Cultural Consensus Theory

Joachim Vandekerckhove Spring 2025

 How can we identify and measure shared knowledge or beliefs within a community?

- How can we identify and measure shared knowledge or beliefs within a community?
- How can we distinguish shared knowledge from individual variation, error, or differing opinions?

- How can we identify and measure shared knowledge or beliefs within a community?
- How can we distinguish shared knowledge from individual variation, error, or differing opinions?
- Traditional methods often rely on subjective assessments.

- How can we identify and measure shared knowledge or beliefs within a community?
- How can we distinguish shared knowledge from individual variation, error, or differing opinions?
- Traditional methods often rely on subjective assessments.
- Need: A formal, quantitative approach to shared cognition.

• A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)
- Core assumptions of original CCT:

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)
- Core assumptions of original CCT:
 - There exists a "common truth"

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)
- Core assumptions of original CCT:
 - There exists a "common truth"
 - Informants respond independently of one another

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)
- Core assumptions of original CCT:
 - There exists a "common truth"
 - Informants respond independently of one another
 - Items are homogeneous (equally difficult to a respondent with fixed competence)

- A statistical model to infer shared cultural knowledge or shared beliefs from individual responses.
- Developed by anthropologists and cognitive scientists in the early 1980s (notably, Romney, Weller, and Batchelder)
- Core assumptions of original CCT:
 - There exists a "common truth"
 - Informants respond independently of one another
 - Items are homogeneous (equally difficult to a respondent with fixed competence)
- In other words, individuals will tend to agree more with each other and with the "truth" if they understand the domain.

Derivations from the Model

We now turn to the task of deriving the cultural competence of the informants from the proportion of matches among them. The parameter D_i is informant i's cultural competence, namely, the probability that informant i "knows" the correct answer to any item $(0 \le D_i \le 1)$. If the informant does not know the correct answer (with probability $[1-D_i]$), then they guess the answer with probability 1/L of a correct answer, where $(1-D_i)$ is the probability of not knowing the answer and L is the number of alternative answers to the question. For example, assume an informant's competence is 0.7 (0.7) for a five-item multiple-choice questionnaire. In addition to expecting that the informant will get 0.7 of the questions correct we would also expect the informant to get some of the 0.7 of the questions correct by guessing. Namely, 0.7 or 0.7 of the remaining 0.7 of the questions or 0.7 of 0.7 of the remaining 0.7 of the questions or 0.7 of the questions of the questions of the questions or 0.7 of the questions of the

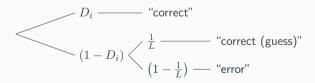
(3)
$$Pr(Y_u = 1) = D_i + (1-D_i)/L$$
,

and the probability of answering incorrectly is given by

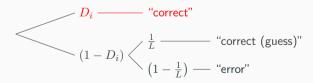
$$Pr(Y_{ik} = 0) = (1-D_i)(L-1)/L.$$

(3)
$$Pr(Y_a = 1) = D_i + (1-D_i)/L$$
,
and the probability of answering incorrectly is given by
$$Pr(Y_a = 0) = (1-D_i) (L-1)/L.$$

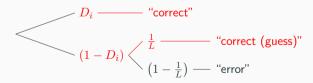
(3)
$$Pr(Y_a = 1) = D_i + (1-D_i)/L$$
,
and the probability of answering incorrectly is given by
$$Pr(Y_a = 0) = (1-D_i) (L-1)/L.$$



(3)
$$Pr(Y_a = 1) = D_i + (1-D_i)/L$$
,
and the probability of answering incorrectly is given by
$$Pr(Y_a = 0) = (1-D_i) (L-1)/L.$$



(3)
$$\Pr(Y_u = 1) = D_i + (1-D_i)/L$$
,
and the probability of answering incorrectly is given by
$$\Pr(Y_u = 0) = (1-D_i) (L-1)/L.$$

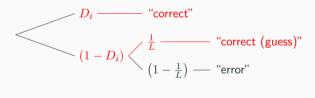


(3)
$$Pr(Y_u = 1) = D_i + (1-D_i)/L$$
,

and the probability of answering incorrectly is given by

$$Pr(Y_{ik} = 0) = (1-D_i)(L-1)/L.$$

These equations might look familiar.



Of course we don't know which answers are "correct"!

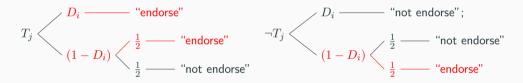
Let's instead think about the data Y_{ij} of participant i on item j, and let's focus on True/False questionnaires (so L=2, and $T_j=1$ if j is really true).

Let's instead think about the data Y_{ij} of participant i on item j, and let's focus on True/False questionnaires (so L=2, and $T_j=1$ if j is really true).

If participant i "endorses" item j, then $Y_{ij} = 1$. How many ways can they endorse it?

Let's instead think about the data Y_{ij} of participant i on item j, and let's focus on True/False questionnaires (so L=2, and $T_j=1$ if j is really true).

