

MCE4101

Robotic Engineering

Assignment 5 SOLUTION
Due: 27 Sept 2021

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Assignment 5: Q1

Q1. With RRR with 3 DOF wrist.

Given DH table and Transformation matrices. Find 2 possible posture solutions for end point location P(2.75,4.763,-2.33).

Given

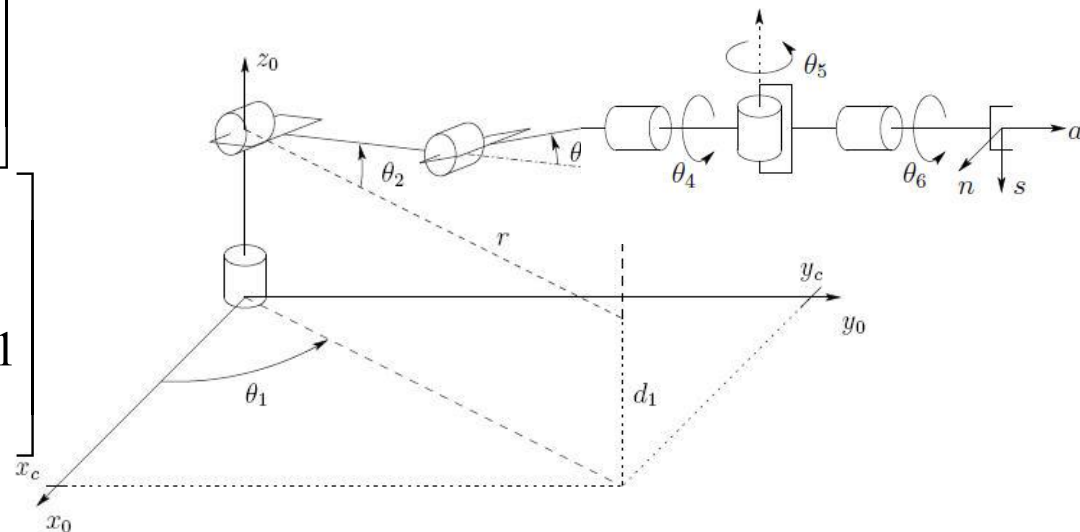
$$a_2 = 3$$

$$a_3 = 5$$

$d_1 = 2$ (Link1 offset from base)

$d_6 = 0$ (Wrist offset)

$$T_3^0 = \begin{bmatrix} 0.25 & 0.433 & 0.866 & 2.75 \\ 0.433 & 0.75 & -0.5 & 4.76 \\ -0.866 & 0.5 & 0 & -2.3301 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$T_6^0 = \begin{bmatrix} 0.397 & 0.433 & 0.8095 & 2.75 \\ 0.34 & 0.75 & -0.568 & 4.76 \\ -0.853 & 0.5 & 0.1504 & -2.3301 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$





Assignment 5 : Q1

RRR

Link	a_i	α_i	d_i	θ_i
1	0	90	d_1	θ_1^*
2	a_2	0	0	θ_2^*
3	a_3	0	0	θ_3^*

3 DOF Wrist

Link	a_i	α_i	d_i	θ_i
4	0	-90	0	θ_4^*
5	0	90	0	θ_5^*
6	0	0	d_6	θ_6^*

$$R_3^0 = A_1 A_2 A_3 = \begin{bmatrix} c_1 c_{23} & -c_1 s_{23} & s_1 \\ s_1 c_{23} & -s_1 s_{23} & -c_1 \\ s_{23} & c_{23} & 0 \end{bmatrix}$$

$$R_6^3 = A_4 A_5 A_6 = \begin{bmatrix} c_4 c_5 c_6 - s_4 s_6 & -c_4 c_5 s_6 - s_4 c_6 & c_4 s_5 \\ s_4 c_5 c_6 + c_4 s_6 & -s_4 c_5 s_6 + c_4 c_6 & s_4 s_5 \\ -s_5 c_6 & s_5 s_6 & c_5 \end{bmatrix}$$



Assignment 5 : Solution Q1

$$R_6^3 = R_0^3 R_6^0 = (R_3^0)^T R_6^0$$

$$R_6^0 = \begin{bmatrix} r_{11} & r_{12} & r_{13} \\ r_{21} & r_{22} & r_{23} \\ r_{31} & r_{32} & r_{33} \end{bmatrix} = \begin{bmatrix} 0.397 & 0.433 & 0.8095 \\ 0.34 & 0.75 & -0.568 \\ -0.853 & 0.5 & 0.1504 \end{bmatrix}$$

$$R_3^0 = \begin{bmatrix} 0.25 & 0.433 & 0.866 \\ 0.433 & 0.75 & -0.5 \\ -0.866 & 0.5 & 0 \end{bmatrix}$$

$$(R_3^0)^T = \begin{bmatrix} 0.25 & 0.433 & -0.866 \\ 0.433 & 0.75 & 0.5 \\ 0.866 & -0.5 & 0 \end{bmatrix}$$

$$R_6^3 = U = \begin{bmatrix} u_{11} & u_{12} & u_{13} \\ u_{21} & u_{22} & u_{23} \\ u_{31} & u_{32} & u_{33} \end{bmatrix}$$

U =

$$\begin{bmatrix} 0.9852 & 0 & -0.1738 \\ 0.0004 & 1.0000 & -0.0003 \\ 0.1738 & -0.0000 & 0.9850 \end{bmatrix}$$

$$c_5 = u_{33} = 0.985$$

$$s_5 = \pm \sqrt{1 - (0.985)^2} = 0.1726$$

$$\theta_5 = A \tan 2(0.985, \pm 0.1726)$$

$$\theta_5 = \pm 9.93^\circ$$



Assignment 5 : Solution Q1

If $\theta_5 = +9.93^\circ$ is chosen

$$\therefore s_5 > 0$$

$$+u_{13} = c_4 \text{ and } +u_{23} = s_4$$

$$\theta_4 = A \tan 2(u_{13}, u_{23})$$

$$\theta_4 = 0^\circ \quad (-180^\circ)$$

$$\therefore s_5 > 0$$

$$-u_{31} = c_6 \text{ and } +u_{32} = s_6$$

$$\theta_6 = A \tan 2(-u_{31}, u_{32})$$

$$\theta_6 = 0^\circ \quad (-180^\circ)$$

If $\theta_5 = -9.93^\circ$ is chosen

$$\therefore s_5 < 0$$

$$-u_{13} = c_4 \text{ and } -u_{23} = s_4$$

$$\theta_4 = A \tan 2(-u_{13}, -u_{23})$$

$$\theta_4 = 0^\circ$$

$$\therefore s_5 < 0$$

$$+u_{31} = c_6 \text{ and } -u_{32} = s_6$$

$$\theta_6 = A \tan 2(u_{31}, -u_{32})$$

$$\theta_6 = 0^\circ$$



Assignment 5 : Solution Q1

$$\cos \theta_3 = \frac{2.75^2 + 4.763^2 + (-2.33 - 2)^2 - 3^2 - 5^2}{2(3)(5)} := 0.5$$

