

---

---

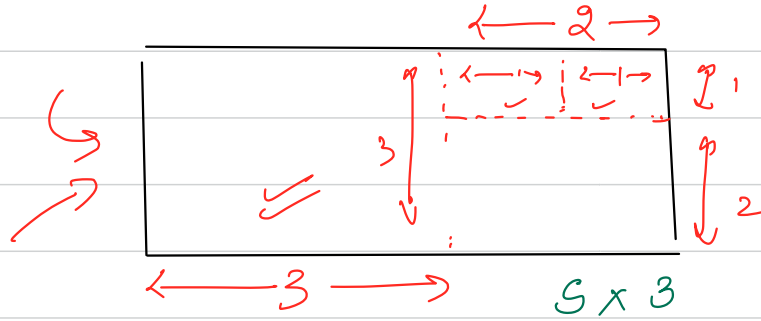
---

---

---

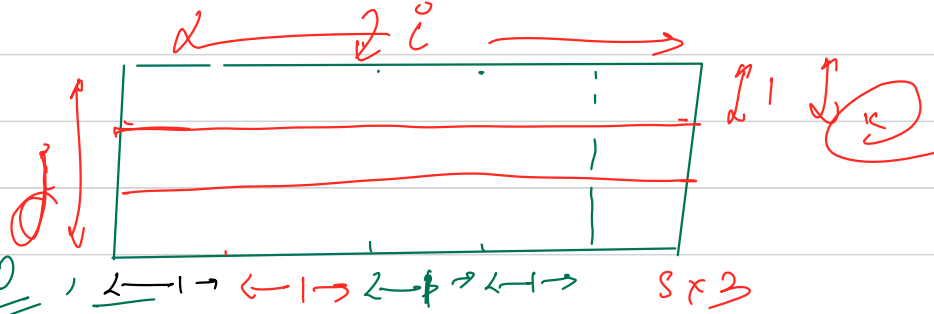


Don't Rectangle  
Cutty



Try all possible cases

$(1 \times 3)$   $(4 \times 3)$   
 $(2 \times 3)$   $(3 \times 3)$   
 $(3 \times 3)$   $(2 \times 3)$   
 $(4 \times 3)$   $(1 \times 3)$



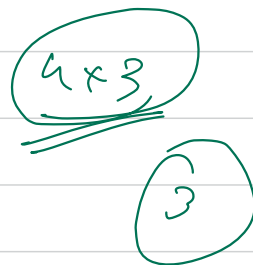
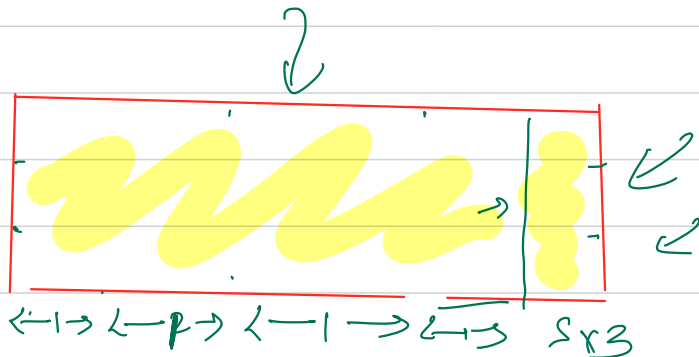
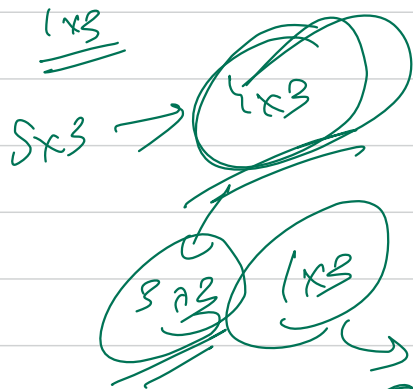
We have choices for cuts both vertically & horizontally

