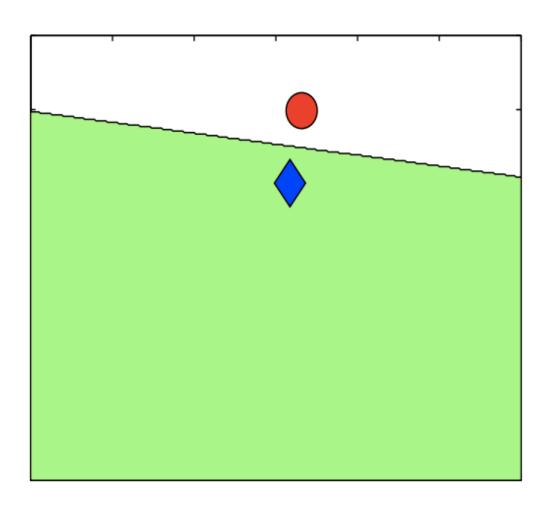
Semi-supervised Learning

Machine Learning 10-601B
Seyoung Kim

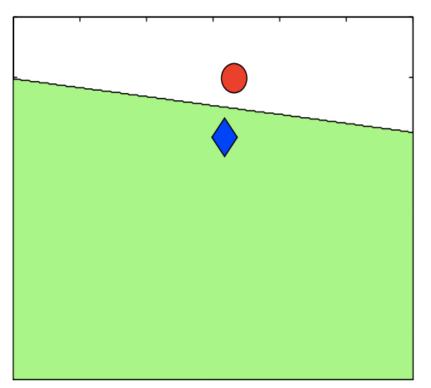
Can Unlabeled Data improve supervised learning?

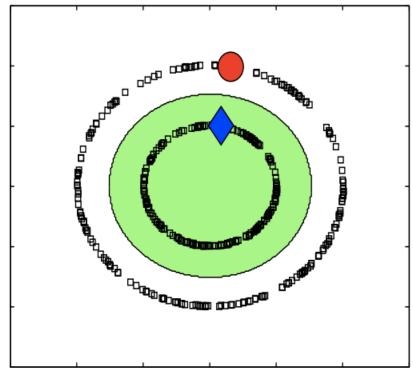
- Important question! In many cases, unlabeled data is plentiful, labeled data expensive
 - Medical outcomes (x=<patient, symptom>, y=treatment outcome)
 - Text classification (x=document, y=labels/category)
 - Customer modeling (x=user actions, y=user intent)

Classification with labeled data



Classification with labeled + unlabeled data





When can Unlabeled Data help supervised learning?

Consider setting:

- Set X of instances drawn from unknown distribution P(X)
- Wish to learn target function f: X → Y (or, P(Y|X))
- Given a set H of possible hypotheses for f

Given:

- iid labeled examples $L = \{\langle x_1, y_1 \rangle \dots \langle x_m, y_m \rangle\}$
- iid unlabeled examples $U = \{x_{m+1}, \dots x_{m+n}\}$

$$\widehat{f} \leftarrow \arg\min_{h \in H} \Pr_{x \in P(X)}[h(x) \neq f(x)]$$

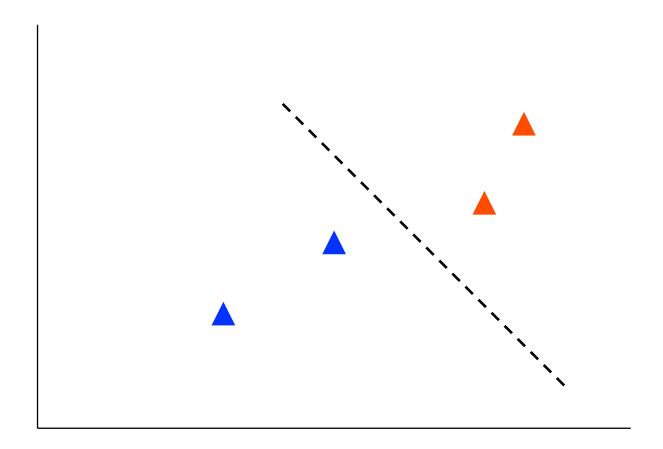
Four Ways to Use Unlabeled Data for Supervised Learning