$$\theta_3 = A \tan 2(D, \pm \sqrt{1 - D^2})$$

$$\theta_3 = \pm 60^\circ$$

$$\theta_2 = A \tan 2\left(\sqrt{x_c^2 + y_c^2}, z_c - d_1\right) - A \tan 2(a_2 + a_3 \cos(\theta_3), a_3 \sin(\theta_3))$$

$$\theta_3 = +60^\circ$$

$$\theta_2 = -76.43^\circ$$

$$\theta_3 = -60^\circ$$

$$\theta_2 = 0^\circ$$

$$\theta_1 = A \tan 2(x_c, y_c)$$

$$\theta_1 = +60^\circ, \theta_1 = +240^\circ$$

$$\theta_1 = +60^\circ, \theta_2 = 0^\circ, \theta_3 = -60^\circ, \theta_4 = 0^\circ, \theta_5 = -10^\circ, \theta_6 = 0^\circ$$

$$\theta_1 = +240^\circ, \theta_2 = -76^\circ, \theta_3 = +60^\circ, \theta_4 = -180^\circ, \theta_5 = +10^\circ, \theta_6 = -180^\circ$$



Assignment 5 : Q2

Q2. With RRR with 3 DOF wrist. (ikine function)

Obtain (theta1-theta6) by ikine() for Q1) with robotic toolbox in MATLAB. Attached your code and result.

Use IG as `[pi/10 -pi/150 pi/150 pi/100 -pi/100 pi/100]`



Assignment 5 : Q2 Solution

```
th1 =  
    59.9993  
    %%RRR with 3 DOF wrist  
    %%inv K Ass5 Q2  
    clear all; clc;  
th2 =  
   -3.6000e+03  
th3 =  
    5.7000e+03  
th4 =  
   -3.9900e+03  
th5 =  
   -90  
th6 =  
    1.8300e+03  
    d1 = 2; a2 =3; a3 = 5; d6 = 0;  
    A1 = link([pi/2 0 0 d1,0]);  
    A2 = link([0 a2 0 0,0]);  
    A3 = link([0 a3 0 0,0]);  
    RRR = robot({A1 A2 A3});  
    %%3 DOF wrist  
    A4 = link([-pi/2 0 0 0,0]);  
    A5 = link([pi/2 0 0 0,0]);  
    A6 = link([0 0 0 d6,0]);  
    RRR_3DOFWRIST = robot({A1 A2 A3 A4 A5 A6});  
    position = transl(2.75,4.763,-2.33);  
    IG = [pi/10 -pi/150 pi/150 pi/100 -pi/100 pi/100];  
    M = [1 1 1 1 1 1];  
    values = ikine(RRR_3DOFWRIST, position, IG, M);
```




Assignment 5 : Q3

Q3. With RRR with 3 DOF wrist.

- a). With answer (theta1-theta6) from Q1, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.
- b). With answer (theta1-theta6) from Q2, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.



Assignment 5 : Q3 Solution

```
clear all; clc;
d1 = 2; a2 = 3; a3 = 5; d6 = 0;
A1 = link([pi/2 0 0 d1,0]);
A2 = link([0 a2 0 0,0]);
A3 = link([0 a3 0 0,0]);
RRR = robot({A1 A2 A3});
%%3 DOF wrist
A4 = link([-pi/2 0 0 0,0]);
A5 = link([pi/2 0 0 0,0]);
A6 = link([0 0 0 d6,0]);
RRR_3DOFWRIST = robot({A1 A2 A3 A4 A5 A6});
position = transl(2.75,4.763,-2.33);
IG = [pi/10 -pi/150 pi/150 pi/100 -pi/100 pi/100];
M = [1 1 1 1 1 1];
values = ikine(RRR_3DOFWRIST, position, IG, M);
|
T06_a = fkine(RRR_3DOFWRIST, [pi/3, 0 -pi/3 0 (-10/180)*pi 0]);
Pend_a = T06_a*[0;0;0;1]
T06_b = fkine(RRR_3DOFWRIST, values);
Pend_b = T06_b*[0;0;0;1]
```

Pend_a =

2.7500
4.7631
-2.3301
1.0000

Pend_b =

2.7500
4.7630
-2.3300
1.0000



Assignment 5 : Q4

Q4. With RRP 1 DOF wrist (SCARA).

Given DH table and Transformation matrix. Obtain the formulas for θ_1 , θ_2 , θ_4 and d_3 with using Atan2 function. Steps must be included in your work. State possible solution values. Find 1 possible solution for end point location P(7.5,2,3.5).

