**Next: Neural Networks** 

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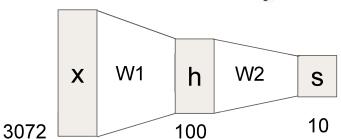
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(Now) 2-layer Neural Network  $f = W_2 \max(0, W_1 x)$ 

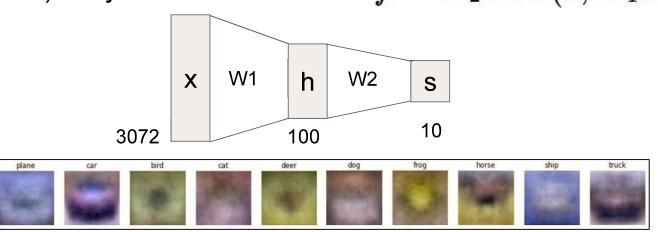
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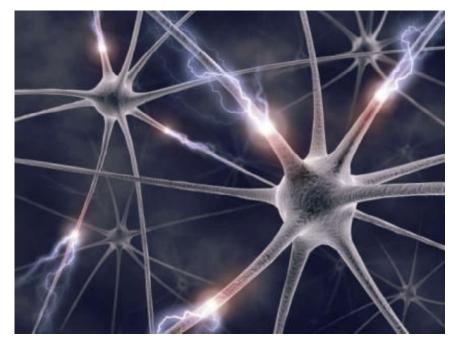
```
(Before) Linear score function: f=Wx (Now) 2-layer Neural Network f=W_2\max(0,W_1x) or 3-layer Neural Network f=W_3\max(0,W_2\max(0,W_1x))
```

#### Full implementation of training a 2-layer Neural Network needs ~20 lines:

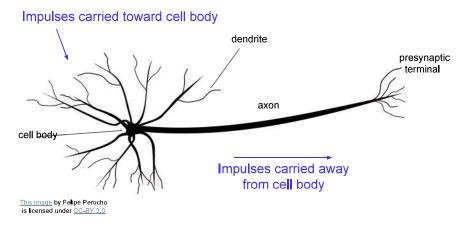
```
import numpy as np
    from numpy.random import randn
4 N, D_in, H, D_out = 64, 1000, 100, 10
5 x, y = randn(N, D_in), randn(N, D_out)
   w1, w2 = randn(D_in, H), randn(H, D_out)
8
   for t in range(2000):
   h = 1 / (1 + np.exp(-x.dot(w1)))
9
    y_pred = h.dot(w2)
     loss = np.square(y_pred - y).sum()
11
      print(t, loss)
13
      grad_y_pred = 2.0 * (y_pred - y)
      grad_w2 = h.T.dot(grad_y_pred)
15
      grad_h = grad_y_pred.dot(w2.T)
17
      grad_w1 = x.T.dot(grad_h * h * (1 - h))
18
      w1 -= 1e-4 * grad_w1
19
      w2 -= 1e-4 * grad_w2
```

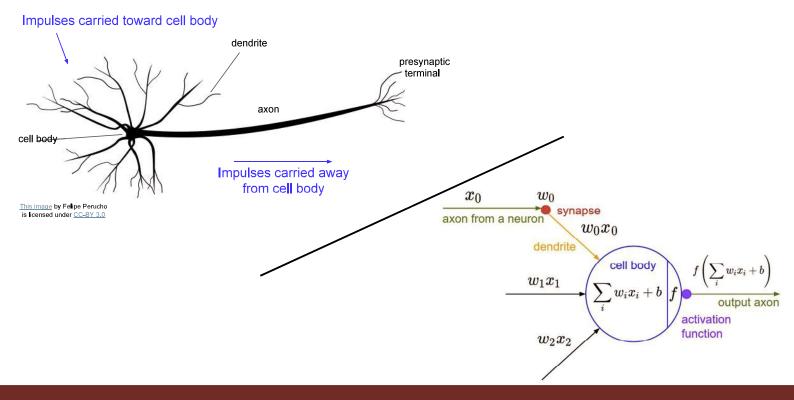
## In HW: Writing a 2-layer net

```
# receive W1,W2,b1,b2 (weights/biases), X (data)
# forward pass:
h1 = #... function of X,W1,b1
scores = #... function of h1,W2,b2
loss = #... (several lines of code to evaluate Softmax loss)
# backward pass:
dscores = #...
dh1,dW2,db2 = #...
dW1,db1 = #...
```



