

Chile Labor Force-Real World Time Series Analysis

Oguzhan Gurbuz

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#The labor force participation rate can be defined as “an estimate of an economy's active workforce” (Investopedia). The formula is the number of people ages 16 and older who are employed or actively seeking employment, divided by the total non-institutionalized, civilian working-age population. #It is important to understand this rate since it yields a strong clue about the country's economy.

#Labor Force Participation Rate = (Number Employed+Number Seeking Work) × 100 / Civilian Non-Institutional Population

#In this time series analysis, we're going to analyse the labor force participation rate trend of a developing country in the Global South, Chile, having a population of 19,5 million according to the World Bank. The main goal of this analysis is to see the current pattern of the country's labour force participation rate and forecast the next 6 years.

#The data I collected from the World Bank has a time period of 30 years between 1990 and 2019. We're going to forecast the value for the next 6 years between 2020 and 2025. This will be possible by using three forecast methods, namely, the Box-Jenkins or ARIMA (Autoregressive Integrated Moving Average), Holt's linear trend and Holt-Winter damped methods.

```
#Let's install the necessary packages
#install.packages("fpp")
#install.packages("forecast")
#install.packages("ggplot2")
```

```
#Let's load the necessary packages.
library(readxl)
library(forecast)
```

```
## Registered S3 method overwritten by 'quantmod':
##   method           from
##   as.zoo.data.frame zoo
```

```
library(ggplot2)
library(fpp)
```

```
## Loading required package: fma
```

```
## Loading required package: expsmooth
```

```
## Loading required package: lmtest
```

```
## Loading required package: zoo
```

```
##  
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':  
##  
##      as.Date, as.Date.numeric
```

```
## Loading required package: tseries
```

#PREPARING AND EXPLORING THE DATA

```
#First, we need to load the dataset and assign to "chile_data".  
chile_data <- read_excel("Chile Labor Force Participation Rate.xlsx")
```

```
#What's the class of the Chile data set.  
class(chile_data) #It's a data frame.
```

```
## [1] "tbl_df"      "tbl"        "data.frame"
```

```
#Let's add a name to top of the data  
names(chile_data) <- c("Labor Force Participation Rate")  
chile_ts <- ts(chile_data, start = 1990, end = 2019, frequency = 1)
```

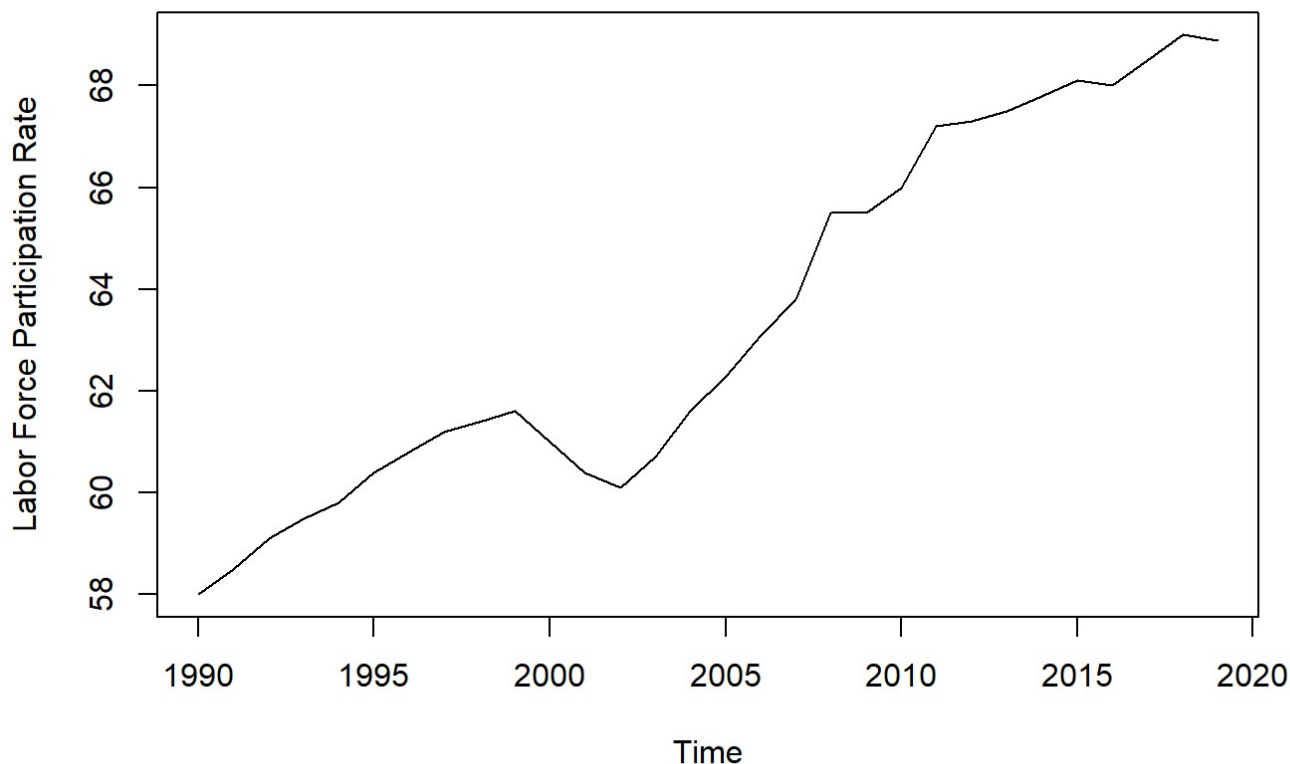
```
#Let's see a few observations from the dataset.  
head(chile_ts)
```

```
## Time Series:  
## Start = 1990  
## End = 1995  
## Frequency = 1  
##      Labor Force Participation Rate  
## [1,]                               58.0  
## [2,]                               58.5  
## [3,]                               59.1  
## [4,]                               59.5  
## [5,]                               59.8  
## [6,]                               60.4
```

```
#Summary of the data  
summary(chile_data)
```

```
## Labor Force Participation Rate  
## Min.      :58.00  
## 1st Qu.:60.48  
## Median :61.95  
## Mean      :63.42  
## 3rd Qu.:67.28  
## Max.      :69.00
```

```
#We can plot the data and see how it increased in time.  
plot(chile_ts)
```



#Based on the plot, we can say the labor force participation rate data set seems trending, but apparently, there is no seasonality. That means the Holt function for a linear trend model will be a good one to forecast.