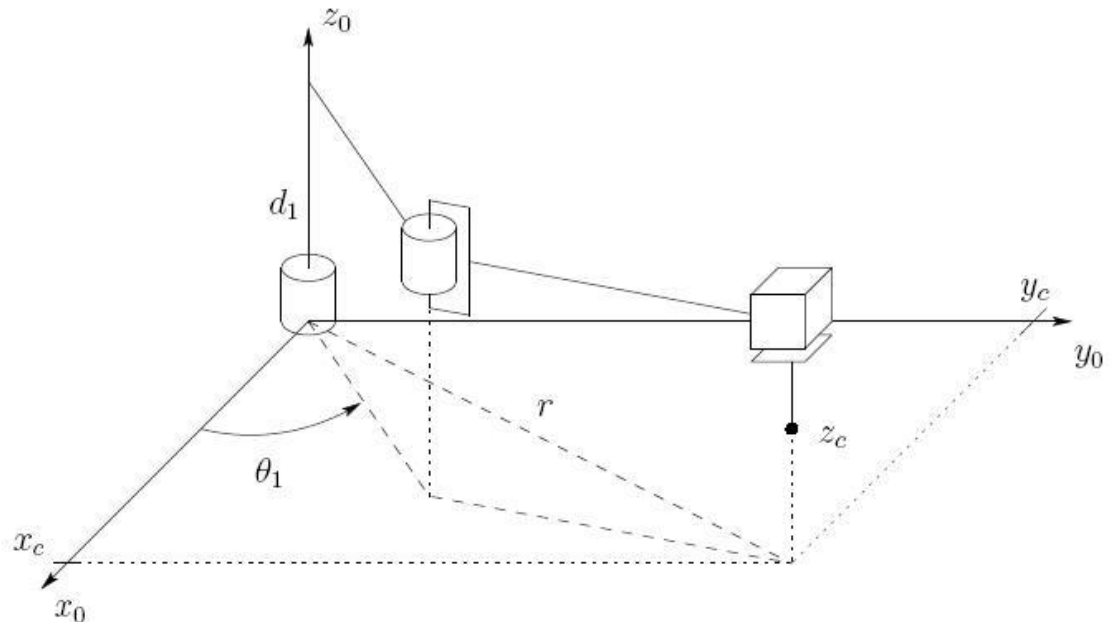
Given

$$a_1 = 3$$

$$a_2 = 5$$

$$d_1 = 5 \text{ (Link1 offset from base)}$$

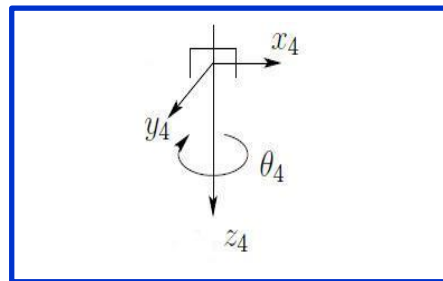
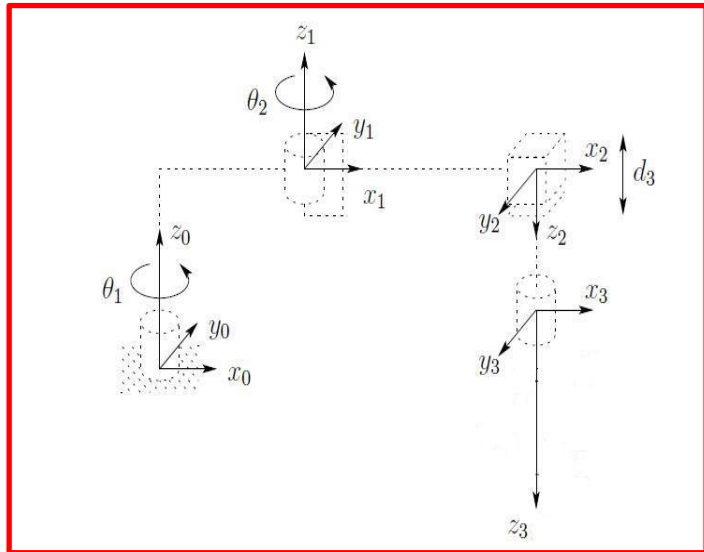
$$d_4 = 1 \text{ (Wrist offset)}$$





Assignment 5 : Q4

RRP



1 DOF Wrist Mechanism

Link	a_i	α_i	d_i	θ_i
1	a_1	0	d_1	θ_1^*
2	a_2	180	0	θ_2^*
3	0	0	d_3^*	0
4	0	0	d_4	θ_4^*

$$T_4^0 = A_1 \cdots A_4$$

$$= \begin{bmatrix} c_{12}c_4 + s_{12}s_4 & -c_{12}s_4 + s_{12}c_4 & 0 & a_1c_1 + a_2c_{12} \\ s_{12}c_4 - c_{12}s_4 & -s_{12}s_4 - c_{12}c_4 & 0 & a_1s_1 + a_2s_{12} \\ 0 & 0 & -1 & d_1 - d_3 - d_4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Assignment 5 : Solution Q4

RRP (SCARA) with 1DOF wrist. no offset.

DH. Table

	a	α	d	θ
l_1	a_1	0	d_1	θ_1^*
l_2	a_2	180	0	θ_2^*
l_3	0	0	d_3^*	0
l_4	0	0	d_4	θ_4^*

$$z_c = d_1 - d_3 - d_4$$

$$d_3 = \cancel{z_c - d_1 - d_4} \quad d_1 = z_c + d_4$$

$$\cos \theta_2 = \frac{x_c^2 + y_c^2 - a_1^2 - a_2^2}{2a_1 a_2} = D \quad \therefore \sin \theta_2 = \pm \sqrt{1 - D^2}$$

$$\theta_2 = \text{Atan2}(D, \pm \sqrt{1 - D^2})$$

$$\theta_1 = \text{Atan2}(y_c, x_c) - \text{Atan2}(a_1 + a_2 \cos \theta_2, a_2 \sin \theta_2)$$

$$R_4^3 = R_0^3 R_4^0$$

$$\therefore R_4^3 = (R_3^0)^T \cdot R_4^0 = u$$

$$R_4^3 = A_4 = \begin{bmatrix} c_4 & -s_4 & 0 \\ s_4 & c_4 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R_4^0 = \begin{bmatrix} c_{12}c_4 + s_{12}s_4 & -a_2s_4 + s_{12}c_4 & 0 \\ s_{12}c_4 - c_{12}s_4 & -s_{12}s_4 - c_{12}c_4 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$(R_3^0)^T = \begin{bmatrix} c_1c_2 - s_1s_2 & c_1s_2 + c_2s_1 & 0 \\ c_1s_2 + c_2s_1 & s_1s_2 - c_1c_2 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} c_2 & s_2 & 0 \\ s_2 & -c_2 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$\therefore u = \begin{bmatrix} c_4 & s_4 & 0 \\ s_4 & c_4 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$



