

## Foundations of Robotics (ROB-GY 6003)

### Homework Assignment | Chapter 3

**Homework Problems:** 3.1, 3.4 (regard  $\{S\}$  as  $\{0\}$ , and  $\{T\}$  as  $\{3\}$ ), 3.8, 3.12, 3.16, 3.17

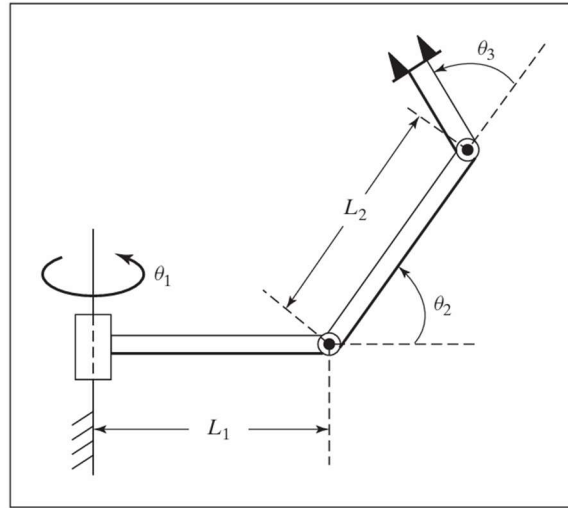


FIGURE 3.29: The 3R nonplanar arm (Exercise 3.3).

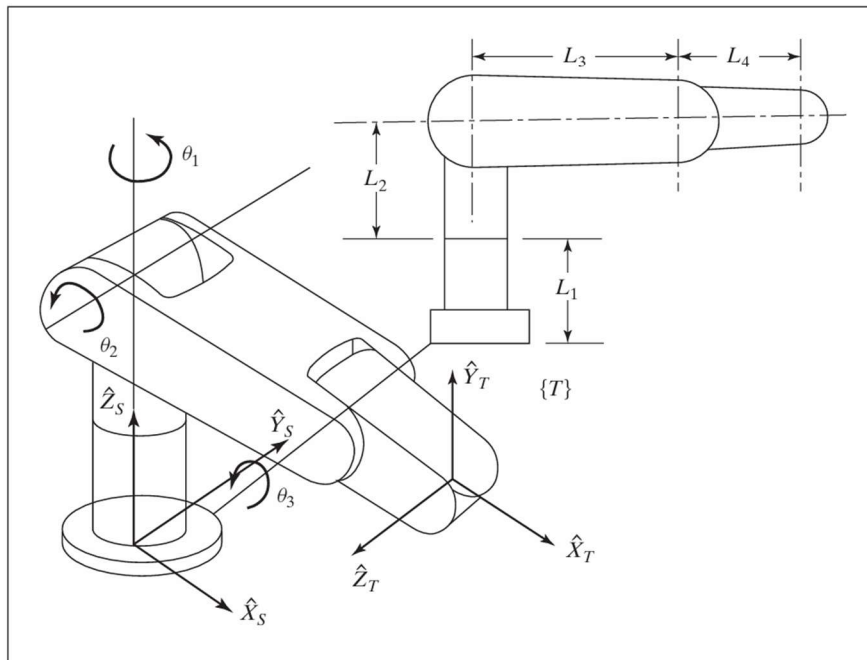
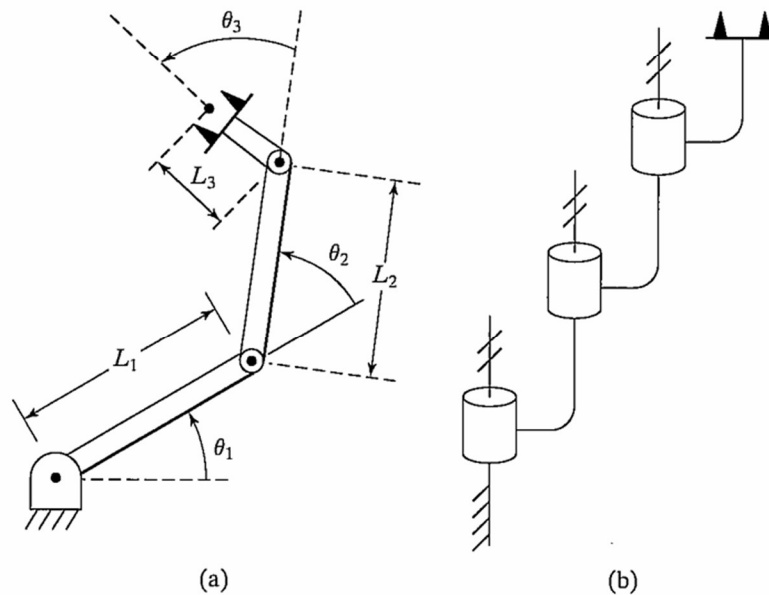