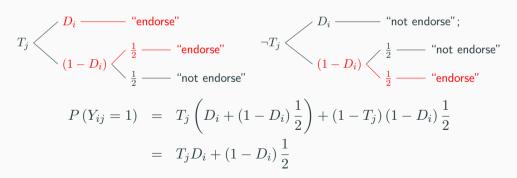
If participant i "endorses" item j, then $Y_{ij} = 1$. How many ways can they endorse it?



5

Let's instead think about the data Y_{ij} of participant i on item j, and let's focus on True/False questionnaires (so L=2, and $T_j=1$ if j is really true).

If participant i "endorses" item j, then $Y_{ij} = 1$. How many ways can they endorse it?



5

Guessing and acquiescence

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) \frac{1}{2}$$

We made the simplifying assumption just now that L=2. Using the diagrams on the previous slide, convince yourself that this assumption was without loss of generality (WLOG) – that is, the same logic is true if L>2.

Guessing and acquiescence

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) \frac{1}{2}$$

We made the simplifying assumption just now that L=2. Using the diagrams on the previous slide, convince yourself that this assumption was without loss of generality (WLOG) – that is, the same logic is true if L>2.

Specifically:

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) \frac{1}{L}$$

Guessing and acquiescence

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) \frac{1}{2}$$

We made the simplifying assumption just now that L=2. Using the diagrams on the previous slide, convince yourself that this assumption was without loss of generality (WLOG) – that is, the same logic is true if L>2.

Specifically:

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) \frac{1}{L}$$

We might even say that respondents have an individual bias g_i towards endorsing anything ("acquiescence bias"):

$$P(Y_{ij} = 1) = T_j D_i + (1 - D_i) g_i$$

Simplifying a little

Let's take out the guessing for now

Now,
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

7

• Individual Competence (D_i) :

- Individual Competence (D_i) :
 - Probability distribution for individual *i*'s knowledge of the tested domain.

- Individual Competence (D_i) :
 - Probability distribution for individual i's knowledge of the tested domain.
 - D_i lives on a probability scale (0 to 1)

- Individual Competence (D_i) :
 - Probability distribution for individual *i*'s knowledge of the tested domain.
 - D_i lives on a probability scale (0 to 1)
 - High probability at high values: Individual knows the consensus well.

- Individual Competence (D_i) :
 - Probability distribution for individual i's knowledge of the tested domain.
 - D_i lives on a probability scale (0 to 1)
 - High probability at high values: Individual knows the consensus well.
- Item Answers/Cultural Truth (T_j) :

- Individual Competence (D_i) :
 - Probability distribution for individual i's knowledge of the tested domain.
 - D_i lives on a probability scale (0 to 1)
 - High probability at high values: Individual knows the consensus well.
- Item Answers/Cultural Truth (T_j) :
 - ullet Probability distribution for the correct answer to question j.

- Individual Competence (D_i) :
 - Probability distribution for individual i's knowledge of the tested domain.
 - D_i lives on a probability scale (0 to 1)
 - High probability at high values: Individual knows the consensus well.
- Item Answers/Cultural Truth (T_j) :
 - Probability distribution for the correct answer to question j.
 - Reflects the estimated consensus or collective understanding.

Model identification

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Model identification

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Model identification

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

$$P(Y_{ij} = 1) = T'_{j}D'_{i} + (1 - T'_{j})(1 - D'_{i})$$

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

$$P(Y_{ij} = 1) = T'_j D'_i + (1 - T'_j) (1 - D'_i)$$

= $(1 - T_j)(1 - D_i) + (1 - (1 - T_j))(1 - (1 - D_i))$

9

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

$$P(Y_{ij} = 1) = T'_j D'_i + (1 - T'_j) (1 - D'_i)$$

$$= (1 - T_j)(1 - D_i) + (1 - (1 - T_j))(1 - (1 - D_i))$$

$$= (1 - T_j)(1 - D_i) + T_j D_i$$

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

$$P(Y_{ij} = 1) = T'_j D'_i + (1 - T'_j) (1 - D'_i)$$

$$= (1 - T_j)(1 - D_i) + (1 - (1 - T_j))(1 - (1 - D_i))$$

$$= (1 - T_j)(1 - D_i) + T_j D_i$$

$$= T_j D_i + (1 - T_j)(1 - D_i)$$

Basic CCT has a tricky identification issue—that sometimes pops up when multiple unknown interact—called label switching

Take
$$P(Y_{ij} = 1) = T_j D_i + (1 - T_j) (1 - D_i)$$

Now suppose all respondents are low in competence and all true items are false:

$$T'_{j} = 1 - T_{j}$$
 and $D'_{i} = 1 - D_{i}$:

$$P(Y_{ij} = 1) = T'_j D'_i + (1 - T'_j) (1 - D'_i)$$

$$= (1 - T_j)(1 - D_i) + (1 - (1 - T_j))(1 - (1 - D_i))$$

$$= (1 - T_j)(1 - D_i) + T_j D_i$$

$$= T_j D_i + (1 - T_j)(1 - D_i)$$

This makes the same predictions!