Assignment 5 : Solution Q4

$$u = \begin{bmatrix} C_{12}(C_{12-4}) + S_{12}(S_{12-4}) & C_{12}(S_{12-4}) + S_{12}(-C_{12-4}) & 0 \\ S_{12}(C_{12-4}) + (-C_{12})(S_{12-4}) & S_{12}(S_{12-4}) + (-C_{12})(-C_{12-4}) & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} C_{12}(C_{12-4}) + S_{12}(S_{12-4}) & C_{12}(S_{12-4}) - S_{12}(C_{12-4}) & 0 \\ S_{12}(C_{12-4}) - C_{12}(S_{12-4}) & S_{12}(S_{12-4}) + C_{12}(C_{12-4}) & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} C_{12} - (12-4) & S_{12} - 12 & 0 \\ S_{12} - (12-4) & C_{12} - (12-4) & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} C_4 & S_4 & 0 \\ S_4 & C_4 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

θ_4 can be any value.

$$P(7.5, 2, 3.5)$$

$$a_1 = 3$$

$$b_3 = 5$$

$$d_1 = 5$$

$$d_4 = 1$$

$$\therefore d_3 = d_1 - z_c - d_4$$

$$= 5 - 3.5 - 1$$

$$d_3 = \underline{\underline{0.5}}$$

$$\theta_2 = \text{Atan2}(D, \pm \sqrt{1-D^2})$$

$$D = \frac{7.5^2 + 2^2 - 3^2 - 5^2}{2(3)(5)} = 0.875$$

$$\therefore \pm \sqrt{1-D^2} = \pm 0.484$$

$$\theta_2 = \text{Atan2}(0.875, \pm 0.484)$$

$$\theta_2 = \underline{\underline{28.95^\circ}}, \quad -28.95^\circ$$

$$\theta_1 = \text{Atan2}(7.5, 2) - \text{Atan2}(7.375, \pm 2.12)$$

$$= 14.93^\circ - (\pm 18.167^\circ)$$

$$\theta_1 = -3.237^\circ, \quad \theta_2 = \underline{\underline{+18.167^\circ - 28.95^\circ}}$$

$$\theta_1 = 33.097^\circ, \quad \theta_2 = \underline{\underline{-18.167^\circ - 28.95^\circ}}$$



Assignment 5 : Q5

Q5. With RRP 1 DOF wrist (SCARA).

Given DH table and Transformation matrix. Find 1 possible posture solution for end point location $P(7.5, 2, 3.5)$ using Inverse Kinematic function `ikine()` from **MATLAB**. Plot this location.

Given

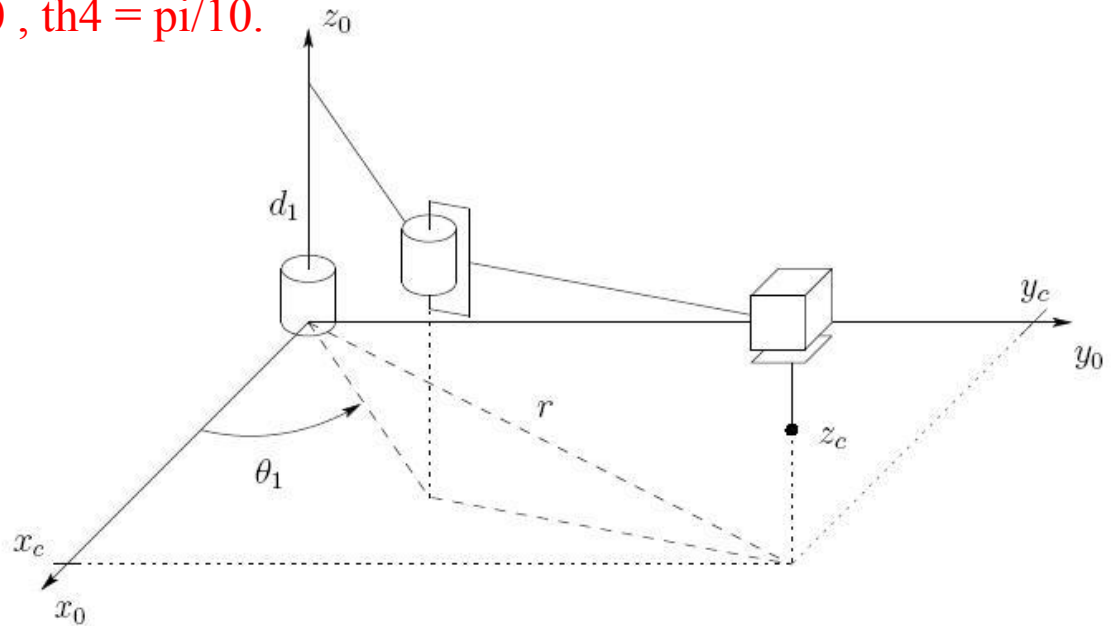
$$a_1 = 3$$

$$a_2 = 5$$

$$d_1 = 5 \text{ (Link1 offset from base)}$$

$$d_4 = 1 \text{ (Wrist offset)}$$

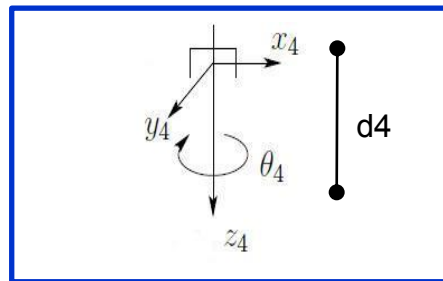
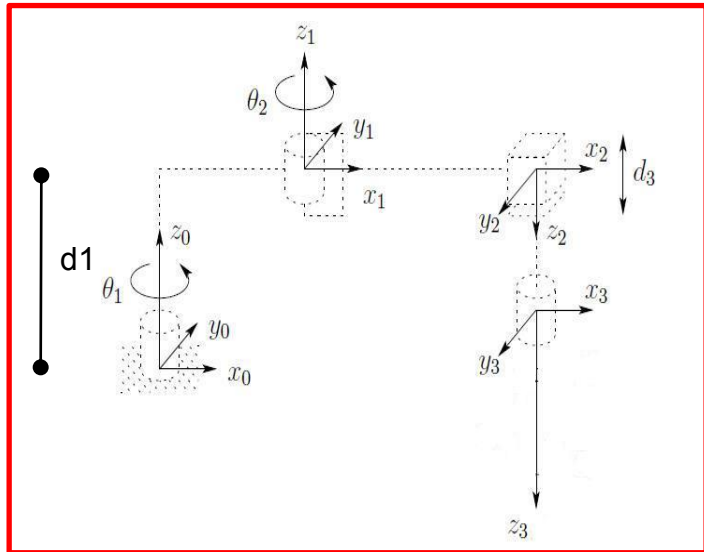
$$\text{Use IG : } \theta_1 = \pi/10, \theta_2 = 0, \theta_3 = 0, \theta_4 = \pi/10.$$





