Design of Induction Motors

Introduction:

Induction motors are the ac motors which are employed as the prime movers in most of the industries. Such motors are widely used in industrial applications from small workshops to large industries. These motors are employed in applications such as centrifugal pumps, conveyers, compressors crushers, and drilling machines etc.

Constructional Details:

Similar to DC machines an induction motor consists of a stationary member called stator and a rotating member called rotor. However the induction motor differs from a dc machine in the following aspects.

- 1. Laminated stator
- 2. Absence of commutator
- 3. Uniform and small air gap
- 4. Practically almost constant speed

The AC induction motor comprises two electromagnetic parts:

- Stationary part called the stator
- Rotating part called the rotor

The stator and the rotor are each made up of

- An electric circuit, usually made of insulated copper or aluminum winding, to carry current
- A magnetic circuit, usually made from laminated silicon steel, to carry magnetic flux

The stator

The stator is the outer stationary part of the motor, which consists of

- The outer cylindrical frame of the motor or yoke, which is made either of welded sheet steel, cast iron or cast aluminum alloy.
- The magnetic path, which comprises a set of slotted steel laminations called stator core pressed into the cylindrical space inside the outer frame. The magnetic path is laminated to reduce eddy currents, reducing losses and heating.
- A set of insulated electrical windings, which are placed inside the slots of the laminated stator. The cross-sectional area of these windings must be large enough for the power rating of the motor. For a 3-phase motor, 3 sets of windings are required, one for each

phase connected in either star or delta. Fig 1 shows the cross sectional view of an induction motor. Details of construction of stator are shown in Figs 4-6.

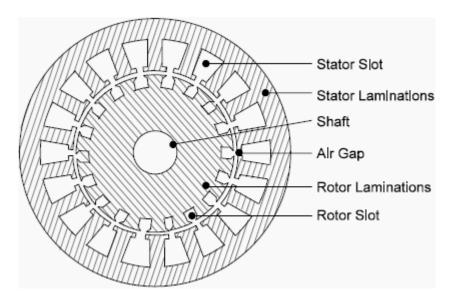


Fig 1: Stator and rotor laminations

The rotor

Rotor is the rotating part of the induction motor. The rotor also consists of a set of slotted silicon steel laminations pressed together to form of a cylindrical magnetic circuit and the electrical circuit. The electrical circuit of the rotor is of the following nature

Squirrel cage rotor consists of a set of copper or aluminum bars installed into the slots, which are connected to an end-ring at each end of the rotor. The construction of this type of rotor along with windings resembles a 'squirrel cage'. Aluminum rotor bars are usually die-cast into the rotor slots, which results in a very rugged construction. Even though the aluminum rotor bars are in direct contact with the steel laminations, practically all the rotor current flows through the aluminum bars and not in the lamination

Wound rotor consists of three sets of insulated windings with connections brought out to three slip rings mounted on one end of the shaft. The external connections to the rotor are made through brushes onto the slip rings as shown in fig 7. Due to the presence of slip rings such type of motors are called slip ring motors. Sectional view of the full induction motor is shown in Fig. 8

Some more parts, which are required to complete the constructional details of an induction motor, are:

- Two end-flanges to support the two bearings, one at the driving-end and the other at the non driving-end, where the driving end will have the shaft extension.
- Two sets of bearings to support the rotating shaft,
- Steel shaft for transmitting the mechanical power to the load

- Cooling fan located at the non driving end to provide forced cooling for the stator and rotor
- Terminal box on top of the yoke or on side to receive the external electrical connections

Figure 2 to show the constructional details of the different parts of induction motor.



Fig. 2 Stator laminations



Fig.4 Stator with ribbed yoke



Fig. 3 stator core with smooth yoke



Fig 5. Squirrel cage rotor

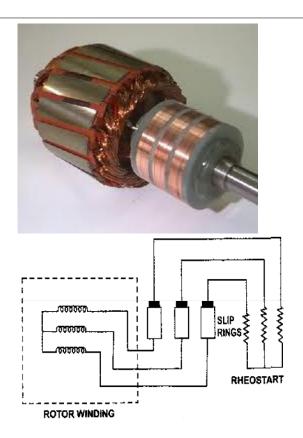


Fig. 6. Slip ring rotor

Fig 7. Connection to slip rings



Fig. 8 Cut sectional view of the induction motor.

Introduction to Design

The main purpose of designing an induction motor is to obtain the complete physical dimensions of all the parts of the machine as mentioned below to satisfy the customer specifications. The following design details are required.

- 1. The main dimensions of the stator.
- 2 Details of stator windings.
- 3. Design details of rotor and its windings
- 4. Performance characteristics.

In order to get the above design details the designer needs the customer specifications

Rated out put power, rated voltage, number of phases, speed, frequency, connection of stator winding, type of rotor winding, working conditions, shaft extension details etc.

In addition to the above the designer must have the details regarding design equations based on which the design procedure is initiated, information regarding the various choice of various parameters, information regarding the availability of different materials and the limiting values of various performance parameters such as iron and copper losses, no load current, power factor, temperature rise and efficiency

Output Equation: output equation is the mathematical expression which gives the relation between the various physical and electrical parameters of the electrical machine.

In an induction motor the out put equation can be obtained as follows

Consider an 'm' phase machine, with usual notations

Out put Q in kW = Input x efficiency

Input to motor = $mV_{ph} I_{ph} \cos \Phi \times 10^{-3} kW$

For a 3 Φ machine m = 3

Input to motor = $3V_{ph} I_{ph} \cos \Phi \times 10^{-3} \text{ kW}$

Assuming Vph = E_{ph} , $V_{ph} = E_{ph} = 4.44 \text{ f } \Phi \text{ T}_{ph} K_{w}$ = $2.22 \text{ f } \Phi Z_{ph} K_{w}$

$$f = PN_S/120 = Pn_s/2$$
,

Output =
$$3 \times 2.22 \times Pn_s/2 \times \Phi Z_{ph} K_w I_{ph} \eta \cos \Phi \times 10^{-3} \, kW$$

Output = $1.11 \times P\Phi \times 3I_{ph} Z_{ph} \times n_s K_w \eta \cos \Phi \times 10^{-3} \, kW$
 $P\Phi = B_{av}\pi DL$, and $3I_{ph} Z_{ph} / \pi D = q$

Output to motor = $1.11 \times B_{av}\pi DL \times \pi Dq \times n_s K_w \eta \cos \Phi \times 10^{-3} \, kW$
 $Q = (1.11 \pi^2 B_{av} q K_w \eta \cos \Phi \times 10^{-3}) \, D^2 L n_s \, kW$
 $Q = (11 B_{av} q K_w \eta \cos \Phi \times 10^{-3}) \, D^2 L n_s \, kW$

Therefore Output $Q = C_o \, D^2 L \, n_s \, kW$

where $Co = (11 B_{av} q K_w \eta \cos \Phi \times 10^{-3})$
 $V_{ph} = phase \, voltage \, ; \, I_{ph} = phase \, current$
 $Z_{ph} = no \, of \, conductors/phase$
 $T_{ph} = no \, of \, turns/phase$
 $N_s = Synchronous \, speed \, in \, rpm$
 $n_s = synchronous \, speed \, in \, rps$
 $p = no \, of \, poles$, $q = Specific \, electric \, loading$
 $\Phi = air \, gap \, flux/pole \, ; \, B_{av} = Average \, flux \, density$
 $k_w = winding \, factor$
 $\eta = efficiency$
 $\cos \Phi = power \, factor$
 $D = Diameter \, of \, the \, stator$,

 $L = Gross \, core \, length$

Fig.9 shows the details of main dimensions of the of an induction motor.

 C_o = Output coefficient

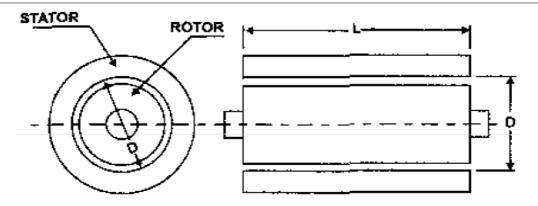


Fig 9. Main dimensions D and L

Choice of Specific loadings

Specific Magnetic loading or Air gap flux density

Iron losses largely depend upon air gap flux density

Limitations:

Flux density in teeth < 1.8 Tesla

Flux density in core 1.3 - 1.5 Tesla

Advantages of Higher value of Bav

- Size of the machine reduced
- Cost of the machine decreases
- Overload capacity increases

For 50 Hz machine, 0.35-0.6 Tesla. The suitable values of B_{av} can be selected from design data hand book.

Specific Electric loading

Total armature ampere conductor over the periphery

Advantages of Higher value of q

- Reduced size
- Reduced cost

Disadvantages of Higher value of q

- Higher amount of copper
- More copper losses
- Increased temperature rise
- Lower overload capacity

Normal range 10000 ac/m – 450000 ac/m. The suitable values of q can be selected from design data hand book.

Choice of power factor and efficiency

Choice of power factor and efficiency under full load conditions will increase with increase in rating of the machine. Percentage magnetizing current and losses will be lower for a larger machine than that of a smaller machine. Further the power factor and efficiency will be higher for a high speed machine than the same rated low speed machine because of better cooling conditions. Taking into considerations all these factors the above parameters will vary in a range based on the output of the machine. Similar to B_{av} and q, efficiency and power factor values can be selected from Design data hand book.

