

Data Structure

Array → Algorithms

↓

Data Structure

↓

Divide & conquer

1) Linear

2) Non-Linear

↳ Recursion

collections of items in a contiguous manner.

Student marks (100) array → index

1000 → Base address 1012

arr[8]

↓ ↓ 47

85	75	70	65	98	99	50	33	47	77
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0 1 2 3 4 5 6 7 8 9

↓ 1004 1008 1016 - - - - - -

index

m = 10

int → 4 Bytes

Last index = 9

i

Address of 9th index

$$1000 + (9 - 0) * 4$$

→ Base address

$$1000 + 36 = 1036$$

+

(i - Lower Bound) *

(16 Digits)

Hexadecimal → (0 - 9, A - F)

Size of each element

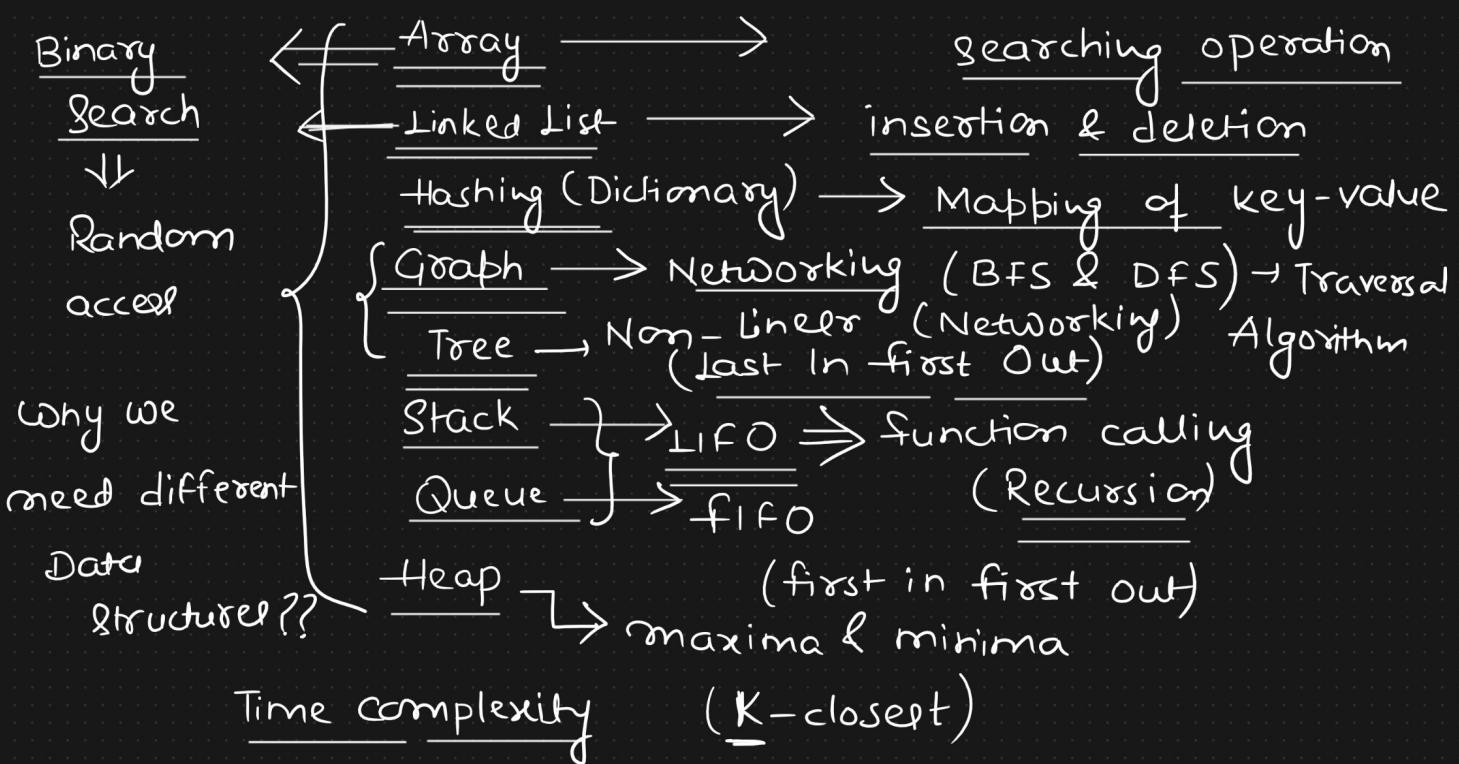
array[7]