Assignment 5 : Q5

RRP



1 DOF Wrist Mechanism

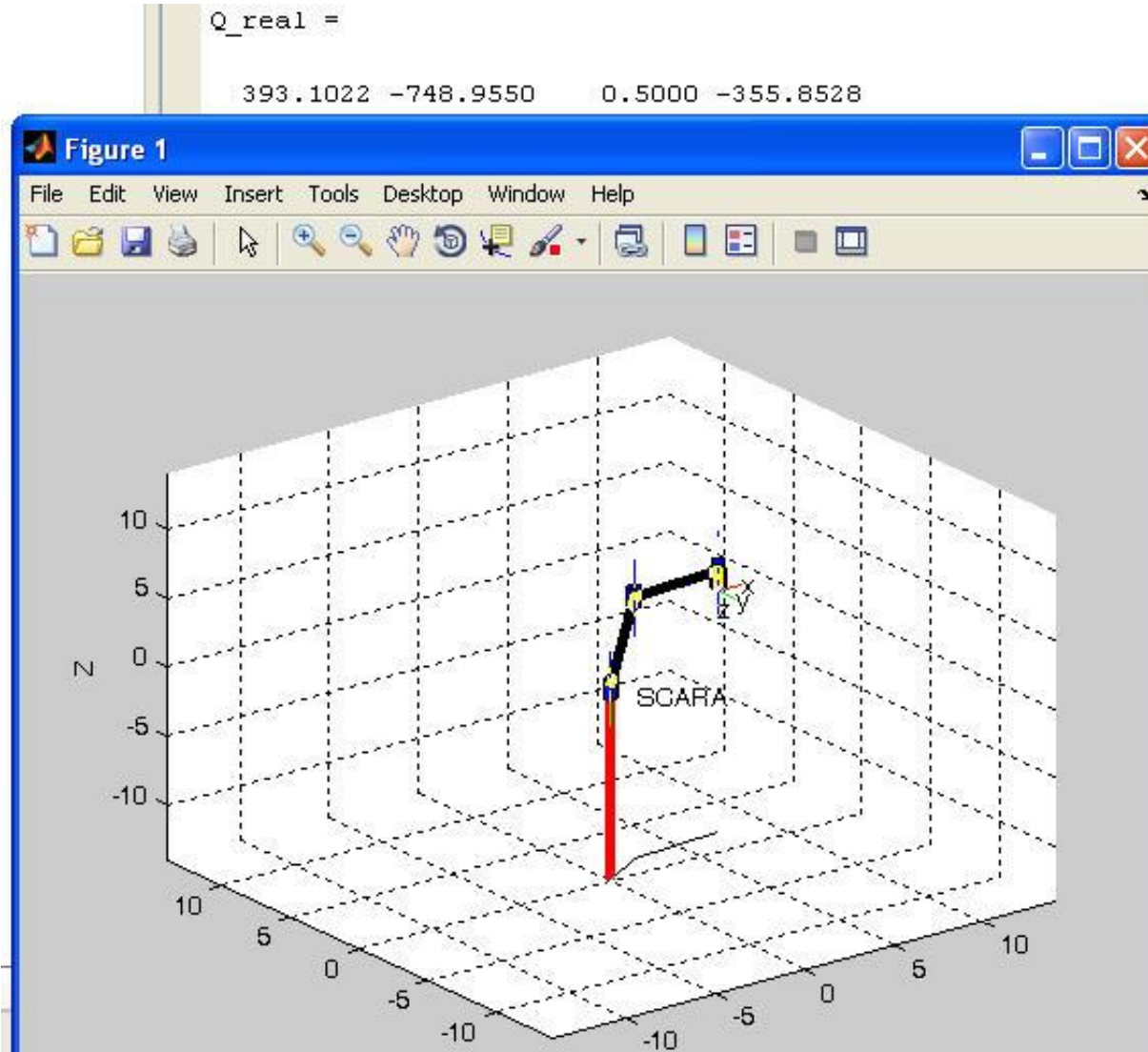
Link	a_i	α_i	d_i	θ_i
1	a_1	0	d_1	θ^*
2	a_2	180	0	θ^*
3	0	0	d^*	0
4	0	0	d_4	θ^*

$$T_4^0 = A_1 \cdots A_4$$

$$= \begin{bmatrix} c_{12}c_4 + s_{12}s_4 & -c_{12}s_4 + s_{12}c_4 & 0 & a_1c_1 + a_2c_{12} \\ s_{12}c_4 - c_{12}s_4 & -s_{12}s_4 - c_{12}c_4 & 0 & a_1s_1 + a_2s_{12} \\ 0 & 0 & -1 & d_1 - d_3 - d_4 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



Assignment 5 : Q5 (1 possible posture answer)





Assignment 5 : Solution Q5

```
%SCARA with 1 DOF Wrist
%alpha a theta D
clear all;
clc;
a1 = 3;
a2 = 5;
d4 = 1;
th1 = 0;
th2 = 0;
th4 = 0;
d3 = 0; %when Pz is 3.5, d3 must be 0.5

%RRP
L1 = Link([0,a1,th1,5], 'standard');
L2 = Link([pi,a2,th2,0], 'standard');
L3 = Link([0,0,0,d3,1], 'standard'); %%To have prismatic joint must set to 1
%1 DOF Wrist
L4 = Link([0,0,th4,d4], 'standard');

RRP = robot({L1 L2 L3 L4});
pos = transl(7.5,2,3.5);
%INVK for RRP with 1 DOF
Q = ikine(RRP, pos, [pi/10 0 0 pi/10], [1 1 1 1 0 0]);
Q_d3 = Q(1,3); %%d3
Q_deg(1,1) = (Q(1,1)/pi)*180;
Q_deg(1,2) = (Q(1,2)/pi)*180;
Q_deg(1,4) = (Q(1,4)/pi)*180;

Q_real = [Q_deg(1,1) Q_deg(1,2) Q_d3 Q_deg(1,4)]

RRP.name = 'SCARA';
plot(RRP, [Q]);
hold on;
hold off;
```



Assignment 5 : Q6

Q6. With RRP 1 DOF wrist (SCARA).

