Discrete Math- HW3

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Section 2.1

- 6a. The set of all people who speak English with an Australian accent are a subset of people who speak English
- 6b. The set of citrus fruits are a subset of fruits.
- 6c. Neither are subsets of each other.
- 11a. False
- 11b. False
- 11c. False
- 11d. True
- 11e. False
- 11f. False
- 11g. True
- 12a. True
- 12b. True
- 12c. False
- 12d. True
- 12e. True
- 12f. True
- 12g. False
- 13a. True
- 13b. True

- 13c. False
- 13d. True
- 13e. True
- 13f. False
- 22a. 0
- 22b. 1
- 22c. 2
- 22d. 3
- 24. Yes
- $25a.\ 8$
- $25b.\ 16$
- 25c. 2

Section 2.2

- 2a. $A \cap B$
- 2b. A B
- 2c. $A \cup B$
- 2d. $\overline{A} \cup \overline{B}$
- 4a. $A \cup B = \{a,b,c,d,e,f,g,h\}$
- 4b. $A \cap B = \{a, b, c, d, e\}$
- 4c. $A B = \{\emptyset\}$
- 4d. $B A = \{f, g, h\}$
- 16e. $A \cup (B A) = A \cup B$

Have to show $A \cup (B - A) \subseteq A \cup B$

$$x \in A \vee x \in B-A$$

$$x \in A \lor (x \in B \land \neg (x \in A))$$

 $x \in A \vee x \in B$

 $x \in A \cup B$

Also have to show $A \cup B \subseteq A \cup (B-A)$

 $x \in A \cup B$

$$x \in A \vee x \in B$$

$$x \in A \lor (x \in B \land \neg (x \in A))$$

$$x \in A \lor x \in B - A$$

This proves $A \cup (B - A) = A \cup B$

38.
$$A \oplus B = \{2, 5\}$$

41.
$$A \oplus B = \{x | x \in A \lor x \in B \land \neg (x \in A \land x \in B)\}$$

$$= \{x | x \in A \cup B\} \land \lnot (x \in A \cup B)\}$$

$$= \{x|x \in (A \cup B) - (A \cap B)\}$$

This proves that $A \oplus B = (A \cup B) - (A \cap B)$

Section 2.3

- 3a. f is not a function. A bit string could start with more than one zero, which would lead to multiple images
- 3b. f is a function
- 3c. Not a function. If there is a string of zeros no value is assigned.
- 4a. Domain: N

Range: $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

4b. Domain: $N - \{0\}$

Range: $N - \{0, 1\}$

4c. Domain: All bit strings

Range: N

4d. Domain: All bit strings

Range: N

- 10a. 1:1
- 10b. Not 1:1
- 10c. Not 1:1
- 14a. Onto
- 14b. Not onto
- 14c. Onto
- 14d. Onto
- 14e. Not onto

- 23a. Bijection
- 23b. Not a bijection
- 23c. Bijection
- 23d. Not a bijection

32a.
$$\{..., -4, -2, 0, 2, 4, ...\}$$

- 32b. $\{0, 2, 4, 6, 8, ...\}$
- 32c. **R**

36.
$$g(x) = g(y)$$
$$= f(g(x)) = f(g(y))$$
$$= f \circ g(x) = f \circ g(y)$$
$$= x = y$$

This proves that g is a one to one function

$$37. \ g:A\rightarrow B$$

$$f:B\rightarrow C$$

$$f(g(x)):A\rightarrow C$$

$$A=\{q,r\}$$

$$B=\{s,t\}$$

$$C=\{v\}$$

Here, g(q) = g(r) = s, and f(s) = f(t) = v. This means that f and $f \circ g$ is onto, but g is not, as it doesn't map to all values of B.

Section 2.5

1c. Countably infinite

$$f(x) = 100 - n$$

= $\{99, 98, 97, ...\}$

- 1d. Uncountable
- 1f. Countably infinite

$$f(x) = 7x$$

= $\{..., -14, -7, 0, 7, 14, ...\}$

2d. Uncountable

- 2e. Countably infinite
 - $\{2,1\},\{2,2\},\{2,3\},\dots$
 - $\{3,1\},\{3,2\},\{3,3\},\dots$
- 2f. Countably infinite
 - f(x) = 10x
 - ..., -20, -10, 0, 10, 20, ...
- 3b. Countable
- 3d. Uncountable
- 4c. Uncountable
- 4d. Uncountable
- 10a. $A = \mathbf{R}$
 - $B = \mathbf{R}$
- 10b. $A = \mathbf{R}$
 - $B = \mathbf{R}$ not containing 1
- 10c. $A = \mathbf{R}$
 - $B = \mathbf{Q}$

Sundry

- a. Jeannie Ren- jr3766
 - Alush Benitez- alb2331
- $b.\ {\tt https://oeis.org/wiki/List_of_LaTeX_mathematical_symbols}$
- c. Roughly 12 hours
- d. 5