33

→ Random access

↓

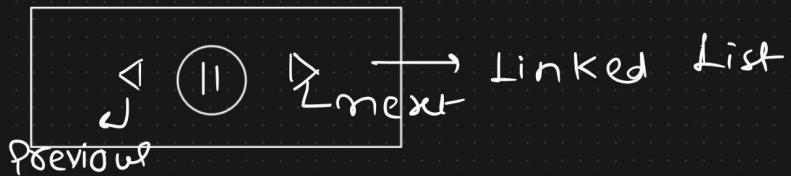
O(1) → constant time complexity



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↳ Post → 7600 followers

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array 1

0	1	2	3
20	45	27	47

range → 0 to n-1

Searching

4	5	6	7	8
55	67	75	88	90

$x = 67$ Output = 5

n = 9

Linear

Search

```

    {   for i in range(0, n):
        if arr(i) == x:
            return i
    return -1
  
```

Pseudocode

$$T(n) = O(n)$$

↳ Worst case (Element present near to last index)

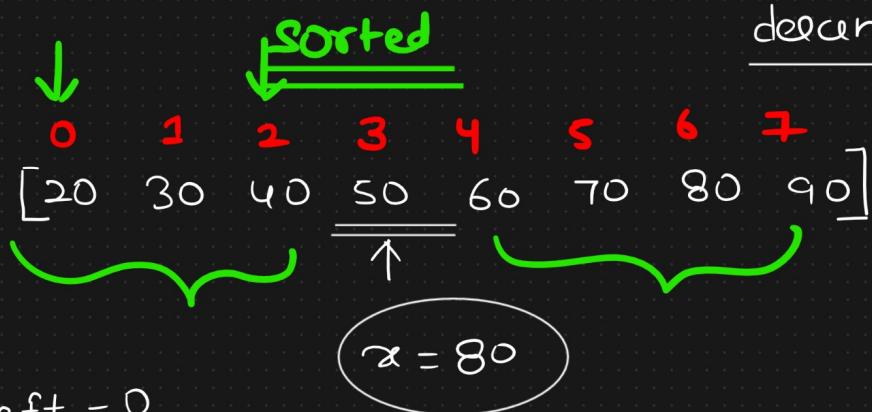
Best case → O(1)

↳ (Element present near to the first index)

$$\text{Average case} \rightarrow \frac{1}{2} \cdot \frac{\text{Worst case}}{O(n)} + \frac{1}{2} \cdot \frac{\text{Best case}}{O(1)}$$

$$\Rightarrow O(n)$$

Binary Search
 ↳ sorted array
 ↓



ascending order or

descending order

$$\begin{aligned}
 \text{arr}(\text{mid}) &= 50 \\
 \alpha &= 80 \\
 \underline{\underline{\alpha = 30}}
 \end{aligned}$$

$\text{left} = 0$

$\text{right} = 7$

$$\underline{\underline{\text{mid} = \frac{0+7}{2} = 3 \text{ (Lower Bound)}}}$$

binarySearch(arr, left, right):

while $\text{left} < \text{right}$:

if $\text{arr}(\text{mid}) == \alpha$:

return mid

$50 < 80$

↑ Recursion

elif $\text{arr}(\text{mid}) < \alpha$: binarySearch(arr,

$\underline{\underline{\text{left} = \text{mid} + 1}}$

$\underline{\underline{\text{mid} + 1, right}})$

↑ $\text{arr}(\text{mid}) > \alpha$:

else:

$\underline{\underline{\text{right} = \text{mid} - 1}}$

return -1

binarySearch(arr, left, mid-1)

