

PURRCEPTION: VARIATIONAL FLOW MATCHING FOR VECTOR-QUANTIZED IMAGE GENERATION

Răzvan-Andrei Măişan^{*,1,3}, Vincent Tao Hu², Grigory Bartosh^{1,4},
Björn Ommer², Cees G. M. Snoek^{1,5}, Max Welling^{1,3,4}, Jan-Willem van de Meent^{1,3,4},
Mohammad Mahdi Derakhshani^{†,1,5}, Floor Eijkelboom^{†,1,3,4}

ABSTRACT

We introduce Purrception, a variational flow matching approach for vector-quantized image generation that provides explicit categorical supervision while maintaining continuous transport dynamics. Our method adapts Variational Flow Matching to vector-quantized latents by learning categorical posteriors over code-book indices while computing velocity fields in the continuous embedding space. This combines the geometric awareness of continuous methods with the discrete supervision of categorical approaches, enabling uncertainty quantification over plausible codes and temperature-controlled generation. We evaluate Purrception on ImageNet-1k 256×256 generation. Training converges faster than both continuous flow matching and discrete flow matching baselines while achieving competitive FID scores with state-of-the-art models. This demonstrates that Variational Flow Matching can effectively bridge continuous transport and discrete supervision for improved training efficiency in image generation.



Figure 1: Purrception generates high-resolution images in vector-quantized latent spaces, sampled as continuous transport learned through discrete supervision.

1 INTRODUCTION

The task of generative modeling is to approximate a data distribution to enable sampling of new instances. Beyond high-fidelity synthesis in images, audio, and text, generative models are increas-

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[†]Equal contribution as last authors.

¹University of Amsterdam, ²CompVis @ LMU Munich, MCML, ³Uva-Bosch Delta Lab, ⁴AMLab, ⁵VISLab.

ingly used for augmentation, restoration, simulation, and in-silico design (e.g., de novo molecules and proteins). Flow Matching (Lipman et al., 2023; Albergo et al., 2023; Liu et al., 2023b) has emerged as an extremely effective approach for the generation of a variety of data modalities. In Flow Matching, one first defines an interpolation between a source (noise) and a target (data) distribution, and then approximate the velocity field of a continuous normalizing flow that transports samples between the two. As the target velocity can be understood as the expected time-derivative of the interpolation, it can be learned in a self-supervised manner by averaging over samples from the source and target distribution. The Flow Matching framework has been extended to general geometries (Chen & Lipman, 2024), discrete data (Gat et al., 2024), and has seen many applications (Wildberger et al., 2024; Dao et al., 2023; Hu et al., 2024; Kohler et al., 2023).

Variational Flow Matching (VFM) (Eijkelboom et al., 2024) reframes Flow Matching as inference. Since the Flow Matching velocity field is the expectation of a conditional velocity, it can be approximated via a variational posterior over endpoints (target samples) given the current interpolation point. Standard Flow Matching is recovered when this posterior is Gaussian, while other choices extend naturally to different modalities. Applied to discrete data, VFM yields *CatFlow*, previously used for graph generation and related to continuous diffusion for categorical data (Dieleman et al., 2022). More broadly, VFM has been applied to mixed modalities (Guzmán-Cordero et al., 2025), molecular generation (Eijkelboom et al., 2025; Sakalyan et al.), and general geometries (Zaghen et al., 2025). The variational view also enables problem-specific constraints, e.g., for sea-ice forecasting, where bounds like non-negative thickness are enforced through the loss (Finn et al., 2025).

This paper leverages VFM in the context of image generation. We consider vector-quantized (VQ) latents, which map images into grids of discrete indices with associated embeddings, yielding compact representations that preserve perceptual fidelity at far lower dimensionality than pixels. However, their dual discrete–continuous nature poses a modeling challenge not addressed by purely continuous or discrete methods. Continuous methods (latent diffusion, flow matching) generate in the embedding space, enabling smooth transport and efficient high-resolution synthesis (Rombach et al., 2022; Dao et al., 2023). Yet they must discretize vectors back to indices: geometry is preserved, but categorical structure is ignored – the model never learns which index to choose or how to represent uncertainty across codes. Conversely, fully discrete approaches (VQ-Diffusion (Gu et al., 2022), discrete flow matching (DFM) (Gat et al., 2024)) treat related embeddings as unrelated tokens, discarding geometry. While DFM could use temperature-based sampling, this only produces stochastic “hops” between indices – each step commits to a single code – whereas continuous flow matching (CFM) cannot use temperature at all, since it lacks logits.

To resolve this tradeoff, we introduce *Purrception*, an adaptation of VFM to vector-quantized latents. By using a categorical posterior over indices while transporting probability in the continuous embedding space, *Purrception* provides a categorical learning signal while still leveraging geometry. This means the model can express uncertainty across plausible codes and translate it into smooth, geometry-aware transport rather than discrete jumps. Logits further enable temperature scaling: lowering temperature sharpens predictions, while raising temperature spreads probability across nearby embeddings, producing smoother and more diverse generations. Empirically, this hybrid approach converges faster than both CFM and DFM on ImageNet-1k, achieving competitive or superior FID while retaining the efficiency of flow matching.

