

Student Information

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Answer 1

a) $G_1 = \{V_1, \Sigma_1, R_1, S_1\}$, $V_1 = \{S_1, a, b\}$, $\Sigma_1 = \{a, b\}$ and

$$R = \{ S_1 \rightarrow S_1 a S_1 b S_1 b S_1,$$

$$S_1 \rightarrow S_1 b S_1 a S_1 b S_1,$$

$$S_1 \rightarrow S_1 b S_1 b S_1 a S_1,$$

$$S_1 \rightarrow e \}$$

b) $G_2 = \{V_2, \Sigma_2, R_2, S_2\}$, $V_2 = \{S_2, K, L, a, b\}$, $\Sigma_2 = \{a, b\}$ and

$$R_2 = \{ S_2 \rightarrow K \mid L,$$

$$K \rightarrow KaKaKaK,$$

$$K \rightarrow KaKbKaK,$$

$$K \rightarrow KbKaKaK,$$

$$K \rightarrow L,$$

$$L \rightarrow LaLbL,$$

$$L \rightarrow LbLaL$$

$$L \rightarrow e \}$$

c) PDA that accepts the L_1 is :

Let $G = \{ V, \Sigma, R, S \}$ and we can construct a PDA M such that $L(G) = L(M)$.

Let $M = (K, \Sigma, \Gamma, \Delta, s, F)$ where

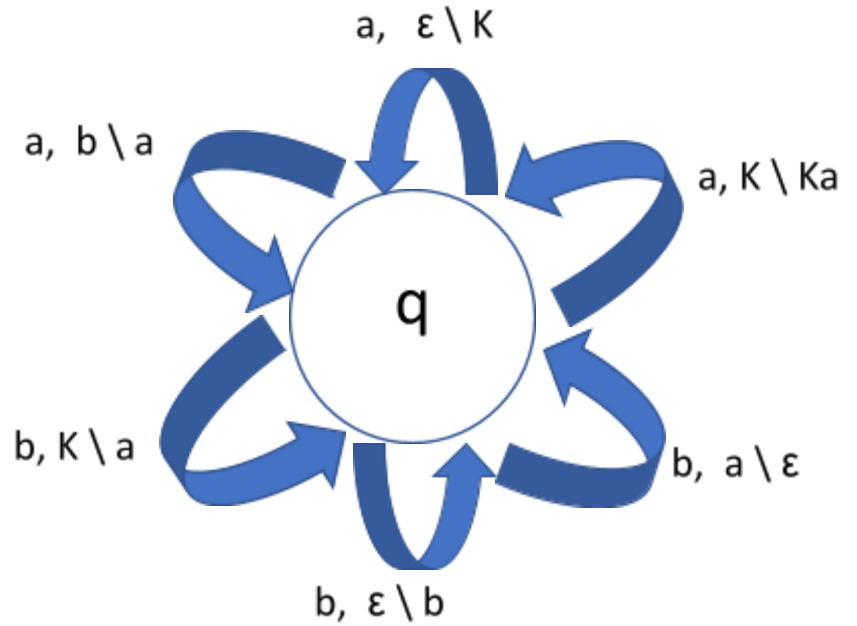
$K = \{ q \}$

$F = \{ q \}$

$\Sigma = \{ a, b \}$

$\Gamma = \{ K, a, b \}$

$\Delta = \{ ((q,a,e),(q,K)),$
 $((q,a,b),(q,a)),$
 $((q,a,K),(q,Ka)),$
 $((q,b,e),(q,b)),$
 $((q,b,K),(q,a)),$
 $((q,b,a),(q,e))) \}$



d) We define grammar G_3 for $L_3 = L_1 \cup L_2$.

$L(G_3) = L(G_1) \cup L(G_2)$.

Firstly ,we should check L_1 and L_2 have disjoint sets of non-terminals.

$V_1 - \Sigma_1 = \{ S_1 \}$

$V_2 - \Sigma_2 = \{ S_2, K, L \}$

We can conclude their sets of non-terminals are disjoint.

According to the Union property of context-free languages (Theorem 3.5.1):

$G_3 = (V_1 \cup V_2 \cup \{S\}, \Sigma_1 \cup \Sigma_2, R_1 \cup R_2 \cup \{S \rightarrow S_1, S \rightarrow S_2\}, S)$

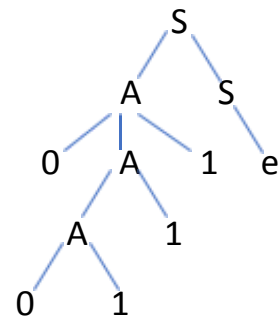
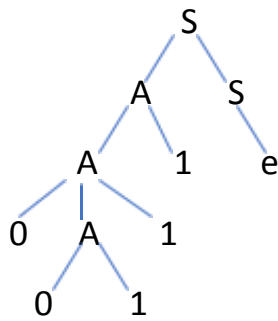
$V_3 = V_1 \cup V_2 \cup \{S\} = \{ S_1, S_2, K, L, a, b \}$

$\Sigma_3 = \Sigma_1 \cup \Sigma_2 = \{ a, b \}$

$R_3 = R_{1 \cup 2} \cup \{ S \rightarrow S_1, S \rightarrow S_2 \} = \{ S_1 \rightarrow S_1 a S_1 b S_1 b S_1 \mid S_1 b S_1 a S_1 b S_1 \mid S_1 b S_1 b S_1 a S_1 \mid S_1 \rightarrow e \}$
 $\cup \{ S_2 \rightarrow K \mid L, K \rightarrow KaKaKaK \mid KaKbKaK \mid KbKaKaK \mid L, L \rightarrow LaLbL \mid LbLaL \mid e \}$
 $\cup \{ S \rightarrow S_1, S \rightarrow S_2 \}$

Answer 2

- a) Grammars such as G' , with strings that have two or more distinct parse trees, are called ambiguous. If we choose sample as "00111" we can draw 2 different parse trees. So, G_1 is ambiguous.



- b) The unambiguous grammar for $L(G_1)$:

$$R = \{ S \rightarrow A$$

$$A \rightarrow AA \mid A1 \mid T$$

$$T \rightarrow 0T1 \mid 01 \}$$

- c) The leftmost derivation of the string "00111" :

$$S \rightarrow A \rightarrow A1 \rightarrow 0T1 \rightarrow 01$$

Parse Tree :