- a). With answer (θ_1 , θ_2 , θ_4 and d_3) from Q4, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.
- b). With answer (θ_1 , θ_2 , θ_4 and d_3) from Q5, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.



Assignment 5 : Q6 Solution

```
a1 = 3;
a2 = 5;
d1 = 5;
d4 = 1;

syms th1 th2 th4 d3
%RRP
L1 = link([0,a1,th1,d1],'standard');
L2 = link([pi,a2,th2,0],'standard');
L3 = link([0,0,0,d3,1],'standard'); %%To have prismatic joint must set to 1
%1 DOF Writs
L4 = link([0,0,th4,d4],'standard');

RRP = robot({L1 L2 L3 L4});
%FK for RRP with 1 DOF
qzRRP = [(-3.237/180)*pi (28.95/180)*pi 0.5 0];
TRRP = fkine(RRP,qzRRP);
LOCATION = double(TRRP*[0;0;0;1])
```



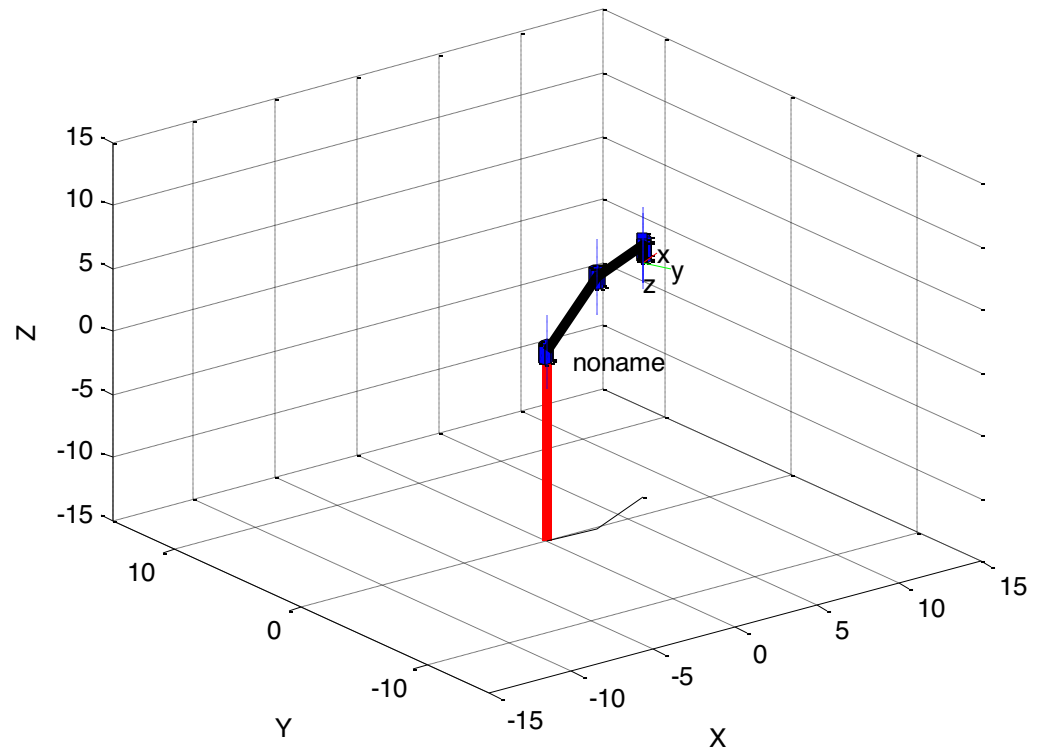
Assignment 5 : Q6 Solution

- a) With answer (theta1, theta2 and d3) from Q4, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure.

```
qzRRP = [(-3.237/180)*pi (28.95/180)*pi 0.5 0];
```

```
LOCATION =
```

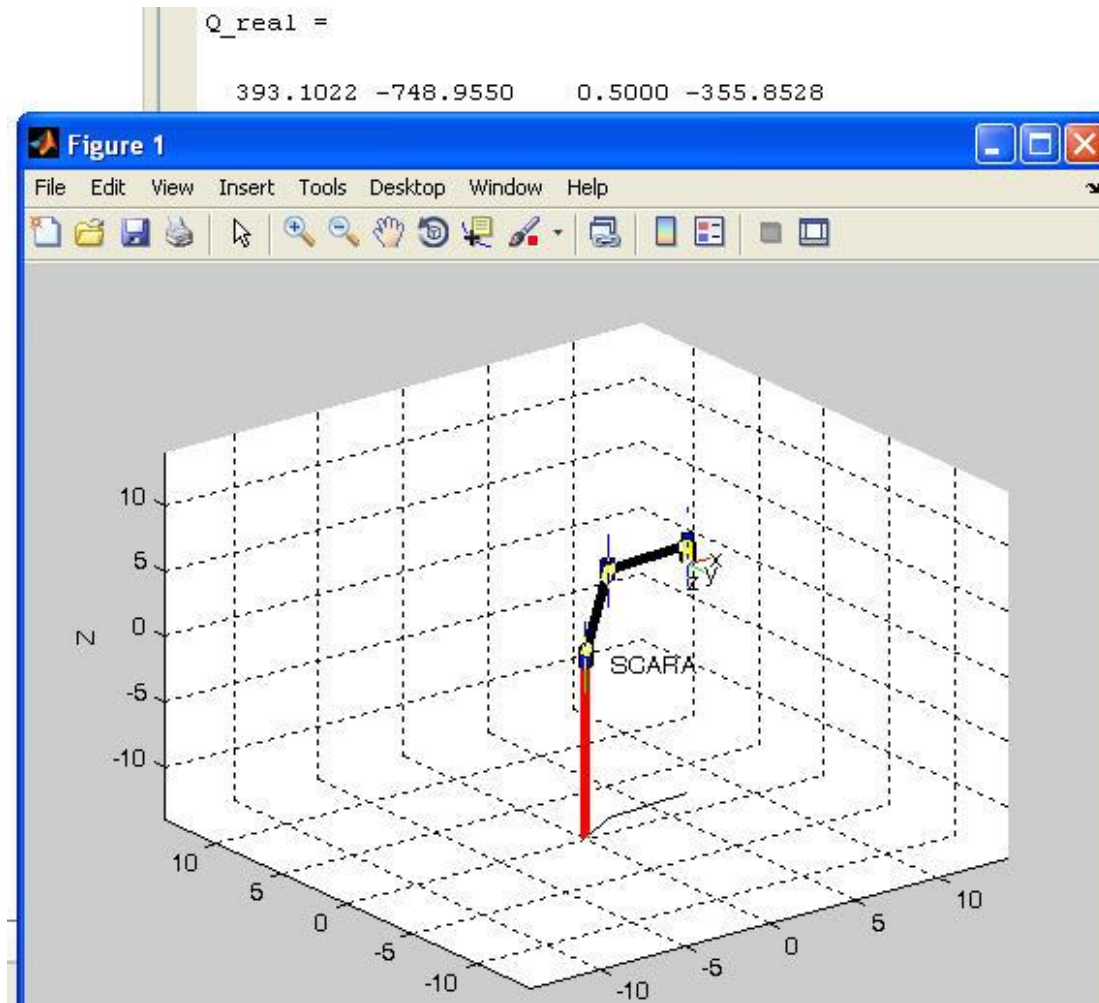
```
7.5001  
1.9999  
3.5000  
1.0000
```