2 BACKGROUND

2.1 FLOW MATCHING

Flow matching (Lipman et al., 2023; Liu et al., 2023a; Albergo et al., 2023) learns a velocity field $v_t^\theta : \mathbb{R}^D \times [0, 1] \rightarrow \mathbb{R}^D$ – parameterized by a network with parameters θ – which induces a transport of samples $x_0 \sim p_0$ from a prior (e.g., standard noise) to D -dimensional points x_1 that should approximate the data distribution. This is done by integrating the ordinary differential equation

$$\frac{dx}{dt} = v_t^\theta(x) \quad \text{with } x_0 \sim p_0, \quad (1)$$

which is equivalent to learning a velocity field that satisfies the continuity equation, also known as a continuous normalizing flow,

$$\partial_t p_t(x) = -\nabla \cdot (v_t^\theta(x) p_t(x)). \quad (2)$$

Flow matching starts from the observation that, given a choice of interpolation between noise and data – e.g., linear, where $x_t = tx_1 + (1 - t)x_0$ – we can derive a conditional velocity field $u_t(x | x_1)$ that satisfies the continuity equation towards (i.e., conditional on) a specific endpoint. A corresponding velocity field $u_t(x)$, which satisfies the continuity equation for the (marginal) probability path, can be expressed in terms of an (intractable) expectation with respect to the posterior

$$u_t(x) = \int u_t(x | x_1) p_t(x_1 | x) dx_1 = \mathbb{E}_{p_t(x_1|x)} [u_t(x | x_1)]. \quad (3)$$

The goal of flow matching is therefore to learn a velocity field $v_t^\theta(x)$ that approximates $u_t(x)$, i.e., to minimize the flow matching objective

$$\mathcal{L}_{\text{FM}}(\theta) = \mathbb{E}_{t,x} [\|v_t^\theta(x) - u_t(x)\|^2], \quad (4)$$

which can be made tractable by optimizing

$$\mathcal{L}_{\text{CFM}}(\theta) = \mathbb{E}_{t,x_1,x} [\|v_t^\theta(x) - u_t(x | x_1)\|^2], \quad (5)$$

i.e., a Monte-Carlo estimate of the marginal objective through our conditional objective. As shown in Lipman et al. (2023), indeed these two objectives have the same gradients w.r.t. θ . This can equivalently be understood as trying to regress towards the expected time-derivative of the interpolant.

2.2 VARIATIONAL FLOW MATCHING

Variational Flow Matching (VFM) (Eijkelboom et al., 2024) treats Flow Matching as a variational inference problem. By realizing (through Equation (3)) the target marginal velocity field u_t can be expressed as an expectation of the conditional field w.r.t. the posterior distribution $p_t(x_1 | x)$, the authors propose to learn this posterior directly, i.e., learn

$$\mathcal{L}_{\text{VFM}}(\theta) := \mathbb{E}_t [\text{KL}(p_t(x_1, x) || q_t^\theta(x_1, x))] = -\mathbb{E}_{t,x_1,x} [\log q_t^\theta(x_1 | x)] + \text{const.}, \quad (6)$$

where $q_t^\theta(x_1 | x)$ is the *variational posterior* approximating the posterior probability path $p_t(x_1 | x)$. The resulting learning velocity field is thus given by

$$v_t^\theta(x) := \mathbb{E}_{q_t^\theta(x_1|x)} [u_t(x | x_1)] \stackrel{\text{OT}}{=} \frac{\mu_t^\theta(x) - x}{1 - t}, \quad (7)$$

where $\mu_t^\theta(x) := \mathbb{E}_{q_t^\theta}[x_1 | x]$ and the conditional field is the linear (or optimal transport) interpolation. Though this objective initially looks intractable, we authors show that the task of learning the variational approximation only needs to be learned dimension-wise in the mean, as $\mathbb{E}_{q_t^\theta(x_1|x)}[x_1^d | x]$ only depends on the marginal $q_t^\theta(x^d | x)$ – an approach called *mean-field VFM*.

VFM is flexible in choosing the variational distribution q_t^θ , which makes it a general framework for different data types. In Eijkelboom et al. (2024), the authors show significant improvement over CFM when the data is discrete and the variational approximation is chosen to be categorical, a model coined *CatFlow*. VFM has also obtained strong performance in tabular data (Guzmán-Cordero et al., 2025), molecular generation tasks (Eijkelboom et al., 2025; Sakalyan et al.), general geometries (Zaghen et al., 2025), and sea-ice modeling (Finn et al., 2025).