Recursion

↳ calling the same function

again inside the

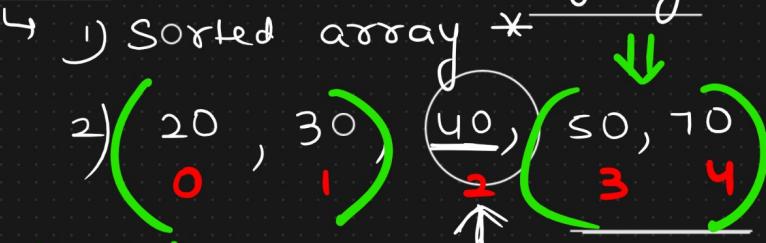
method definition

Note

$x = 20$

$\{ i = 0$
 $j = 4 \}$

Sorted array



(Logically)

$x = 50$

$$\text{mid} = (i + j)/2 = 2$$

binarySearch(arr, 0, 4) 50 == 50

while i <= j : arr(mid) == x :

40 == 50 X

return mid

Pseudocode

Binary

Left

Right

arr(mid) < x :

40 < 50

right

binarySearch(arr, 3, 4)

arr(mid) > x :

binarySearch(arr, 0,

left

$$\text{mid} = (3+4)/2 = 3$$

i → starting index, j → ending index

Preferable

$$\text{mid} = i + (j-i)/2$$

$$= 3 + 1/2$$

$$\Rightarrow 3$$

$$\text{mid} = (i+j)/2$$

$$\text{mid} = (3+4)/2$$

$$= 7/2 = 3$$

$$i = 3$$

$$j = 4$$

binarySearch(arr, 0, 4)



binarySearch(arr, 3, 4)

mid = 3

result → 3

i = 1, arr, mn

4, ∞, ∞

J = 4, ∞, ∞

(i + J) / 2

mid = 5, ∞, ∞

2

mid =

1, ∞, ∞ + 3 ∞ % 2

if $i = j$: \Rightarrow only one element
if $arr(i) = x$:
 return i
else:
 return -1
Termination Condition

else:
Recursive call

T(n) Recurrence Relation

↳ binarySearch(arr, i, j, x):

 while $i \leq j$:

$$\quad \quad \quad \underline{mid = i + (j-i)/2} \rightarrow c$$

$$\quad \quad \quad \text{if } arr(\text{mid}) == x: \rightarrow c$$

 return mid

 elif $arr(\text{mid}) < x$:



binarySearch(arr, mid+1, j, x)

$$\underline{T(m/2)}$$

 else: OR

binarySearch(arr, i, mid-1, x)



 return -1

Binary Search Algorithm

$$T(n) = T(m/2) + c$$

Substitution
Method

Marks:-

Theorem

$$T(n) = 2T(m/2) + c$$

$$a=1 \quad k=0$$

$$b=2$$

$$p=0$$

$$\log_b a = \log_2 1 = 0$$

$$\begin{array}{l}
 \text{case 2} \quad \Rightarrow \quad \log_b^a = k \\
 \underline{\qquad\qquad\qquad} \quad \underline{\qquad\qquad\qquad} \quad \underline{\qquad\qquad\qquad} \\
 p > -1 \quad \Rightarrow \quad \Theta(n^k \log^{p+1} n) \\
 \underline{\qquad\qquad\qquad} \quad \underline{\qquad\qquad\qquad} \\
 \Theta(\log n)
 \end{array}$$

Substitution

$$\begin{aligned}
 T(n) &= T\left(\frac{n}{2}\right) + c \\
 &= T\left(\frac{n}{2^2}\right) + c + c = T\left(\frac{n}{2^2}\right) + 2c \\
 &= T\left(\frac{n}{2^3}\right) + 3c
 \end{aligned}$$

$$\frac{n}{2^k} = 1 \quad \downarrow \quad \text{k times}$$

$$k = \log_2 n \Rightarrow T\left(\frac{n}{2^k}\right) + k \cdot c$$

$$= T\left(\frac{n}{2^{\log_2 n}}\right) + c \cdot \log_2 n$$

$$= T\left(\frac{n}{n}\right) + c \cdot \log_2 n$$

$$\Rightarrow \Theta(\log_2 n)$$