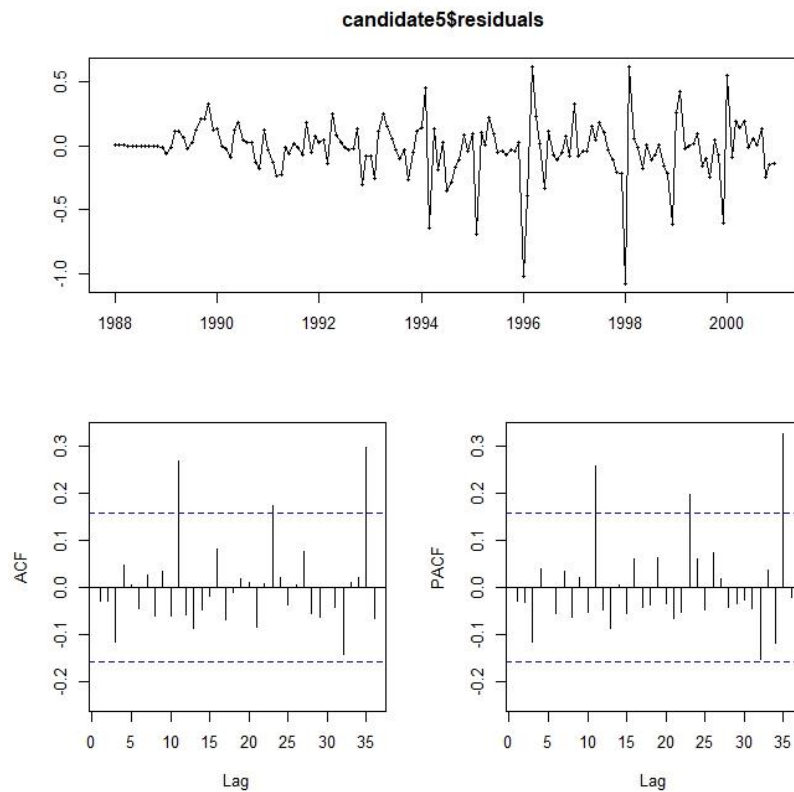
## 5- Best model choice

To choose the best model minimum aic and bic values and noncorrelated residuals are searched. Candidate6 has the minimum AIC value and candidate2 has the minimum BIC value. All of the ACF and PACF have significant values with similar plots. Overall, candidate 5 has the best AIC&BIC value among others, that's why candidate5 is chosen.

```
Series: log(BS.ts)
ARIMA(2,1,1)(0,1,2)[12]

Coefficients:
      ar1      ar2      ma1      sma1      sma2
    -0.2228 -0.1436 -0.9290 -0.5019  0.1902
s.e.   0.0900  0.0859  0.0281  0.0867  0.0896

sigma^2 estimated as 0.05736:  log likelihood=0.92
AIC=10.16  AICc=10.78  BIC=27.94
```



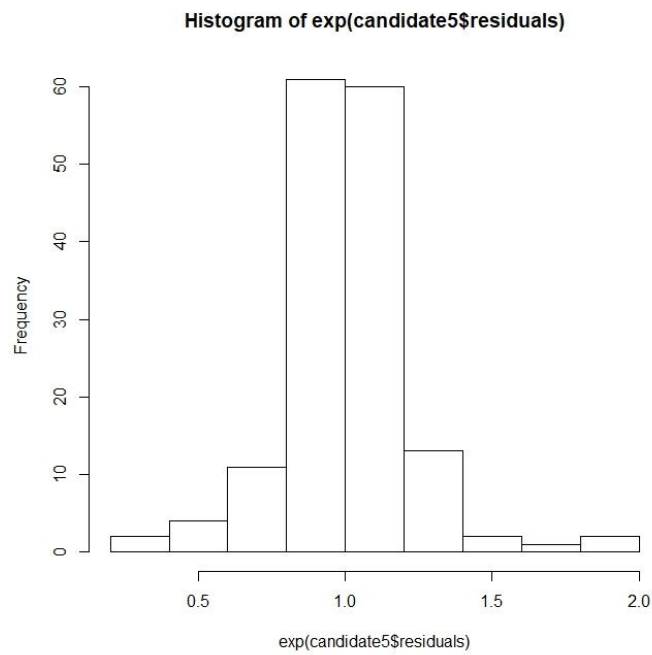
## 6- Validity of analysis

Residuals are should be checked for validity. They should have constant variance and mean that is close to 0.

```
mean(exp(candidate5$residuals))
[1] 1.004584
```

Mean of the residuals are close to one which is desirable for multiplicative process. In multiplicative processes residuals are normally distributed around one. So, this assumption holds.