#Holt Linear and Holt-Winter's Models

#Let's set up a linear trend model for the Chile labor participation time series. We can use the holt() function, being a component of the forecast package. The argument h is used to specify the forecast length. For the first observation, let's go with 10 (h = 10). In other words, that is a forecast of 10 years into the future.

```
# Exponential smoothing with holt-trend
```

```
holt.linear = holt(chile_ts, h = 10)
```

```
summary(holt.linear)
```

```
##
## Forecast method: Holt's method
##
## Model Information:
## Holt's method
##
## Call:
## holt(y = chile_ts, h = 10)
##
## Smoothing parameters:
##   alpha = 0.9999
##   beta  = 0.4021
##
## Initial states:
##   l = 57.5226
##   b = 0.4805
##
## sigma: 0.5106
##
##      AIC      AICc      BIC
## 67.41627 69.91627 74.42226
##
## Error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -0.02438653 0.4753705 0.3501402 -0.03513517 0.5468293 0.7100745
##              ACF1
## Training set 0.05602751
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## 2020      69.08635 68.43195 69.74075 68.08553 70.08717
## 2021      69.27265 68.14573 70.39958 67.54917 70.99614
## 2022      69.45895 67.82686 71.09105 66.96288 71.95503
## 2023      69.64526 67.46626 71.82425 66.31277 72.97774
## 2024      69.83156 67.06366 72.59946 65.59842 74.06469
## 2025      70.01786 66.62051 73.41521 64.82207 75.21365
## 2026      70.20416 66.13863 74.26970 63.98646 76.42186
## 2027      70.39046 65.61976 75.16116 63.09431 77.68662
## 2028      70.57677 65.06556 76.08797 62.14810 79.00543
## 2029      70.76307 64.47748 77.04865 61.15010 80.37604
```

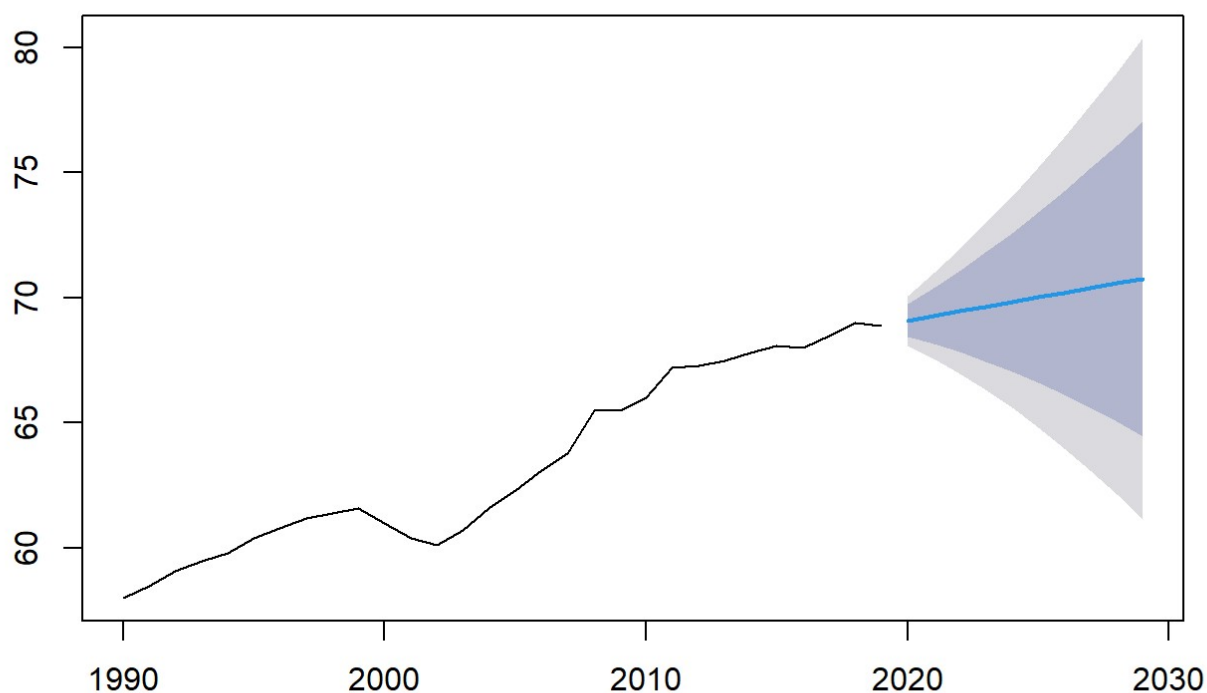
#When we look at the values from the summary, we get the values for the alpha and beta parameters, alpha is 0.999 and beta is 0.402. This shows the trend (the slope of the time series plot) is fairly constant throughout. Here, alpha and beta needs further investigation:

#Alpha(α): The Level component smoothing parameter is Alpha specifying the weight attributed to the most recent data in the prediction (the year of 2019). A value close to 1 highlights the most recent observation, whereas a value close to 0 highlights past observations. In this case, alpha is 0.9999, suggesting that the model gives the most recent observation virtually full weight.

#The Beta (β) smoothing parameter for the slope component changes the weight assigned to the most recent forecast error in the prediction. A value close to 1 emphasizes the most recent prediction mistake, whereas a value close to 0 emphasizes previous forecast errors. In this case, beta is 0.4021, showing the model prioritizes earlier forecast errors above the most recent forecast error.

#Let's see the plot of the Holt linear model to visualize the pattern.
`plot(holt.linear)`

Forecasts from Holt's method



#The line in blue is the forecasted ten years 2020 to 2029. And the light and dark shaded zones are the confidence intervals with the 80 and 95% confidence. We can also see that the slope of the forecasted period is nearly the same as with the period between 2010 and 2020 and between 1990 and 2000. This simply means the model takes a trend slope of at least the last 10 years.

#Of course, the level value is added to this slope to get the corresponding forecasted value. But let's go back to the summary output. Under initial states, we get the values for the slope and the level value. These values are used together with the smoothing parameters in the initial level and slope equations. To calculate the first forecasted observation, we get information criteria for the model as well as arrow measures, and we get the forecast points and the confidence intervals which are used in the plot.

#One of the problems in the data is the trend. It is not realistic and the trend cannot continue indefinitely. I mean, for a country's labor force participation rate, it's not possible to converge to the level of 100%. There will always be people unwilling to participate in the labor market. That means the curve will likely flatten out in the range of 90%.