2.3 VECTOR-QUANTIZED AND LATENT GENERATIVE MODELS

High-resolution image modeling in pixel space is computationally prohibitive; a common remedy is to learn a lower-dimensional latent space with an autoencoder. Vector-Quantized VAEs (Van Den Oord et al., 2017) and VQ-GANs (Esser et al., 2021) use a discrete codebook $\mathcal{C} = \{e_k\}_{k=1}^K \subseteq \mathbb{R}^D$. By mapping images into a compact set of discrete tokens, vector-quantized latents provide an efficient and stable representation: they alleviate posterior collapse and often yield sharper, higher-fidelity reconstructions than pixel-space models at comparable compute.

Given an image x , the encoder output is *quantized* to its nearest code:

$$z(x) = \text{Quantize}(\text{Encoder}(x)) = \arg \min_{e_k \in \mathcal{C}} \|\text{Encoder}(x) - e_k\|_2^2. \quad (8)$$

Equivalently, one can store the index

$$c(x) = \arg \min_{k \in [K]} \|\text{Encoder}(x) - e_k\|_2^2, \quad [K] := \{1, \dots, K\}. \quad (9)$$

After training the encoder, decoder, and codebook, a generative model is learned *in latent space* and samples are decoded to pixels. For a grid of D discrete latents $c \in [K]^D$, a common choice is an autoregressive model:

$$p(c) = \prod_{d=1}^D p(c_d \mid c_{<d}). \quad (10)$$

While this formulation provides a powerful and efficient representation, it also introduces a fundamental modeling tension: each latent is at once a discrete code index and a continuous embedding vector. Existing generative methods resolve this tension by making a trade-off – either operating in the continuous embedding space and ignoring the categorical structure, or modeling indices directly while discarding geometric information. This limitation motivates the hybrid perspective developed in Section 3.

3 PURRCEPTION: VQ-VFM FOR IMAGES

3.1 MOTIVATION: A HYBRID APPROACH TO VQ-LATENT FLOWS

Vector-quantized (VQ) latents encode data in two ways simultaneously: as discrete indices drawn from a finite codebook and as continuous embeddings that capture geometric relations such as proximity and direction. Existing generative models are typically forced into one of two degenerate extremes, each of which breaks part of this dual structure:

- **Continuous flow models** (e.g., latent diffusion and flow matching) operate in \mathbb{R}^D , treating codebook vectors as continuous. From the perspective of Variational Flow Matching (VFM), this corresponds to a Gaussian relaxation: endpoints are approximated as continuous samples rather than categorical indices. Geometry is preserved, but discreteness is lost – the model never receives a categorical learning signal, cannot express uncertainty over multiple plausible codes, and has no logits from which to derive controls such as temperature scaling.
- **Fully discrete flow models** instead predict categorical indices directly. While this aligns with the quantized structure, it collapses geometry: once reduced to raw indices, semantically related codes are treated as unrelated tokens. Predictions degenerate into discrete “teleports” between indices, eliminating interpolation and making both uncertainty modeling and temperature scaling meaningless.

An ideal solution should combine the strengths of both worlds: exploit the smooth geometry of embeddings *and* provide categorical supervision over indices. Our approach adapts VFM with a *categorical variational posterior*, so that the velocity field evolves in continuous space while learning is driven by cross-entropy over codebook entries. This hybridization allows the model to receive a categorical learning signal, to reason over multiple plausible indices, and to convert that uncertainty into geometry-aware transport rather than discrete jumps. Crucially, working with logits also unlocks a temperature knob: lowering τ enforces stronger commitments, which improves global fidelity but oversimplifies samples, while raising τ redistributes probability more broadly, adding detail and variety at the cost of overall quality.

3.2 THE VQ-VFM OBJECTIVE

We begin from the key observation underlying VFM and CatFlow: the velocity at time t can be expressed as an expectation over conditional continuations weighted by a posterior over endpoints (Eijkelboom et al., 2024):

$$u_t(z_t) = \mathbb{E}_{p_t(z_1 | z_t)} [u_t(z_t | z_1)]. \quad (11)$$

This perspective reframes the learning problem: rather than predicting the vector field directly, we may approximate the posterior $p_t(z_1 | z_t)$ with a variational distribution $q_t^\theta(z_1 | z_t)$ and compute the velocity as its expectation.