- 1. Use to re-weight labeled examples
- 2. Use to help EM learn class-specific generative models
- 3. If problem has redundantly sufficient features, use CoTraining
- 4. Use to detect/preempt overfitting

1. Use unlabeled data to reweight labeled examples

- Most machine learning algorithms (neural nets, decision trees) attempt to minimize errors over labeled examples
- But our ultimate goal is to minimize error over future examples drawn from the same underlying distribution
- If we know the underlying distribution, we should weight each training example by its probability according to this distribution
- Unlabeled data allows us to estimate this distribution more accurately, and to reweight our labeled examples accordingly

Example



1. reweight labeled examples

Can use $U \to \hat{P}(X)$ to alter optimization problem

Wish to find

$$\hat{f} \leftarrow \underset{h \in H}{\operatorname{argmin}} \sum_{x \in X} \delta(h(x) \neq f(x)) P(x)$$

Often approximate as

$$\hat{f} \leftarrow \underset{h \in H}{\operatorname{argmin}} \frac{1}{|L|} \sum_{\langle x, y \rangle \in L} \delta(h(x) \neq y)$$

1 if hypothesis
h disagrees
with true
function f,
else 0

1. reweight labeled examples

Can use $U \to \hat{P}(X)$ to alter optimization problem

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$$\hat{f} \leftarrow \operatorname*{argmin}_{h \in H} \mathop{\textstyle \sum}_{x \in X} \delta(h(x) \neq f(x)) \frac{n(x,L)}{|L|}$$

1 if hypothesis h disagrees with true function f, else 0

of times we have x in the labeled set

1. reweight labeled examples

Can use $U \to \hat{P}(X)$ to alter optimization problem

Wish to find

$$\hat{f} \leftarrow \operatorname*{argmin}_{h \in H} \mathop{\textstyle \sum}_{x \in X} \delta(h(x) \neq f(x)) P(x)$$

Often approximate as

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$$\hat{f} \leftarrow \operatorname*{argmin}_{h \in H} \mathop{\textstyle \sum}_{x \in X} \delta(h(x) \neq f(x)) \frac{n(x,L)}{|L|}$$

 \bullet Can use U for improved approximation:

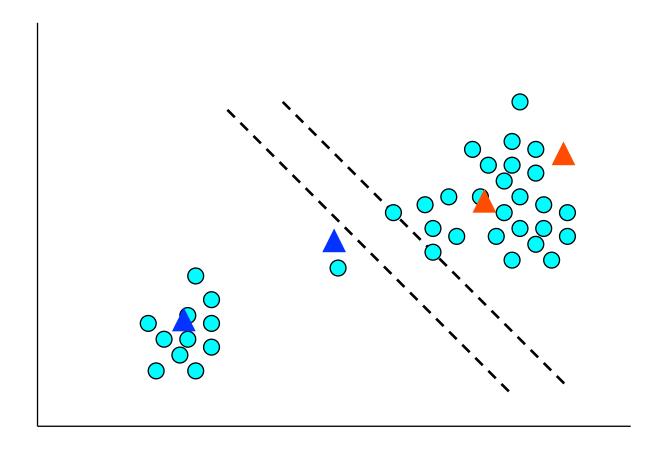
$$\hat{f} \leftarrow \operatorname*{argmin}_{h \in H} \mathop{\textstyle \sum}_{x \in X} \delta(h(x) \neq f(x)) \frac{n(x,L) + n(x,U)}{|L| + |U|}$$