#We can do this with the Holt function using the damped argument. A damped Holt linear trend model assumes that the trend cannot be constant forever. Using this model, we suggest growth needs to come to an end at some point. The curve needs to flatten out. Here the damping parameter ϕ comes into play. Let's first have a look at the formula:

Forecasting formula = $yt+h|t = l + hbt$

Damped forecasting formula = $yt+h|t = l + (\phi + \phi^2 + \phi^3 + \dots + \phi^h)bt$

$0 < \text{Damping parameter } \phi < 1$

#If ϕ is one, it is the same as a standard Holt linear model, whereas when ϕ is close to 0, the curve gets flat fairly soon. In practice, the parameter ϕ is set somewhere between 0.8 and 0.98. Using a ϕ at around 0.8, we make sure that short run forecasts still contain the trend, whereas the longer forecast legs are at a flat curve, we can easily adjust our whole model with a damping parameter.

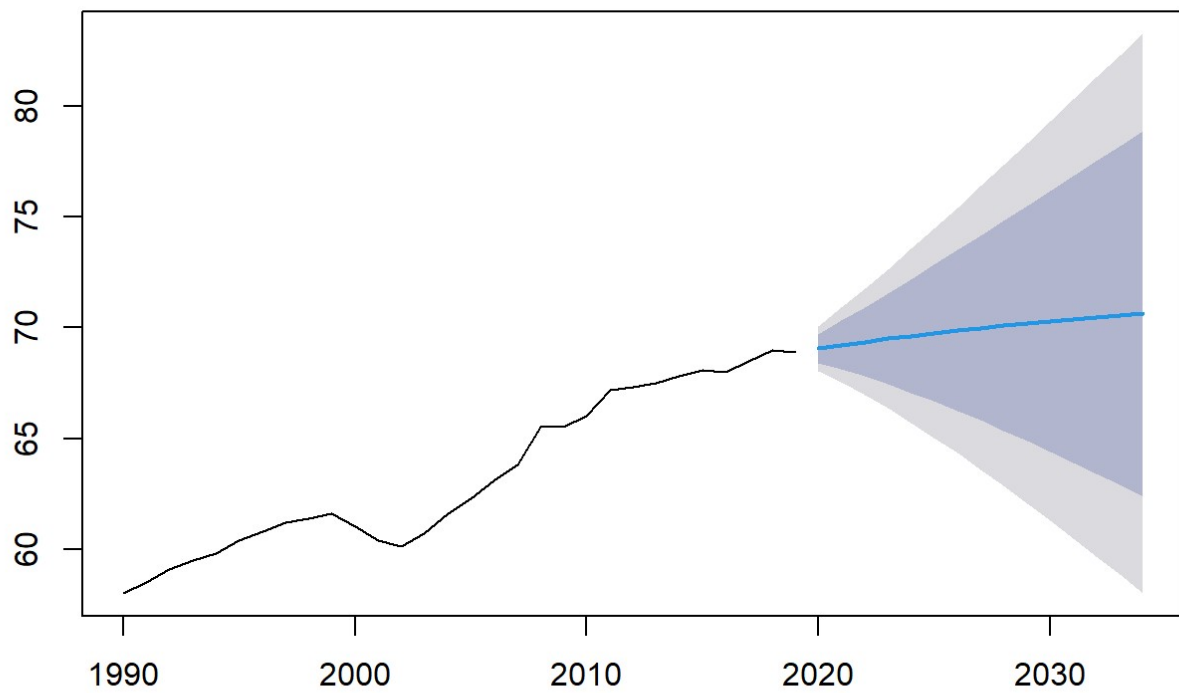
#Let's also have a look at the values, l and b . The initial level ($l = 57.5226$) and initial slope ($b = 0.4805$) are the starting values that the Holt's method uses to generate its forecast. The accuracy of the forecast is influenced by the initial level and slope. These values are estimated based on the historical data and are used to calculate the first forecasted value. The level refers to the baseline value or average value of the series, while the slope represents the rate of change over time. The level and slope values determine the overall shape and direction of the forecast. If the level is high, the forecasted values will tend to be higher, while a low level will result in lower forecasted values. The slope determines the rate of change of the series over time. A positive slope means that the series is increasing, while a negative slope means that it is decreasing.

#To show such a Holt model with a damping parameter, I will directly plot the Holt model with $h=15$. So that the flat or damped curve gets optimally visualized. The code itself is the same as with a standard Holt model. However, you need to set damped to "TRUE" or "T" that we are just going to select the best suitable parameter ϕ for you.

ϕ auto generated

plot(holt(chile_ts, h = 15, damped = T))