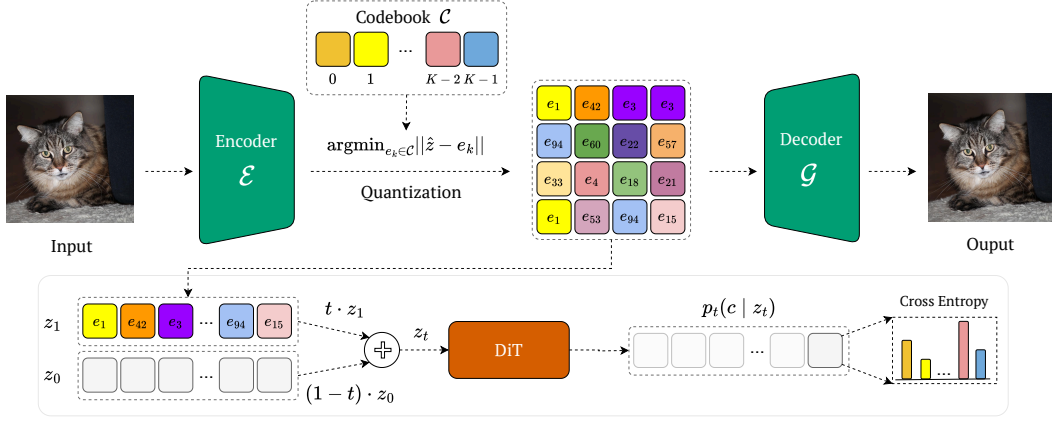


Figure 2: **Purrrception approach.** Purrrception generates high-resolution images in a vector quantized latent space. For training, we use a pretrained encoder \mathcal{E} and a codebook vector of size K to encode and quantize an image in latent space to obtain z_1 . Then, we train a diffusion transformer that predicts, given a linear interpolant z_t , a categorical distribution over the codebook vectors for each patch of the target z_1 via a cross-entropy objective. For sampling, we generate a quantized latent which we further pass through the decoder \mathcal{G} to obtain the image in pixel-space.

In the case of VQ-latents, this insight becomes particularly powerful. Each endpoint z_1 must be one of the finite codebook embeddings $\{e_k\}_{k=1}^K$, so the posterior is categorical over the discrete latent codes. That is, our variational posterior should be given by

$$q_t^\theta(c | z_t) = \text{Cat}(c | \pi_t^\theta(z_t)). \quad (12)$$

Conditioning this posterior on the noisy latent z_t yields a distribution over discrete indices while still defining transport in continuous embedding space, as we can compute

$$v_t^\theta(z_t) = \sum_{k=1}^K \pi_t^{\theta,k} \left(\frac{e_k - z_t}{1-t} \right) = \frac{\mu_t(z_t) - z_t}{1-t}, \quad (13)$$

where $\mu_t(z_t) := \sum_{k=1}^K \pi_t^{\theta,k}(z_t) e_k$. This ensures that uncertainty over multiple plausible codes is translated into smooth, geometry-aware motion, rather than discrete “teleports” between unrelated indices.

Training follows from the VFM objective, which in this case reduces to the cross-entropy loss between the predicted posterior and the ground-truth code indices:

$$\mathcal{L}_{\text{Purr}}(\theta) = -\mathbb{E}_{t,x,z_t} [\log q_\theta(c | z_t)], \quad (14)$$

where $x \sim \mathcal{D}$ is sampled from the data, z_1 and c is the corresponding quantized image and latent code respectively, and z_t is obtained through $z_t := tz_1 + (1-t)z_0$ for $z_0 \sim p_0$ and $t \sim \mathcal{U}(0, 1)$.

Softmax temperature. Because $\pi_t^\theta(z_t)$ is obtained from logits $\tilde{\pi}_t^\theta(z_t)$ via a softmax with temperature τ ,

$$\pi_t^{\theta,k}(z_t) = \frac{\exp(\tilde{\pi}_t^k(z_t)/\tau)}{\sum_{i=1}^K \exp(\tilde{\pi}_t^i(z_t)/\tau)}, \quad (15)$$

our framework naturally inherits an inference-time degree of freedom that regulates how categorical uncertainty is expressed in the velocity field. When τ is small, the posterior distribution collapses toward the most likely index, enforcing early commitments and producing sharp, high-fidelity outputs that may, however, become overly simplistic as alternative hypotheses are ignored. Conversely, large τ values flatten the distribution, assigning non-negligible weight to multiple neighboring codes.

This broadening injects more detail and variability into the generated samples, but can reduce overall fidelity as the barycenter drifts away from the most plausible embedding. Intermediate τ values often strike the best balance, echoing the bias–variance trade-off familiar from other generative frameworks. Such controllability is absent in continuous FM, where no categorical logits exist, and meaningless in fully discrete FM, where indices are collapsed immediately; it arises directly from the hybrid VQ–VFM formulation, turning temperature into a principled knob for task-adaptive inference.

3.3 TRAINING STABILITY

Architecturally, we use a diffusion transformer (DiT) Peebles & Xie (2023) as a backbone to predict the codebook indices that compound the target datapoint. One of the biggest challenges we encountered was maintaining a stable training for larger DiT variants (i.e., DiT-L/2, DiT-XL/2), especially because such training instabilities occurred in the later stages of the training phase.

