Time series forecasting

This notebook adapts the Tensorflow tutorial on Time series forecasting to data generated from a model for epidemic processes.

Steps

- 1. Imports and setup
- 2. Load and prepare the generated data
- 3. Baseline forecasting
- 4. Univariate GRU based forecasting
- 5. Multivariate GRU based forecasting Single Step
- 6. Multivariate GRU based forecasting Multiple Steps

Imports and setup

```
import tensorflow as tf

import matplotlib as mpl
import matplotlib.pyplot as plt
import numpy as np
import os
import pandas as pd

mpl.rcParams['figure.figsize'] = (8, 6)
mpl.rcParams['axes.grid'] = False
```

Load and prepare the generated data

We load data from the ODE model introduced in the notebook "Probability and Information Theory". For each of the 150 virtuel outbreaks (randomized and with different model parameters), we have time series (with 500 steps) for four the variables "Susceptible", "Infected", "Recovered", and "Deceased".

```
In [ ]: csv_path = "../data/epidemic_process_raw_data.csv"
    df = pd.read_csv(csv_path)
    df.head()
```

Out[]:		1	2	3	4	5	6	7	
	0	100.287149	103.541223	95.879814	96.354848	96.980932	97.855310	98.940537	100.18749
	1	0.993774	1.017558	1.070030	1.116168	1.142078	1.134735	1.182418	1.2723
	2	0.000000	0.017741	0.036585	0.054735	0.074266	0.096065	0.117691	0.13918
	3	0.000000	0.000178	0.000364	0.000562	0.000757	0.000947	0.001160	0.00138
	4	103.489688	100.282780	96.634270	98.532514	99.089272	97.440900	98.416534	101.4049(
	-		L						

 $5 \text{ rows} \times 501 \text{ columns}$

```
In [ ]: dfSusceptible = df[df.index % 4 == 0]
    dfSusceptible.head()
```

Out[]:		1	2	3	4	5	6	7	
	0	100.287149	103.541223	95.879814	96.354848	96.980932	97.855310	98.940537	100.18
	4	103.489688	100.282780	96.634270	98.532514	99.089272	97.440900	98.416534	101.40
	8	101.527421	97.711732	96.168179	95.677962	95.575326	96.109792	96.943831	98.00
	12	101.061107	99.112815	106.651686	101.622904	97.726686	95.692173	97.438263	102.08
	16	101.957189	101.898022	100.881113	99.892000	98.939878	98.048565	98.220024	99.20

5 rows × 501 columns

```
In [ ]: dfInfected = df[df.index % 4 == 1]
    dfInfected.head()
```

Out[]:		1	2	3	4	5	6	7	8	!
	1	0.993774	1.017558	1.070030	1.116168	1.142078	1.134735	1.182418	1.272310	1.35656
	5	1.021677	1.045410	1.120324	1.175914	1.236878	1.306676	1.387931	1.477973	1.54987
	9	1.020043	1.011238	1.031122	1.048642	1.049479	1.022891	1.035862	1.079177	1.11453
	13	1.035248	1.014189	1.133178	1.135622	1.157984	1.213088	1.281406	1.359858	1.42323
	17	1.012666	1.016949	1.053194	1.097599	1.143640	1.192369	1.238880	1.283688	1.32430

5 rows × 501 columns

Out[]:		1	2	3	4	5	6	7	8	9	
	2	0.0	0.017741	0.036585	0.054735	0.074266	0.096065	0.117691	0.139184	0.163615	0.1
	6	0.0	0.017909	0.035748	0.056118	0.076620	0.097338	0.119592	0.143024	0.171253	0.2
	10	0.0	0.016990	0.034644	0.052866	0.071444	0.090609	0.108733	0.126058	0.142408	0.1
	14	0.0	0.017002	0.036315	0.057484	0.078381	0.098831	0.119563	0.140509	0.166486	0.1
	18	0.0	0.017589	0.037434	0.056572	0.076275	0.096907	0.116533	0.135387	0.157592	0.1

5 rows × 501 columns

```
In []: dfDead = df[df.index % 4 == 3]
    dfDead.head()
Out[ ]:
                3
                     4
                          5
                               6
                                   7
                                        8
                                             9
     3 0.0
        0.001389 0.001635
                                              0.0
        0.001719
                                              0.0
        0.001488
                                              0.0
      0.0 0.000181 0.000364 0.000563 0.000774 0.001003 0.001192 0.001351
```

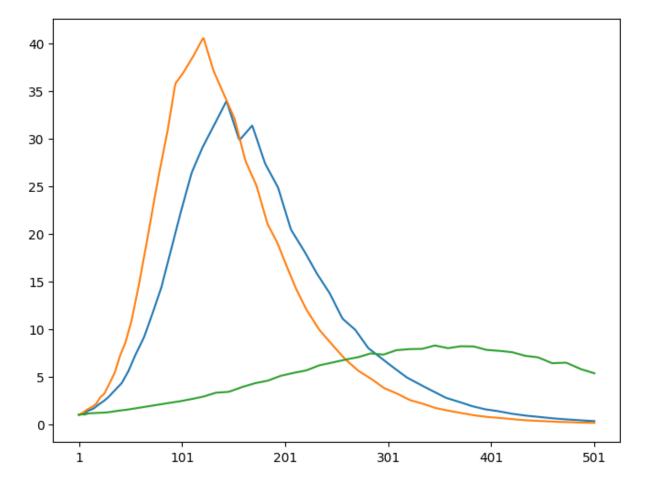
0.0 0.000180 0.000358 0.000550 0.000740 0.000931 0.001138 0.001359 0.001574 0.0

5 rows × 501 columns

Below a plot of three infection time series for the three first outbreaks.

```
In [ ]: dfInfected.loc[1,:].plot()
    dfInfected.loc[5,:].plot()
    dfInfected.loc[9,:].plot()
```

Out[]: <AxesSubplot:>



We define a 90% / 10% of data for training / testing.

Out[]: **135**

We standardize the data.

```
In [ ]: uni_train_mean = dfInfected_arr[:TRAIN_SPLIT].mean()
    uni_train_std = dfInfected_arr[:TRAIN_SPLIT].std()
    uni_data = (dfInfected_arr-uni_train_mean)/uni_train_std
    print ('\n Univariate data shape')
    print(uni_data.shape)
```

Univariate data shape (150, 501)