Separation of D and L

The output equation gives the relation between D^2L product and output of the machine. To separate D and L for this product a relation has to be assumed or established. Following are the various design considerations based on which a suitable ratio between gross length and pole pitch can be assumed.

i. To obtain minimum over all cost	1.5 to 2.0
ii. To obtain good efficiency	1.4 to 1.6
iii. To obtain good over all design	1.0 to 1.1
iv. To obtain good power factor	1.0 to 1.3

As power factor plays a very important role the performance of induction motors it is advisable to design an induction motor for best power factor unless specified. Hence to obtain the best power factor the following relation will be usually assumed for separation of D and L.

or
$$(\pi D/p) / L = 0.18 / (\pi D/p)$$
 i.e $D = 0.135 P\sqrt{L}$ where D and L are in meter.

Using above relation D and L can be separated from D^2L product. However the obtained values of D and L have to satisfy the condition imposed on the value of peripheral speed.

Peripheral Speed

For the normal design of induction motors the calculated diameter of the motor should be such that the peripheral speed must be below 30 m/s. In case of specially designed rotor the peripheral speed can be 60 m/s.

Design of Stator

Stator of an induction motor consists of stator core and stator slots.

Stator slots: in general two types of stator slots are employed in induction motors viz, open clots and semiclosed slots. Operating performance of the induction motors depends upon the shape of the slots and hence it is important to select suitable slot for the stator slots.

- (i) Open slots: In this type of slots the slot opening will be equal to that of the width of the slots as shown in Fig 10. In such type of slots assembly and repair of winding are easy. However such slots will lead to higher air gap contraction factor and hence poor power factor. Hence these types of slots are rarely used in 3Φ induction motors.
- (ii) Semiclosed slots: In such type of slots, slot opening is much smaller than the width of the slot as shown in Fig 10 and Fig 11. Hence in this type of slots assembly of windings is more difficult and takes more time compared to open slots and hence it is costlier. However the air gap characteristics are better compared to open type slots.
- (iii) Tapered slots: In this type of slots also, opening will be much smaller than the slot width. However the slot width will be varying from top of the slot to bottom of the slot with minimum width at the bottom as shown in Fig. 10.

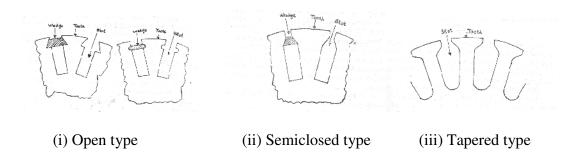


Fig. 10 Different types type slots

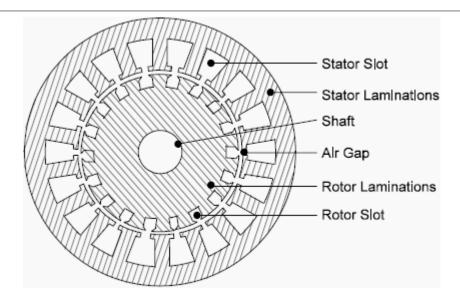


Fig. 11 Semiclosed slots

Selection of number of stator slots: Number of stator slots must be properly selected at the design stage as such this number affects the weight, cost and operating characteristics of the motor. Though there are no rules for selecting the number of stator slots considering the advantages and disadvantages of selecting higher number slots comprise has to be set for selecting the number of slots. Following are the advantages and disadvantages of selecting higher number of slots.

Advantages:(i) Reduced leakage reactance.

- (ii) Reduced tooth pulsation losses.
- (iii) Higher over load capacity.

Disadvantages:

- (i) Increased cost
- (ii) Increased weight
- (iii) Increased magnetizing current
- (iv) Increased iron losses
- (v) Poor cooling
- (vi) Increased temperature rise
- (vii) Reduction in efficiency

Based on the above comprise is made and the number of slots/pole/phase may be selected as three or more for integral slot winding. However for fractional slot windings number of slots/pole/phase may be selected as 3.5. So selected number of slots should satisfy the consideration of stator slot pitch at the air gap surface, which should be between 1.5 to 2.5 cm.

Stator slot pitch at the air gap surface = $\tau_{ss} = \pi D/S_{ss}$ where S_{ss} is the number of stator slots

Turns per phase

EMF equation of an induction motor is given by $E_{ph} = 4.44 f \Phi T_{ph} k_w$

Hence turns per phase can be obtained from emf equation $Tph = E_{ph}/4.44f\Phi k_w$

Generally the induced emf can be assumed to be equal to the applied voltage per phase

Flux/pole, $\Phi = B_{av} \times \pi DL/P$,

winding factor k_w may be assumed as 0.955 for full pitch distributed winding unless otherwise specified.

Number conductors /phase, $Z_{ph} = 2 \text{ x } T_{ph}$, and hence Total number of stator conductors $Z = 6 T_{ph}$ and conductors /slot $Z_s = Z/S_s$ or $6 T_{ph}/S_s$, where Z_s is an integer for single layer winding and even number for double layer winding.

Conductor cross section: Area of cross section of stator conductors can be estimated from the stator current per phase and suitably assumed value of current density for the stator windings.

Sectional area of the stator conductor $a_s = I_s / \delta_s$ where δ_s is the current density in stator windings

Stator current per phase $I_s = Q / (3V_{ph} \cos \Phi)$

A suitable value of current density has to be assumed considering the advantages and disadvantages.

Advantages of higher value of current density:

- (i) reduction in cross section
- (ii) reduction in weight
- (iii) reduction in cost

Disadvantages of higher value of current density

- (i) increase in resistance
- (ii) increase in cu loss
- (iii) increase in temperature rise
- (iv) reduction in efficiency

Hence higher value is assumed for low voltage machines and small machines. Usual value of current density for stator windings is 3 to 5 amps.

Based on the sectional area shape and size of the conductor can be decided. If the sectional area of the conductors is below 5 mm² then usually circular conductors are employed. If it is above 5 mm² then rectangular conductors will be employed. Standard bare size of round and rectangular conductors can be selected by referring the tables of conductors given in Design data Hand book. In case of rectangular conductors width to thickness ratio must be between 2.5 to 3.5.

Area of stator slot: Slot area is occupied by the conductors and the insulation. Out of which almost more than 25 % is the insulation. Once the number of conductors per slot is decided approximate area of the slot can be estimated.

Slot space factor = Copper area in the slot /Area of each slot

This slot space factor so obtained will be between 0.25 and 0.4. The detailed dimension of the slot can be estimated as follows.

Size of the slot: Normally different types of slots are employed for carrying stator windings of induction motors. Generally full pitched double layer windings are employed for stator windings. For double layer windings the conductor per slot will be even. These conductors are suitably arranged along the depth and width of the winding. Stator slots should not be too wide, leading to thin tooth width, which makes the tooth mechanically weak and maximum flux density may exceed the permissible limit. Hence slot width should be so selected such that the flux density in tooth is between 1.6 to 1.8 Tesla. Further the slots should not be too deep also other wise the leakage reactance increases. As a guideline the ratio of slot depth to slot width may assumed as 3 to 5. Slot insulation details along the conductors are shown in Fig. 12.

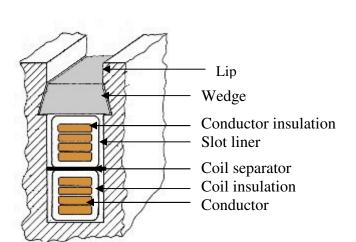


Fig. 12 Slot insulation detail with conductor

Proper slot insulation as per the voltage rating of the machine has to be provided before inserting the insulated coil in the slots. This slot insulation is called the slot liner, thickness of which may be taken as 0.5 mm to 0.7 mm. Suitable thickness of insulation called coil separator separates the two layers of coils. Thickness of coil separator is 0.5 mm to 0.7 mm for low voltage machines and 0.8 mm to 1.2 mm for high voltage machines. Wedge of suitable thickness (3.5 mm to 5 mm) is placed at the top of the slot to hold the coils in position. Lip of the slot is taken 1.0 to 2.0 mm. Figure 13 shows the coils placed in slots.



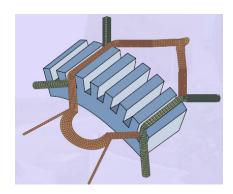


Fig 13. Stator coils, placed in slots

Length of the mean Turn:

Length of the mean turn is calculated using an empirical formula $l_{\text{mt}} = 2L + 2.3 \tau_p + 0.24$ where L is the gross length of the stator and τ_p is pole pitch in meter.

Resistance of stator winding: Resistance of the stator winding per phase is calculated using the formula = $(0.021 \text{ x } l_{\text{mt}} \text{ x T}_{\text{ph}})$ / a_{s} where l_{mt} is in meter and a_{s} is in mm². Using so calculated resistance of stator winding copper losses in stator winding can be calculated as

Total copper losses in stator winding = $3 (I_s)^2 r_s$

Flux density in stator tooth: Knowing the dimensions of stator slot pitch, width of the slot and width of the stator tooth flux density in the stator tooth can be calculated. The flux density in the stator tooth is limited to 1.8 Tesla. As the stator tooth is tapering towards the bottom, the flux density is calculated at $1/3^{rd}$ height from the narrow end of the tooth. The flux density at the $1/3^{rd}$ height from the narrow end of the tooth can be calculated as follows.

Diameter at $1/3^{rd}$ height from narrow end $D' = D + 1/3 x h_{ts} x 2$

Slot pitch at $1/3^{rd}$ height = $\tau'_s = \pi \times D'/S_s$

Tooth width at this section = $b_t = \tau_s - b_s$

Area of one stator tooth = $a_t = b_t \times l_i$

Area of all the stator tooth per pole $A_t = b_t \times l_i \times l_$

Mean flux density in stator teeth $B'_t = \Phi / A'_t$

Maximum flux density in the stator teeth may be taken to be less than 1.5 times the above value.

Depth of stator core below the slots: There will be certain solid portion below the slots in the stator which is called the depth of the stator core. This depth of the stator core can be calculated by assuming suitable value for the flux density B_c in the stator core. Generally the flux density in the stator core may be assumed varying between 1.2 to 1.4 Tesla. Depth of the stator core can be calculated as follows.