FIGURE 3.30: Two views of a 3R manipulator (Exercise 3.4).

### EXAMPLE 3.3

Figure 3.6(a) shows a three-link planar arm. Because all three joints are revolute, this manipulator is sometimes called an **RRR** (or **3R**) **mechanism**. Fig. 3.6(b) is a schematic representation of the same manipulator. Note the double hash marks

#### 70 Chapter 3 Manipulator kinematics



**3.1** [15] Compute the kinematics of the planar arm from Example 3.3.

**3.4** [22] The arm with three degrees of freedom shown in Fig. 3.30 has joints 1 and 2 perpendicular, and joints 2 and 3 parallel. As pictured, all joints are at their zero location. Note that the positive sense of the joint angle is indicated. Assign link frames  $\{0\}$  through  $\{3\}$  for this arm—that is, sketch the arm, showing the attachment of the frames. Then derive the transformation matrices  ${}^0_1T$ ,  ${}^1_2T$ , and  ${}^2_3T$ .

**3.8** [13] In Fig. 3.31, the location of the tool,  ${}^W_T T$ , is not accurately known. Using force control, the robot feels around with the tool tip until it inserts it into the

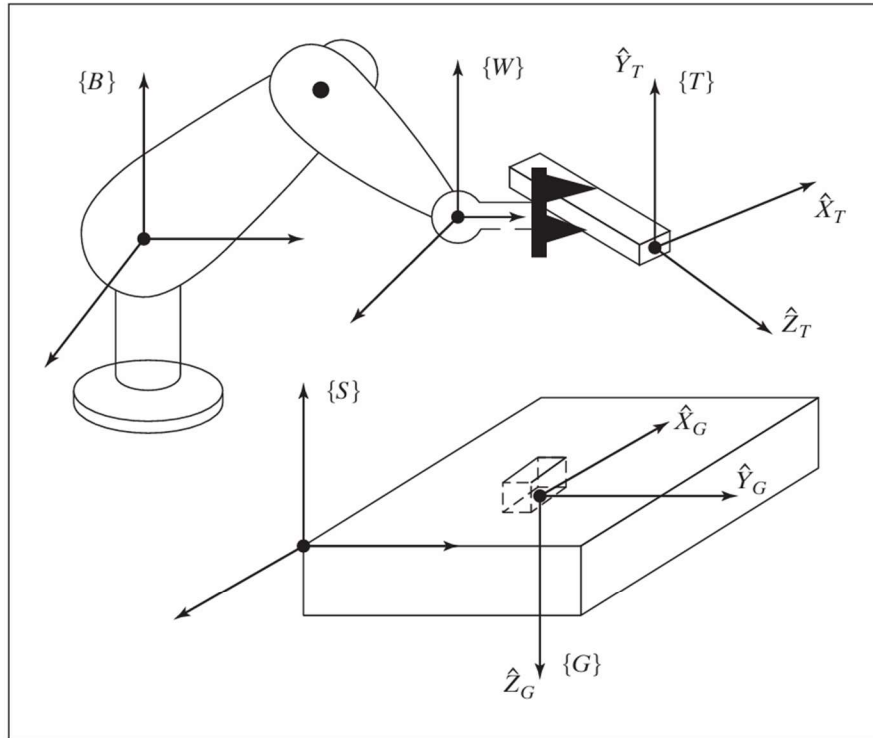


FIGURE 3.31: Determination of the tool frame (Exercise 3.8).