1 if hypothesis h disagrees with true function f, else 0

of times we have x in the labeled set

of times we have x in the unlabeled set

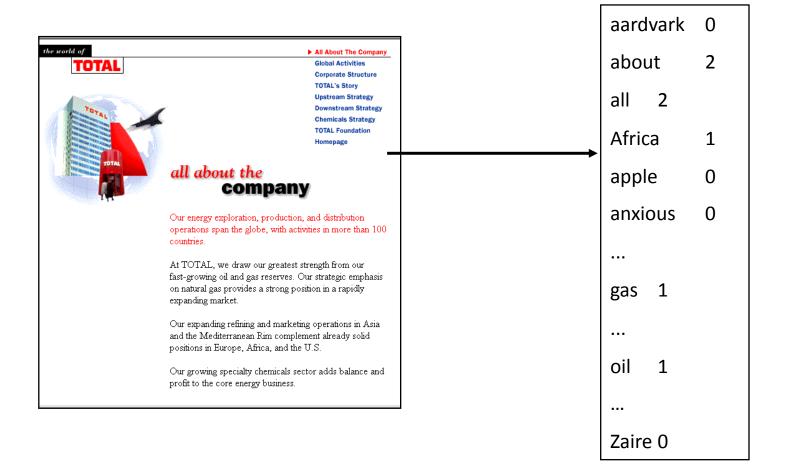
Example



2. Improve EM clustering algorithms

- Consider completely unsupervised clustering, where we assume data X is generated by a mixture of probability distributions, one for each cluster
 - For example, Gaussian mixtures
- Some classifier learning algorithms such as Gaussian Bayes classifiers also assumes the data X is generated by a mixture of distributions, one for each class Y
- Supervised learning: estimate P(X|Y) from labeled data
- Opportunity: estimate P(X|Y) from labeled and unlabeled data, using EM as in clustering

Bag of Words Text Classification



Baseline: Naïve Bayes Learner

Train:

For each class c_i of documents

- 1. Estimate $P(c_i)$
- 2. For each word w_i estimate $P(w_i \mid c_i)$

Classify (doc):

Assign doc to most probable class

$$\underset{j}{\operatorname{arg\,max}} P(c_j) \prod_{w_i \in doc} P(w_i \mid c_j)$$

Naïve Bayes assumption: words are conditionally independent, given class

Fac	u1	ty
Pac	uJ	ty

	_
associate	0.00417
chair	0.00303
member	0.00288
рħ	0.00287
director	0.00282
fax	0.00279
journal	0.00271
recent	0.00260
received	0.00258
award	0.00250

Students

resume	0.00516
advisor	0.00456
student	0.00387
working	0.00361
stuff	0.00359
links	0.00355
homepage	0.00345
interests	0.00332
personal	0.00332
favorite	0.00310

Courses

- Vouise		
homework	0.00413	
syllabus	0.00399	
assignments	0.00388	
exam	0.00385	
grading	0.00381	
midterm	0.00374	
рm	0.00371	
instructor	0.00370	
due	0.00364	
final	0.00355	

Departments

departmental	0.01246
colloquia	0.01076
epartment	0.01045
seminars	0.00997
schedules	0.00879
webmaster	0.00879
events	0.00826
facilities	0.00807
eople	0.00772
postgraduate	0.00764

Research Projects

research i rojects		
investigators	0.00256	
group	0.00250	
members	0.00242	
researchers	0.00241	
laboratory	0.00238	
develop	0.00201	
related	0.00200	
агра	0.00187	
affiliated	0.00184	
project	0.00183	

Others

~ —		
type	0.00164	
jan	0.00148	
enter	0.00145	
random	0.00142	
program	0.00136	
net	0.00128	
time	0.00128	
format	0.00124	
access	0.00117	
begin	0.00116	

Expectation Maximization (EM) Algorithm

Use labeled data L to learn initial classifier h

Loop:

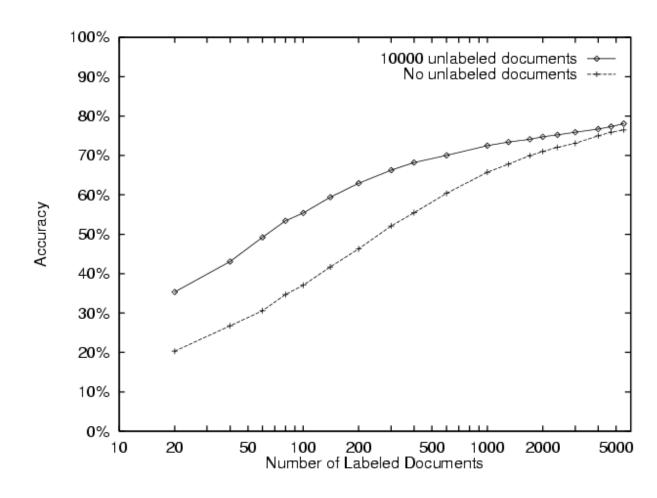
- E Step:
 - Assign probabilistic labels to U, based on h
- M Step:
 - Retrain classifier h using both L (with fixed membership) and assigned labels to U (soft membership)
- Under certain conditions, guaranteed to converge to locally maximum likelihood h

Table 3. Lists of the words most predictive of the course class in the WebKB data set, as they change over iterations of EM for a specific trial. By the second iteration of EM, many common course-related words appear. The symbol D indicates an arbitrary digit.