We split the data into time series of univariate_past_history=20 days length and predict the future of the current day, i.e., univariate_future_target=0, for the "infected" variable.

```
In [ ]: def univariate data(dataset, start series, end series, history size, target size):
            data = []
            labels = []
            start index = history size
            end_index = len(dataset[0]) - target_size
            for c in range(start_series, end_series):
                for i in range(start_index, end_index):
                    indices = range(i-history_size, i)
                    # Reshape data from (history_size,) to (history_size, 1)
                    data.append(np.reshape(dataset[c][indices], (history_size, 1)))
                    labels.append(dataset[c][i+target_size])
            return np.array(data), np.array(labels)
In [ ]: univariate_past_history = 20 #days
        univariate_future_target = 0 #current day
        x_train_uni, y_train_uni = univariate_data(uni_data, 0, TRAIN_SPLIT,
                                                    univariate_past_history,
                                                    univariate_future_target)
        x_val_uni, y_val_uni = univariate_data(uni_data, TRAIN_SPLIT, len(uni_data),
                                                univariate_past_history,
                                                univariate_future_target)
In [ ]: | print ('Single window of past history')
        print (x_train_uni[0])
        print ('\n Target number to predict')
        print (y_train_uni[0])
        print ('\n Number of traing data points')
        print (y_train_uni.shape[0])
        print ('\n Number of test data points')
```

print (x_val_uni.shape[0])

Single window of past history

In []: def create_time_steps(length):

return list(range(-length, 0))

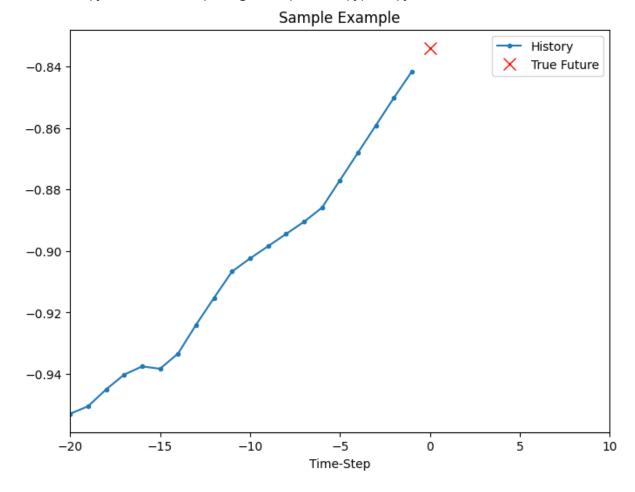
[[-0.95291296] [-0.95044298] [-0.94499366] [-0.9402021]

```
[-0.93751136]
        [-0.93827393]
        [-0.93332191]
        [-0.92398652]
        [-0.91523643]
        [-0.90667772]
        [-0.90243571]
        [-0.89846308]
        [-0.89449045]
        [-0.89051782]
        [-0.88593997]
        [-0.87701137]
        [-0.86808277]
        [-0.85915417]
        [-0.85022557]
        [-0.84167481]]
       Target number to predict
       -0.8339932964893617
       Number of traing data points
       64935
       Number of test data points
        Create test data where the infection reached the peak
In [ ]: peak_idx = np.argmax(uni_data, axis=1)
        peak_uni = []
        for i in range(len(uni_data)):
            idx = peak_idx[i]
            start = max(idx - univariate_past_history, 0)
            end = min(idx + univariate_past_history, uni_data.shape[1])
            temp_peak_uni = []
            for j in range(start, end+1):
                 temp_peak_uni.append(uni_data[i,j])
            peak_uni.append(np.array(temp_peak_uni))
        peak_uni = np.array(peak_uni)
In [ ]: x_peak_uni, y_peak_uni = univariate_data(peak_uni, 0, len(uni_data),
                                                 univariate_past_history,
                                                 univariate_future_target)
```

```
In [ ]: def show_plot(plot_data, delta, title):
            labels = ['History', 'True Future', 'Model Prediction']
            marker = ['.-', 'rx', 'go']
            time_steps = create_time_steps(plot_data[0].shape[0])
            if delta:
                future = delta
            else:
                future = 0
            plt.title(title)
            for i, x in enumerate(plot_data):
                if i:
                    plt.plot(future, plot_data[i], marker[i], markersize=10,label=labels[i]
                else:
                    plt.plot(time_steps, plot_data[i].flatten(), marker[i], label=labels[i]
            plt.legend()
            plt.xlim([time_steps[0], (future+5)*2])
            plt.xlabel('Time-Step')
            return plt
```

```
In [ ]: show_plot([x_train_uni[0], y_train_uni[0]], 0, 'Sample Example')
```

Out[]: <module 'matplotlib.pyplot' from '/media/home/ngundermann/workspace/DML_notebooks/venv/lib/python3.10/site-packages/matplotlib/pyplot.py'>



Baseline forecasting

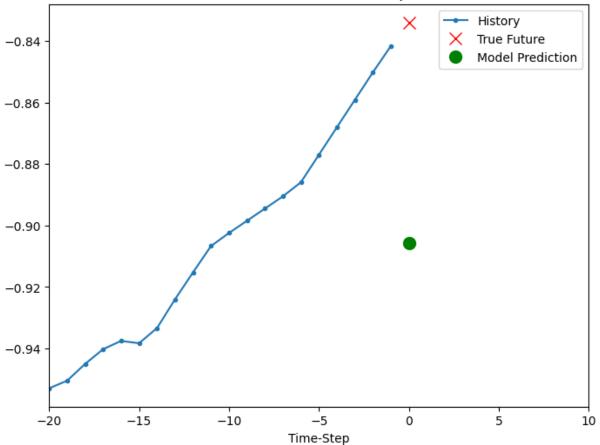
Predicts the mean of the history.

```
In [ ]: def baseline(history):
    return np.mean(history)

In [ ]: show_plot([x_train_uni[0], y_train_uni[0], baseline(x_train_uni[0])], 0, 'Baseline
```

Out[]: <module 'matplotlib.pyplot' from '/media/home/ngundermann/workspace/DML_notebooks/venv/lib/python3.10/site-packages/matplotlib/pyplot.py'>

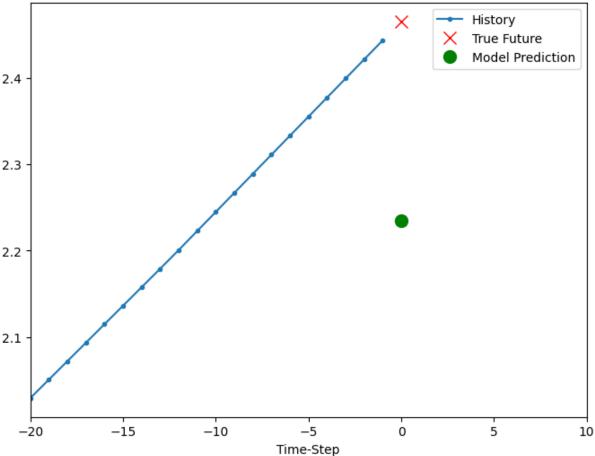
Baseline Prediction Example



In []: show_plot([x_peak_uni[0], y_peak_uni[0], baseline(x_peak_uni[0])], 0, 'Baseline Pre

Out[]: <module 'matplotlib.pyplot' from '/media/home/ngundermann/workspace/DML_notebooks/v env/lib/python3.10/site-packages/matplotlib/pyplot.py'>





Univariate GRU based forecasting

```
In [ ]: print (x_train_uni.shape)
    print (y_train_uni.shape)
    x_train_uni.dtype

    (64935, 20, 1)
    (64935,)
Out[ ]: dtype('float64')
```