Flux in the stator core section $\Phi_c = \frac{1}{2} \Phi$

Area of stator core $A_c = \Phi/2B_c$

Area of stator core $A_c = L_i \times d_{cs}$

Hence, depth of the core = A_c / L_i

Using the design data obtained so far outer diameter of the stator core can be calculated as

 $D_0 = D + 2h_{ss} = 2 d_{cs}$ where h_{ss} is the height of the stator slot.

Problems

Ex. 1. Obtain the following design information for the stator of a 30 kW, 440 V, 3Φ , 6 pole, 50 Hz delta connected, squirrel cage induction motor, (i) Main dimension of the stator, (ii) No. of turns/phase (iii) No. of stator slots, (iv) No. of conductors per slot. Assume suitable values for the missing design data.

Soln: Various missing data are assumed from referring to Design data Hand Book or tables in Text Book considering the size, economics and performance

Specific Magnetic loading, Bav = 0.48 Tesla

Specific Electric loading, q = 26000 ac/m

Full load efficiency, $\eta = 0.88$

Full load power factor $\cos \Phi = 0.86$

Winding factor Kw = 0.955

(i) Main dimensions

We have from output equation:

$$D^2L = Q/(C_o n_s) m^3$$

$$Co = 11 \text{ B}_{av} \text{ q K}_w \text{ } \eta \cos \Phi \text{ x } 10^{-3}$$

$$= 11x \ 0.48 \text{ x } 26000 \text{ x } 0.955 \text{ x } 0.88 \text{ x } 0.86 \text{ x } 10^{-3}$$

$$= 99.2$$
and $n_s = 16.67 \text{ rps}$

$$D^2L = 30/(99.2 \text{ x } 16.67)$$

$$= 0.0182 \text{ m3}$$

Designing the m/c for bets power factor

$$D = 0.135 PVL$$
$$= 0.135 \times 6VL$$

Solving for D and L D = 0.33 m and L = 0.17 m

(ii) No. of stator turns

$$\Phi = (\pi DL/p) B_{av} = (\pi \times 0.33 \times 0.17/6) \times 0.48 = 0.141 \text{ wb}$$

Assuming $E_{ph} = V_{ph} = 440$ volts

$$T_{ph} = E_{ph} / 4.44 f \Phi k_w = 440/(4.44 \text{ x } 50 \text{ x } 0.0141 \text{ x } 0.955)$$

= 148

(iii) No. of stator slots

Assuming no of slot/pole/phase =3

Total no. of slots = $3 \times 3 \times 6 = 54$

(iv) No of conductors /slot

Total no of conductors = $148 \times 2 = 296$

No. of conductors /slot = 296/54 = 5.5

Assuming 76 conductors/ slot

Total no. of conductors = $54 \times 6 = 324$

Revised no. of turns/phase = 162

Ex. 2 A 15 kW 440m volts 4 pole, 50 Hz, 3 phase induction motor is built with a stator bore of 0.25 m and a core length of 0.16 m. The specific electric loading is 23000 ac/m. Using data of this_machine determine the core dimensions, number of slots and number of stator conductors for a 11kW, 460 volts,6 pole, 50 Hz motor. Assume full load efficiency of 84 % and power factor of 0.82. The winding factor is 0.955.

Soln: For 15 kW motor:

Motor Input = 15 / 0.84 = 17.857 kW; Synchronous speed $n_s = 120 \times 50 / (4 \times 60) = 25 \text{ rps}$;

we have output coefficient $C_0 = \text{out put } / D^2 L n_s = 15 / (0.25^2 \times 0.16 \times 25) = 60$

we have $C_o = 11~B_{av}~q~K_w~\eta~cos\Phi~x~10^{-3} = 11~x~B_{av}~x~23000~x~0.955x~0.84~x~0.82~x~10^{-3}$

$$= 166.42 B_{av}$$

Hence $B_{av} = 60/166.42 = 0.36$ Tesla

Pole pitch $\tau_p = \pi D/p = \pi \times 0.25/4 = 0.196 \text{ m}$; L/ $\tau_p = 0.815$

For 11kW motor: the design data from 15 kW machine has to be taken

So
$$B_{av} = 0.36$$
 Tesla; $q = 23000$ ac/m ; L/ $\tau_p = 0.815$; and $C_0 = 60$

Synchronous speed = $120 \times 50 / (6 \times 60) = 16.667 \text{ rps}$;

$$D^2L = Q/(C_o n_s) m^3$$

$$= 11 / (60 \times 16.667) = 0.01099 \text{ m}^3$$

$$L/(\pi D/p) = 0.815$$
, So $L/D = 0.815 \times \pi/6 = 0.427$ or $L = 0.427 D$

Substituting this value in D²L product and solving for D and L

$$0.427 \text{ D}^3 = 0.01099$$
 hence D = 0.30 m and L = 0.125 m

Number of slots: Considering the slot pitch at the air gap between 1.5 cm and 2.5 cm

Number of slots = π x D/ τ s for slot pitch 1.5 cm, S_s = π x 30 / 1.5 = 63

For slot pitch 2.5 cm $S_s = \pi \times 30 / 2.5 = 37$ Hence number of slots must be between 37 & 63

Assuming no. of stator slots /pole/phase = 3, S_s = 6 x 3 x 3 = 54

Flux per pole $\Phi = B_{av} \times D \times L / p = 0.36 \times \pi \times 0.3 \times 0.125 / 6 = 7.07 \times 10^{-3} \text{ wb}$

Assuming star delta connection for the machine, under running condition using Delta connection

Stator turns per phase $T_{ph} = E_{ph} / (4.44 \text{ f } \Phi \text{ K}_w) = 460 / (4.44 \text{ x } 50 \text{ x } 7.07 \text{ x } 10^{-3} \text{ x } 0.955) = 307$

Number conductors/phase = 307×2 ,

Total number of stator conductors = $307 \times 2 \times 3 = 1872$

Number of conductors per slot = $1872/54 = 34.1 \approx 34$

Hence total number of conductor = $34 \times 54 = 1836$.

Ex. 3 Determine main dimensions, turns/phase, number of slots, conductor size and area of slot of 250 HP, 3 phase, 50 Hz, 400 volts, 1410 rpm, slip ring induction motor. Assume $B_{av} = 0.5 \text{wb/m}^2$, q = 30000 ac/m, efficiency = 90 % and power factor = 0.9, winding factor = 0.955, current density =3.5 a/mm², slot space factor = 0.4 and the ratio of core length to pole pitch is 1.2. the machine is delta connected. (July 2007)

Soln.

Ex. 4. During the preliminary design of a 270 kW, 3600 volts, 3 phase, 8 pole 50 Hz slip ring induction motor the following design data have been obtained.

Gross length of the stator core = 0.38 m, Internal diameter of the stator = 0.67 m, outer diameter of the stator = 0.86 m, No. of stator slots = 96, No. of conductors /slot = 12, Based on the above information determine the following design data for the motor. (i) Flux per pole (ii) Gap density (iii) Conductor size (iv) size of the slot (v) copper losses (vi) flux density in stator teeth (vii) flux density in stator core.

Soln. (i) Flux per pole

Number of slots per phase 96/3 = 32

Number of turns per phase $T_{ph} = 32 \times 12/2 = 192$,

Assuming full pitched coils, $k_w = 0.955$, $E_{ph} = V_{ph}$ and star connected stator winding,

$$E_{ph} = 3600/\sqrt{3} = 2078 \text{ volts},$$

We have $E_{ph} = 4.44 f \Phi T_{ph} k_w$, ie

$$\Phi = E_{ph} / (4.44 f T_{ph} k_w) = 2078 / (4.44 \text{ x } 50 \text{ x } 192 \text{ x } 0.955) = 0.051 \text{wb}$$

(ii) Gap flux density $A_g = \pi DL/p = \pi \times 0.67 \times 0.38 / 8 = 0.1 \text{ m}^2$

$$B_g = \Phi / A_g = 0.051 / 0.1 = 0.51 \text{ Tesla}$$

(iii) Conductor size

Assuming an efficiency of 91% and a full load power factor of 0.89

Input power to the motor = $270 \times 10^3 / 0.91 = 296703 \text{ w}$

Full load current per phase = $296703 / (3 \times 2078 \times 0.89) = 53.47$ amps

Assuming a current density of 4.1 amp/mm^2 , area of cross section of the conductor = $53.47 / 4.1 = 13.04 \text{ mm}^2$ as the conductor section is $> 5 \text{ mm}^2$ rectangular conductor is selected. Standard size of the conductor selected satisfying the requirements is $2.5 \text{ mm} \times 5.5 \text{ mm}$.

Thus sectional area of the conductor 13.2 mm²

Size of the conductor with insulation thickness of 0.2 mm is 2.9 mm x 5.9 mm

(iv) size of the slot

12 conductors per slot are arranged in two layers with 6 conductors in each layer. Six conductors in each layer are arranged as 2 conductors depth wise and 3 conductors width wise. With this arrangement the width and depth of the slot can be estimated as follows.

(a) Width of the slot

Space occupied by insulated conductor, 3 x 2.9	8.7 mm
Coil insulation, 2 x 1.0	2.0 mm
Slot liner, 2 x 0.2	0.4 mm
Clearance	0.9 mm
Total width of the slot	12.0 mm

(b) Depth of the slot

Space occupied by insulated conductor, 4 x 5.9	23.6 mm
Coil insulation, 4 x 1.0	4.0 mm
Slot liner, 3 x 0.2	0.6 mm
Coil separator, 1 x 1.0	0.5 mm
Top liner, 1 x 1.0	0.5 mm
Wedge	3.0 mm
Lip	1.5 mm
Clearance	1.3 mm
Total height of the slot	35.0 mm

Thus the dimension of the slot 12.0 mm x 35.0 mm

(v) Copper losses in stator winding

Length of the mean turn, $l_{mt} = 2L + 2.3 \tau_p + 0.24 = 2 \times 0.38 + 2.3 \times \pi \times 0.67/8 + 0.24 = 1.6 \text{ m}$ Resistance per phase = $(0.021 \times l_{mt} \times T_{ph}) / a_s = 0.021 \times 1.6 \times 192 / 13.2 = 0.49 \text{ ohm}$.