• What if informants are unsure?

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly
- Benefits:

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly
- Benefits:
 - Provides a more accurate model of response behavior.

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly
- Benefits:
 - Provides a more accurate model of response behavior.
 - Reduces bias caused by forced choices.

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly
- Benefits:
 - Provides a more accurate model of response behavior.
 - Reduces bias caused by forced choices.
 - Identifies true lack of knowledge or uncertainty vs. guessing incorrectly.

- What if informants are unsure?
- An explicit "Don't Know" (DK) option is useful.
- CCT models can be extended to include a process for DK responses
- Model accounts for the possibility that an informant:
 - Gives the correct answer (if competent).
 - If not, selects "Don't Know" with some probability, or...
 - ... Guesses randomly
- Benefits:
 - Provides a more accurate model of response behavior.
 - Reduces bias caused by forced choices.
 - Identifies true lack of knowledge or uncertainty vs. guessing incorrectly.
 - Can estimate the probability of guessing vs. knowing/DK.

• **Study:** Understanding local knowledge about diseases (e.g., diarrhea) symptoms, causes, and treatments in different communities.

- **Study:** Understanding local knowledge about diseases (e.g., diarrhea) symptoms, causes, and treatments in different communities.
- Method: Used CCT on yes/no questions about symptoms and treatments.

- **Study:** Understanding local knowledge about diseases (e.g., diarrhea) symptoms, causes, and treatments in different communities.
- Method: Used CCT on yes/no questions about symptoms and treatments.
- **Findings:** Identified widely shared models of illness within cultures and variations between cultures. Estimated individual knowledge.

- **Study:** Understanding local knowledge about diseases (e.g., diarrhea) symptoms, causes, and treatments in different communities.
- Method: Used CCT on yes/no questions about symptoms and treatments.
- Findings: Identified widely shared models of illness within cultures and variations between cultures. Estimated individual knowledge.
- Use: Essential for effective public health interventions, understanding treatment seeking behavior, and communication strategies.

• **Study:** Investigating shared perceptions of risks related to environmental issues (e.g., climate change, water contamination) in specific communities.

- **Study:** Investigating shared perceptions of risks related to environmental issues (e.g., climate change, water contamination) in specific communities.
- Method: Applied CCT to understand consensus on causes, impacts, and solutions.

- **Study:** Investigating shared perceptions of risks related to environmental issues (e.g., climate change, water contamination) in specific communities.
- Method: Applied CCT to understand consensus on causes, impacts, and solutions.
- Findings: Revealed differences in consensus levels across different types of risks and identified key informants.

- **Study:** Investigating shared perceptions of risks related to environmental issues (e.g., climate change, water contamination) in specific communities.
- Method: Applied CCT to understand consensus on causes, impacts, and solutions.
- **Findings:** Revealed differences in consensus levels across different types of risks and identified key informants.
- Use: Informs risk communication strategies, resource management plans, and community engagement efforts by tailoring messages to local knowledge.

• The basic CCT assumes a single dominant "truth."

- The basic CCT assumes a single dominant "truth."
- What if the agreement patterns suggest multiple distinct viewpoints or subcultures?

- The basic CCT assumes a single dominant "truth."
- What if the agreement patterns suggest multiple distinct viewpoints or subcultures?
- Multiple Consensus Models: Extensions that look for evidence of multiple latent factors in the agreement data.

- The basic CCT assumes a single dominant "truth."
- What if the agreement patterns suggest multiple distinct viewpoints or subcultures?
- Multiple Consensus Models: Extensions that look for evidence of multiple latent factors in the agreement data.
- Bayesian frameworks are flexible and can be adapted to estimate parameters for multiple potential consensus models simultaneously.

• Cultural Consensus Theory offers a powerful way to measure what is collectively known or believed in a group.

- Cultural Consensus Theory offers a powerful way to measure what is collectively known or believed in a group.
- The Bayesian approach provides a robust method that explicitly models uncertainty and can handle complexities like "Don't Know" responses.

- Cultural Consensus Theory offers a powerful way to measure what is collectively known or believed in a group.
- The Bayesian approach provides a robust method that explicitly models uncertainty and can handle complexities like "Don't Know" responses.
- By analyzing agreement patterns, we can identify shared knowledge and the individuals who are most knowledgeable within that domain.

- Cultural Consensus Theory offers a powerful way to measure what is collectively known or believed in a group.
- The Bayesian approach provides a robust method that explicitly models uncertainty and can handle complexities like "Don't Know" responses.
- By analyzing agreement patterns, we can identify shared knowledge and the individuals who are most knowledgeable within that domain.
- It's a valuable but slightly underappreciated tool for researchers across social sciences and applied fields seeking to understand shared cognition.

Cultural Consensus Theory

Joachim Vandekerckhove Spring 2025