Batching and resampling; the dataset is repeated indefinitely. Check the tutorial for the details.

```
In [ ]:
        BATCH SIZE = 256
        BUFFER SIZE = 10000
        train univariate = tf.data.Dataset.from tensor slices((x train uni, y train uni))
        train_univariate = train_univariate.cache().shuffle(BUFFER_SIZE).batch(BATCH_SIZE).
        val_univariate = tf.data.Dataset.from_tensor_slices((x_val_uni, y_val_uni))
        val univariate = val univariate.batch(BATCH SIZE).repeat()
        peak_val_univariate = tf.data.Dataset.from_tensor_slices((x_peak_uni, y_peak_uni))
        peak_val_univariate = peak_val_univariate.batch(1).repeat()
        train_univariate
```

Out[]: <_RepeatDataset element_spec=(TensorSpec(shape=(None, 20, 1), dtype=tf.float64, nam e=None), TensorSpec(shape=(None,), dtype=tf.float64, name=None))>

We define the first GRU model with 8 units.

```
simple_lstm_model = tf.keras.models.Sequential([
    tf.keras.layers.GRU(8, input_shape=x_train_uni.shape[-2:]),
    tf.keras.layers.Dense(1)
])
simple_lstm_model.compile(optimizer='adam', loss='mae')
simple_lstm_model.summary()
x_train_uni.shape[-2:]
```

/media/home/ngundermann/workspace/DML_notebooks/venv/lib/python3.10/site-packages/ke ras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` ob ject as the first layer in the model instead.

```
super().__init__(**kwargs)
Model: "sequential 9"
```

Layer (type)	Output Shape	Param #
gru_12 (GRU)	(None, 8)	264
dense_9 (Dense)	(None, 1)	9

Total params: 273 (1.07 KB) Trainable params: 273 (1.07 KB) Non-trainable params: 0 (0.00 B)

```
Out[]: (20, 1)
```

The GRU layer comes with less parameters than the LSTM layer (320) we have seen in the original notebook. This is becaust the GRU architecture is much simpler than LSTMs'.

```
In [ ]: | for x, y in val_univariate.take(1):
            print(simple_lstm_model.predict(x).shape)
            print(y.shape)
```

```
8/8 — 0s 1ms/step (256, 1) (256,)
```

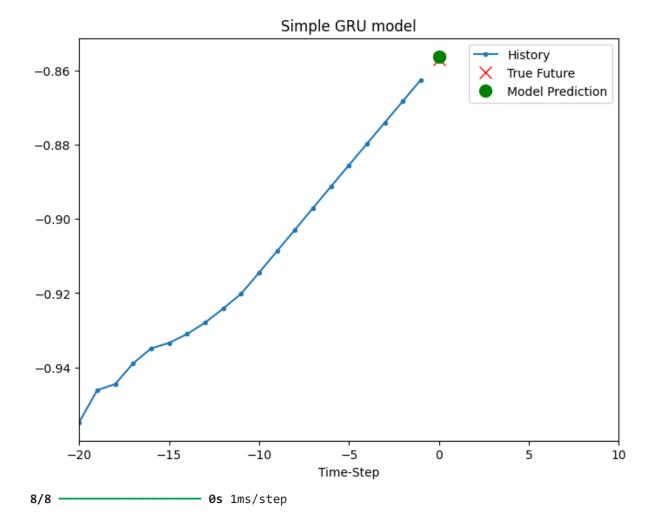
2024-05-30 09:00:21.924564: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

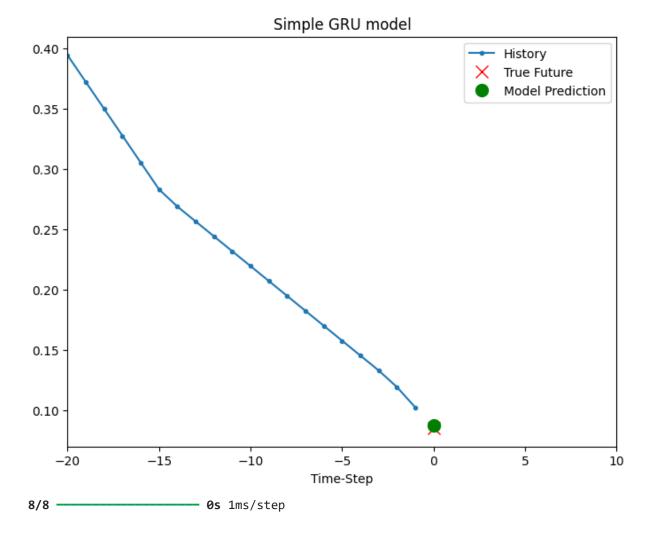
When passing an indefinitely repeated training data set, we need to specify the numbre of steps per training interval (epoch).

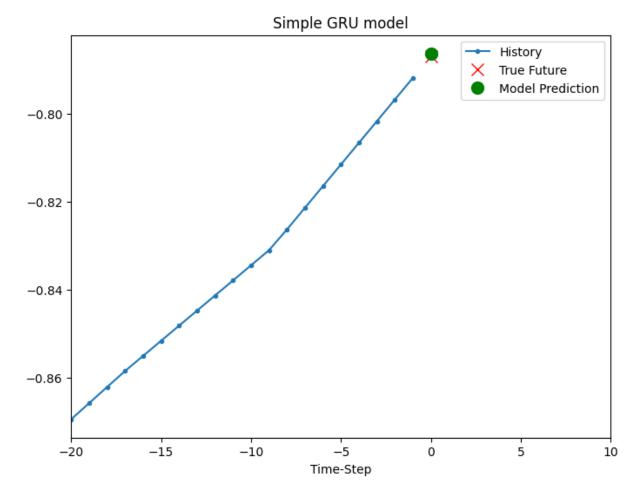
```
Epoch 1/10
2000/2000
                              - 8s 3ms/step - loss: 0.0792 - val_loss: 0.0031
Epoch 2/10
2000/2000
                              7s 3ms/step - loss: 0.0029 - val_loss: 0.0026
Epoch 3/10
                              • 7s 3ms/step - loss: 0.0024 - val_loss: 0.0016
2000/2000
Epoch 4/10
2000/2000
                              - 7s 3ms/step - loss: 0.0022 - val_loss: 0.0014
Epoch 5/10
                               7s 3ms/step - loss: 0.0020 - val_loss: 0.0015
2000/2000
Epoch 6/10
                              7s 3ms/step - loss: 0.0019 - val_loss: 0.0013
2000/2000
Epoch 7/10
2000/2000
                              7s 3ms/step - loss: 0.0017 - val_loss: 0.0012
Epoch 8/10
                              - 7s 3ms/step - loss: 0.0017 - val_loss: 0.0018
2000/2000
Epoch 9/10
                              6s 3ms/step - loss: 0.0017 - val_loss: 8.7684e-04
2000/2000
Epoch 10/10
2000/2000
                              - 6s 3ms/step - loss: 0.0017 - val_loss: 0.0012
```

The training loss went down very fast and convereged after a few epochs. However, the validation loss stated very low at the beginning, but did decrease quite fast. The training of one epoch finished faster, which could be caused by the fewer parameters of the model but also by the different machine on that the training was ran.