Since the major difference between training Flow Matching and Purrrception is the training objective (i.e., mean-squared error for the former one, cross-entropy for the latter one) and Flow Matching does not have such training instabilities, we hypothesize that the cause might be the final softmax operation. Indeed, this divergence in the output logits from the log probabilities has been reported often as an instability issue by the research community when training large models at scale (Chowdhery et al., 2023; Wortsman et al., 2023). In their paper, Wortsman et al. (2023) name this issue the *logit drift problem*. To mitigate this issue, they propose regularizing the training using an additional *z-loss* which proved effective in training recent state-of-the-art, billion-parameter models such as Chameleon (Chameleon Team, 2024).

Inspired by its success, we apply *z-loss* regularization as well. Similar to Chameleon Team (2024), we add $10^{-5} \log^2 Z$ to Purrrception’s loss function, where $Z = \sum_{i=1}^K e^{x_i}$ and $\{x_i\}_{i=1}^K$ are the logits outputted by the backbone. Figure 3 shows Purrrception achieves stability when *z-loss* is integrated. Thus, we used the *z-loss* by default when training Purrrception.

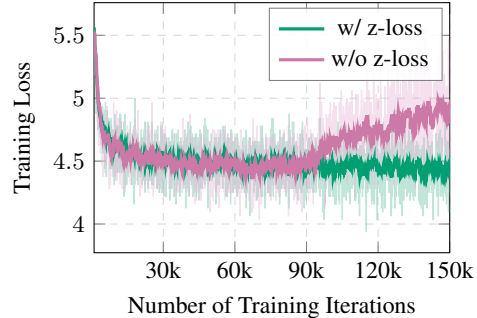


Figure 3: **Training loss curves with and without *z-loss*.** An additional *z-loss* avoids training divergence. Raw data is shown in lighter colors, while exponentially smoothed curves (EMA) are shown in bold. We used the same hyperparameters for both runs and a DiT-XL/2 backbone. EMA smoothing factor is $\alpha = 0.9$.

4 EXPERIMENTS AND RESULTS

We validate the performance of Purrrception through a series of experiments. In our experiments, we evaluate on ImageNet-1k (Deng et al., 2009) on 256×256 resolution, using Stable Diffusion’s `vq-f8` tokenizer (Esser et al., 2021) and DiT-L/2 and DiT-XL/2 backbones (Peebles & Xie, 2023). We provide a full description of the implementation details in Appendix C.

First, we perform a comparative study between Purrrception, continuous flow matching (CFM) (Lipman et al., 2023), and discrete flow matching (DFM) (Gat et al., 2024). We show that Purrrception *converges faster* (i.e., in fewer training iterations) to a low FID, hence reducing computational resources. Then, we show that Purrrception generates high-fidelity and high-quality samples when trained at scale, achieving a competitive FID against a variety of state-of-the-art autoregressive, diffusion, and masked generative baselines. Finally, we show that the softmax temperature parameter can be used to *control* the sharpness and diversity at inference time, a property unique to hybrid discrete-continuous models.

4.1 CONVERGENCE SPEED

A key requirement for practical generative modeling is the ability to reach high sample quality quickly, since faster convergence directly reduces training cost and compute requirements. To evaluate this, we compare the convergence speed of Purrrception against two strong baselines: the continuous flow model (CFM) (Lipman et al., 2023) and the fully discrete flow model (DFM) (Gat et al., 2024).

Figure 4 reports FID-10k scores over one million training iterations for both DiT-L/2 and DiT-XL/2 backbones. Across settings, Purrrception not only achieves lower final FID but also reaches baseline performance substantially earlier. With DiT-L/2, Purrrception matches CFM’s final score after $\sim 700k$ iterations ($1.4\times$ faster) and DFM’s final score after $\sim 325k$ iterations ($3.0\times$ faster). With the larger

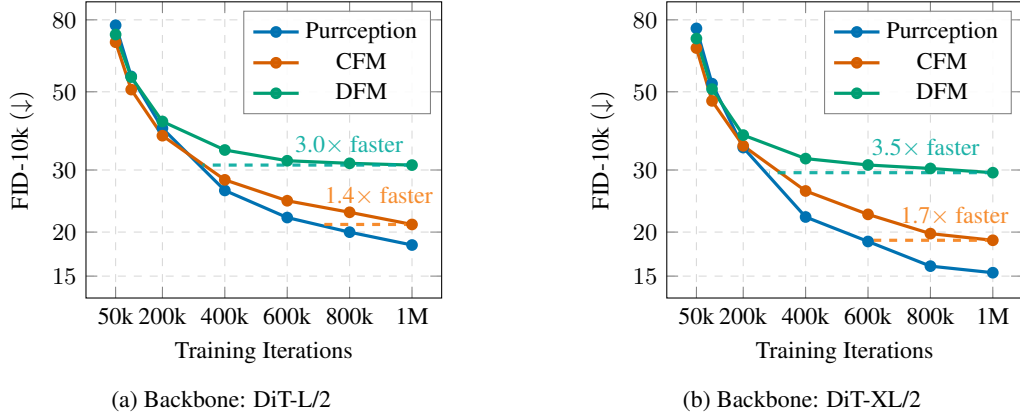


Figure 4: **Convergence speed comparison on ImageNet-1k.** FID-10k scores are plotted against training iterations for Purrrception, CFM, and DFM. Results are shown for two DiT backbones: (a) DiT-L/2 and (b) DiT-XL/2. For Purrrception, we used the softmax temperature $\tau = 0.9$ during inference for all checkpoints. The plots show that Purrrception achieves lower final FID scores and converges significantly faster, matching the final performance of CFM and DFM in fewer training iterations. Full training details are provided in Appendix C.

