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Solution of Q12.13.3.21

SUJAL GUPTA - EE22BTECH11052

A shopkeeper sells three types of flower seeds A1, A2 and A3. They are sold as a mixture where the proportions are 4:4:2 respectively. The germination rates of the three types of seeds are 0.45, 0.60 and 0.35. Calculate the probability:

- 1) of a randomly chosen seed to germinate
- 2) that it will not germinate given that the seed is of type A_3 ,
- 3) that it is of the type A_2 given that a randomly chosen seed does not germinate.

Solution: Let the two random variables be X and Y for denoting type of seed and germination status.

Variable	Description	Value
X	Type of seed 1: A_1 , 2: A_2 , 3: A_3	{1, 2, 3}
Y	0:germinates, 1:not germinate	{0, 1}

$$p_X(X) = \begin{cases} \frac{4}{10}, & if X = 1\\ \frac{4}{10}, & if X = 2\\ \frac{2}{10}, & if X = 3 \end{cases}$$
 (1)

$$Pr(Y = 0|X = 1) = 0.45$$
 (2)

$$\Pr(Y = 0|X = 2) = 0.60 \tag{3}$$

$$Pr(Y = 0|X = 3) = 0.35 \tag{4}$$

(5)

1)

$$p_Y(0) = \Pr(Y = 0|X = 1) \Pr(X = 1) + \Pr(Y = 0|X = 2) \Pr(X = 2) + \Pr(Y = 0|X = 3) \Pr(X = 3)$$
 (6)

$$=\frac{49}{100}$$
 (7)

$$=0.49$$

2)

$$Pr(Y = 1|X = 2) = 1 - Pr(Y = 0|X = 2)$$
(9)

$$= 1 - 0.35$$
 (10)

$$= 0.65$$
 (11)

3)

$$Pr(X = 2|Y = 1) = \frac{Pr(Y = 1|X = 2) Pr(X = 2)}{Pr(Y = 1)}$$

$$= \frac{(1 - Pr(Y = 0|X = 2)) Pr(X = 2)}{1 - Pr(Y = 0)}$$
(12)

$$= \frac{(1 - \Pr(Y = 0|X = 2)) \Pr(X = 2)}{1 - \Pr(Y = 0)}$$
 (13)

$$=\frac{16}{51}\tag{14}$$