Forecasts from Damped Holt's method



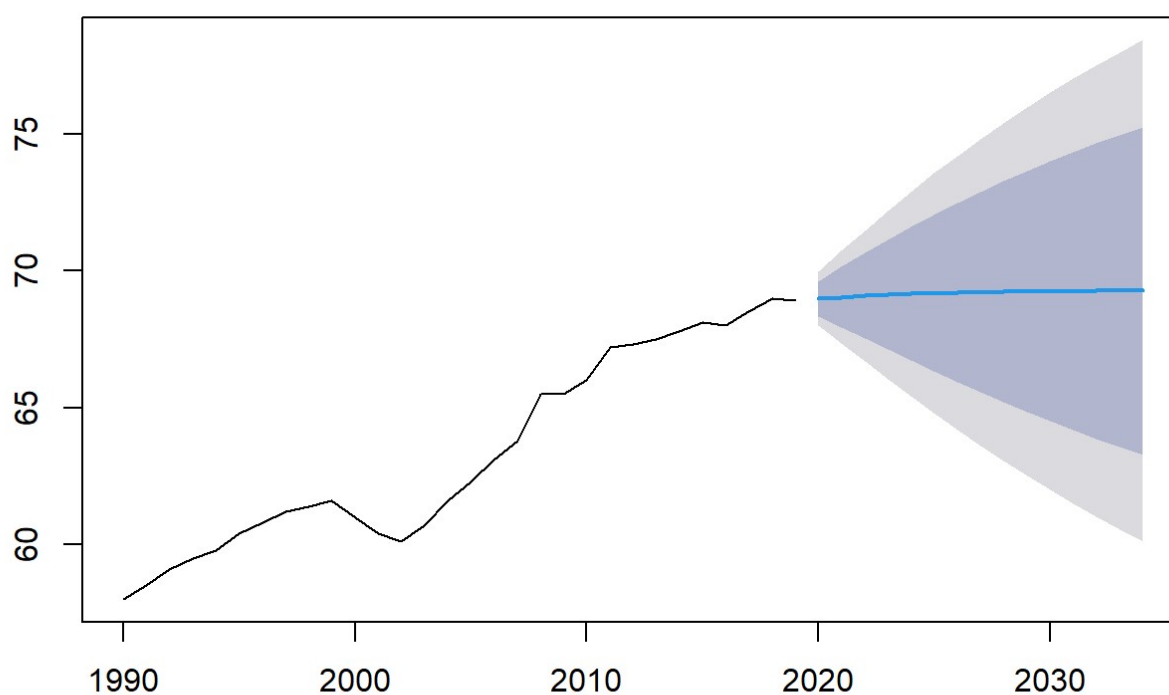
```
# To see the generated value for  $\phi(\varphi)$   
summary(holt(chile_ts, h = 15, damped = T))
```

```
##
## Forecast method: Damped Holt's method
##
## Model Information:
## Damped Holt's method
##
## Call:
## holt(y = chile_ts, h = 15, damped = T)
##
## Smoothing parameters:
##   alpha = 0.9999
##   beta  = 0.3769
##   phi   = 0.9507
##
## Initial states:
##   l = 57.3834
##   b = 0.3774
##
## sigma: 0.512
##
##      AIC      AICc      BIC
## 68.39650 72.04868 76.80369
##
## Error measures:
##
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.03037541 0.4673593 0.3463455 0.05159627 0.5428329 0.702379
##
##              ACF1
## Training set 0.05511592
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## 2020      69.06198 68.40587 69.71809 68.05855 70.06542
## 2021      69.21593 68.10933 70.32253 67.52353 70.90833
## 2022      69.36228 67.79165 70.93290 66.96022 71.76434
## 2023      69.50141 67.44523 71.55758 66.35676 72.64605
## 2024      69.63367 67.07132 72.19602 65.71489 73.55244
## 2025      69.75940 66.67276 72.84605 65.03879 74.48002
## 2026      69.87893 66.25255 73.50531 64.33286 75.42500
## 2027      69.99256 65.81350 74.17162 63.60124 76.38388
## 2028      70.10059 65.35814 74.84304 62.84763 77.35354
## 2029      70.20328 64.88869 75.51787 62.07532 78.33124
## 2030      70.30091 64.40716 76.19465 61.28720 79.31461
## 2031      70.39372 63.91530 76.87213 60.48584 80.30159
## 2032      70.48194 63.41468 77.54921 59.67350 81.29039
## 2033      70.56582 62.90668 78.22496 58.85218 82.27946
## 2034      70.64555 62.39253 78.89857 58.02365 83.26746
```

Here the $\phi = 0.9507$: It is close to 1, meaning the damping component is highly persistent. This implies that the trend component may change slowly over time. Let's change it manually to 0.8.

```
# Manual setting of phi
plot(holt(chile_ts, h = 15, damped = T, phi = 0.8))
```


Forecasts from Damped Holt's method



#Simple Exponential Smoothing Method (SES)

#We can apply the SES method if it's non-stationary. Let's apply a ADF test and see the stationarity:

adf.test(chile_ts) #Because the p-value is greater than 0.05, we cannot reject the alternative hypothesis and the time series seems to be non-stationary.

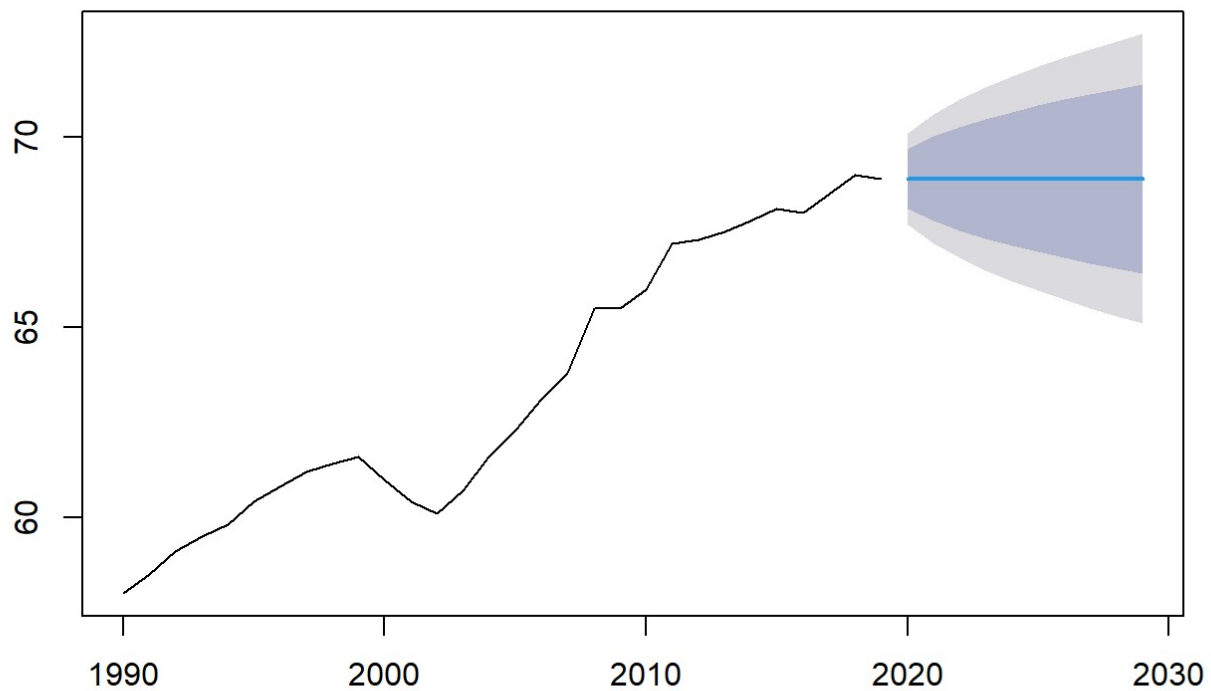
```
##
## Augmented Dickey-Fuller Test
##
## data:  chile_ts
## Dickey-Fuller = -2.7818, Lag order = 3, p-value = 0.2723
## alternative hypothesis: stationary
```

```
#SES Method
ses.model = ses(chile_ts, h = 10)
summary(ses.model)
```

```
##
## Forecast method: Simple exponential smoothing
##
## Model Information:
## Simple exponential smoothing
##
## Call:
## ses(y = chile_ts, h = 10)
##
## Smoothing parameters:
##   alpha = 0.9999
##
## Initial states:
##   l = 58.0002
##
##   sigma: 0.6139
##
##       AIC      AICc      BIC
## 76.68724 77.61032 80.89083
##
## Error measures:
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.3633638 0.5930491 0.4767109 0.5697154 0.7542966 0.9667563
##               ACF1
## Training set 0.2977159
##
## Forecasts:
##      Point Forecast      Lo 80      Hi 80      Lo 95      Hi 95
## 2020      68.90001 68.11331 69.68671 67.69686 70.10316
## 2021      68.90001 67.78751 70.01251 67.19858 70.60144
## 2022      68.90001 67.53750 70.26252 66.81623 70.98379
## 2023      68.90001 67.32673 70.47329 66.49389 71.30613
## 2024      68.90001 67.14104 70.65898 66.20990 71.59012
## 2025      68.90001 66.97316 70.82686 65.95315 71.84687
## 2026      68.90001 66.81878 70.98124 65.71704 72.08298
## 2027      68.90001 66.67509 71.12493 65.49728 72.30274
## 2028      68.90001 66.54012 71.25990 65.29088 72.50914
## 2029      68.90001 66.41247 71.38755 65.09565 72.70437
```

```
plot(ses.model)
```