Total copper losses = $3I_s^2 r_s = 3 \times 53.47^2 \times 0.49 = 4203$ watts

(vi) Flux density in stator tooth

Diameter at $1/3^{rd}$ height, $D = D + 1/3 \times h_{ts} \times 2 = 0.67 + 1/3 \times 0.035 \times 2 = 0.693 \text{ m}$

Slot pitch at $1/3^{rd}$ height = $\tau_s = \pi \times D'/S_s = \pi \times 0.693/96 = 0.02268 m$

Tooth width at this section = $b_t = \tau_s - b_s = 0.02268 - 0.012 = 0.0168 \text{ m}$

assuming 3 ventilating ducts with 1cm width $\,$ and iron space factor of 0.95

Iron length $l_i = (0.38 - 3 \times 0.01) 0.95 = 0.3325 \text{ m}$

Area of the stator tooth per pole $A_t = b_t \times l_i \times$

=
$$b_t \times l_i \times S_s / p = 0.01068 \times 0.3325 \times 96/8$$

= 0.04261 m^2

Mean flux density in stator teeth $B'_t = \Phi / A'_t = 0.051/0.04261 = 1.10$ Tesla

Maximum flux density in stator tooth = $1.5 \times 1.10 = 1.65$ Tesla

(vii) Flux density in stator core

Depth of the stator core $d_{cs} = \frac{1}{2} (D_0 - D - 2h_{ss}) = \frac{1}{2} (0.86 - 0.67 - 2 \times 0.035) = 0.06 \text{ m}$

Area of stator core $A_c = L_i \times d_{cs} = 0.3325 \times 0.06 = 0.01995 \text{ m}^2$

Flux in stator core = $\frac{1}{2}$ x $\Phi = \frac{1}{2}$ x 0.051 = 0.0255 wb

Flux density in stator core, $B_c = \Phi_c / A_c = 0.0255 / 0.01995 = 1.28$ Tesla

Design of Rotor:

There are two types of rotor construction. One is the squirrel cage rotor and the other is the slip ring rotor. Most of the induction motor are squirrel cage type. These are having the advantage of rugged and simple in construction and comparatively cheaper. However they have the disadvantage of lower starting torque. In this type, the rotor consists of bars of copper or aluminum accommodated in rotor slots. In case slip ring induction motors the rotor complex in construction and costlier with the advantage that they have the better starting torque. This type of rotor consists of star connected distributed three phase windings.

Between stator and rotor is the air gap which is a very critical part. The performance parameters of the motor like magnetizing current, power factor, over load capacity, cooling and noise are affected by length of the air gap. Hence length of the air gap is selected considering the advantages and disadvantages of larger air gap length.

Advantages:

- (i) Increased overload capacity
- (ii) Increased cooling
- (iii) Reduced unbalanced magnetic pull
- (iv) Reduced in tooth pulsation
- (v) Reduced noise

Disadvantages

- (i) Increased Magnetising current
- (ii) Reduced power factor

Effect of magnetizing current and its effect on the power factor can be understood from the phasor diagram of the induction motor shown in Fig. 14.

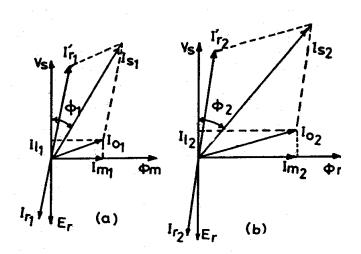


Fig. 14 Phasor diagram of induction motor

Magnetising current and power factor being very important parameters in deciding the performance of induction motors, the induction motors are designed for optimum value of air gap or minimum air gap possible. Hence in designing the length of the air gap following empirical formula is employed.

Air gap length
$$l_g = 0.2 + 2\sqrt{DL}$$
 mm

The following Fig. 15 show the different types of rotor construction.





Fig. 15 Squrrel cage rotor



Slip ring rotor

Number of slots: Proper numbers of rotor slots are to be selected in relation to number of stator slots otherwise undesirable effects will be found at the starting of the motor. Cogging and Crawling are the two phenomena which are observed due to wrong combination of number of rotor and stator slots. In addition, induction motor may develop unpredictable hooks and cusps in torque speed characteristics or the motor may run with lot of noise. Let us discuss Cogging and Crawling phenomena in induction motors.

Crawling: The rotating magnetic field produced in the air gap of the will be usually nonsinusoidal and generally contains odd harmonics of the order 3rd, 5th and 7th. The third harmonic flux will produce the three times the magnetic poles compared to that of the fundamental. Similarly the 5th and 7th harmonics will produce the poles five and seven times the fundamental respectively. The presence of harmonics in the flux wave affects the torque speed characteristics. The Fig. 16 below shows the effect of 7th harmonics on the torque speed characteristics of three phase induction motor. The motor with presence of 7th harmonics is to have a tendency to run the motor at one seventh of its normal speed. The 7th harmonics will produce a dip in torque speed characteristics at one seventh of its normal speed as shown in torque speed characteristics.

Cogging: In some cases where in the number of rotor slots are not proper in relation to number of stator slots the machine refuses to run and remains stationary. Under such conditions there will be a locking tendency between the rotor and stator. Such a phenomenon is called cogging.

Hence in order to avoid such bad effects a proper number of rotor slots are to be selected in relation to number of stator slots. In addition rotor slots will be skewed by one slot pitch to minimize the tendency of cogging, torque defects like synchronous hooks and cusps and noisy operation while running. Effect of skewing will slightly increase the rotor resistance and increases the starting torque. However this will increase the leakage reactance and hence reduces the starting current and power factor.

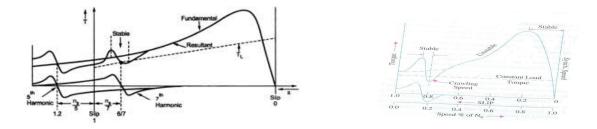


Fig 16 Torque speed characteristics

Selection of number of rotor slots: The number of rotor slots may be selected using the following guide lines.

- (i) To avoid cogging and crawling: (a) $S_s \neq S_r$ (b) $S_s S_r \neq \pm 3P$
- (ii) To avoid synchronous hooks and cusps in torque speed characteristics $\neq \pm P$, $\pm 2P$, $\pm 5P$.
- (iii) To noisy operation $S_s S_r \neq \pm 1, \pm 2, (\pm P \pm 1), (\pm P \pm 2)$

Rotor Bar Current: Bar current in the rotor of a squirrel cage induction motor may be determined by comparing the mmf developed in rotor and stator.

Hence the current per rotor bar is given by $I_b = (K_{ws} \times S_s \times Z'_s) \times I'_r / (K_{wr} \times S_r \times Z'_r)$;

where K_{ws} – winding factor for the stator, S_s – number of stator slots, Z'_s – number of conductors / stator slots, K_{wr} – winding factor for the rotor, S_r – number of rotor slots, Z'_r – number of conductors / rotor slots and I'_r – equivalent rotor current in terms of stator current and is given by $I'_r = 0.85 I_s$ where is stator current per phase.

Cross sectional area of Rotor bar: Sectional area of the rotor conductor can be calculated by rotor bar current and assumed value of current density for rotor bars. As cooling conditions are better for the rotor than the stator higher current density can be assumed. Higher current density will lead to reduced sectional area and hence increased resistance, rotor cu losses and reduced efficiency. With increased rotor resistance starting torque will increase. As a guide line the rotor bar current density can be assumed between 4 to 7 Amp/mm² or may be selected from design data Hand Book.

Hence sectional area of the rotor bars can be calculated as $A_b = I_b/\delta_b \ mm^2$. Once the cross sectional area is known the size of the conductor may be selected form standard table given in data hand book.

Shape and Size of the Rotor slots: Generally semiclosed slots or closed slots with very small or narrow openings are employed for the rotor slots. In case of fully closed slots the rotor bars are force fit into the slots from the sides of the rotor. The rotors with closed slots are giving better performance to the motor in the following way. (i) As the rotor is closed the rotor surface is smooth at the air gap and hence the motor draws lower magnetizing current. (ii) reduced noise as the air gap characteristics are better (iii) increased leakage reactance and (iv) reduced starting current. (v) Over load capacity is reduced (vi) Undesirable and complex air gap characteristics. From the above it can be concluded that semiclosed slots are more suitable and hence are employed in rotors.

Copper loss in rotor bars: Knowing the length of the rotor bars and resistance of the rotor bars cu losses in the rotor bars can be calculated.

Length of rotor bar $l_b = L + allowance$ for skewing

Rotor bar resistance = $0.021 \times l_b/A_b$

Copper loss in rotor bars = $I_b^2 \times r_b \times r_b$

End Ring Current: All the rotor bars are short circuited by connecting them to the end rings at both the end rings. The rotating magnetic filed produced will induce an emf in the rotor bars which will be sinusoidal over one pole pitch. As the rotor is a short circuited body, there will be current flow because of this emf induced. The distribution of current and end rings are as shown in Fig. 17 below. Referring to the figure considering the bars under one pole pitch, half

of the number of bars and the end ring carry the current in one direction and the other half in the opposite direction. Thus the maximum end ring current may be taken as the sum of the average current in half of the number of bars under one pole.

