# Simplex Algorithm Implementation

This README document explains the implementation of the simplex algorithm to solve linear programming problems by maximization of the objective function. The program takes a CSV file (testcases) as input and outputs the sequence of vertices visited and the corresponding value of the objective function at that vertex.

#### **Problem Statement:**

Implement the simplex algorithm to maximize the objective function with respect to the constraints mentioned for each assignment. The input and output formats are as follows:

### Input:

A CSV file with (m+1) rows and (n+1) columns:

- The first row (excluding the last element) represents the cost vector (c) of length (n).
- The last column (excluding the top element) represents the constraint vector (b) of length (m).
- Rows 2 to (m + 1) and columns 1 to (n) form the matrix (A) of size (m x n).

# **Output:**

- The sequence of vertices visited during the simplex process.
- The value of the objective function at each vertex.

# **Assignments and Assumptions**

# **Assignment 1**

#### **Assumptions:**

- The polytope is non-degenerate.
- The polytope is bounded.
- The rank of matrix (A) is (n).

#### **Test Cases and Observations:**

- Input: Test file 1 Initial feasible point, Non-degenerate, Bounded
- Results: Test Case 1: SUCCESS

# **Assignment 2**

## **Assumptions:**

- The polytope is non-degenerate.
- The rank of matrix (A) is (n).

#### **Test Cases and Observations:**

- Input:
  - Test file 1 Initial feasible point, Non-degenerate, Bounded
  - Test file 2 Initial feasible point, Non-degenerate, Unbounded
- Results:
  - Test Case 1: SUCCESSTest Case 2: SUCCESS

### **Assignment 3**

#### **Assumptions:**

• The rank of matrix (A) is (n).

#### **Test Cases and Observations:**

#### • Input:

- Test file 1 Initial feasible point, Non-degenerate, Bounded
- Test file 2 Initial feasible point, Non-degenerate, Unbounded
- o Test file 3 Initial feasible point, Degenerate, Bounded
- Test file 4 Initial feasible point, Degenerate, Unbounded

#### Results:

- Test Case 1: SUCCESS
- o Test Case 2: SUCCESS
- Test Case 3: SUCCESS
- Test Case 4: SUCCESS

# **Assignment 4**

#### **Assumptions:**

• The rank of matrix (A) is (n).

#### **Test Cases and Observations:**

#### • Input:

- Test file 5: No initial feasible point, Non-degenerate, Bounded (all positive bounds).
- Test file 6: No initial feasible point, Non-degenerate, Bounded (at least one negative bound).
- Test file 7: No initial feasible point, Non-degenerate, Unbounded (all positive bounds).
- Test file 8: No initial feasible point, Non-degenerate, Unbounded (at least one negative bound).
- Test file 9: No initial feasible point, Degenerate, Bounded (all positive bounds).

#### Results:

• Test Case 5: SUCCESS

• Test Case 6: SUCCESS

• Test Case 7: SUCCESS

• Test Case 8: SUCCESS

• Test Case 9: SUCCESS

# **How to Use the Programs:**

- 1. First generate some test cases for the input in CSV file according to the described format.
- 2. Run the program file for each assignment i (1 to 4) with the test case csv inputs by changing the name in the function.
- 3. The program will display the sequence of vertices visited and the objective function's values at those vertices.