Iteration 0		Iteration 1	Iteration 2
intelligence		DD	D
DD		D	DD
artificial	Using one	lecture	lecture
understanding	labeled example	cc	cc
DDw	per class	D^{\star}	DD:DD
dist	per class	DD:DD	due
identical		handout	D^{\star}
rus		due	homework
arrange		problem	assignment
games		set	handout
dartmouth		tay	set
natural		DDam	hw
cognitive		yurttas	exam
logic		homework	problem
proving		kfoury	DDam
prolog		sec	postscript
knowledge		postscript	solution
human		exam	quiz
representation		solution	chapter
field		assaf	ascii

Experimental Evaluation

Newsgrop postings
- 20 newsgroups,
1000/group



3. If Problem Setting Provides Redundantly Sufficient Features, use CoTraining

- In some settings, available data features are so redundant that we can train two classifiers using different features
- In this case, the two classifiers should agree on the classification for each unlabeled example
- Therefore, we can use the unlabeled data to constrain training of both classifiers, forcing them to agree

CoTraining

```
learn f: X \rightarrow Y

where X = X_1 \times X_2

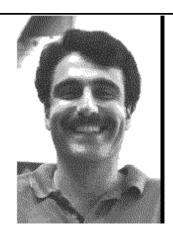
where x drawn from unknown distribution

and \exists g_1, g_2 \ (\forall x) g_1(x_1) = g_2(x_2) = f(x)
```

Redundantly Sufficient Features

Professor Faloutsos

my advisor



U.S. mail address:

Department of Computer Science University of Maryland College Park, MD 20742 (97-99: on leave at CMU)

Office: 3227 A.V. Williams Bldg.

Phone: (301) 405-2695
Fax: (301) 405-6707
Email: christos@cs.umd.edu

Christos Faloutsos

Current Position: Assoc. Professor of Computer Science. (97-98: on leave at CMU)

Join Appointment: Institute for Systems Research (ISR).

Academic Degrees: Ph.D. and M.Sc. (University of Toronto.); B.Sc. (Nat. Tech. U. Ath

Research Interests:

- · Query by content in multimedia databases;
- · Fractals for clustering and spatial access methods;
- · Data mining;

CoTraining Algorithm

[Blum&Mitchell, 1998]

Given: labeled data L,

unlabeled data U

Loop:

Train g1 (hyperlink classifier) using L

Train g2 (page classifier) using L

Allow g1 to label p positive, n negative examps from U

Allow g2 to label p positive, n negative examps from U

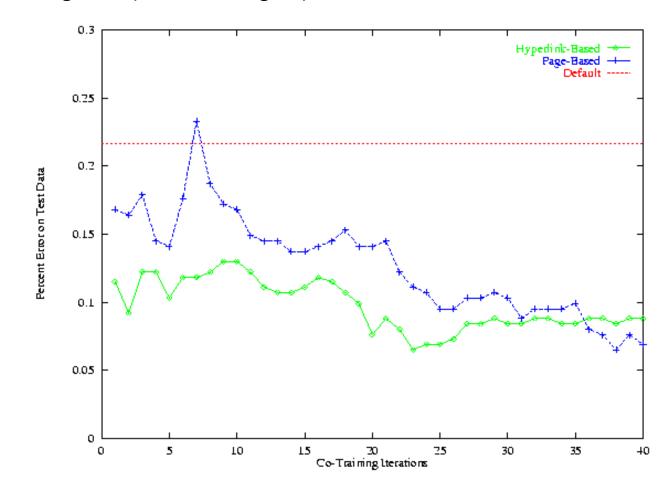
Add the intersection of the self-labeled examples to L

CoTraining: Experimental Results

- begin with 12 labeled web pages (academic course)
- provide 1,000 additional unlabeled web pages

Typical run:

- average error: learning from labeled data 11.1%;
- average error: cotraining 5.0% (when both agree)



4. Use Unlabeled Data to Detect/Preempt Overfitting

- Overfitting is a problem for many learning algorithms (e.g., decision trees, neural networks)
- The symptom of overfitting: complex hypothesis h2 performs better on training data than simpler hypothesis h1, but worse on test data
- Unlabeled data can help detect overfitting, by comparing predictions of h1 and h2 over the unlabeled examples
 - The rate at which h1 and h2 disagree on U should be the same as the rate on L, unless overfitting is occurring