DiT-XL/2 backbone, the gap grows further: Purrrception converges $1.7\times$ faster than CFM and $3.5\times$ faster than DFM.

These results underscore the advantage of Purrrception’s hybrid formulation. By receiving direct categorical supervision (unlike CFM), the model learns discrete structure more efficiently, while its use of continuous embedding space (unlike DFM) enables smooth geometry-aware transport rather than slow, discrete jumps. This combination accelerates optimization, leading to both faster convergence and stronger final sample quality.

4.2 OPTIMIZING SAMPLE QUALITY VIA SOFTMAX TEMPERATURE SCALING



Figure 5: **Generated samples at different softmax temperatures.** We can control the output of Purrrception by changing the softmax temperature. A low temperature creates simpler, cleaner samples, while a high temperature adds more fine-grained details but can sometimes introduce flaws and reduce the image quality. Here we vary τ from 0.1 to 1.5.

Temperature scaling is a long-standing technique in language modeling, used to balance coherence and diversity during sampling. Because Purrrception employs a categorical learning objective, it inherits this mechanism in a natural way for vector-quantized image generation – a flexibility that continuous flow models such as CFM do not possess. We investigate whether adjusting the softmax temperature τ provides meaningful control over image fidelity and diversity.

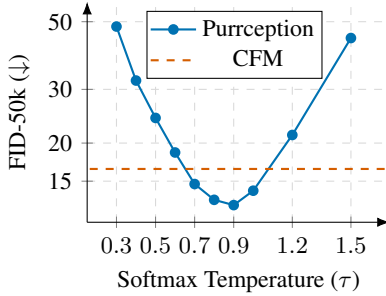


Figure 6: **The effect of the softmax temperature on FID score.** The plot depicts a U-shape relationship between τ parameter used in Purrception and the FID score. This parameter is not present in CFM. Both models have been trained for 1M training iterations and under the same training conditions.

We conduct an ablation study with a DiT-XL/2 backbone trained for one million iterations, varying the temperature at inference. Figures 5 and 6 show the effect on sample quality and FID-50k scores, respectively. We observe a clear U-shaped curve: performance improves as τ increases from very low values, reaches an optimum around $\tau \approx 0.8$ – 0.9 , and then degrades as τ becomes larger. The qualitative samples illustrate this trade-off: low τ produces overly deterministic and simplistic images, while high τ leads to noisy and incoherent generations.

These findings highlight that Purrception provides a meaningful “temperature knob” for controlling the fidelity–diversity trade-off. Continuous flow methods (e.g., CFM) cannot exploit this mechanism at all, since they lack categorical logits. Fully discrete models (DFM) can in principle apply temperature scaling to their logits, but because they commit to hard index selections at each step, adjusting τ has little practical effect – the sampling collapses to discrete jumps regardless of the distribution’s softness. In contrast, Purrception retains uncertainty in the logits while transporting through the continuous embedding space, so temperature scaling produces smooth and interpretable changes in sample quality.

4.3 QUALITATIVE AND QUANTITATIVE RESULTS

We train Purrception for 3.5M iterations with a DiT-XL/2 backbone, and report quantitative results on class-conditional ImageNet-1k generation at 256×256 resolution (Table 1).

Purrception achieves a FID of 4.72, placing it among the top-performing models in this setting. It substantially outperforms discrete diffusion approaches, and delivers results competitive with leading autoregressive models despite using comparable or fewer parameters. Against continuous diffusion methods, Purrception remains strong; while the very best models (e.g., DiT-XL/2 with FID 2.27) achieve lower scores, they do not use a VQ autoencoder, making the comparison not one-to-one.

These findings underline the promise of hybrid discrete–continuous modeling. Purrception combines categorical supervision with geometry-aware transport, yielding competitive sample quality while retaining the efficiency and compression benefits of VQ latents. Although we omit a full CFM baseline here due to computation limitations, Section 4.1 (Figure 4) already shows Purrception converges faster and reaches better FID after 1M iterations. This strongly suggests that, with longer training, Purrception would still surpass a CFM baseline.

