

Tarski's World

First assume that our domain is set of all cubes.

Every cube is in front of b

$\forall x \text{ FrontOf}(x, b)$

b is in front of everything

$\forall x \text{ FrontOf}(b, x)$

If our domain contains not only cubes:

b is in front of every cube

$\forall x (\text{Cube}(x) \rightarrow \text{FrontOf}(b, x))$

b is in front of every small cube

$\forall x ((\text{Cube}(x) \wedge \text{Small}(x)) \rightarrow \text{FrontOf}(b, x))$

It's not the case that b is a large cube

$\neg \exists y (\text{Large}(y) \wedge \text{Cube}(y) \wedge b = y)$

It's not the case that something is a large cube

$\neg \exists y (\text{Large}(y) \wedge \text{Cube}(y) \wedge \exists x x = y)$

Everything between c and b is a

$\forall x (\text{Between}(x, c, b) \rightarrow x = a)$

Everything between c and b is a cube

$\forall x (\text{Between}(x, c, b) \rightarrow \exists y (\text{Cube}(y) \wedge x = y))$

Every cube is to the left of a tetrahedron

$\forall x [\text{Cube}(x) \rightarrow \exists y (\text{Tet}(y) \wedge \text{LeftOf}(x, y))]$

Some tetrahedron is in front of every small cube

$\exists x [\text{Tet}(x) \wedge \forall y ((\text{Small}(y) \wedge \text{Cube}(y)) \rightarrow \text{FrontOf}(x, y))]$

Some cube with nothing in front of it has something in back of it

$\exists x [(\text{Cube}(x) \wedge \forall y \neg \text{FrontOf}(y, x)) \wedge \exists z \text{BackOf}(z, x)]$

Every cube is the same size as a particular tetrahedron

$\exists y [\text{Tet}(y) \wedge \forall x (\text{Cube}(x) \rightarrow \text{SameSize}(x, y))]$