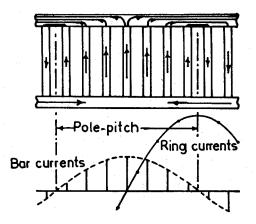


Fig. 17 currents in cage rotor bars and end rings

Maximum end ring current $I_e(max) = \frac{1}{2}$ (Number rotor bars / pole) $I_b(av)$

$$= \frac{1}{2} \times S_r/P \times I_b/1.11$$

Hence rms value of

$$I_e = 1/2\sqrt{2} \times S_r/P \times I_b/1.11$$

$$= 1/\pi \times S_r/P \times I_b/1.11$$

Area of end ring: Knowing the end ring current and assuming suitable value for the current density in the end rings cross section for the end ring can be calculated as

Area of each end ring $A_e = I_e / \delta_e \ mm^2$, current density in the end ring may be assume as 4.5 to 7.5 amp/mm².

Copper loss in End Rings: Mean diameter of the end ring (D_{me}) is assumed as 4 to 6 cms less than that of the rotor. Mean length of the current path in end ring can be calculated as $l_{me} = \pi D_{me}$. The resistance of the end ring can be calculated as

$$r_e = 0.021 \text{ x } l_{me} / A_e$$

Total copper loss in end rings = $2 \times I_e^2 \times r_e$

Equivalent Rotor Resistance: Knowing the total copper losses in the rotor circuit and the equivalent rotor current equivalent rotor resistance can be calculated as follows.

Equivalent rotor resistance $r_r = \text{Total rotor copper loss } / 3 \times (I_r)^2$

Design of wound Rotor: These are the types of induction motors where in rotor also carries distributed star connected 3 phase winding. At one end of the rotor there are three slip rings mounted on the shaft. Three ends of the winding are connected to the slip rings. External resistances can be connected to these slip rings at starting, which will be inserted in series with the windings which will help in increasing the torque at starting. Such type of induction motors are employed where high starting torque is required.

Number of rotor slots: As mentioned earlier the number of rotor slots should never be equal to number of stator slots. Generally for wound rotor motors a suitable value is assumed for number of rotor slots per pole per phase, and then total number of rotor slots are calculated. So selected number of slots should be such that tooth width must satisfy the flux density limitation. Semiclosed slots are used for rotor slots.

Number of rotor Turns: Number of rotor turns are decided based on the safety consideration of the personal working with the induction motors. The volatge between the slip rings on open circuit must be limited to safety values. In general the voltage between the slip rings for low and medium voltage machines must be limited to 400 volts. For motors with higher voltage ratings and large size motors this voltage must be limited to 1000 volts. Based on the assumed voltage between the slip rings comparing the induced voltage ratio in stator and rotor the number of turns on rotor winding can be calculated.

Voltage ratio Er/Es = (Kwr x Tr) / (Kws x Ts)

Hence rotor turns per phase Tr = (Er/Es) (Kws/Kwr) Ts

Er = open circuit rotor voltage/phase

Es = stator voltage /phase

Kws = winding factor for stator

Kwr = winding factor for rotor

Ts = Number of stator turns/phase

Rotor Current

Rotor current can be calculated by comparing the amp-cond on stator and rotor

$$Ir = (K_{ws} \times S_s \times Z'_s) \times I'_r / (K_{wr} \times S_r \times Z'_r);$$

Kws – winding factor for the stator,

Ss – number of stator slots.

Z's – number of conductors / stator slots,

Kwr – winding factor for the rotor,

Sr – number of rotor slots,

Z'r – number of conductors / rotor slots and

I'r – equivalent rotor current in terms of stator current

I'r = 0.85 Is where Is is stator current per phase.

Area of Rotor Conductor: Area of rotor conductor can be calculated based on the assumed value for the current density in rotor conductor and calculated rotor current. Current density rotor conductor can be assumed between 4 to 6 Amp/mm2

$$Ar = Ir / \delta r \ mm^2$$

 $Ar < 5 \text{mm}^2$ use circular conductor, else rectangular conductor, for rectangular conductor width to thickness ratio = 2.5 to 4. Then the standard conductor size can be selected similar to that of stator conductor.

Size of Rotor slot: Mostly Semi closed rectangular slots employed for the rotors. Based on conductor size, number conductors per slot and arrangement of conductors similar to that of stator, dimension of rotor slots can be estimated. Size of the slot must be such that the ratio of depth to width of slot must be between 3 and 4.

Total copper loss: Length of the mean Turn can be calculated from the empirical formula $l_{\text{mt}} = 2L + 2.3 \tau_{\text{p}} + 0.08 \text{ m}$

Resistance of rotor winding is given by $Rr = (0.021 \text{ x } l_{mt} \text{ x } T_r) / A_r$ Total copper loss = 3 Ir² R_r Watts

Flux density in rotor tooth: It is required that the dimension of the slot is alright from the flux density consideration. Flux density has to be calculated at 1/3rd height from the root of the teeth. This flux density has to be limited to 1.8 Tesla. If not the width of the tooth has to be increased and width of the slot has to be reduced such that the above flux density limitation is satisfied. The flux density in rotor can be calculated by as shown below.

Diameter at 1/3rd height $Dr' = D - 2/3 \times h_{tr} \times 2$

Slot pitch at 1/3rd height = $\tau'_r = \pi \times D_r' / S_r$

Tooth width at this section = $b'_{tr} = \tau'_{sr} - b_{sr}$

Area of one rotor tooth = $a'_{tr} = b'_{tr} \times l_i$

Iron length of the rotor $l_i = (L - w_d \times n_d)k_i$, $k_i = iron$ space factor

Area of all the rotor tooth / pole $A'_{tr} = b'_{t} \times l_{i} \times S_{r} / P$

Mean flux density in rotor teeth $B'_{tr} = \Phi / A'_{tr}$

Maximum flux density in the rotor teeth < 1.5 times B'_{tr}

Depth of stator core below the slots: Below rotor slots there is certain solid portion which is called depth of the core below slots. This depth is calculated based on the flux

density and flux in the rotor core. Flux density in the rotor core can be assumed to be between 1.2 to 1.4 Tesla. Then depth of the core can be found as follows.

Flux in the rotor core section $\Phi c = \frac{1}{2} \Phi$

Area of stator core $A_{cr} = \Phi/2B_{cr}$

Area of stator core $A_{cr} = L_i \times d_{cr}$

Hence, depth of the core $d_{cr} = A_{cr} / L_i$

Inner diameter of the rotor can be calculated as follows Inner diameter of rotor = D - $2l_g$ - $2h_{tr}$ - $2d_{cr}$

Ex.1. During the stator design of a 3 phase, 30 kW, 400volts, 6 pole, 50Hz, squirrel cage induction motor following data has been obtained. Gross length of the stator = 0.17 m, Internal diameter of stator = 0.33 m, Number of stator slots = 45, Number of conductors per slot = 12. Based on the above design data design a suitable rotor.

Soln: (i) Diameter of the rotor

Length of the air gap
$$lg = 0.2 + 2 \sqrt{DL} \text{ mm}$$

= $0.2 + 2 \sqrt{0.33} \times 0.17 \text{ mm}$
= 0.67 mm
Outer diameter of rotor Dr = D - 2 lg
= $0.33 - 2 \times 0.67 \times 10^{-3}$
= 0.328 m

- (ii) Number of rotor slots
- (a) Ss > Sr
- (b) To avoid cogging and crawling: $Sr \neq Ss$, $Ss Sr \neq \pm 3P$ $Sr \neq 45$, $Ss - Sr \neq \pm 3P \rightarrow 45 - 18 \neq 27$,
- (c) To avoid synchronous hooks and cusps in torque speed characteristics Ss Sr $\neq \pm P$, $\pm 2P$, $\pm 5P$

Ss - Sr
$$\neq$$
 (45 - 6), (45 - 12), (45 - 03) \neq 39, 33, 15

To avoid noisy operation Ss - Sr
$$\neq \pm 1, \pm 2, (\pm P \pm 1), (\pm P \pm 2)$$

Ss - Sr $\neq (45 - 1), (45 - 2), (45 - 7), (45 - 8)$

Considering all the combination above Sr = 42

Rotor slot pitch = π Dr / Sr = π x 32.8 / 42 = 2.45 cm (quite satisfactory)

(iii) Rotor bar current

Assuming star – delta connection for stator winding

$$Vph = 400 \text{ volts}$$

Assuming
$$\eta = 88 \%$$
 and p.f = 0.86

Motor input =
$$30/0.88 = 30.1 \text{ kW}$$

Full load stator current = input / 3 vph
$$\cos \Phi$$

$$= 30.1 \times 103/3 \times 440 \times 0.86$$

= 33 amps

$$I'_r = 0.85 I_s = 0.85 \times 33 = 28 \text{ amps}$$

Assuming $K_{ws} = 0.955$ & No. of rotor cond/slot = 1

$$I_b = (K_{ws} \times S_s \times Z'_s) \times I'_r / (K_{wr} \times S_r \times Z'_r)$$

$$= (0.955 \times 45 \times 12) \times 28 / (1 \times 42 \times 1)$$

$$343.8 \text{ amps}$$

(iv) Size of rotor bar and slot

Assuming the current density in rotor bars = 6.0 amps/mm^2

$$A_r = I_r / \delta_r \ mm^2$$

$$A_r = 343.8/6.0$$

$$= 57.3 \text{ mm}^2$$

Selecting rectangular standard conductor available

Area of conductor = 57.6 mm^2

Hence standard conductor size = 13 mm x 4.5 mm

Size of rotor slot to fit the above cond = 13.5 mm x 5 mm

(v) Resistance of rotor bar

Length of rotor bar $l_b = L + \text{allowance for skewing} + \text{allowance between end rings and rotor core}$

$$l_b = 0.17 + 0.05 = 0.22 \text{ m}$$

Rotor bar resistance =
$$0.021 \times l_b / A_b$$

$$= 0.021 \times 0.22 / 57.6$$

$$= 8.02 \times 10^{-5} \text{ ohm}$$

Copper loss in rotor bars = I_b^2 x r_b x number of rotor bars

$$= 343.8^2 \times 8.02 \times 10^{-5} \times 42$$

= 398 watts

(vii) End ring current
$$Ie$$
 = $1/\pi \times Sr/P \times Ib$
= $1/\pi \times 343.8 \times 7$
= 765.8 amps