Out[]: <keras.src.callbacks.history.History at 0x7f04384e0e50>



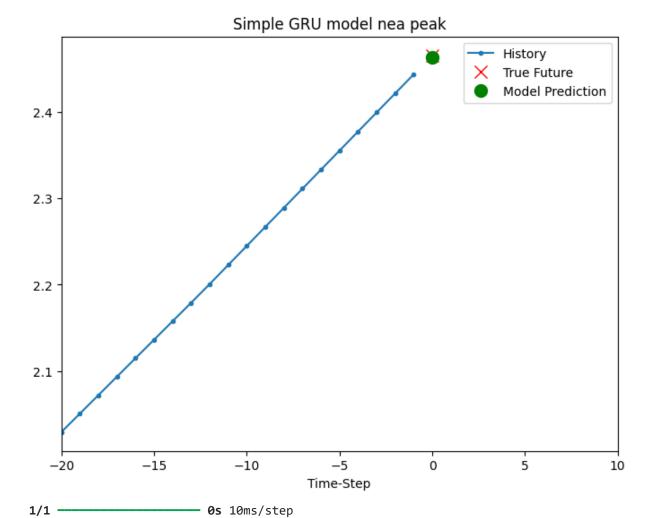


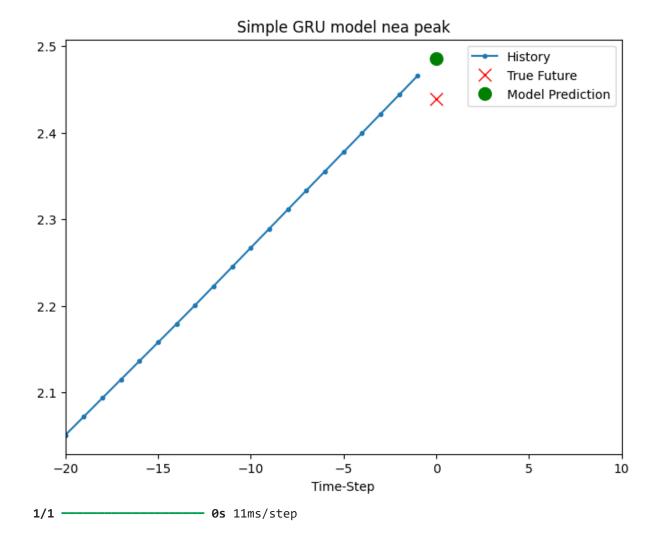


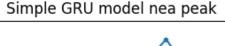
2024-05-30 09:01:29.437318: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

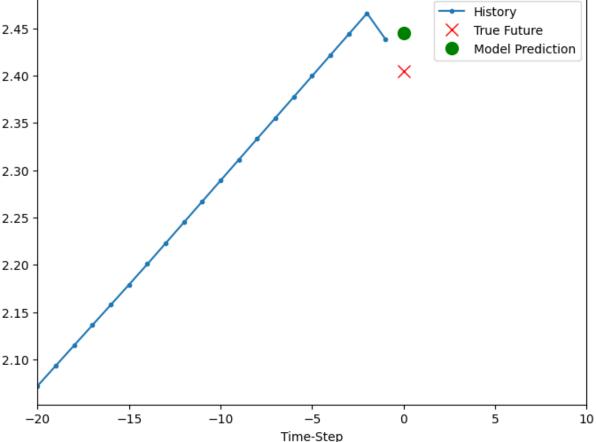
The predictions look quite good, since the validataion loss was quite low the whole time. The prediction are not exactly at the true value, but very close to it.

Diagrams with the peek of infection









2024-05-30 09:01:29.878153: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

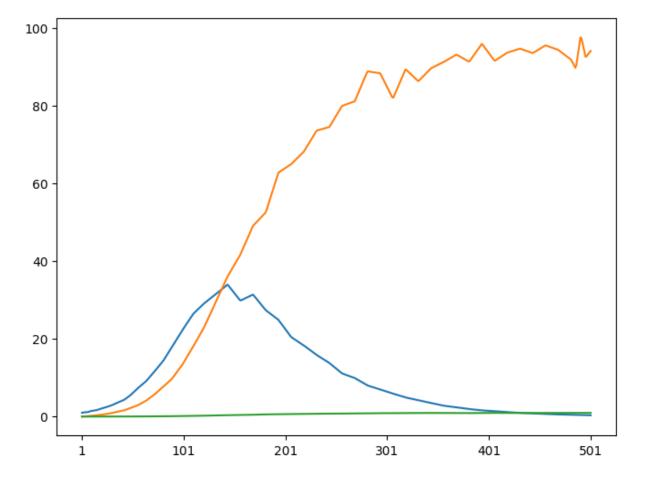
Even the prediction near infection peak were not that good. It seems that the model has problems with changing slopes of the ground truths trajectory, i.e. when the infection starts to decline.

Multivariate GRU based forecasting - Single Step

We use three variables "Infected", "Recovered", and "Deceased", to forcast "Infected" at one single day in the future.

Here a plot of the time series of the three variables for one outbreak.

```
In []: dfInfected.loc[1,:].plot()
    dfRecovered.loc[2,:].plot()
    dfDead.loc[3,:].plot()
    dfInfected = dfInfected.values
    dfRecovered_arr = dfRecovered.values
    dfDead_arr = dfDead.values
```



We prepare the dataset.

```
In [ ]:
        #as before
        dfInfected_train_mean = dfInfected_arr[:TRAIN_SPLIT].mean()
        dfInfected train std = dfInfected arr[:TRAIN SPLIT].std()
        dfInfected_data = (dfInfected_arr-dfInfected_train_mean)/dfInfected_train_std
        #for Recovered
        dfRecovered_train_mean = dfRecovered_arr[:TRAIN_SPLIT].mean()
        dfRecovered_train_std = dfRecovered_arr[:TRAIN_SPLIT].std()
        dfRecovered_data = (dfRecovered_arr-dfRecovered_train_mean)/dfRecovered_train_std
        #for Dead
        dfDead_train_mean = dfDead_arr[:TRAIN_SPLIT].mean()
        dfDead_train_std = dfDead_arr[:TRAIN_SPLIT].std()
        dfDead_data = (dfDead_arr-dfDead_train_mean)/dfDead_train_std
In [ ]:
        dataset = np.array([dfInfected_data, dfRecovered_data, dfDead_data])
        dataset.shape
        print ('\n Multivariate data shape')
        print(dataset.shape)
       Multivariate data shape
       (3, 150, 501)
```

```
In [ ]: def multivariate_data(dataset, target, start_series, end_series, history_size,
                              target_size, step, single_step=False):
            data = []
            labels = []
            start_index = history_size
            end_index = len(dataset[0][0]) - target_size
            for c in range(start_series, end_series):
                for i in range(start_index, end_index):
                    indices = range(i-history_size, i, step)
                    one = dataset[0][c][indices]
                    two = dataset[1][c][indices]
                    three = dataset[2][c][indices]
                    data.append(np.transpose(np.array([one, two, three])))
                    if single step:
                        labels.append(target[c][i+target_size])
                    else:
                        labels.append(np.transpose(target[c][i:i+target_size]))
            return np.array(data), np.array(labels)
```

We get training and valdation data for time series with a past_history = 20 days for every other day (STEP = 2) and want to predict the "Infected" five days ahead (future_target = 5).

```
In [ ]: print ('Single window of past history : {}'.format(x_train_single[0].shape))
    print(dataset.shape)
    Single window of past history : (10, 3)
```

As before, creating a dataset around the infection peak.

