# Notes for MATH 3210: Foundation of Analysis I

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## 1 Basic Topology

Metric (distance function) of  $x_0$  and x:  $d(x_0, x) = |x - x_0|$ 

### 1.1 Metric Space

Metric space X

$$d: M \times M \to \mathbf{R}$$
 (1)

- 1.  $d(x_0, x_1) \ge 0$  where  $x_0, x_1 \in X$
- 2.  $d(x_0, x_1) \iff x_0 = x_1$
- 3.  $d(x_0, x_1) = d(x_1, x_0)$  (irrespective of order)
- 4.  $d(x,z) \le d(x,y) + d(y,z)$  (triangular inequity)

Euclidean metric on  $\mathbf{R}^2$ :  $d(x,y) = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}$ Discrete metric:  $d(x,y) = \begin{cases} 1 & \text{if } x \neq y \\ 0 & \text{if } x = y \end{cases}$ Open ball of radius  $\epsilon$ :  $B_{\epsilon}(x_0) = B(x_0, \epsilon) = \{ y \in M \mid d(x_0, y) < \epsilon \}$ 

#### 1.2 Open Sets in X