## 00 Chapter 3 Manipulator Kinematics

socket (or Goal) at location  ${}^S_G T$ . Once in this “calibration” configuration (in which  $\{G\}$  and  $\{T\}$  are coincident), the position of the robot,  ${}^B_W T$ , is figured out by reading the joint angle sensors and computing the kinematics. Assuming  ${}^B_S T$  and  ${}^S_G T$  are known, give the transform equation to compute the unknown tool frame,  ${}^W_T T$ .

**3.12** [08] Can an arbitrary rigid-body transformation always be expressed with four parameters  $(a, \alpha, d, \theta)$  in the form of equation (3.6)?

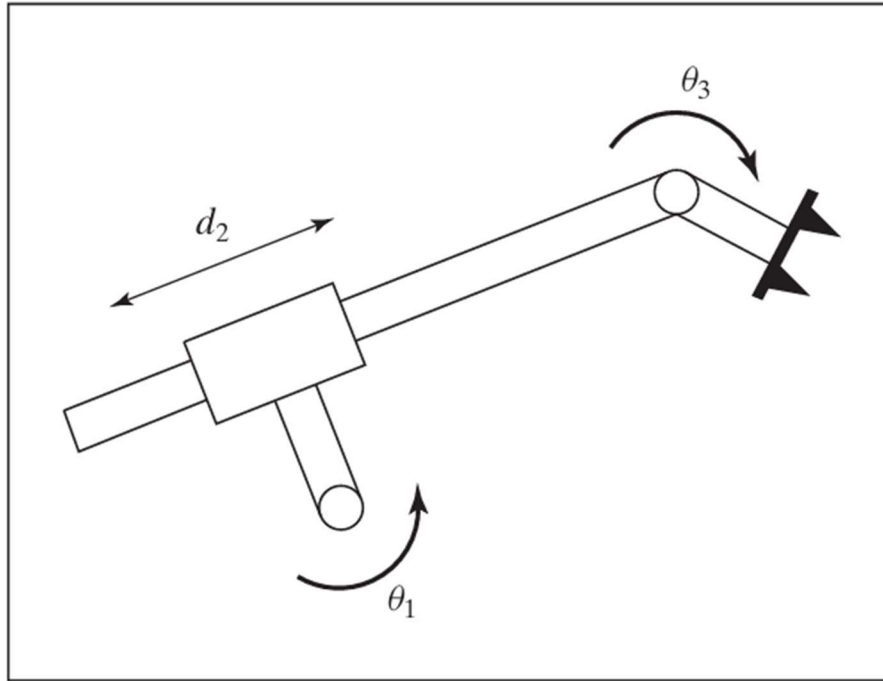


FIGURE 3.36: *RPR* planar robot (Exercise 3.16).

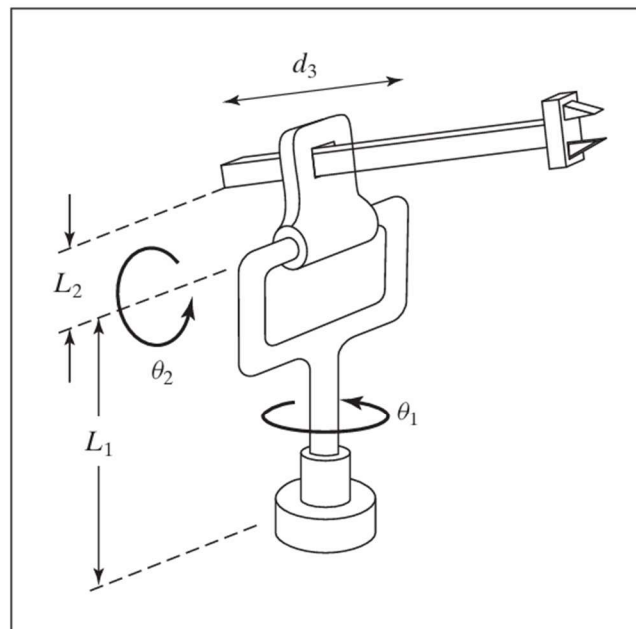


FIGURE 3.37: Three-link *RRP* manipulator (Exercise 3.17).

- 3.16** [15] Assign link frames to the  $RPR$  planar robot shown in Fig. 3.36, and give the linkage parameters.
- 3.17** [15] Show the attachment of link frames on the three-link robot shown in Fig. 3.37.