(3, 150, 501)

```
In [ ]: def multivariate data near peak infection(dataset, past history, future target):
            peak_idx = np.argmax(dataset[0], axis=1)
            peak_infected = []
            peak infected recovered = []
            peak_infected_dead = []
            for i in range(len(dataset[1])):
                idx = peak_idx[i]
                start = max(idx - 1 - past_history - future_target // 2 , 0)
                end = min(idx + future_target // 2 + future_target % 2, dataset.shape[2])
                temp_peak_infected = []
                temp_peak_infected_recovered = []
                temp_peak_infected_dead = []
                for j in range(start, end):
                    temp_peak_infected.append(dataset[0,i,j])
                    temp_peak_infected_recovered.append(dataset[1,i,j])
                    temp_peak_infected_dead.append(dataset[2,i,j])
                peak infected.append(np.array(temp peak infected))
                peak_infected_recovered.append(np.array(temp_peak_infected_recovered))
                peak_infected_dead.append(np.array(temp_peak_infected_dead))
            return np.array([peak infected, peak infected recovered, peak infected dead])
        peak_data = multivariate_data_near_peak_infection(dataset, past_history, future_tar
        peak_data.shape
Out[]: (3, 150, 26)
In [ ]: |x_peak_single, y_peak_single = multivariate_data(peak_data, peak_data[0], 0, peak_d
                                                        past history, future target, STEP,
                                                        single step=True)
In [ ]: x_peak_single.shape
Out[]: (150, 10, 3)
        As before, batching and resampling; the dataset is repeated indefinitely.
In [ ]: | train_data_single = tf.data.Dataset.from_tensor_slices((x_train_single, y_train_sin
        train_data_single = train_data_single.cache().shuffle(BUFFER_SIZE).batch(BATCH_SIZE
        val_data_single = tf.data.Dataset.from_tensor_slices((x_val_single, y_val_single))
        val_data_single = val_data_single.batch(BATCH_SIZE).repeat()
        peak_data_single = tf.data.Dataset.from_tensor_slices((x_peak_single, y_peak_single)
        peak_data_single = peak_data_single.batch(1).repeat()
In [ ]: single_step_model = tf.keras.models.Sequential()
        single_step_model.add(tf.keras.layers.GRU(32, input_shape=x_train_single.shape[-2:]
        single_step_model.add(tf.keras.layers.Dense(1))
        single_step_model.compile(optimizer=tf.keras.optimizers.RMSprop(), loss='mae')
        single_step_model.summary()
        x_train_single.shape[-2:]
```

steps_per_epoch=EVALUATION_INTERVAL,
validation_data=val_data_single,

validation_steps=50)

/media/home/ngundermann/workspace/DML_notebooks/venv/lib/python3.10/site-packages/ke ras/src/layers/rnn/rnn.py:204: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential models, prefer using an `Input(shape)` ob ject as the first layer in the model instead.

```
super().__init__(**kwargs)
```

Model: "sequential_10"

Layer (type)	Output Shape	Param #
gru_13 (GRU)	(None, 32)	3,552
dense_10 (Dense)	(None, 1)	33

```
Total params: 3,585 (14.00 KB)

Trainable params: 3,585 (14.00 KB)

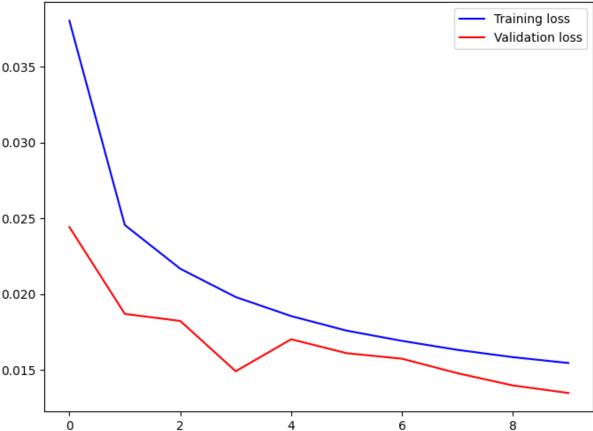
Non-trainable params: 0 (0.00 B)
```

```
Out[]: (10, 3)
```

Again we got a network with fewer parameters, since the GRU architecture comes with less parameters than the LSTM architecture.

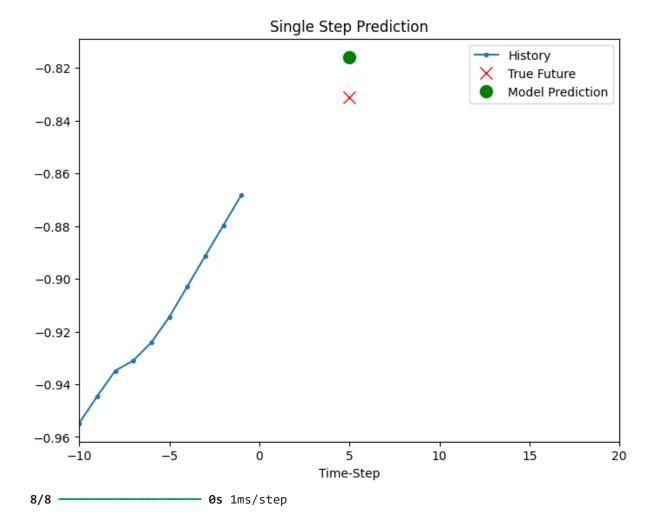
```
Epoch 1/10
       2000/2000
                                     • 8s 3ms/step - loss: 0.0670 - val_loss: 0.0244
       Epoch 2/10
       2000/2000
                                      7s 3ms/step - loss: 0.0256 - val_loss: 0.0187
       Epoch 3/10
                                     • 7s 3ms/step - loss: 0.0222 - val_loss: 0.0182
       2000/2000
       Epoch 4/10
       2000/2000
                                     - 7s 3ms/step - loss: 0.0202 - val_loss: 0.0149
       Epoch 5/10
                                     - 7s 3ms/step - loss: 0.0188 - val_loss: 0.0170
       2000/2000
       Epoch 6/10
       2000/2000
                                     • 7s 3ms/step - loss: 0.0177 - val_loss: 0.0161
       Epoch 7/10
       2000/2000
                                      7s 3ms/step - loss: 0.0170 - val_loss: 0.0157
       Epoch 8/10
                                     • 7s 3ms/step - loss: 0.0164 - val_loss: 0.0148
       2000/2000
       Epoch 9/10
       2000/2000
                                     - 7s 3ms/step - loss: 0.0159 - val_loss: 0.0140
      Epoch 10/10
       2000/2000
                                     - 7s 3ms/step - loss: 0.0155 - val_loss: 0.0135
In [ ]: def plot_train_history(history, title):
            loss = history.history['loss']
            val_loss = history.history['val_loss']
            epochs = range(len(loss))
            plt.figure()
            plt.plot(epochs, loss, 'b', label='Training loss')
            plt.plot(epochs, val_loss, 'r', label='Validation loss')
            plt.title(title)
            plt.legend()
            plt.show()
In [ ]: | plot_train_history(single_step_history,'Single Step Training and validation loss')
```