We can add the cuts both horizontally & vertically

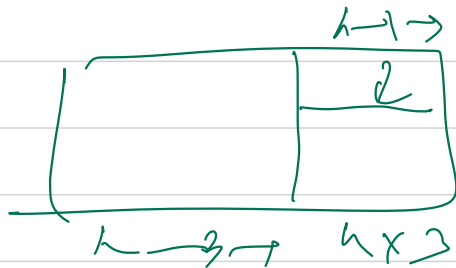
$$f(\underbrace{i, j}_{(x, y)}) = \min \left( \begin{array}{l} \min(f(i, j), 1 + \underbrace{f(i, k)} + \underbrace{f(i, j-k)}) \\ \min(f(i, j), 1 + \underbrace{f(k, j)} + \underbrace{f(i-k, j)}) \end{array} \right)$$

cut horizontally  
 $\forall k \in [1, j-1]$

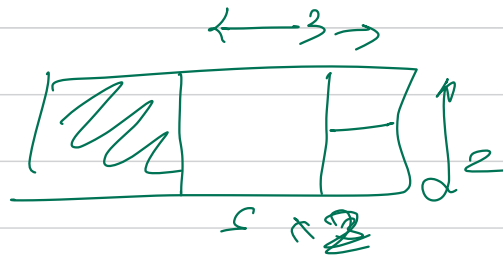
cut vertically  
 $\forall k \in [1, i-1]$



$ans = \underline{9} / \underline{2} \text{ (3)}$



$1 + 5 + 3$   
 $3 + 3 + 1$   
 $0 + 2 + 1$



Q.2

Money Sums

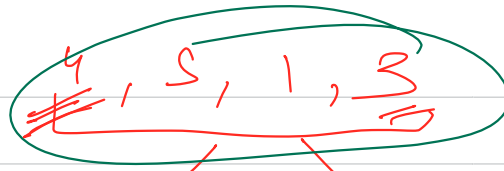
2 2  
4 2 5 2

1.