Forecasts from Simple exponential smoothing



#ARIMA Model

#ARIMA or a form of the Box-Jenkins model is a standard modelling system for time series. ARIMA models are flexible and very general. The random walks, exponential smoothing or autoregressive models can all be explained with that system of ARIMA.

#The most important thing to keep in mind is the trend of the data set. There is a trend in the time series meaning the autocorrelation is present. This implies that an observation at an earlier time point influences the later observations. The values tend to increase or decrease over time. Since this is a yearly data set without season, a standard ARIMA model is suitable to create a model.

Auto Generated ARIMA

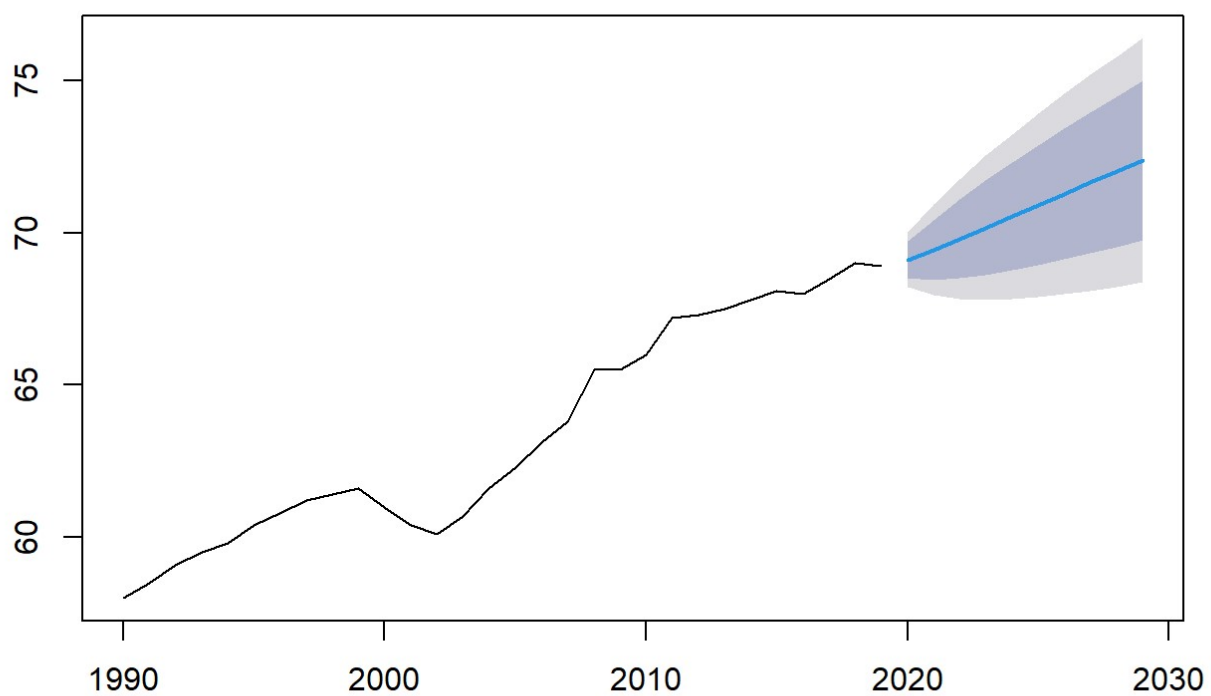
```
arima.chile = auto.arima(chile_ts)
```

```
summary(arima.chile)
```

```
## Series: chile_ts
## ARIMA(1,1,0) with drift
##
## Coefficients:
##          ar1    drift
##          0.3114  0.3705
## s.e.    0.1758  0.1189
##
## sigma^2 = 0.2152: log likelihood = -17.88
## AIC=41.77   AICc=42.73   BIC=45.87
##
## Training set error measures:
##              ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.0003628838 0.4401274 0.3230306 -0.0001701745 0.5057719 0.655097
##              ACF1
## Training set -0.0004546612
```

```
plot(forecast(arima.chile, h = 10))
```

Forecasts from ARIMA(1,1,0) with drift



```
# Exact calculation of ARIMA parameters
auto.arima(chile_ts, stepwise=F, approximation=F)
```

```
## Series: chile_ts
## ARIMA(1,1,0) with drift
##
## Coefficients:
##          ar1    drift
##      0.3114  0.3705
## s.e.  0.1758  0.1189
##
## sigma^2 = 0.2152: log likelihood = -17.88
## AIC=41.77   AICc=42.73   BIC=45.87
```

#The first coefficient, ar1, represents the AutoRegressive (AR) term, and it measures the influence of past values on the current value of the time series. In this case, the estimated value of ar1 is 0.3114, which means that past values of the time series have a positive impact on the current value. The standard error of the ar1 coefficient, 0.1758, indicates the uncertainty in the estimated value.