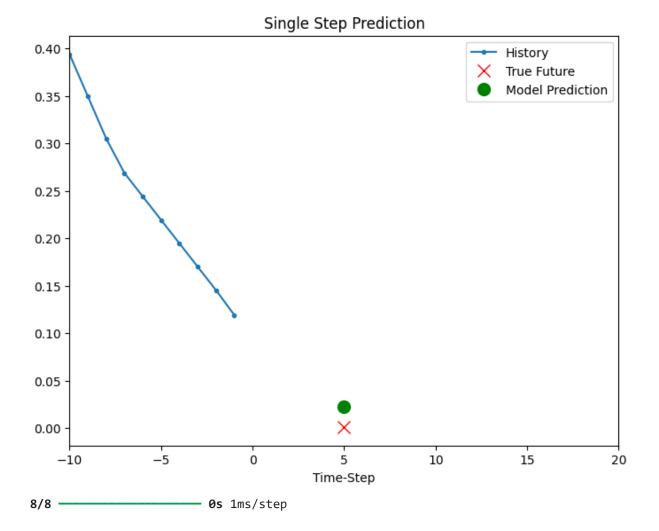
Single Step Training and validation loss

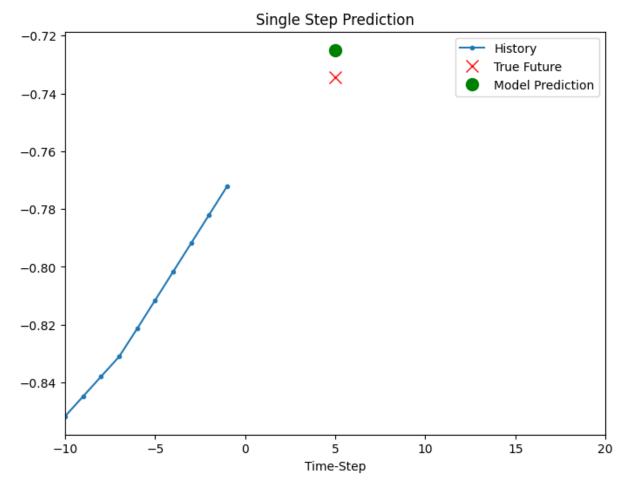


Here, we see once again a big decrease in training loss at the very beginning. However, here, the validation loss tend to shrink next to the training loss, which could indicate that the resulting network will not suffer from overfitting and is, thus, more general compared to the previous one. Moreover, I think the training needs some more epochs in order to let the loss converge at a certain value. This was probably not reached after 10 epochs.

According to time, once again it was a little bit fast than the training of the model from the original notebook, which could be due to the architecture coming with fewer parameters but also to the different machine on that the training was ran.



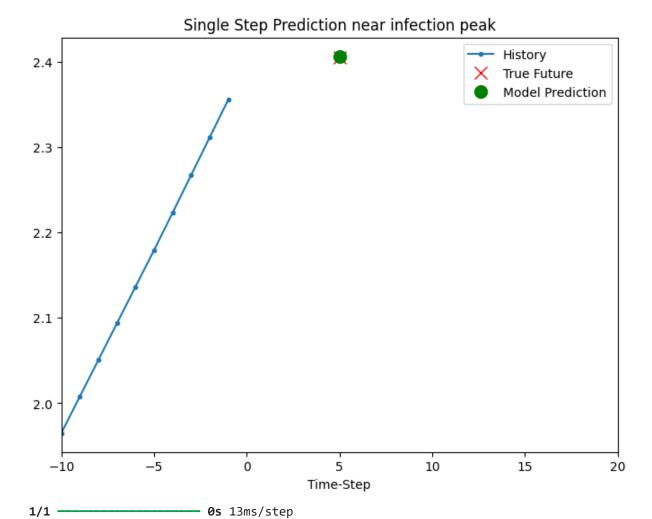




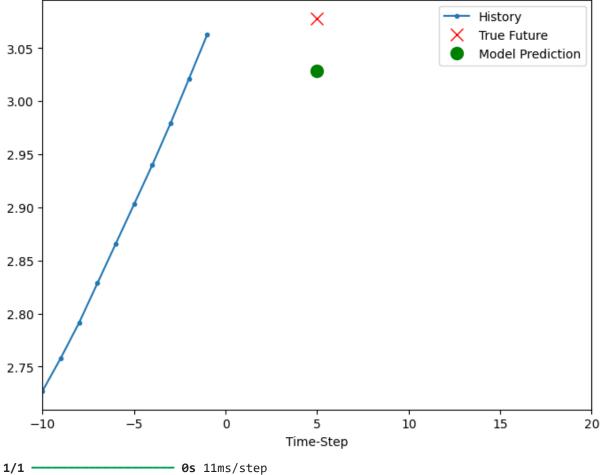
2024-05-30 09:02:40.198774: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT OF RANGE: End of sequence

Looking at the predictions they a a bit worse compared to the previous model. Here, we have to keep in mind, that both models performed different predictions. Here, we wanted to predict the 5 day future, while with the first model we wanted to predict the 1 day future. So maybe the error, we have seen in the previous model is likely to add up when the number of days we want to forcast into the future increases. Anyway, that the prediction is worse than in the preivous model, could have been noticed when comparing the validation loss of the models.

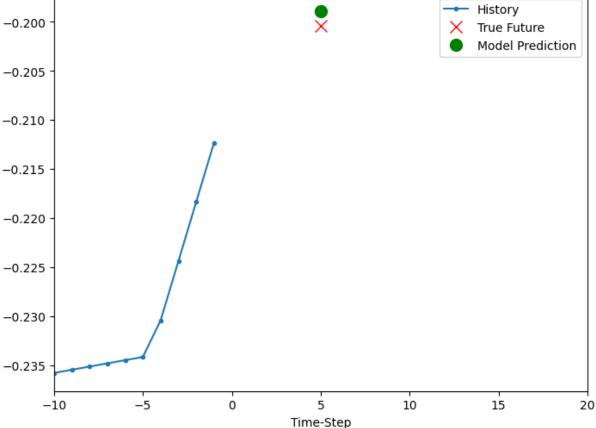
Now, let's plot some predictions near the infection peak.