Defining a distance metric

- Definition of distance metric
 - Non-negative $d(f,g) \ge 0$;
 - symmetric d(f,g)=d(g,f);
 - triangle inequality d(f,g) < d(f,h)+d(h,g)
- Classification with zero-one loss:

$$d(h_1, h_2) \equiv \int \delta(h_1(x) \neq h_2(x)) p(x) dx$$

Regression with squared loss:

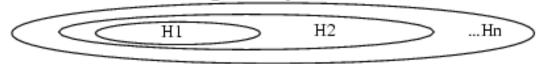
$$d(h_1, h_2) \equiv \sqrt{\int (h_1(x) - h_2(x))^2 p(x) dx}$$

Using the distance metric

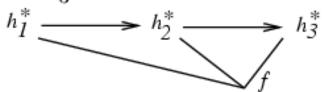
Define metric over $H \cup \{f\}$

$$d(h_1, h_2) \equiv \int \delta(h_1(x) \neq h_2(x)) p(x) dx$$
$$\hat{d}(h_1, f) = \frac{1}{|L|} \sum_{x_i \in L} \delta(h_1(x_i) \neq y_i)$$
$$\hat{d}(h_1, h_2) = \frac{1}{|U|} \sum_{x \in U} \delta(h_1(x) \neq h_2(x))$$

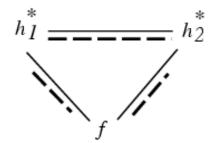
Organize H into complexity classes



Let h_i^* be hypothesis with lowest $\hat{d}(h, f)$ in H_i Prefer h_1^* , h_2^* , or h_3^* ?



Idea: Use U to Avoid Overfitting



Note:

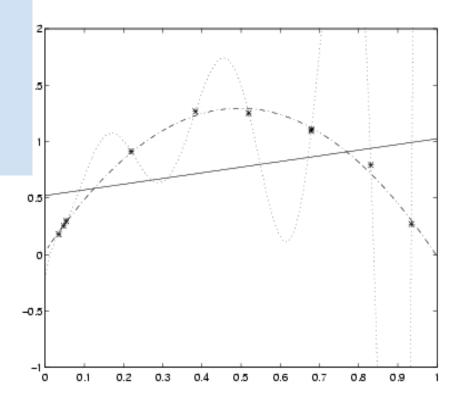
- $\hat{d}(h_i^*, f)$ optimistically biased (too short)
- $\hat{d}(h_i^*, h_j^*)$ unbiased
- Distances must obey triangle inequality!

$$d(h_1, h_2) \le d(h_1, f) + d(f, h_2)$$

- \rightarrow Heuristic:
 - Continue training until $\hat{d}(h_i, h_{i+1})$ fails to satisfy triangle inequality

Generated y values contain zero mean Gaussian noise &

$$Y=f(x)+E$$



An example of minimum squared error polynomials of degrees 1, 2, and 9 for a set of 10 training points. The large degree polynomial demonstrates erratic behavior off the training set.

Experimental Evaluation of TRI

[Schuurmans & Southey, MLJ 2002]

- Use it to select degree of polynomial for regression
- Compare to alternatives such as cross validation, structural risk minimization, ...

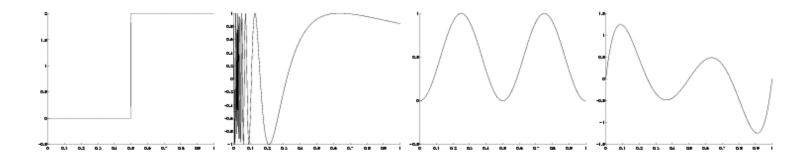


Figure 5: Target functions used in the polynomial curve fitting experiments (in order): $step(x \ge 0.5)$, sin(1/x), $sin^2(2\pi x)$, and a fifth degree polynomial.

Summary

Several ways to use unlabeled data in supervised learning

- 1. Use to reweight labeled examples
- 2. Use to help EM learn class-specific generative models
- 3. If problem has redundantly sufficient features, use CoTraining
- 4. Use to detect/preempt overfitting

Ongoing research area