(viii) Area of cross section of end ring

Assuming a current density of 6.5 Amp/mm²

Area of each end ring $Ae = Ie / \delta e \text{ mm}^2$,

$$= 765.7 / 6.5$$

$$= 117.8 \text{ mm}^2$$

(ix) Rotor dia Dr = 32.8 cm,

Assuming Dme 4.8 cms less than that of the rotor $D_{me} = 28 cms$

Mean length of the current path in end ring $l_{me} = \pi D_{me} = 0.88 \text{ m}$

Resistance of each end ring $re = 0.021 \text{ x } l_{me}/A_e$

$$= 0.021 \times 0.88 / 117.8$$

$$= 1.57 \times 10^{-4} \text{ ohms}$$

Total copper loss in end rings = $2 \times Ie^2 \times r_e$

$$= 2 \times 765.72 \times 1.57 \times 10^{-4}$$

= 184 watts

(x) Equivalent rotor resistance

Total copper loss = copper loss in bars + copper loss in end rings

$$= 398 + 184 = 582$$
 watts

Equivalent rotor resistance $r' = \text{Total rotor copper loss } / (3 \text{ x Ir}^2)$

$$= 582 / (3 \times 282)$$

= 0.247 ohms

Ex.2. A 3 phase 200 kW, 3.3 kV, 50 Hz, 4 pole induction motor has the following dimensions. Internal diameter of the stator = 56.2 cm, outside diameter of the stator = 83cm, length of the stator = 30.5 cm, Number of stator slots = 60, width of stator slot = 1.47 cm, depth of stator slot = 4.3 cm, radial gap = 0.16 cm, number of rotor slots = 72, depth of rotor slot 3.55 cm, width of rotor slots = 0.95 cm. Assuming air gap flux density to be 0.5 Tesla, calculate the flux density in (i) Stator teeth (ii) Rotor teeth (iii) stator core.

Soln: (i) Flux density in Stator teeth

Internal diameter of stator = 56.2 cm, Depth of stator slot = 4.3 cm,

Diameter at $1/3^{rd}$ height from narrow end of the stator teeth $D = D + 1/3 \times h_{ts} \times 2$

$$= 56.2 + 1/3 \times 4.3 \times 2$$

$$= 59.1 \text{ cm}$$

Slot pitch at $1/3^{rd}$ height $\tau'_s = \pi \times D'/S_s$

$$= \pi \times 59.1/60 = 3.1 \text{ cm}$$

Tooth width at this section $b_t = \tau_s - b_s$

$$= 3.1 - 1.47$$

$$= 1.63$$
 cm

Area of one stator tooth $a_t = b_t \times l_i$

$$l_i = k_i(L - n_d x w_d) = 0.93(30.5 - 3 x 1) = 25.6 \text{ cm}$$

Area of stator tooth $A_t = b_t \times l_i$

$$= 25.6 \times 1.63$$

$$= 0.00418 \text{ m}^2$$

Number of stator teeth per pole = 60 / 4 = 15

Air gap area = π DL = π x 0.562 x 0.305 = 0.535 m²

Total flux = B_{av} x π DL = 0.5 x 0.535 = 0.2675 wb

Hence flux per pole 0.2675/4 = 0.06679 wb

Mean flux density in stator teeth $B'_t = \Phi / (A'_t \times no)$ of teeth per pole)

 $= 0.0669 / (0.00418 \times 15)$

= 1.065 Tesla

Max flux density in stator teeth = $1.5 \times 1.065 = 1.6 \text{ Tesla}$.

(ii) Flux density in rotor teeth

Diameter of the rotor = $D - 2lg = 56.2 - 2 \times 0.16 = 55.88$ cm

Depth of rotor slot = 3.55 cm

Diameter at 1/3rd height Dr' = D - 2/3 x h_{tr} x 2 = 55.88 - 2/3 x 3.55 x 2 = 51.14 cm

Slot pitch at 1/3rd height = $\tau'_r = \pi \times D_r' / S_r = \pi \times 51.14 / 72 = 2.23$ cm

Width of the rotor slot = 0.95 cm

Tooth width at this section = $b'_{tr} = \tau'_{sr} - b_{sr} = 2.23 - 0.95 = 1.28$ cm

Iron length $l_i = 25.6$ cm

Area of one rotor tooth = $a'_{tr} = b'_{tr} \times l_i = 1.28 \times 25.6 = 32.8 \text{ cm}^2 = 0.00328 \text{ m}^2$

Number of rotor tooth per pole = 72/4 = 18

Area of all the rotor tooth / pole $A'_{tr} = b'_{t} \times l_{i} \times S_{r} / P = 0.00328 \times 18 = 0.05904 \text{ m}^{2}$

Mean flux density in rotor teeth $B'_{tr} = \Phi / A'_{tr} = 0.0669 / 0.05904 = 1.13$ Tesla

Maximum flux density in the rotor teeth = $1.5 \times 1.13 = 1.69$ Tesla

(iii) Flux density in Stator core

Depth of the stator core $d_c = \frac{1}{2} (D_0 - D - 2h_t) = \frac{1}{2} (83 - 56.2 - 2 \times 4.3) = 9.1 \text{ cm}$

Area of stator core Ac = l_i x d_c = 25.6 x 9.1 = 233 cm² = 0.0233 m²

Flux in stator core $\Phi = \frac{1}{2} \Phi_c = 0.5 \times 0.0669 = 0.03345 \text{ wb}$

Flux density in stator core = Φ_c / Ac = 0.03345 / 0.0233 = 1.435 Tesla

Ex.3. A 3 phase 3000 volts 260 kW, 50 Hz, 10 pole squirrel cage induction motor gave the following results during preliminary design.

Internal diameter of the stator = 75 cm, Gross length of the stator = 35 cm, Number of stator slots = 120, Number of conductor per slot = 10. Based on the above data calculate the following for the squirrel cage rotor. (i) Total losses in rotor bars, (ii) Losses in end rings, (iii) Equivalent resistance of the rotor.

Soln. (i) Total losses in rotor bars

Number of stator slots = 120,

To confirm to the requirements the rotor slots can be selected in the following way

Number of rotor slots

- a) Ss > Sr
- (b) To avoid cogging and crawling: $Sr \neq Ss$, $Ss Sr \neq \pm 3P$ $Sr \neq 120$, $Ss - Sr \neq \pm 3P \rightarrow 120 - 30 \neq 90$,
- (c) To avoid synchronous hooks and cusps in torque speed characteristics Ss Sr \neq \pm P, \pm 2P, \pm 5P

Ss - Sr
$$\neq$$
 (120 – 10), (120 – 20), (120 – 50) \neq 110, 100, 70

(d) To avoid noisy operation Ss - Sr
$$\neq \pm 1, \pm 2, (\pm P \pm 1), (\pm P \pm 2)$$

Ss - Sr $\neq (120 - 1), (120 - 2), (120 - 11), (120 - 12) \neq 119, 118, 109, 108$

Considering all the combination above Sr = 115

Rotor slot pitch = πD / Sr = π x 75 / 115 = 2.048 cm (quite satisfactory)

Rotor bar current

Assuming
$$\eta = 90\%$$
 and p.f = 0.9
Motor input = 260/0.9 = 288.88 kW
Assuming star connection
Full load stator current = input / ($\sqrt{3}$ V_L cos Φ)
= 288.88 x 10³/ ($\sqrt{3}$ x 3000 x 0.9)
= 61.5 amps

$$I'_r = 0.85 I_s = 0.85 \times 61.5 = 52.275 \text{ amps}$$

Assuming $K_{ws} = 0.955$ & No. of rotor cond/slot = 1

$$I_b = (K_{ws} \times S_s \times Z'_s) \times I'_r / (K_{wr} \times S_r \times Z'_r)$$

$$= (0.955 \times 120 \times 10) \times 52.275 / (1 \times 115 \times 1)$$

$$= 521 \text{ amps}$$

Area of rotor bar

Assuming the current density in rotor bars = 6.5 amps/mm^2

$$A_b = I_b / \delta_b \ mm^2$$

$$A_b = 521 / 6.5$$

$$= 80.2 \text{ mm}^2$$

Length of rotor bar $l_b = L + \text{allowance}$ for skewing + allowance between end rings and rotor core

$$l_b = 0.35 + 0.05 = 0.4 \text{ m}$$

Rotor bar resistance = $0.021 \times l_b / A_b$

$$= 0.021 \times 0.4 / 80.2$$

$$= 1.05 \times 10^{-4} \text{ ohm}$$

Copper loss in rotor bars = I_b^2 x r_b x number of rotor bars

$$= 521^2 \times 1.05 \times 10^{-4} \times 115$$

= 3278 watts

(ii) Losses in end rings

End ring current
$$Ie$$
 = $1/\pi \times Sr/P \times I_b$
= $1/\pi \times (115/10) \times 521$
= 1906 amps

Area of cross section of end ring

Assuming a current density of 6.5 Amp/mm²

Area of each end ring $Ae = Ie / \delta e \text{ mm}^2$,

$$= 1906/6.5$$

$$= 293.2 \text{ mm}^2$$

Air gap length
$$l_g = 0.2 + 2\sqrt{DL}$$
$$= 0.2 + 2\sqrt{0.75} \times 0.35$$

$$= 1.22 \ mm$$

Rotor diameter $D_r = D - 2 l_g$

$$= 75 - 0.122$$

$$= 74.878 cm$$

Rotor dia Dr = 74.878 cm,

Assuming D_{me} 6.878 cms less than that of the rotor D_{me} = 68 cms

Mean length of the current path in end ring $l_{me} = \pi D_{me} = 2.136$ m

Resistance of each end ring $re = 0.021 \text{ x } l_{me}/A_e$

$$= 1.529 \times 10^{-4} \ ohms$$

Total copper loss in end rings = $2 \times Ie^2 \times r_e$

$$= 2 \times 1906^2 \times 1.529 \times 10^{-4}$$

$$= 1111.55$$
 watts

(iii) Equivalent rotor resistance

Total copper losses in the rotor = Copper loss in bars + copper loss in end rings

$$= 3278 + 1111.55$$

= 4389.55 watts

Equivalent Rotor resistance = Rotor cu loss /
$$(3 \text{ I}^2)$$

= $4389.55/(3 \text{ x } 52.275^2)$
= 0.535 ohm

Ex.4. Following design data have been obtained during the preliminary design of a 3 phase, 850 kW, 6.6 kV, 50 Hz, 12 pole slip ring induction motor. Gross length of stator core = 45 cm, internal diameter of the stator core = 122 cm, number of stator slots = 144, Number of conductors per slot = 10. For the above stator data design a wound rotor for the motor.