(4, 6, 2) 9, 11, 7, 5

4, 6, 2, 9, 11, 7, 5, 8, 13

→ 9

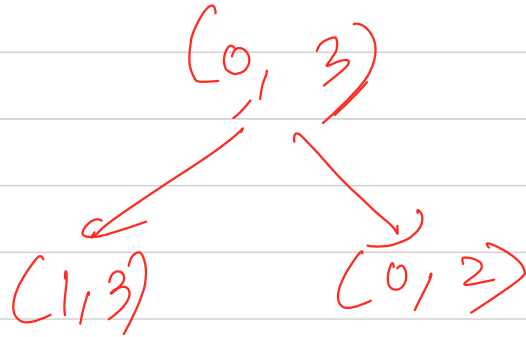


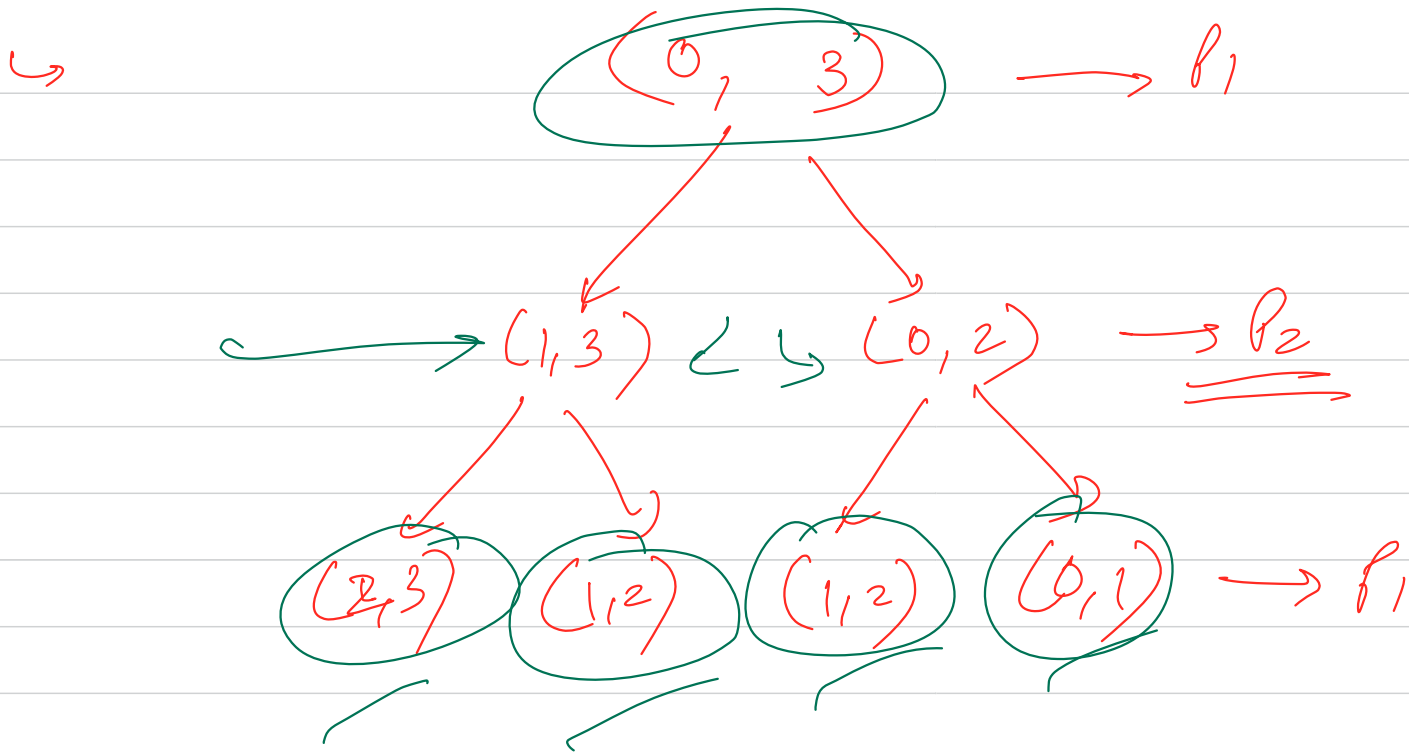
P<sub>1</sub>

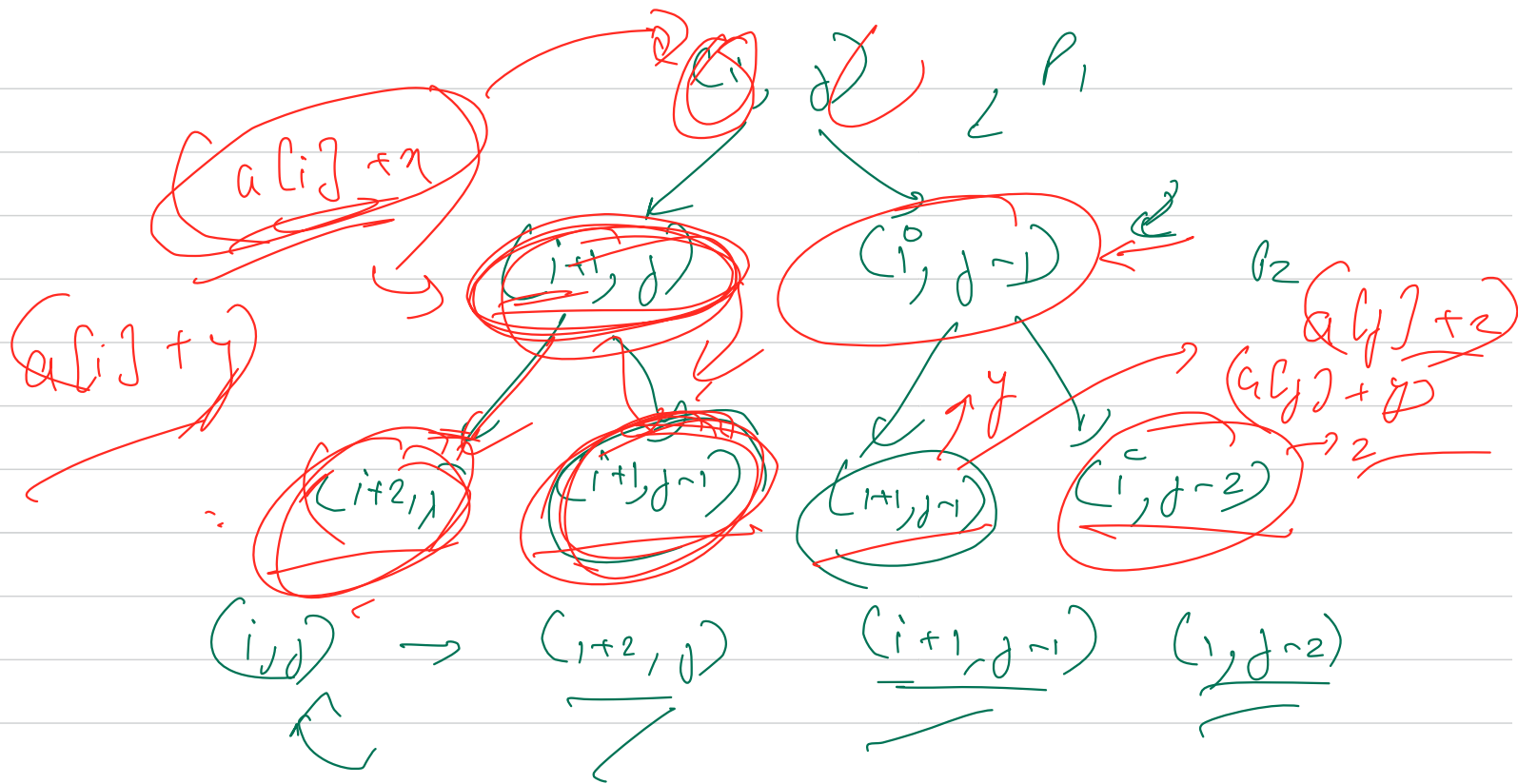
[5, 1, 3]