Assignment 5 : Q6 Solution

- b) With answer (θ_1 , θ_2 and d_3) from Q5, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure.





Assignment 5 : Q7

Q7. With RPP 3-DOF wrist.

Given DH table and Transformation matrices. Find possible posture solutions for end point location $P(1.5, 2.75, 5)$.

Given $L_1 = 2.5, L_2 = 0$ and $L_6 = 0.15$

and transformation data are given as

$T_{06} =$

-1.0000	-0.0000	0.0000	1.5000
0.0000	-0.0000	1.0000	2.7500
0	1.0000	0.0000	5.0000
0	0	0	1.0000

$T_{03} =$

-0.8660	-0.0000	0.5000	1.5000
0.5000	-0.0000	0.8660	2.5981
0	1.0000	0.0000	5.0000
0	0	0	1.0000



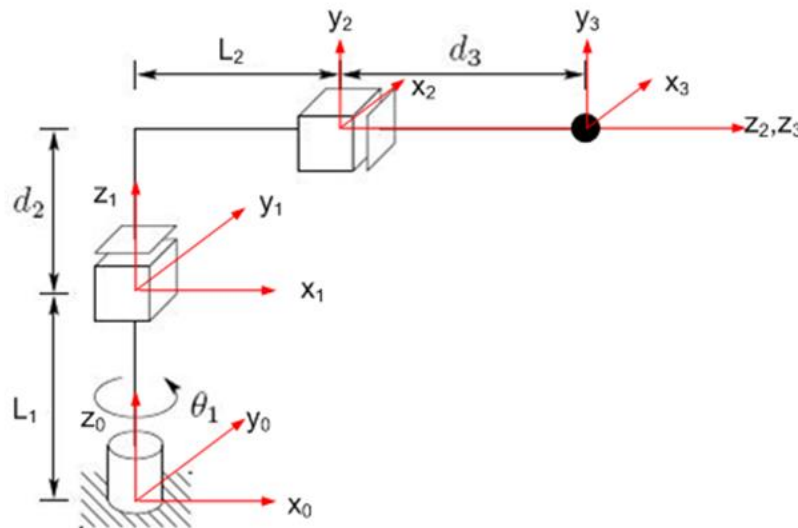
Assignment 5 : Q7

Link	α	a	d	θ
1	0	0	L_1	θ_1^*
2	90°	0	d_2^*	90°
3	0	0	$L_2 + d_2^*$	0

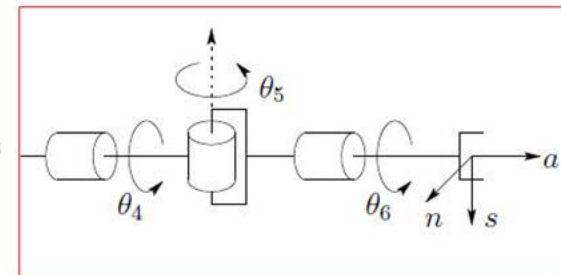
Link	a_i	α_i	d_i	θ_i
4	0	-90	0	θ_4^*
5	0	90	0	θ_5^*
6	0	0	d_6	θ_6^*