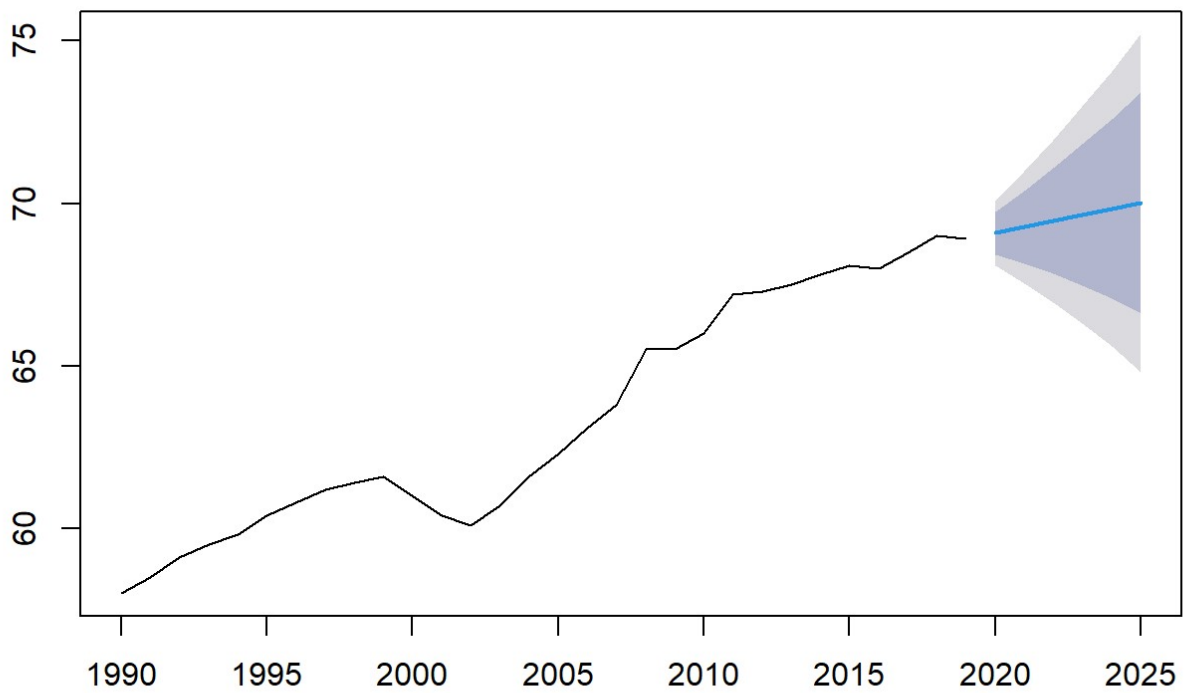
#The second coefficient, drift, represents the linear trend in the time series data. The estimated value of drift is 0.3705, which means that the labor force participation rate in Chile is increasing at a rate of 0.3705 units per time step on average. The standard error of the drift coefficient, 0.1189, indicates the uncertainty in the estimated value of the trend.

#FORECASTING AND DATA VISUALIZATION

```
#As I declared before in the first section, the final model forecasts the next 6 years.
# Creating final models
holt.linear.final = holt(chile_ts, h = 6)
holt.damped.final = holt(chile_ts, h = 6, damped = T)
ses.model.final = ses(chile_ts, h = 6)
arma.chile.final = forecast(auto.arima(chile_ts), h = 6)
```

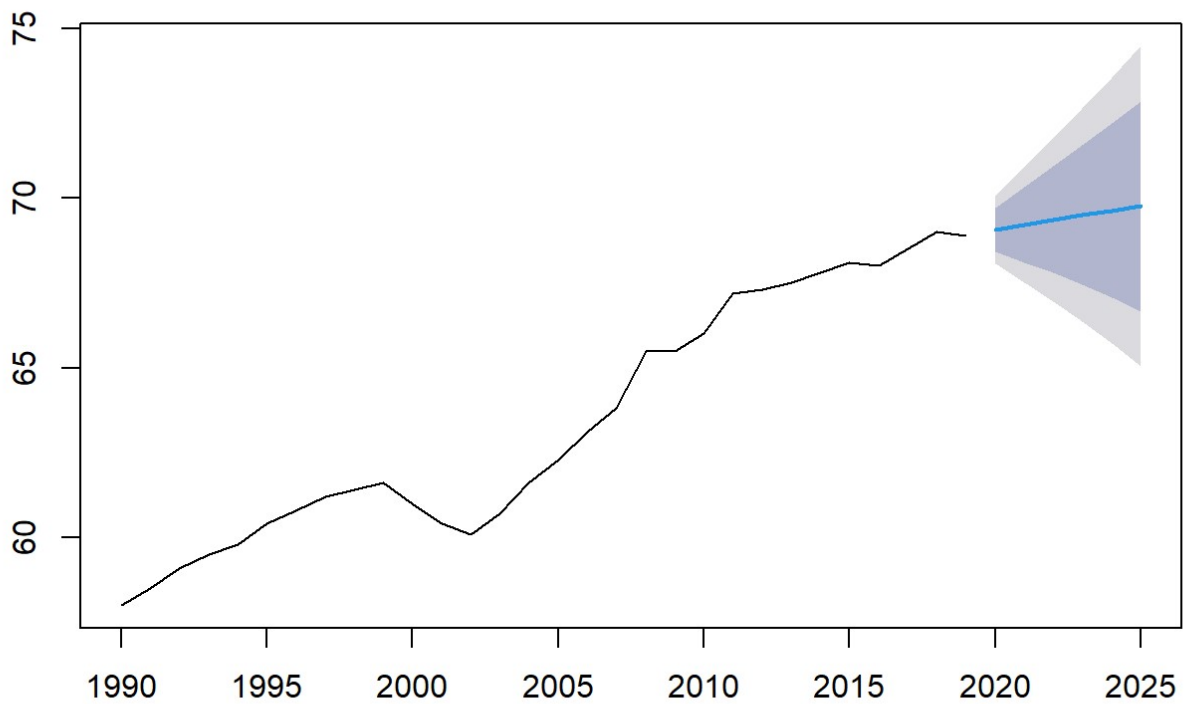
```
#Plotting the forecasts of the three models we set
plot(holt.linear.final)
```