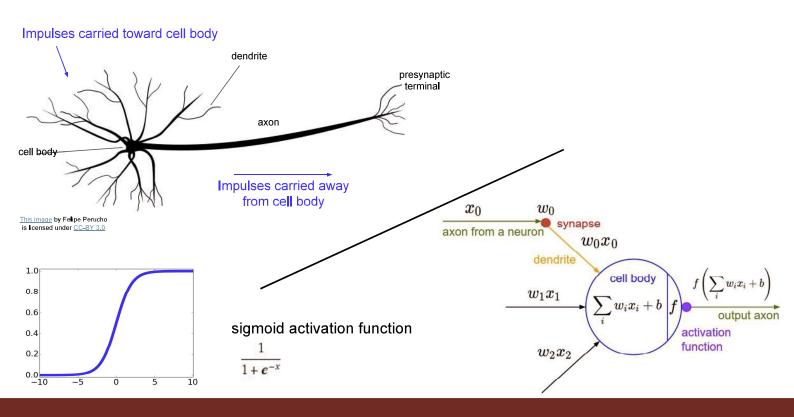
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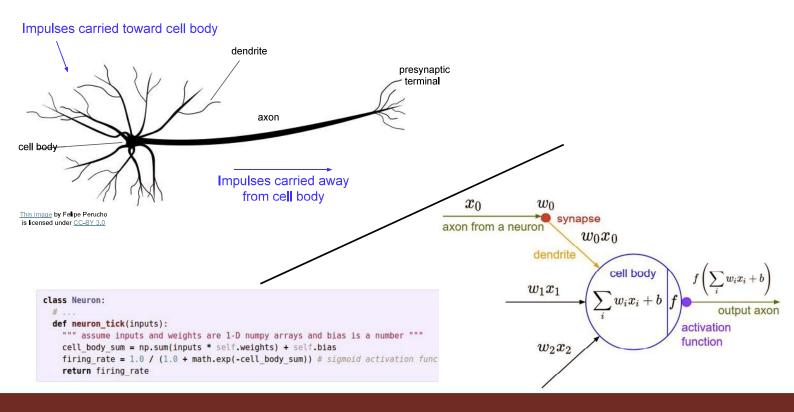
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#### Be very careful with your brain analogies!

#### **Biological Neurons:**

- Many different types
- Dendrites can perform complex non-linear computations
- Synapses are not a single weight but a complex non-linear dynamical system
- Rate code may not be adequate

[Dendritic Computation. London and Hausser]

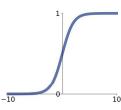
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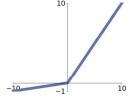
#### **Activation functions**

# Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

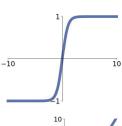


# Leaky ReLU $\max(0.1x, x)$



#### tanh

tanh(x)

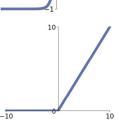


#### **Maxout**

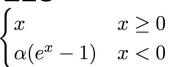
 $\max(w_1^T x + b_1, w_2^T x + b_2)$ 

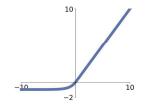
#### **ReLU**

 $\max(0, x)$ 



#### **ELU**

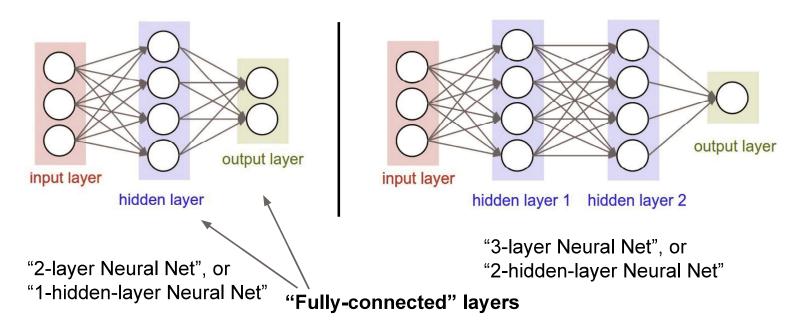




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## Neural networks: Architectures



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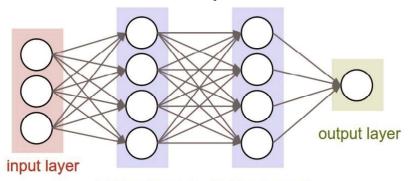
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## Example feed-forward computation of a neural network

```
class Neuron:
    # ...
    def neuron_tick(inputs):
        """ assume inputs and weights are 1-D numpy arrays and bias is a number """
        cell_body_sum = np.sum(inputs * self.weights) + self.bias
        firing_rate = 1.0 / (1.0 + math.exp(-cell_body_sum)) # sigmoid activation function
        return firing_rate
```

We can efficiently evaluate an entire layer of neurons.

### Example feed-forward computation of a neural network



hidden layer 1 hidden layer 2

```
# forward-pass of a 3-layer neural network:

f = lambda x: 1.0/(1.0 + np.exp(-x)) # activation function (use sigmoid)

x = np.random.randn(3, 1) # random input vector of three numbers (3x1)

h1 = f(np.dot(W1, x) + b1) # calculate first hidden layer activations (4x1)

h2 = f(np.dot(W2, h1) + b2) # calculate second hidden layer activations (4x1)

out = np.dot(W3, h2) + b3 # output neuron (1x1)
```

# **Summary**

- We arrange neurons into fully-connected layers
- The abstraction of a **layer** has the nice property that it allows us to use efficient vectorized code (e.g. matrix multiplies)
- Neural networks are not really neural
- Next time: Convolutional Neural Networks