5 RELATED WORK

Diffusion, flow matching, and latent spaces. Diffusion and score-based models synthesize data via iterative denoising (Sohl-Dickstein et al., 2015; Ho et al., 2020; Song et al., 2020), while Flow Matching learns a time-dependent velocity field that transports a source distribution to the data distribution, yielding continuous normalizing flows with strong empirical results (Lipman et al., 2023; Liu et al., 2023a; Albergo et al., 2023). To reduce cost without sacrificing quality, many works apply these dynamics in vector-quantized latent spaces, where autoencoders provide compact discrete indices with associated embeddings (Van Den Oord et al., 2017; Razavi et al., 2019). Such latents underlie VQ-GAN and large-scale generative systems (Esser et al., 2021; Ramesh et al., 2021; 2022), and running diffusion/flows on them enables efficient high-fidelity synthesis (Vahdat et al., 2021; Rombach et al., 2022; Dao et al., 2023), with recent work scaling to stronger backbones and resolutions (Ma et al., 2024; Esser et al.).

Discrete dynamics and relaxations. Beyond continuous latents, discrete diffusion and flow models operate directly on tokens or pixels (Hoogeboom et al., 2021a;b; Austin et al., 2021; Gat et al., 2024; Stark et al., 2024; Davis et al., 2024). Closer to our setting, discrete *latent* diffusion denoises over

Table 1: **Class-conditional generation on ImageNet-1k 256×256 .** We compare Purrception against various autoregressive, diffusion, and masked generative models. We report the number of parameters in millions (M) or billions (B), as well as the FID scores for each model. Purrception achieves a competitive FID of 4.72, showcasing the effectiveness of our hybrid discrete-continuous approach against strong baselines.

Model	#Parameters	FID ↓
<i>Autoregressive & Masked Generative Models</i>		
VQGAN (Esser et al., 2021)	1.4B	5.20
ViT-VQGAN (Yu et al., 2021)	1.7B	3.04
RQTransformer (Lee et al., 2022)	3.8B	3.80
LlamaGen-XL (Sun et al., 2024)	775M	3.39
MaskGIT (Chang et al., 2022)	227M	6.18
Open-MAGViT2-L (Luo et al., 2024)	804M	2.51
<i>Continuous Diffusion</i>		
ADM (Dhariwal & Nichol, 2021)	554M	10.94
CDM (Ho et al., 2022)	-	4.88
LDM-4 Rombach et al. (2022)	400M	3.60
DiT-XL/2 (Peebles & Xie, 2023)	675M	2.27
<i>Discrete Diffusion & Masked Generative Models</i>		
VQ-Diffusion (Gu et al., 2022)	-	5.84
Implicit Timestep Model Hu & Ommer (2024)	546M	5.30
<i>Hybrid Discrete-Continuous Models</i>		
Purrception ($\tau = 0.9, \text{cfg} = 1.3$)	750M	4.72

VQ indices (Gu et al., 2022; Tang et al., 2022), making the indices explicit but typically discarding the geometry of their embeddings. A complementary approach is to embed categorical data into a continuous space and run diffusion there, as in Continuous Diffusion for Categorical Data (CDCD) (Dieleman et al., 2022), developed primarily for language modelling. CDCD preserves the continuous-time formulation by operating on noisy embeddings while training with cross-entropy over token predictions, thereby capturing uncertainty and retaining guidance mechanisms. However, because the embeddings are learned jointly, the approach relies on continuous relaxations and may diverge from the true categorical structure. Our approach follows the same general spirit of combining categorical supervision with continuous transport.

6 CONCLUSIONS

We introduced Purrception, an adaptation of VFM to vector-quantized image generation. The method retains continuous transport in the embedding space while supervising with a categorical posterior over codebook indices. This coupling addresses the core trade-off of existing approaches: unlike CFM, Purrception benefits from categorical supervision, and unlike DFM, it avoids collapsing geometry into hard index jumps. The result is a model that learns, broadly speaking, what to choose and where to go, expressing uncertainty over plausible codes in a geometry-aware way. Empirically, Purrception outperforms both CFM and DFM on ImageNet-1k 256×256 benchmark, converging faster and achieving superior FID while preserving the efficiency of flow matching. Further ablations confirm that logits provide a controllable quality–diversity knob through temperature scaling.

Limitations and Future Work. Our approach is currently limited by its reliance on a fixed, pretrained VQ autoencoder, which makes performance dependent on the initial tokenization quality. While the model is competitive on 256×256 ImageNet-1k, its generalization to other datasets or higher resolutions needs validation, and it does not yet match the performance of top-tier continuous diffusion models. Future work could directly address these limitations by exploring different VQ models or jointly training the autoencoder with the flow model. Broader research directions include extending this hybrid perspective to domains like audio, video, and 3D shapes, as well as developing principled temperature schedules and a stronger theory for categorical objectives. Finally, because the model remains a continuous flow, it supports distillation into highly efficient, few-step samplers and can incorporate guidance, paving the way for practical generative pipelines.