Forecasts from Holt's method



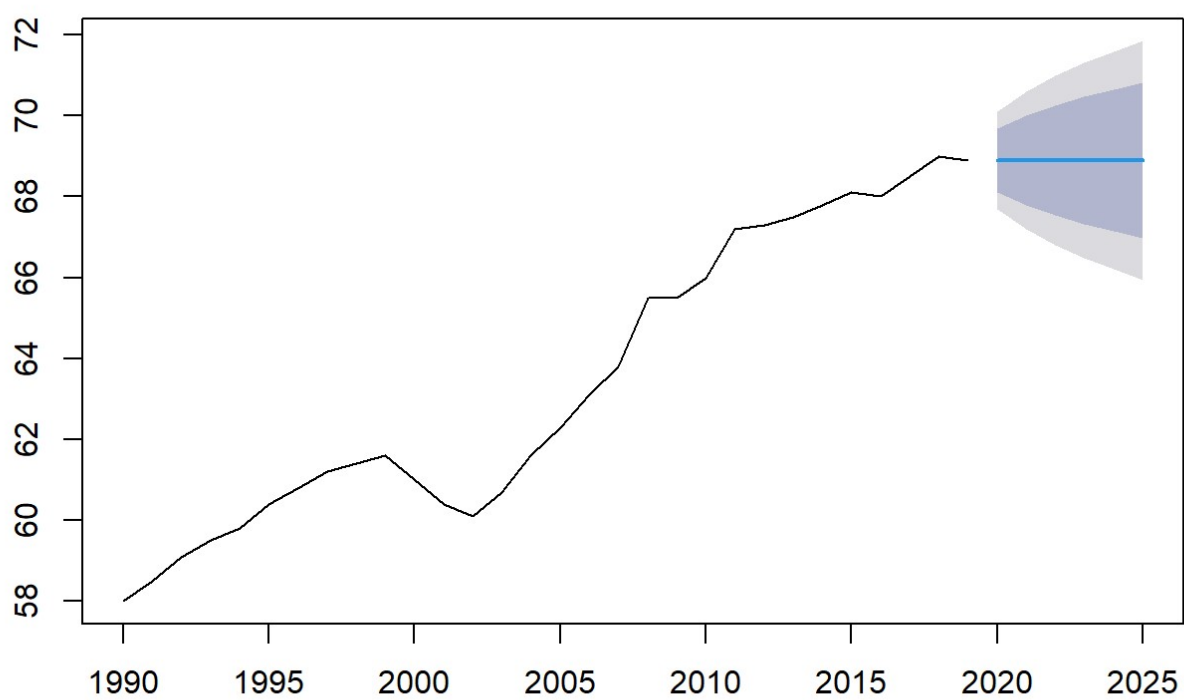
```
plot(holt.damped.final)
```

Forecasts from Damped Holt's method



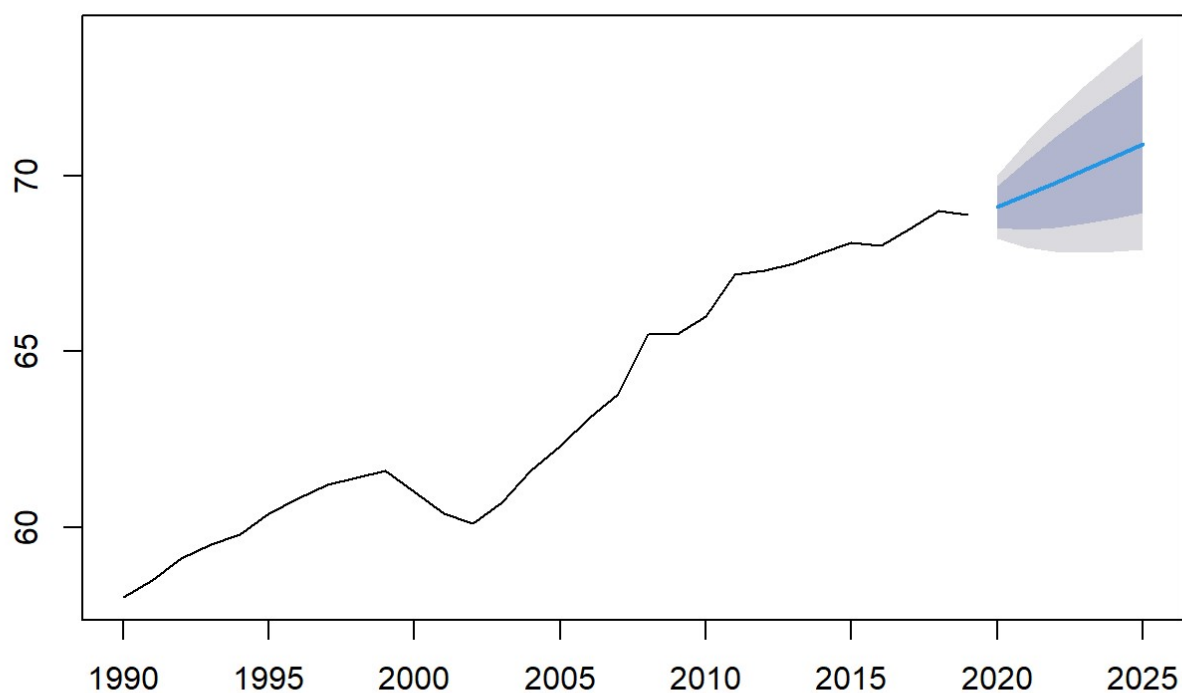
```
plot(ses.model.final)
```

Forecasts from Simple exponential smoothing



```
plot(arima.chile.final)
```

Forecasts from ARIMA(1,1,0) with drift



```
#Checking the forecasting results of the Holt trend model
print(holt.linear.final)
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## 2020	69.08635	68.43195	69.74075	68.08553	70.08717
## 2021	69.27265	68.14573	70.39958	67.54917	70.99614
## 2022	69.45895	67.82686	71.09105	66.96288	71.95503
## 2023	69.64526	67.46626	71.82425	66.31277	72.97774
## 2024	69.83156	67.06366	72.59946	65.59842	74.06469
## 2025	70.01786	66.62051	73.41521	64.82207	75.21365

```
#Checking the forecasting results of the Holt damped model
print(holt.damped.final)
```

##	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## 2020	69.06198	68.40587	69.71809	68.05855	70.06542
## 2021	69.21593	68.10933	70.32253	67.52353	70.90833
## 2022	69.36228	67.79165	70.93290	66.96022	71.76434
## 2023	69.50141	67.44523	71.55758	66.35676	72.64605
## 2024	69.63367	67.07132	72.19602	65.71489	73.55244
## 2025	69.75940	66.67276	72.84605	65.03879	74.48002

```
#Checking the forecasting results of the Simple Exponential Smoothing model
print(ses.model.final)
```



```
##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## 2020      68.90001 68.11331 69.68671 67.69686 70.10316
## 2021      68.90001 67.78751 70.01251 67.19858 70.60144
## 2022      68.90001 67.53750 70.26252 66.81623 70.98379
## 2023      68.90001 67.32673 70.47329 66.49389 71.30613
## 2024      68.90001 67.14104 70.65898 66.20990 71.59012
## 2025      68.90001 66.97316 70.82686 65.95315 71.84687
```