[4, 5, 1]

← P<sub>2</sub>

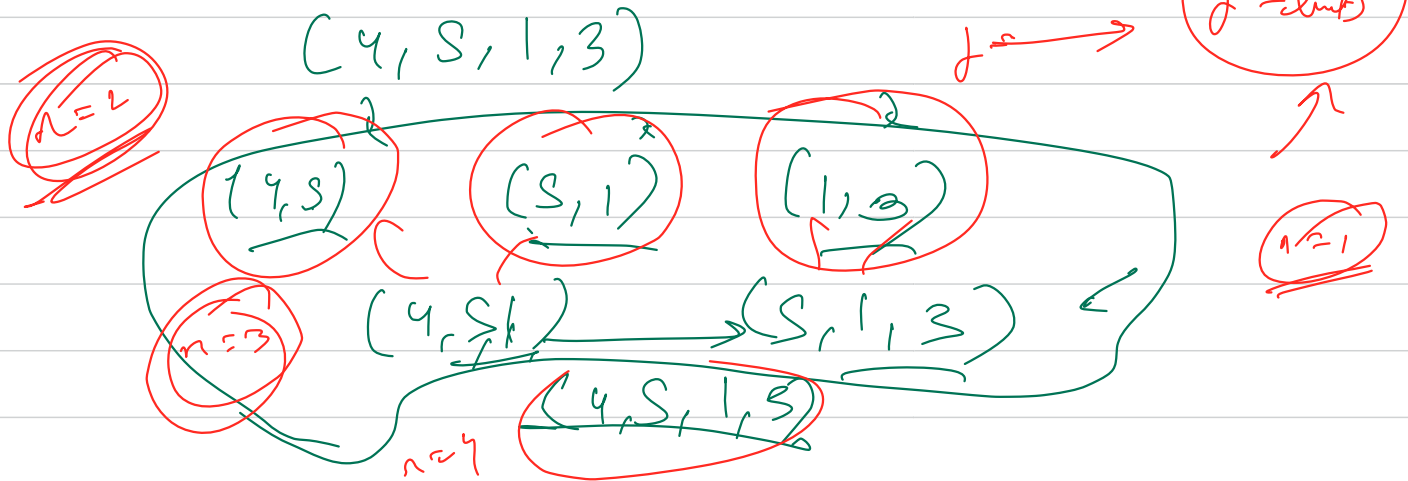








$$f(i, j) = \max \left( \min \left( \begin{aligned} & \overbrace{a[i] + f(i+2, j)}^{\text{min}}, \overbrace{a[i] + f(i+1, j-1)}^{\text{min}}, \overbrace{a[j] + f(i, j-2)}^{\text{min}}, \\ & \overbrace{a[j] + f(i+1, j-1)}^{\text{min}} \end{aligned} \right), \overbrace{a[j]}^{\text{min}} + f(i, j-2) \right)$$