3 DOF Wrist

RPP



Wrist mechanism





Assignment 5 : Solution Q7

$$c_1 = 0.5$$

$$s_1 = 0.866$$

$$\theta_1 = A \tan 2(0.5, 0.866)$$

$$\theta_1 = 60^\circ$$

$$c_1(d_3) = 1.5 \quad \Rightarrow \quad d_3 = 3$$

$$L_1 + d_2 = 5 \quad \Rightarrow \quad d_2 = 2.5$$



Assignment 5 : Solution Q7

$$c_5 = u_{33} = 0.866$$

$$s_5 = \pm \sqrt{1 - (0.866)^2}$$

$$\theta_5 = A \tan 2(0.866, \pm \sqrt{1 - (0.866)^2})$$

$$\theta_5 = \pm 30^\circ$$

$$\theta_5 = +30^\circ$$

$$\therefore s_5 > 0$$

$$+u_{13} = c_4 \text{ and } +u_{23} = s_4$$

$$\theta_4 = A \tan 2(u_{13}, u_{23})$$

$$\theta_4 = 0^\circ$$

$$\therefore s_5 > 0$$

$$-u_{31} = c_6 \text{ and } +u_{32} = s_6$$

$$\theta_6 = A \tan 2(-u_{31}, u_{32})$$

$$\theta_6 = 0^\circ$$

$$\theta_5 = -30^\circ$$

$$\therefore s_5 < 0$$

$$-u_{13} = c_4 \text{ and } -u_{23} = s_4$$

$$\theta_4 = A \tan 2(-u_{13}, -u_{23})$$

$$\theta_4 = 180^\circ$$

$$\therefore s_5 < 0$$

$$+u_{31} = c_6 \text{ and } -u_{32} = s_6$$

$$\theta_6 = A \tan 2(u_{31}, -u_{32})$$

$$\theta_6 = 180^\circ$$



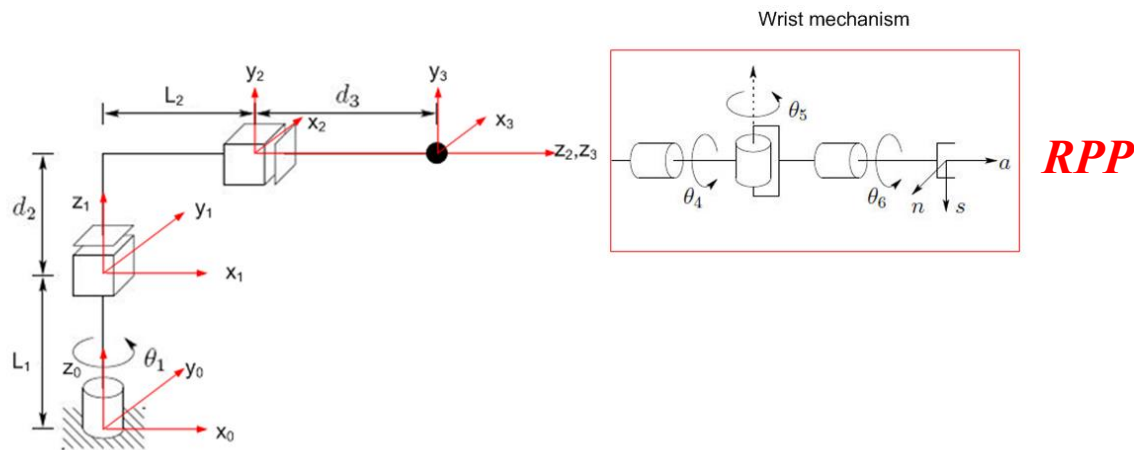
Assignment 5 : Q8

Q8. With RPP 3-DOF wrist. (ikine function)

Given DH table and Transformation matrices. Find possible posture solutions for end point location P(1.5, 2.75, 5), using Inverse Kinematic function `ikine()` from **MATLAB**. Plot this location.

Given $L_1 = 2.5, L_2 = 0$ and $L_6 = 0.15$

IG [0.1 0.5 0 0 0 0]



3 DOF Wrist

Link	α	a	d	θ
1	0	0	L_1	θ_1^*
2	90°	0	d_2^*	90°
3	0	0	$L_2 + d_3^*$	0

Link	a_i	α_i	d_i	θ_i
4	0	-90	0	θ_4^*
5	0	90	0	θ_5^*
6	0	0	d_6	θ_6^*



Assignment 5 : Q8 Solution

```
th1_deg =
    61.3895

d2 =
    2.3500

d3 =
    3.1325

th4_deg =
   -270

th5_deg =
   -270

th6_deg =
   118.6105

clear all; clc;
L1 = 2.5; L2 = 0; d6 = 0.15;
th1 = pi/3; d2 = 2.5; d3 = 3; th4 = 0; th5 = pi/6; th6 = 0;
%%RPP
A1 = link([0 0 0 L1,0]);
A2 = link([pi/2 0 pi/2 0,1]);
A3 = link([0 0 0 0,1]);
RPP_A5 = robot({A1 A2 A3});
T03 = fkine(RPP_A5,[th1 d2 d3])
%%3 DOF wrist
A4 = link([-pi/2 0 0 0,0]);
A5 = link([pi/2 0 0 0,0]);
A6 = link([0 0 0 d6,0]);
Wrist_A5 = robot({A4 A5 A6});
T36 = fkine(Wrist_A5,[th4 th5 th6])

RPP_3DOF_WRIST = robot({A1 A2 A3 A4 A5 A6});

position = transl([1.5,2.75,5]);
IG = [0.1 0.5 0 0 0 0]
values = ikine(RPP_3DOF_WRIST, position, IG, [1 1 1 1 1 1]);
th1_deg = (values(1,1)/pi)*180
d2 = values(1,2)
d3 = values(1,3)
th4_deg = (values(1,4)/pi)*180
th5_deg = (values(1,5)/pi)*180
th6_deg = (values(1,6)/pi)*180
```



Assignment 5 : Q9

Q9. With RPP 3-DOF wrist.

- a). With answer (θ_1 , d_2 , d_3 , θ_4 , θ_5 , θ_6) from Q7, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.
- b). With answer (θ_1 , d_2 , d_3 , θ_4 , θ_5 , θ_6) from Q8, check your answer with Forward Kinematic function in MATLAB, whether you obtain the correct desirable position. Plot the figure with MATLAB. Attached your code and result.



Assignment 5 : Q9 Solution

Pend_ikine =

1.5000

2.7500

5.0000

1.0000

```
L1 = 2.5; L2 = 0; d6 = 0.15;
th1 = pi/3; d2 = 2.5; d3 = 3; th4 = 0; th5 = pi/6; th6 = 0;
%%RPP
A1 = link([0 0 0 L1,0]);
A2 = link([pi/2 0 pi/2 0,1]);
A3 = link([0 0 0 0,1]);
RPP_A5 = robot({A1 A2 A3});
T03 = fkine(RPP_A5,[th1 d2 d3])
%%3 DOF wrist
A4 = link([-pi/2 0 0 0,0]);
A5 = link([pi/2 0 0 0,0]);
A6 = link([0 0 0 d6,0]);
RPP_3DOF_WRIST = robot({A1 A2 A3 A4 A5 A6});

position = transl([1.5,2.75,5]);
IG = [0.1 0.5 0 0 0 0]
values = ikine(RPP_3DOF_WRIST, position, IG, [1 1 1 1 1 1]);
th1_deg = (values(1,1)/pi)*180
d2 = values(1,2)
d3 = values(1,3)
th4_deg = (values(1,4)/pi)*180
th5_deg = (values(1,5)/pi)*180
th6_deg = (values(1,6)/pi)*180
%%check answer
T06_ikine = fkine(RPP_3DOF_WRIST, values);
Pend_ikine = T06_ikine*[0;0;0;1]
```