Assignment 14 – Data Structures

Questions: 7, 8

Submission Deadline: May 3, 2025

Assignment Weight: 2%

Question 1 (32 points – 8 for each)

The array PARTITION contains the following values:

PARTITION:

Index: 0 1 2 3 4 Value: A B A B A

You are required to answer the following questions:

- a. What does the array rpA look like after applying the PARTITION algorithm?
- **b.** What is the purpose of the **QUICKSORT** algorithm in general?
- c. What is the role of the PARTITION procedure within the QUICKSORT algorithm?
- **d.** What is the time complexity of the **QUICKSORT** algorithm in the best-case, worst-case, and average-case scenarios?

Question 2 (36 points – A:16p, B:8p, C:12p)

You are given three sorted arrays in ascending order, each of size n, which contain only natural numbers (positive integers) — no duplicates within each individual array.

- Suggest an efficient algorithm for finding a number that appears in all three arrays (i.e., a common element).
- What is the time complexity of your suggested algorithm?
- Is it possible to achieve better complexity?

Please explain your answer.

Question 3 (10 points)

Regarding the array:

```
A = (3, 7, 8, 1, 8, 3, 9, 1, 8, 7, 8)
```

- a. Demonstrate the operation of the COUNTING-SORT algorithm on the array A.
- Show the contents of the array c at the beginning of executing line 6 in the subroutine (as appears on page 161).
 - Show the contents of the array c at the beginning of executing line 9.
 - Show the contents of the array $\[\mathbf{B} \]$ at the end of executing the subroutine.

Note: In line 9 of the **COUNTING-SORT** subroutine (as appears on page 140 of the textbook), the for loop is defined as follows:

for
$$j \leftarrow 1$$
 to length[A]

Show that the algorithm still functions correctly.

b. Is the algorithm still stable after this change? Justify your answer.