{ 1, 2, 3, 4, 5 }  $\rightarrow$  { 5 }

Sum/2

$\sum_{i=1}^n i \rightarrow$  is odd no

cur

$\rightarrow$  Sum of elements is equal to

of subset

Sum/2

$\uparrow$

Knapsack

$$f(i, j) = f(i-1, j) + f(i-1, j-i)$$

Diagram illustrating the recurrence relation for the number of ways to reach a sum  $j$  using elements from an array. The function  $f(i, j)$  is defined as the sum of the number of ways to reach  $j$  using the first  $i-1$  elements, and the number of ways to reach  $j-i$  using the first  $i-1$  elements.

$j \rightarrow \text{sum}$

$i \rightarrow \text{no. of elements}$   
observed

count in ways

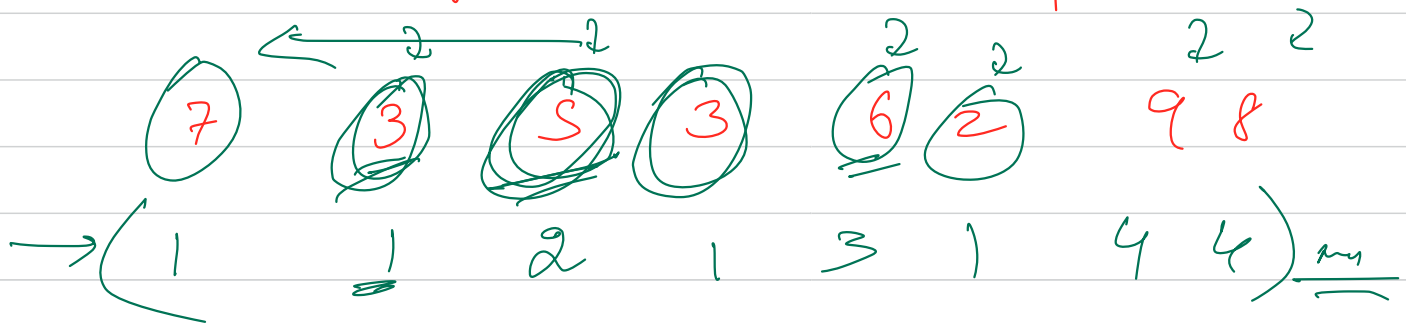
every element has 2 choices  
 add / avoid

<sup>1</sup>2   <sup>2</sup>3   <sup>2</sup>5   <sup>2</sup>3   <sup>2</sup>6   <sup>2</sup>2   <sup>2</sup>9   <sup>2</sup>8  
 2, 3, 5, 3, 6, 2, 9, 8

Qp

$f(i)$

length of longest inc subseq ending at i



7 9  
 3 9

3, 6  
 3, 5, 6 → 3  
 3, 6

3, 5, 9 →  
 3, 9  
 3, 5, 6, 9  
 2, 9

4

For every elms, iterate from 0 to i

$$\downarrow \underline{f(i)} = 1 + f(j) \quad \forall j \in [0, i-1] \text{ \& } a[j] < a[i]$$