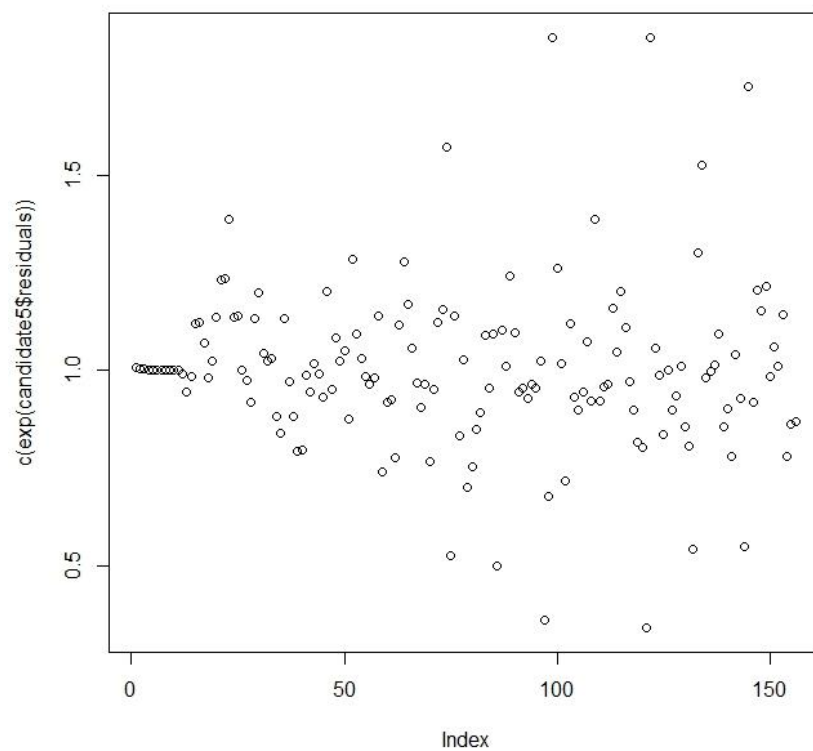
```
hist(exp(candidate5$residuals))
```



Histogram also shows residuals are normally distributed around 1.

```
plot(c(exp(candidate5$residuals)))
```

Residual plot is shown below and as can be inferred that residuals have constant variance



## 7- Prediction of beer sales for 2001

```
forecast(candidate5, h=12)
plot(forecast(candidate5, h=12))
```

The R code above is used in order to forecast beer sales by chosen model candidate 5. Outputs and forecast plot are listed below:

Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95	
Jan 2001	16.87892	16.57200	17.18585	16.40952	17.34832
Feb 2001	17.49081	17.18037	17.80125	17.01604	17.96559
Mar 2001	17.53732	17.22665	17.84799	17.06219	18.01244
Apr 2001	17.69414	17.38192	18.00636	17.21664	18.17164
May 2001	18.00843	17.69577	18.32109	17.53026	18.48661
Jun 2001	17.97792	17.66496	18.29088	17.49929	18.45655
Jul 2001	18.02857	17.71518	18.34195	17.54928	18.50785
Aug 2001	18.02294	17.70914	18.33674	17.54302	18.50286
Sep 2001	17.80220	17.48800	18.11640	17.32167	18.28273
Oct 2001	17.53815	17.22355	17.85276	17.05700	18.01930
Nov 2001	17.27987	16.96486	17.59488	16.79810	17.76164
Dec 2001	16.63514	16.31973	16.95056	16.15276	17.11753

**Forecasts from ARIMA(2,1,1)(0,1,2)[12]**

