

# Greedy Algorithms

LOOK: In high level, there is no definition of greedy algorithm. It is more of a solution technique.

## Schedule of a set of intervals that are non-overlapping in a line

GREEDY ALGORITHMS

Ex: scheduling

input:  $A = \{(x_1, y_1), (x_2, y_2), \dots\}$   $x_i < y_i$   
 $x_i, y_i \in \mathbb{N}$

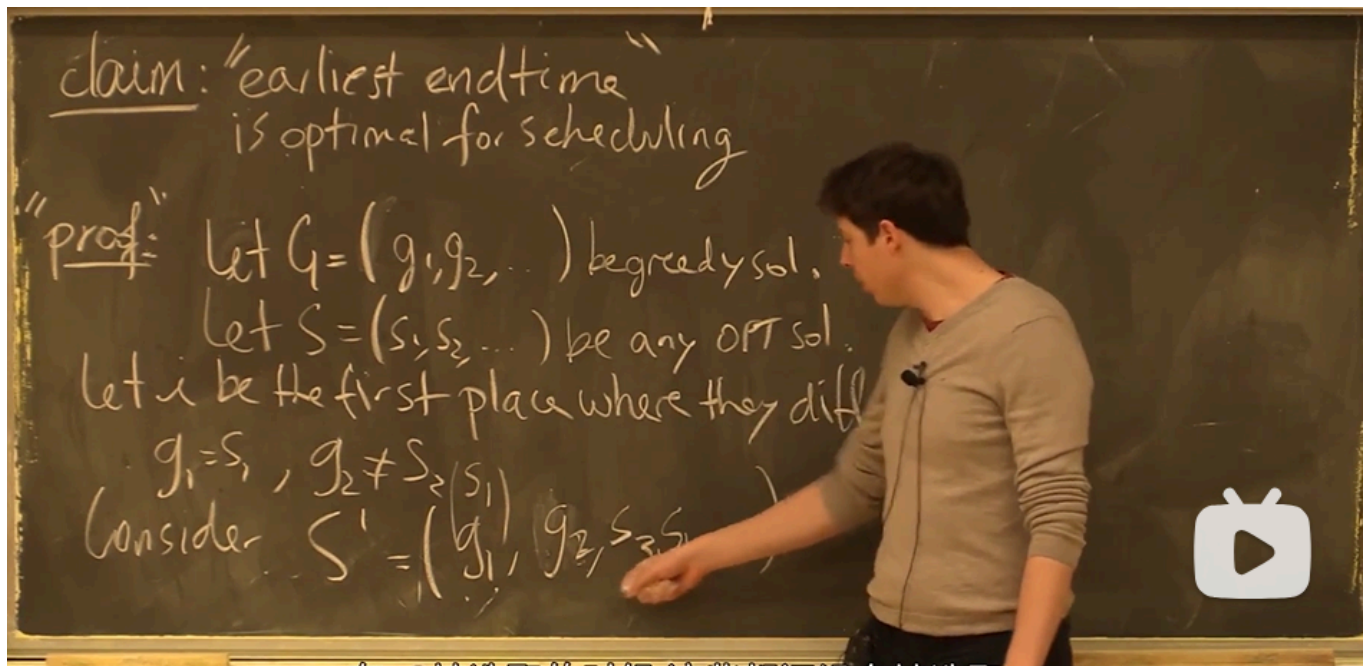
output:  $S \subseteq A$  non-overlapping

goal: maximize  $|S|$

这个问题的经典解法是取尽量多区间  
So the classical interpretation of this one, you know, is trying to take many courses.

way: just sort by endpoint time and pick the earliest not chosen one. (选择最早的未被选择的。)

proof: The main idea is that  $g_n$  will be chosen before  $s_n$ . ( $S$  is a set of optimal set.)



## Set Cover

```
#include<iostream>
#include<vector>
#include<unordered_set>
using namespace std;

//函数用于找到集合覆盖
vector<int> setCover(vector<unordered_set<int>>
&sets, unordered_set<int>&universe)
{
    vector<int> result;
    unordered_set<int> covered;

    while(covered!=universe)
    {
        int bestSet = -1;
        int maxElement = 0;
        for(int i=0; i<sets.size(); ++i)
        {
            unordered_set<int> temp;
            for(int element:sets[i])
            {
                if(universe.count(element)&&!covered.count(element))
                {
```

```

        temp.insert(element);
    }
}
if(temp.size()>maxElement)
{
    maxElement=temp.size();
    bestSet=i;
}
}

if(bestSet==-1)
{
    break;
}

result.push_back(bestSet);
for(int element:sets[bestSet])
{
    covered.insert(element);
}
}

return result;
}

int main()
{
    vector<unordered_set<int>> sets = {
        {1, 2, 3},
        {2, 4},
        {3, 4},
        {4, 5}
    };

    unordered_set<int> universe = {1, 2, 3, 4, 5};
    vector<int> result = setCover(sets, universe);
    cout << "集合覆盖的集合索引: ";
    for (int i : result)

```

```

{
    cout << i << " ";
}
cout << endl;

return 0;
}

```

# MST

## Kruskal Algorithm

[Graph > kruskal Algorithm](#)

## Prim Algorithm

[Graph > Prim Algorithm](#)

## Set\_cover

We have a universe set{1,2,3,4,5}.

We also have some small sets:

{1, 2, 3},

{2, 4},

{3, 4},

{4, 5}

We need choose the least number of small sets to cover the universe set.

```

#include<iostream>
#include<vector>
#include<unordered_set>
using namespace std;

//函数用于找到集合覆盖
vector<int> setCover(vector<unordered_set<int>>
&sets,unordered_set<int>&universe)
{
    vector<int> result;
    unordered_set<int> covered;

    while(covered!=universe)

```

```

{
    int bestSet = -1;
    int maxElement = 0;
    for(int i=0;i<sets.size();++i)
    {
        unordered_set<int> temp;
        for(int element:sets[i])
        {
            if(universe.count(element)&&!covered.count(element))
            {
                temp.insert(element);
            }
        }
        if(temp.size()>maxElement)
        {
            maxElement=temp.size();
            bestSet=i;
        }
    }

    if(bestSet==-1)
    {
        break;
    }

    result.push_back(bestSet);
    for(int element:sets[bestSet])
    {
        covered.insert(element);
    }
}

return result;
}

int main()
{
    vector<unordered_set<int>> sets = {
        {1, 2, 3},

```

```
        {2, 4},  
        {3, 4},  
        {4, 5}  
};
```

```
unordered_set<int> universe = {1, 2, 3, 4, 5};  
vector<int> result = setCover(sets, universe);  
cout << "集合覆盖的集合索引: ";  
for (int i : result)  
{  
    cout << i << " ";  
}  
cout << endl;  
  
return 0;  
}
```