$$\text{LIS}(0, n-1) = \max f(i) \quad \forall i \in [0, n-1]$$

$$\underline{\text{TC}} \rightarrow \underline{O(n^2)}$$

$$\underline{O(n \log n)}$$

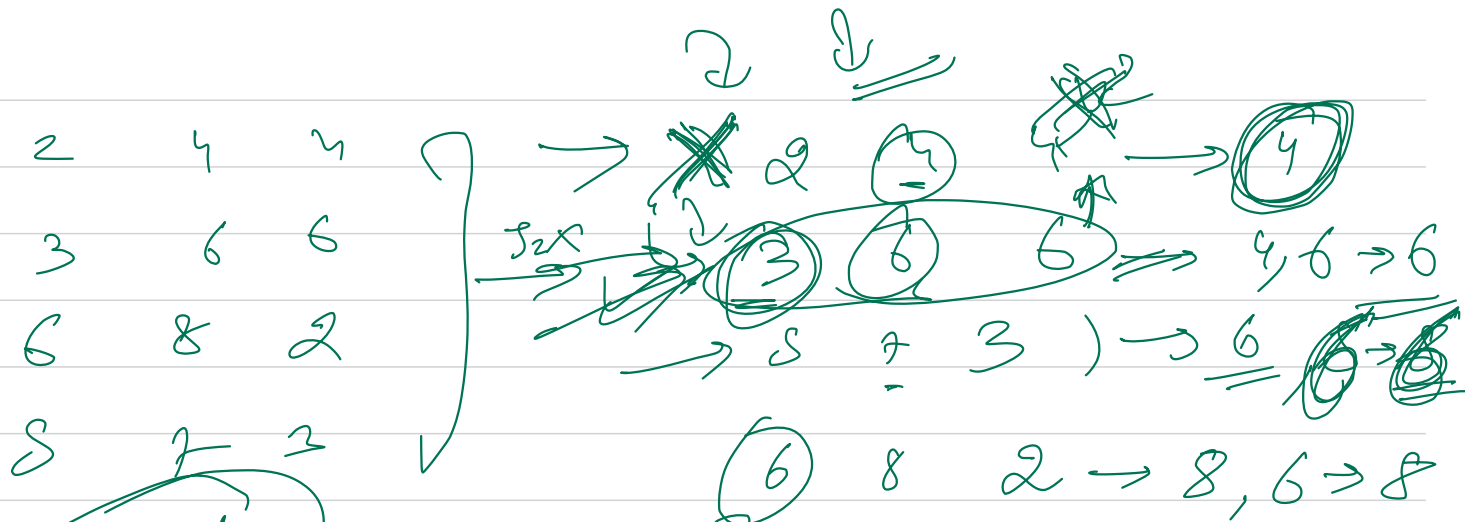
Binary Search  
Segment Tree

→ sort the array based on end  $\swarrow$   
 $\nwarrow$

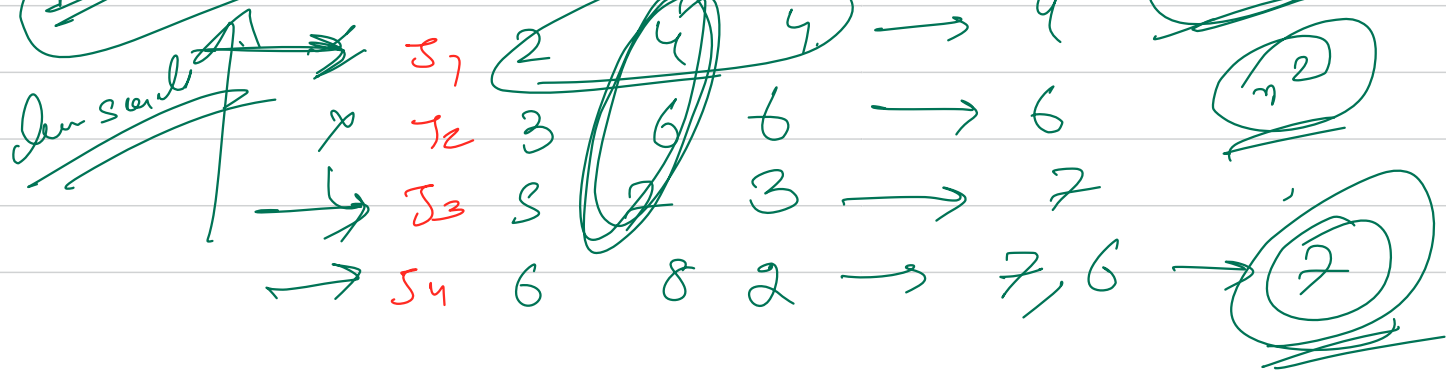
→ for any  $i^{\text{th}}$  job → we can either pick it  
or leave it

pick → check all  $(0-i-1)$  jobs

end < starts



Binary Search



$n \log n$

$n^2$