Soln: (i) Diameter of the rotor

Length of the air gap
$$lg = 0.2 + 2 \sqrt{DL} \text{ mm}$$

= $0.2 + 2 \sqrt{1.22} \times 0.45 \text{ mm}$
= 1.68 mm
Outer diameter of rotor Dr = D - 2 lg
= $1.22 - 2 \times 1.68 \times 10^{-3}$
= 1.217 m

(ii) Number of rotor slots: Considering all the factors for selection of number of rotor slots, and selecting fractional slot winding, assuming number of rotor slots per pole per phase as $3\frac{1}{2}$

```
Total number of rotor slots = 3.5 \times 12 \times 3 = 126

Rotor slot pitch = \pi D_r / S_r

= \pi \times 1.217 / 126

= 0.0303 \text{ m} (quite satisfactory)
```

(iii) Number of rotor turns: For this motor the voltage between slip rings must be less than 1000 volts. Assume the voltage between slip rings as 600 volts.

Assuming star connection for stator winding $E_s = 6600/\sqrt{3} = 3810$ volts, Assuming $K_{ws} = K_{wr} = 1$

Rotor winding will always be star connected

Total number of stator conductors = 144×10

Total number of stator turns per phase = $144 \times 10 / (3 \times 2) = 240$

Rotor turns per phase Tr = (Er/Es) x (Kws/Kwr) Ts
=
$$600/\sqrt{3}$$
 x 1 x 240 / 3810
= 22 turns

Rotor conductors per phase = 44,

Number of slots per phase = 126/3 = 42,

Therefore number of conductors per slot = 1.

Final rotor turns/phase = number of conductors per phase / 2 = 42/2 = 21

(iv) Rotor current

As the motor is of 850 kW, efficiency will be high, assuming an efficiency of 92% and $\cos\Phi = 0.91$

Input to the motor = 850/0.92 = 924 kW,

Full load stator current per phase $I_s = 924 \times 10^3 / (3 \times 3180 \times 0.91)$

$$= 88.8 \text{ amps}$$

Equivalent rotor current $I_r = 0.85 I_s = 0.85 \times 88.8 = 75.5$ amps

$$Ir = (K_{ws} \times S_s \times Z'_s) \times I'_r / (K_{wr} \times S_r \times Z'_r);$$

= (144 x 10 x 75.5) / 126 x 1
= 863 amps

(v) Size of rotor conductors

Assuming a current density of 5 Amp/ mm² for the rotor conductors,

Cross sectional area of the rotor conductor = $863/5 = 172.6 \text{ mm}^2$

Size of the rotor conductors is too large and this conductor can not be used as it is and hence has to be stranded. Stranding the conductors into 4 rectangular strips of each area 43.1 mm², in parallel,

Standard size of the rectangular strip selected = 11 mm x 4 mm,

Thus sectional area of the rectangular conductor $43.1 \text{ x } 4 = 172.4 \text{ mm}^2$

Size of the rectangular conductor with insulation = 11.5 mm x 4.5 mm

(vi) Size of the rotor slot

Four strips of the rectangular conductor are arranged as 2 strips widthwise and 2 strips depthwise, with this arrangement the size of the slot can be estimated as follows

(a) width of the slot

Space occupied by the conductor	2 x4.5	9.0 mm
Slot liner	2 x 1.5	3.0 mm
Clearance		1.0 mm
Total width of the slot		13.0 mm
(b) Depth of the slot		
Space occupied by the conductor	2 x11.5	23.0 mm
Slot liner	3 x 1.5	4.5 mm
Wedge		3.5 mm
Lip		1.0 mm
Clearance		1.0 mm
Total depth of the slot		34.0 mm

Thus size of the rotor slot = 13 mm x 34 mm

(vi) Resistance and copper losses

Length of the mean Turn
$$l_{\rm mt}$$
 = 2L + 2.3 $\tau_{\rm p}$ + 0.08 m
 $l_{\rm mt}$ = 2x 0.45 + 2.3 (π x 1.22 / 12) + 0.08 m
= 1.72 m

Resistance of rotor winding is given by Rr =
$$(0.021 \text{ x } l_{\text{mt}} \text{ x T}_{\text{r}}) / A_{\text{r}}$$

= $(0.021 \text{ x } 1.72 \text{ x } 21) / 172.4$
= 0.0044 ohm

Total copper loss =
$$3 \text{ Ir}^2 R_r$$
 Watts
= $3 \times 863^2 \times 0.0044$
= 9831 watts

Performance Evaluation:

Based on the design data of the stator and rotor of an induction motor, performance of the machine has to be evaluated. The parameters for performance evaluation are iron losses, no load current, no load power factor, leakage reactance etc. Based on the values of these parameters design values of stator and rotor can be justified.

Iron losses: Iron losses are occurring in all the iron parts due to the varying magnetic field of the machine. Iron loss has two components, hysteresis and eddy current losses occurring in the iron parts depend upon the frequency of the applied voltage. The frequency of the induced voltage in rotor is equal to the slip frequency which is very low and hence the iron losses occurring in the rotor is negligibly small. Hence the iron losses occurring in the induction motor is mainly due to the losses in the stator alone. Iron losses occurring in the stator can be computed as given below.

(a) Losses in stator teeth:

The following steps explain the calculation of iron loss in the stator teeth

- (i) Calculate the area of cross section of stator tooth based on the width of the tooth at $1/3^{rd}$ height and iron length of the core as $A'_{ts} = b'_{ts} \times l_i \text{ m}^2$
- (ii) Calculate the volume all the teeth in stator $V_{ts} = A'_{ts} \times h_{ts} \times S_s \text{ m}^3$
- (iii) Compute the weight of all the teeth based on volume and density of the material as $W_{ts} = V_{ts} x$ density. (density of the material can be found in DDH) (7.8 x 10^{-3} kg/m³)
- (iv) Corresponding to the operating flux density in the stator teeth of the machine iron loss per kg of the material can be found by referring to the graph on pp179 of DDH
- (v) Total iron losses in teeth= Iron loss /kg x weight of all teeth W_{ts} ie result of (iii) x (iv)

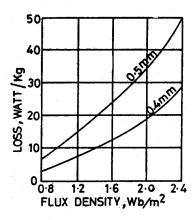


Fig. 18. Flux density vs iron loss

(c) Losses in stator core

Similar to the above calculation of iron loss in teeth, iron loss in stator core can be estimated.

(i) Calculate the area of cross section of the core as $A_{cs} = d_{cs} \times l_i \text{ m}^2$

- (ii) Calculate the mean diameter of the stator core below the slots as D_{mcs} = D + 2 h_{ts} + d_{cs} m
- (iii) Compute the volume of stator core as $V_{cs} = A_{cs} \times \pi D_{mcs} \text{ m}^3$
- (iv) Calculate the weight of the stator core as $W_{cs} = V_{cs} x$ density
- (v) Corresponding to the operating flux density in the stator core of the machine iron loss per kg of the material can be found by referring to the graph on pp 179 of DDH.
- (vi) Total iron losses in core = Iron loss /kg x weight of core W_{cs} ie result of (iv) x (v)

Total iron losses in induction motor = Iron loss in stator core + iron losses in stator teeth.

In addition friction and windage loss can be taken into account by assuming it as 1-2 % of the out put of the motor.

Hence total no load losses = Total iron losses + Friction and windage loss.

No load current: As seen from Fig 14, the no load current of an induction motor has two components magnetizing component, I_m and iron loss component, I_w . Phase relation between these currents is shown in Fig. 14.

Thus the no load current $I_0 = \sqrt{(I_m)^2 + (I_w)^2}$ amps

Magnetising current: Magnetising current of an induction motor is responsible for producing the required amount of flux in the different parts of the machine. Hence this current can be calculated from all the magnetic circuit of the machine. The ampere turns for all the magnetic circuit such as stator core, stator teeth, air gap, rotor core and rotor teeth gives the total ampere turns required for the magnetic circuit. The details of the magnetic circuit calculations are studied in magnetic circuit calculations. Based on the total ampere turns of the magnetic circuit the magnetizing current can be calculated as

Magnetising current $I_m = p AT_{30} / (1.17 k_w T_{ph})$

where p – no of pairs of poles, AT_{30} – Total ampere turns of the magnetic circuit at 30^0 from the centre of the pole, T_{ph} – Number of stator turns per phase.