Single Step Prediction near infection peak



2024-05-30 09:02:40.919216: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

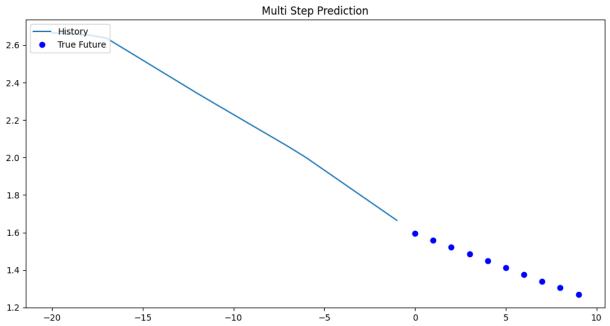
Here, we should take into account that the prediction made is for 3 days after the peak infection. So it is likely that the ground truth is declining in the time stamp to be predicted. Therefore, this model seems to encounter the same problem with making predictions after the direction of the trend has changed, since the second predictions is a way off compared to the ture value. Maybe example 1 and 3 seems to be better, because there is some kind of platoe in infection.

Multivariate GRU - Multiple Steps

Still, we use a series of observed values of the three variables "Infected", "Recovered", and "Deceased" (past_history = 40, STEP =2), but now to forcast the "Infected" values for a series day in the future (future_target = 10).

```
In [ ]: | print ('Single window of past history : {}'.format(x_train_multi[0].shape))
        print ('\nTarget window to predict : {}'.format(y_train_multi[0].shape))
        print ('\nNumber of traing data points: {}'.format(x_train_multi.shape[0]))
        print ('\nNumber of test data points: {}'.format(x val multi.shape[0]))
       Single window of past history : (20, 3)
       Target window to predict : (10,)
       Number of traing data points: 60885
       Number of test data points: 6765
        As before, retrieve data points near infection peak.
In [ ]: |peak_data = multivariate_data_near_peak_infection(dataset, past_history, future_tar
        peak_data.shape
Out[]: (3, 150, 51)
In [ ]: |x_peak_multi, y_peak_multi = multivariate_data(peak_data, peak_data[0], 0, peak_dat
                                                         past_history, future_target, STEP)
        As before, batching and resampling; the dataset is repeated indefinitely.
        train_data_multi = tf.data.Dataset.from_tensor_slices((x_train_multi, y_train_multi)
        train_data_multi = train_data_multi.cache().shuffle(BUFFER_SIZE).batch(BATCH_SIZE).
        val_data_multi = tf.data.Dataset.from_tensor_slices((x_val_multi, y_val_multi))
        val_data_multi = val_data_multi.batch(BATCH_SIZE).repeat()
        peak_data_multi = tf.data.Dataset.from_tensor_slices((x_peak_multi, y_peak_multi))
        peak data multi = peak data multi.batch(1).repeat()
In [ ]: | def multi_step_plot(history, true_future, prediction, title='Multi Step Prediction'
            plt.figure(figsize=(12, 6))
            num_in = create_time_steps(len(history))
            num_out = len(true_future)
            plt.plot(num_in, np.array(history[:, 0]), label='History')
            plt.plot(np.arange(num_out), np.array(true_future), 'bo', label='True Future')
            if prediction.any():
                 plt.plot(np.arange(num_out), np.array(prediction), 'ro', label='<mark>Predicted F</mark>
            plt.legend(loc='upper left')
            plt.title(title)
            plt.show()
In [ ]: | for x, y in train_data_multi.take(1):
            multi_step_plot(x[0], y[0], np.array([0]))
```

2024-05-30 09:02:41.757811: W tensorflow/core/kernels/data/cache_dataset_ops.cc:858] The calling iterator did not fully read the dataset being cached. In order to avoid unexpected truncation of the dataset, the partially cached contents of the dataset will be discarded. This can happen if you have an input pipeline similar to `datase t.cache().take(k).repeat()`. You should use `dataset.take(k).cache().repeat()` inste ad.



2024-05-30 09:02:41.847356: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

Now we bild a model with two GRU layers.

Model: "sequential_11"

Layer (type)	Output Shape	Param #
gru_14 (GRU)	(None, 20, 32)	3,552
gru_15 (GRU)	(None, 16)	2,400
dense_11 (Dense)	(None, 10)	170

Total params: 6,122 (23.91 KB)

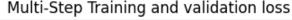
Trainable params: 6,122 (23.91 KB)

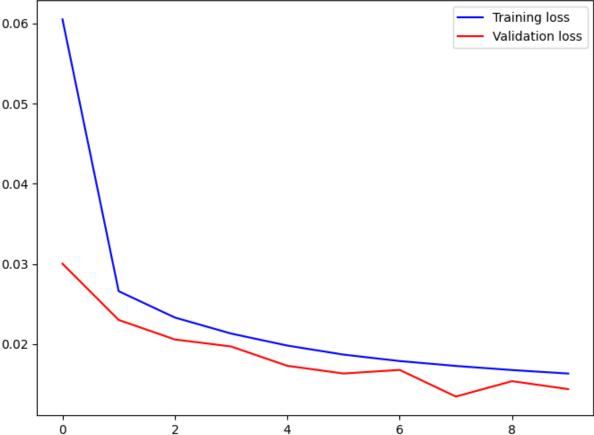
Non-trainable params: 0 (0.00 B)

```
Out[]: (20, 3)
```

As before, we observe that the number of parameter is smaller compared to the model with the LSTM layers, due to the different architectures.