```
#Checking the forecasting results of the ARIMA model
print(arima.chile.final)
```

```
##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## 2020      69.12400 68.52944 69.71856 68.21470 70.03330
## 2021      69.44890 68.46836 70.42944 67.94930 70.94851
## 2022      69.80523 68.51579 71.09468 67.83319 71.77727
## 2023      70.17135 68.62400 71.71869 67.80488 72.53781
## 2024      70.54051 68.76978 72.31124 67.83241 73.24861
## 2025      70.91062 68.94092 72.88032 67.89823 73.92301
```

```
autoplot(chile_ts) + geom_line(size=1) +
  forecast::autolayer(holt.linear.final$mean, series = "Holt Linear Trend") + geom_line(size=1) +
  forecast::autolayer(holt.damped.final$mean, series = "Holt Damped Trend") + geom_line(size=1) +
  forecast::autolayer(ses.model.final$mean, series = "SES") + geom_line(size=1) +
  forecast::autolayer(arima.chile.final$mean, series = "ARIMA") + geom_line(size=1) +
  xlab("year") + ylab("Labour Force Participation Rate in Chile (Age 15-64)") +
  guides(colour=guide_legend(title="Forecast Method")) + theme(legend.position = c(0.8, 0.2)) +
  ggtitle("Chile") + theme(plot.title=element_text(family="Calibri", hjust = 0.5, color = "blue",
                                                    face="bold", size=15))
```

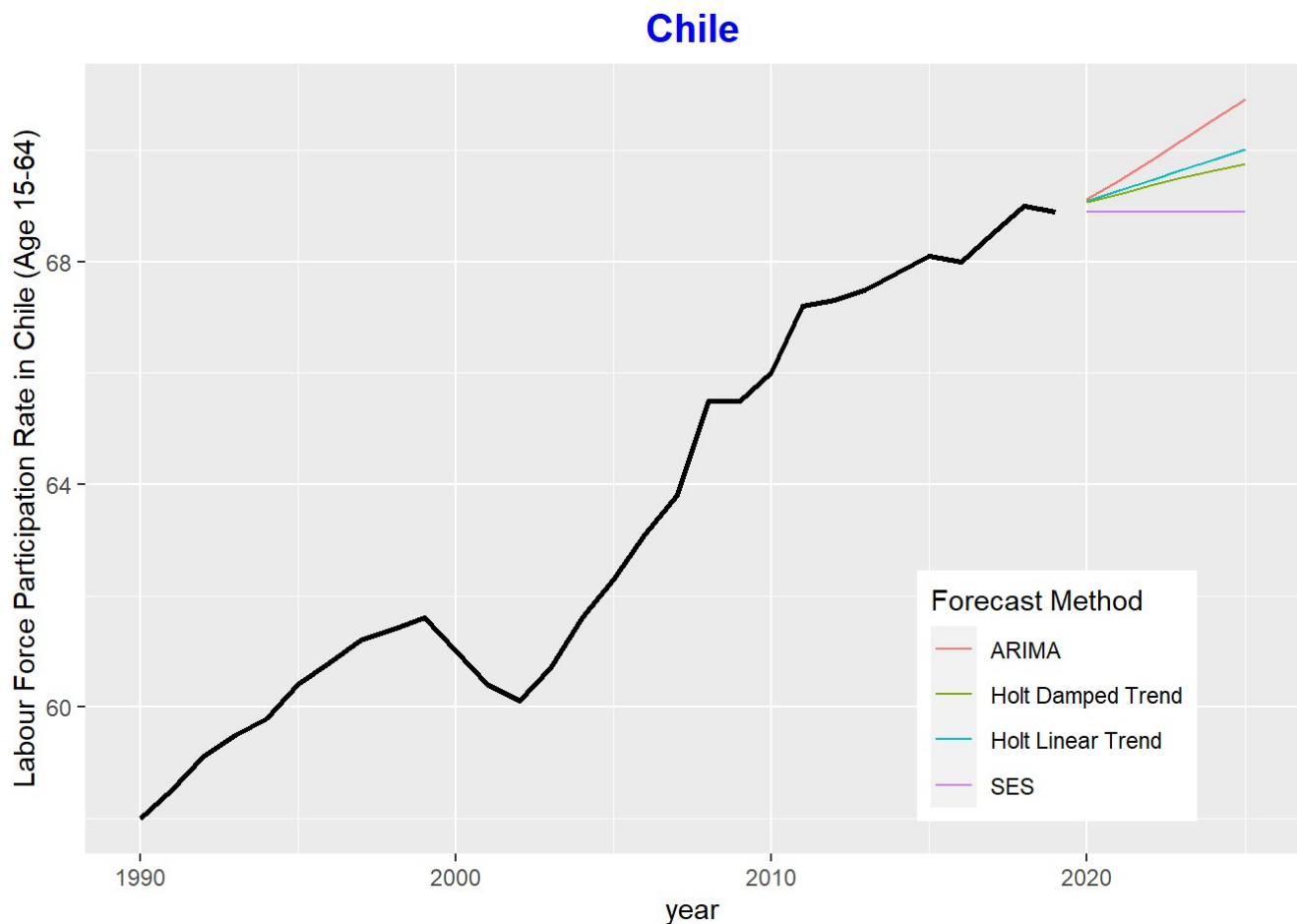
```
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
```

```
## Warning in grid.Call(C_stringMetric, as.graphicsAnnot(x$label)): font family not
## found in Windows font database
```

```
## Warning in grid.Call(C_textBounds, as.graphicsAnnot(x$label), x$x, x$y, : font
## family not found in Windows font database
```

```
## Warning in grid.Call(C_textBounds, as.graphicsAnnot(x$label), x$x, x$y, : font
## family not found in Windows font database
```

```
## Warning in grid.Call(C_textBounds, as.graphicsAnnot(x$label), x$x, x$y, : font
## family not found in Windows font database
```



#Final Comments

#The point forecast values show that the labor force participation rate in Chile will increase to around 70%.

#It can be seen that the predicted values and prediction intervals increase steadily from 2020 to 2025. This may suggest that the time series has a positive trend.

#However, this is a simple time series analysis with one year frequency and with 30 observations. Without additional information on the labor force participation rate and more frequent data, it is difficult to make any further conclusions.