Iron loss component of current: This component of current is responsible for supplying the iron losses in the magnetic circuit. Hence this component can be calculated from no load losses and applied voltage.

Iron loss component of current I_w = Total no load losses / (3 x phase voltage)

No load Power Factor: No load power factor of an induction motor is very poor. As the load on the machine increases the power factor improves. No load power factor can be calculated knowing the components of no load current.

No load power factor $\cos \Phi_0 = I_w / I_0$

Ex. While designing the stator of a 3 phase 10 kW, 400 volts, 50 Hz, 4 pole, wound rotor induction motor, following data are obtained.

Internal diameter of stator = 0.19 m Gross length = 0.125 m Number of stator slots = 36 Number of conductors/slot = 38

Dimension of stator slot = 1.1 cm x 3.5 cm

Depth of the stator core = 3 cm Number of rotor slots = 30

Dimension of the rotor slot = 0.7 cm x 3.0 cm

Depth of rotor core = 3.0 cmCarter's coefficient for the air gap = 1.33

Based on the above data, calculate the following performance data for this motor.

- (i) Flux per pole (ii) Iron losses (iii) Active component of no load current (iv) No load current
- (v) No load power factor

Soln. (i) Flux per pole

Total number of stator conductors = $36 \times 38 = 1368$

Stator turns per phase $T_{ph} = 1368 / 6 = 228$

Assuming star delta connection for the motor $V_{ph} = 400$ volts

Assuming $E_{ph} = V_{ph} = 400$ volts, winding factor = 0.955

Air gap flux per pole
$$\Phi = \text{Eph/}(4.44fT_{ph} k_w)$$

= 400/(4.44 x 50 x 228 x 0.955)
= 0.00827 wb

(ii) Iron losses

Total Iron losses = Iron losses in stator teeth + Iron losses in stator core

Iron losses in stator teeth:

For the given stator length assuming one ventilating duct of width 1cm and iron space factor of 0.95,

$$L_i = (L - n_d \times w_d)k_i$$

= (0.125 -1 x 0.01)0.95
= 0.109 m

Diameter at $1/3^{rd}$ height, $D^{'} = D + 1/3 \ x \ h_{ts} \ x \ 2 = 0.19 + 1/3 \ x \ 0.035 \ x \ 2 = 0.213 \ m$

Slot pitch at $1/3^{rd}$ height = $\tau_s = \pi \times D'/S_s = \pi \times 0.213/36 = 0.0186$ m

Tooth width at this section = $b_t = \tau_s - b_s = 0.0186 - 0.011 = 0.0076$ m

Area of the stator tooth per pole $A_t = b_t \times l_i \times$

$$= b_t \times l_i \times S_s / p = 0.0076 \times 0.109 \times 36/4$$

$$= 0.00746 \text{ m}^2$$

Mean flux density in stator teeth $B'_t = \Phi / A'_t = 0.00827 / 0.00746 = 1.109$ Tesla

Maximum flux density in stator tooth = $1.5 \times 1.109 = 1.66 \text{ Tesla}$

Volume of all the stator teeth = $b_t \times l_i \times l$

 $= 0.0076 \times 0.109 \times 0.035 \times 36$

 $= 0.001044 \text{ m}^3$

Weight of all the teeth = volume x density

Assuming a density of 7.8 x 10³ kg/ m³

Weight of all the teeth = $0.001044 \times 7.8 \times 10^3 = 8.14 \text{ kg}$

Total iron losses in the stator teeth = Total weight $x \cdot loss/kg$

Iron loss in the material at a flux density of 1.66 Tesla from graph PP-22 of DDH loss/kg = 23 w/kg

Total iron losses in the stator teeth = $23 \times 8.14 = 187.22$ watts

Iron losses in stator core : Sectional area of the stator core = $l_i \times d_c = 0.109 \times 0.03$ = 0.00327 m²

Mean diameter of the stator core below the slots = $0.19 + 2 \times 0.035 + 0.03 = 0.29 \text{ m}$

Volume of the stator core = π x D x Acs = π x 0.29 x 0.00327 = 0.002979 m³

Weight of the stator core = $0.002979 \times 7.8 \times 10^3 = 23.23 \text{ kg}$

Flux density in stator core = Φ_c / Acs = 0.00827/(2 x 0.00327) = 1.264 Tesla

At this flux density iron loss/kg = 17 watts/kg

Iron losses in the stator core = $17 \times 23.23 = 394.91$ watts

Total iron losses in the stator = 187.22 + 394.91 = 582.13 watts

(iii) Active component of no load current

Assuming the friction and windage losses as 1% of output Friction and windage loss = 100 w Total no load losses = 582.13 + 100 = 682.13 watts

Active component of no load current = Iron loss component of current

 I_w = Total no load losses / (3 x phase voltage) = 682.13/(3 x 400) = 0.568 amps

- (iv) Magnetising current: In order to calculate the magnetizing current ampere turns required for the various parts of the magnetic circuits are to be calculated.
 - (a) Ampere turns for the stator core:

Pole pitch at he mean diameter of the stator core = π x D/ P = π x 0.29/ 4 = 0.23 m Length of the flux path in stator core = 1/3 x 0.23 = 0.077 m

Ampere turns per meter at a flux density of 1.264 Tesla from graph (PP-22 of DDH) 400 AT

Hence total ampere turns required for the stator core = $400 \times 0.077 = 31$

(b) Ampere turns for the stator teeth:

Length of the flux path in stator teeth = 0.035m

Flux density in stator teeth at 30° from the pole centre = 1.36 B_t

$$= 1.36 \times 1.109 = 1.508$$
 Tesla

Ampere turns per meter at a flux density of 1.508 Tesla (from graph PP-22 of DDH) is 1000 AT

Hence total ampere turns for the stator teeth = $1000 \times 0.035 = 35$

(c) Ampere turns for the air gap:

Length of the air gap = $0.2 + 2\sqrt{DL} = 0.2 + 2\sqrt{0.19} \times 0.125 = 0.51$ mm

Average flux density in the air gap = Φ / (π x DL/P) = 0.4696 Tesla

Carter's coefficient for the air gap = 1.33

Air gap flux density at 30° from the centre of the pole B_g = 1.36 x Bav

 $= 1.36 \times 0.4696$

= 0.6387 Tesla

Hence Ampere turns for the air gap = $796000B_gk_gl_g$

$$AT_g = 796000 \times 0.687 \times 1.33 \times 0.51 \times 10^{-3}$$

= 371 AT

(d) Ampere turns for the rotor Teeth:

Diameter of the rotor = D $-2l_g = 0.19 - 2 \times 0.00051 = 0.189 \text{ m}$

Diameter at $1/3^{rd}$ height form the narrow end of the teeth $D_r = D - 2 \times 2/3h_{rs}$ = $0.189 - 4/3 \times 0.03$

$$= 0.189 - 4/3 \times 0.03$$

= 0.149 m

Slot pitch at $1/3^{rd}$ height = $\tau_r = \pi \times D_r / S_r = \pi \times 0.149 / 30 = 0.0156$ m

Tooth width at this section = $b_{tr}^{'} = \tau_r^{'} - b_r = 0.0156 - 0.007 = 0.0086 \text{ m}$

Area of the stator tooth per pole $A_{tr} = b_{tr} \times l_i \times n$ number of teeth per pole

$$= 0.0086 \times 0.107 \times 30/4 = 0.0069 \text{ m}^2$$

Flux density in rotor teeth at 30° from pole centre = 1.36 x 0.00827/0.0069 = 1.63 Tesla

Ampere turns/m at this flux density, from graph (PP-22 of DDH) = 2800

Length of flux path in rotor teeth = 0.03 m

Ampere turns for the rotor teeth $2800 \times 0.03 = 84$

(e) Ampere turns for the rotor core

Depth of the rotor core $d_{cr} = 3$ cm

Area of the rotor core $A_{cr} = 0.03 \times 0.107 = 0.00321 \text{ m}^2$

Flux in the rotor = $\frac{1}{2}$ x 0.00827 = 0.004135 wb

Flux density in the rotor core = 0.004135/0.00321 = 1.29 Tesla

Ampere turns/m at this flux density, from graph (PP-22 of DDH) = 380

Mean diameter of the rotor core = $D_r - 2 \times hr_s - d_{cr} = 0.189 - 2 \times 0.03 - 0.03 = 0.099 \text{ m}$

Pole pitch at this section = π x 0.099 /4 = 0.078 m

Length of the flux path in rotor core = $1/3 \times 0.078 = 0.026 \text{ m}$

Total ampere turns for the rotor core = $380 \times 0.026 = 10$

Total Ampere turns for the magnetic circuit = 31 + 35 + 371 + 84 + 10 = 531 AT

Magnetising current
$$I_m = p(AT_{30}) / (1.17 \text{ x } K_w \text{ x } T_{ph})$$

= 2 x 531 /(1.17 x 0.955 x 228)
= 4.2 amps

(v) No load current

No load current per phase $I_o = \sqrt{(I_w^2 + I_m^2)}$ = $\sqrt{(0.56^2 + 4.2^2)}$ = 4.24 amps

(vi) No load power factor $\cos \Phi_0 = I_w/I_0 = 0.56 / 4.24 = 0.132$

References

- 1. A Course in Electrical Machine Design A. K. Sawhney
- 2. Design of Electrical Machines V. N. Mittle
- 3. Performance and Design of A C Machines M G Say
- 4. Design and Testing of Electrical Machines M. V. Deshapande
- 5. Electrical Machine Design Data Book Shanmugsundaram and Palani
- 6. www.google.com and related websites
- 7. www.phasemotorparts.com
- 8. www.wikipedia.org
- 9. Krishna Vasudevan et. al. Electrical Machines II, Indian Institute of Technology, Madras