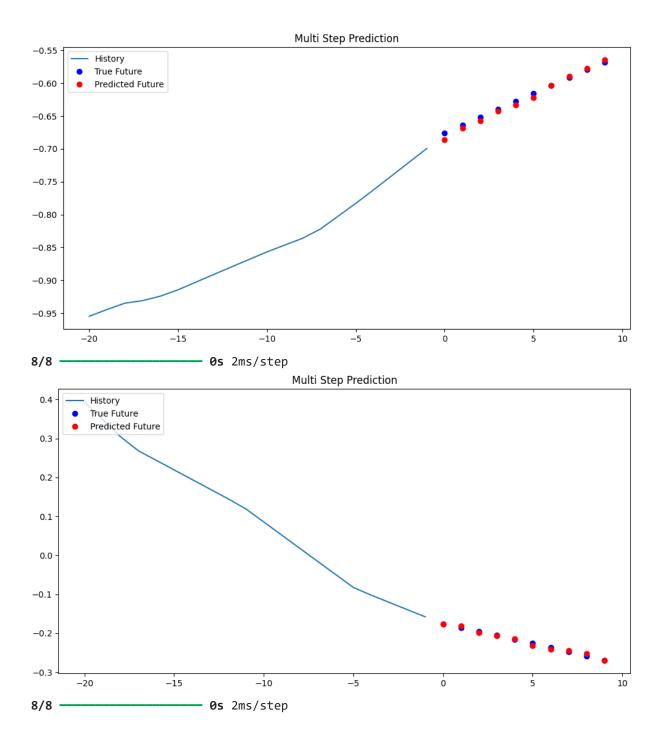
```
In [ ]: for x, y in val data multi.take(1):
            print (multi_step_model.predict(x).shape)
       8/8 -
                              - 0s 2ms/step
       (256, 10)
       2024-05-30 09:02:42.115515: W tensorflow/core/framework/local_rendezvous.cc:404] Loc
       al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence
        The training time is longer for this more complex model.
In [ ]: |multi_step_history = multi_step_model.fit(train_data_multi, epochs=EPOCHS,
                                                   steps_per_epoch=EVALUATION_INTERVAL,
                                                   validation data=val data multi,
                                                   validation_steps=50)
       Epoch 1/10
       2000/2000
                                     - 22s 10ms/step - loss: 0.1428 - val_loss: 0.0300
       Epoch 2/10
                                      20s 10ms/step - loss: 0.0277 - val_loss: 0.0230
       2000/2000
       Epoch 3/10
       2000/2000
                                      20s 10ms/step - loss: 0.0239 - val_loss: 0.0206
       Epoch 4/10
                                      21s 10ms/step - loss: 0.0217 - val_loss: 0.0197
       2000/2000
       Epoch 5/10
                                      20s 10ms/step - loss: 0.0202 - val_loss: 0.0173
       2000/2000
       Epoch 6/10
                                      20s 10ms/step - loss: 0.0190 - val_loss: 0.0163
       2000/2000
       Epoch 7/10
                                      20s 10ms/step - loss: 0.0181 - val_loss: 0.0168
       2000/2000
       Epoch 8/10
       2000/2000
                                      21s 10ms/step - loss: 0.0174 - val_loss: 0.0135
       Epoch 9/10
                                      21s 10ms/step - loss: 0.0169 - val_loss: 0.0154
       2000/2000
       Epoch 10/10
       2000/2000
                                     - 20s 10ms/step - loss: 0.0164 - val_loss: 0.0144
In [ ]: |plot_train_history(multi_step_history, 'Multi-Step Training and validation loss')
```

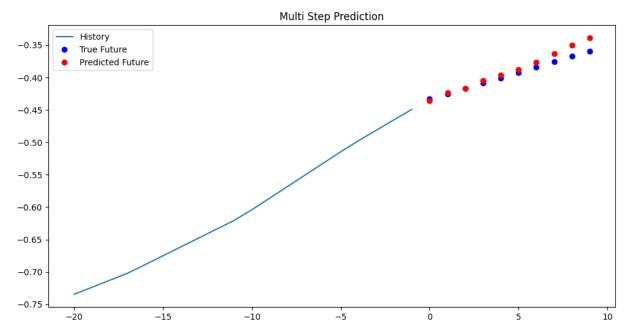




Here, we see once again a big decrease in training loss at the very beginning. The validation loss tend to shrink next to the training loss, which could indicate that the resulting network will not suffer from overfitting. Moreover, it is possible that the training needs some more epochs in order to let the loss converge at a certain value. However, the situation here looks quite better (regarding to that the model already reached to optimum) compared to the previous model.

According to time, the training was slower compared to the other models. This is due to the more complex architecture which come with more parameters and, thus, a higher computational effort. Anyway, once again it was a little bit fast than the training of the model from the original notebook, which could be due to the architecture coming with fewer parameters but also to the different machine on that the training was ran.

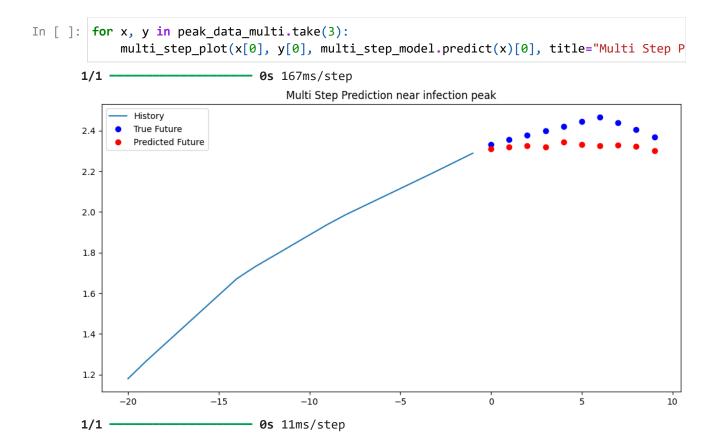


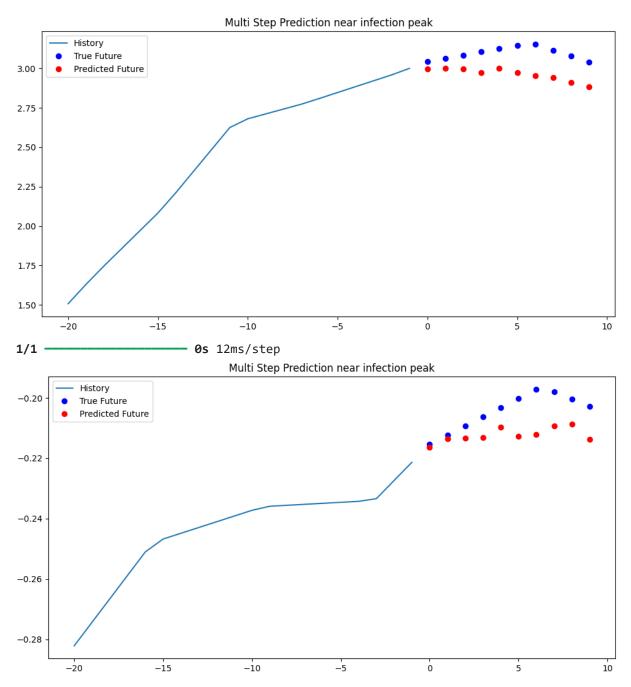


2024-05-30 09:06:08.637510: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

Looking at the predictions they are quite good. In some cases, one sees that the difference between true value and prediction is larger when forcasting is made for a more distant future (third example).

Now, let's look at the prediction near infection peak.





2024-05-30 09:06:09.171313: W tensorflow/core/framework/local_rendezvous.cc:404] Loc al rendezvous is aborting with status: OUT_OF_RANGE: End of sequence

Here, we see that the model is likely to miss the peak and predicts a mor flat trajectory. So once again, it seems to have trouble with the change in the direction of the trajectory, i.e. from increasing infections to decreasing infections. This could be due to the training data. As we have seen in the plotted examples, there are some timelines that are likely to haven't reached the peak yet, and, therefore, were increasing all the time. So maby, one could try to focus the training on timelines showing a global within the, e.g., first 300 days, in order to ensure a complete infection cycle - if those data exists.