Ethics Statement. All experiments in this work rely exclusively on *publicly available* datasets (i.e., ImageNet) used under their original licenses. We do not collect or annotate any new human data. As with other generative models, there exists a risk of misuse in privacy-invasive or unauthorized applications. We strongly caution against such uses and emphasize the importance of adhering to license terms, governance standards, and applicable legal requirements, though, as our approach is primarily methodological, we do not see immediate risks.

Reproducibility Statement. We aim to ensure the full reproducibility of our results. All datasets, baselines, and model architectures will be made publicly available. We provide pseudocode for training and sampling Purrception (Appendix B) as well as detailed implementation specifics in Appendix C, which covers optimization settings and evaluation protocols. To facilitate replication, we will release the full codebase.

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A USAGE OF LARGE LANGUAGE MODELS

During the preparation of this submission, Large Language Models (LLMs) were utilized as a tool to enhance the quality and presentation of our work. Specifically, we employed LLMs for text refinement, including improving grammar, syntax, and clarity to ensure the readability of our research. Additionally, these models assisted in refining the aesthetic and structural layout of our data visualizations and plots, providing suggestions for more effective data presentation. It is important to note that the LLMs served solely as an assistive tool. The authors retained full responsibility for all intellectual content, including the underlying research, data analysis, interpretation of results, and the final articulation of all arguments and conclusions presented in this paper.

B ALGORITHMS

TRAINING

```

for  $x \sim \mathcal{D}$  do
   $z_1 \leftarrow \text{Quantize}(\text{Encoder}(x));$ 
   $c \leftarrow \text{LatentCode}(z_1);$ 
   $z_0 \sim p_0;$ 
   $t \sim \mathcal{U}(0, 1);$ 
   $z_t \leftarrow tz_1 + (1 - t)z_0;$ 
   $\mathcal{L}(\theta) = \text{CrossEntropy}(c, \pi_t^\theta(z_t));$ 
  Backprop and update  $\theta$ ;
end

```

SAMPLING (EULER INTEGRATION)

```

 $z_0 \sim p_0;$ 
for  $s \in \{0, \dots, T - 1\}$  do
   $t \leftarrow s/T;$ 
   $\pi_t \leftarrow \text{softmax}(\tilde{\pi}_t^\theta(z_s), \tau);$ 
   $v_s \leftarrow \frac{\sum_{k=1}^K \pi_t^k \cdot e_k - z_s}{1 - t};$ 
   $z_{s+1} \leftarrow z_s + (1/T)v_s;$ 
end
 $x \leftarrow \text{Decoder}(\text{Quantize}(z_T));$ 
Return  $x;$ 

```

Figure 7: Training and sampling algorithms for Purrrception.

C IMPLEMENTATION DETAILS

Training specifications. We use DiT architectures of different sizes as backbones for all models (i.e., Purrrception, CFM, DFM). To train them, we mostly use the specifications from the original paper (Peebles & Xie, 2023): we initialize the final linear layer of DiT with zeros and otherwise we use the initialization techniques from the ViT (Dosovitskiy et al., 2020). We optimize our models using AdamW (Kingma & Ba, 2016; Loshchilov et al., 2017) with a constant learning rate $1e - 4$, a weight decay 0.01, $(\beta_1, \beta_2) = (0.9, 0.999)$. For Purrrception, we use $\text{eps} = 1e - 6$. We also use a global batch size 256. Based on the training details of prior image generation methods, we compute the exponential moving average (EMA) of the backbone parameters over training using a decay rate of 0.9999, and we do inference using solely the EMA model.

Additionally, we use the Stable Diffusion’s tokenizer `vq-f8` with a downsampling factor $f = 8$ and a codebook \mathcal{C} of shape 16,384 \times 4 (Esser et al., 2021). This means that for a given RGB image x of 256×256 resolution, the shape of the latent $z = \mathcal{E}(x)$ is $32 \times 32 \times 4$, which is further quantized according to \mathcal{C} . During sampling, we use the decoder \mathcal{G} to map the generated latent back into pixel space. The encoder, decoder, and codebook are kept frozen during training.

Sampling and FID score computation. Flow models need to simulate an ODE in order to solve the generative modeling task. We use the `torchdiffeq` library in PyTorch and the usual Euler method with 100 steps when generating samples.

For computing the FID scores, we first generate 10,000 samples for computing FID-10k scores and 50,000 samples for the FID-50k. Then, we use the `torch-fidelity` PyTorch library (Obukhov et al., 2020) to compute the FID score. For both FID-10k and FID-50k, we use 50k real samples (i.e., the entire validation set with 256×256 resolution) to compute the statistics for the target dataset. Unless otherwise specified, we do *not* use classifier-free guidance for the models trained conditionally on ImageNet-1k.

Computational resources. All methods were trained in a distributed way, using a total of 16 AMD MI250x GPUs, each GPU having 128GB of HBM2e memory.