

Memory Hierarchy and Cache Memories

CENG331 - Computer Organization

Instructor:

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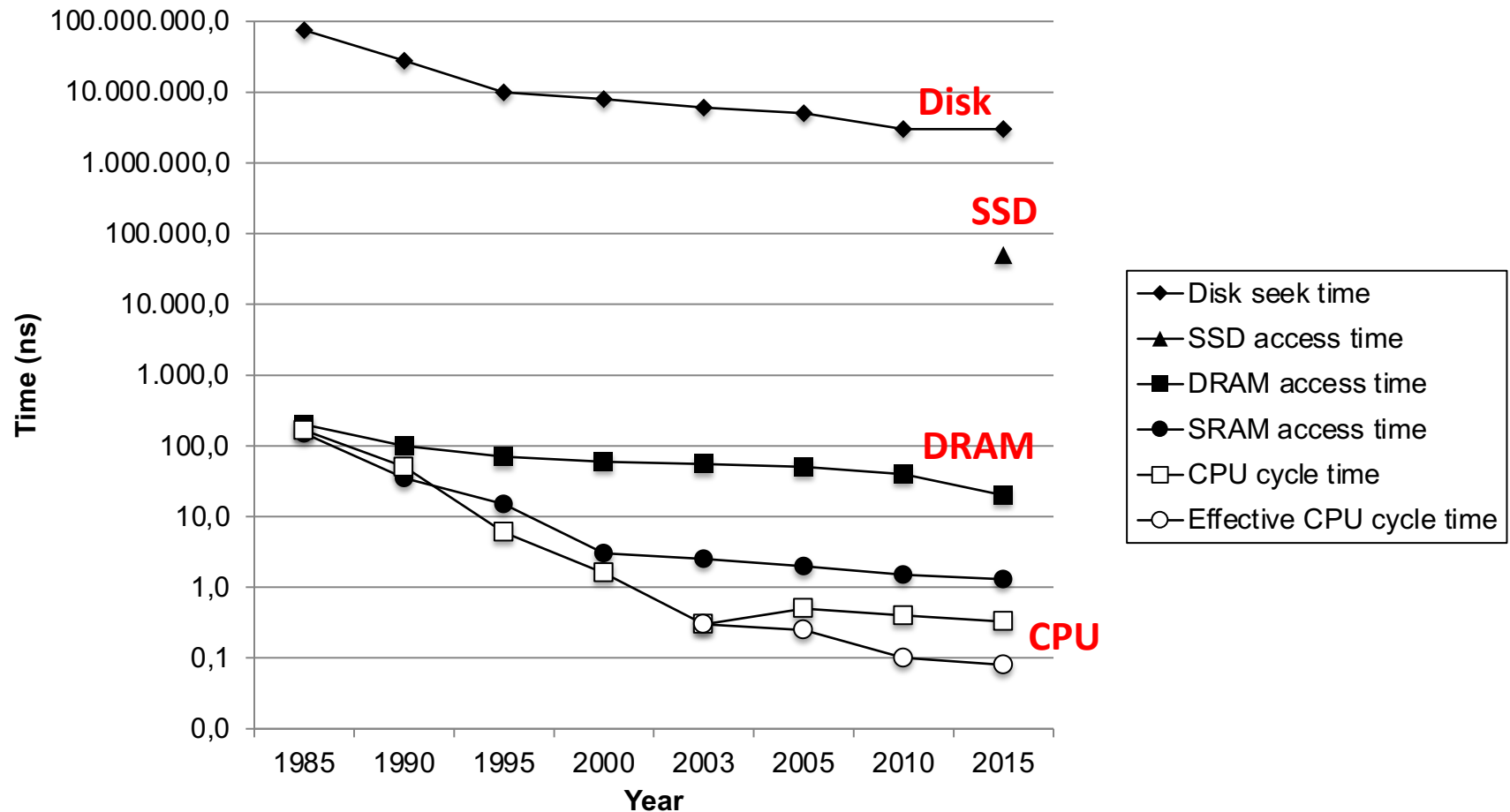
Adapted from: <http://csapp.cs.cmu.edu/> and <http://inst.eecs.berkeley.edu/~cs152>

Today

- **Cache memory organization and operation**
- **Performance impact of caches**
 - The memory mountain
 - Rearranging loops to improve spatial locality
 - Using blocking to improve temporal locality

The CPU-Memory Gap

The gap widens between DRAM, disk, and CPU speeds.



Locality to the Rescue!

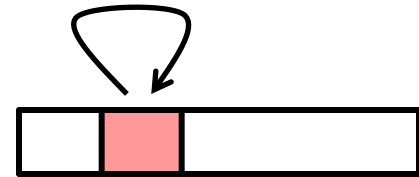
The key to bridging this CPU-Memory gap is a fundamental property of computer programs known as **locality**

Locality

- **Principle of Locality:** Programs tend to use data and instructions with addresses near or equal to those they have used recently

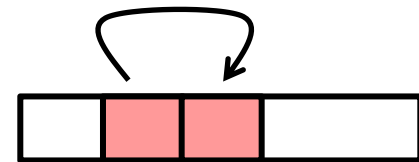
- **Temporal locality:**

- Recently referenced items are likely to be referenced again in the near future



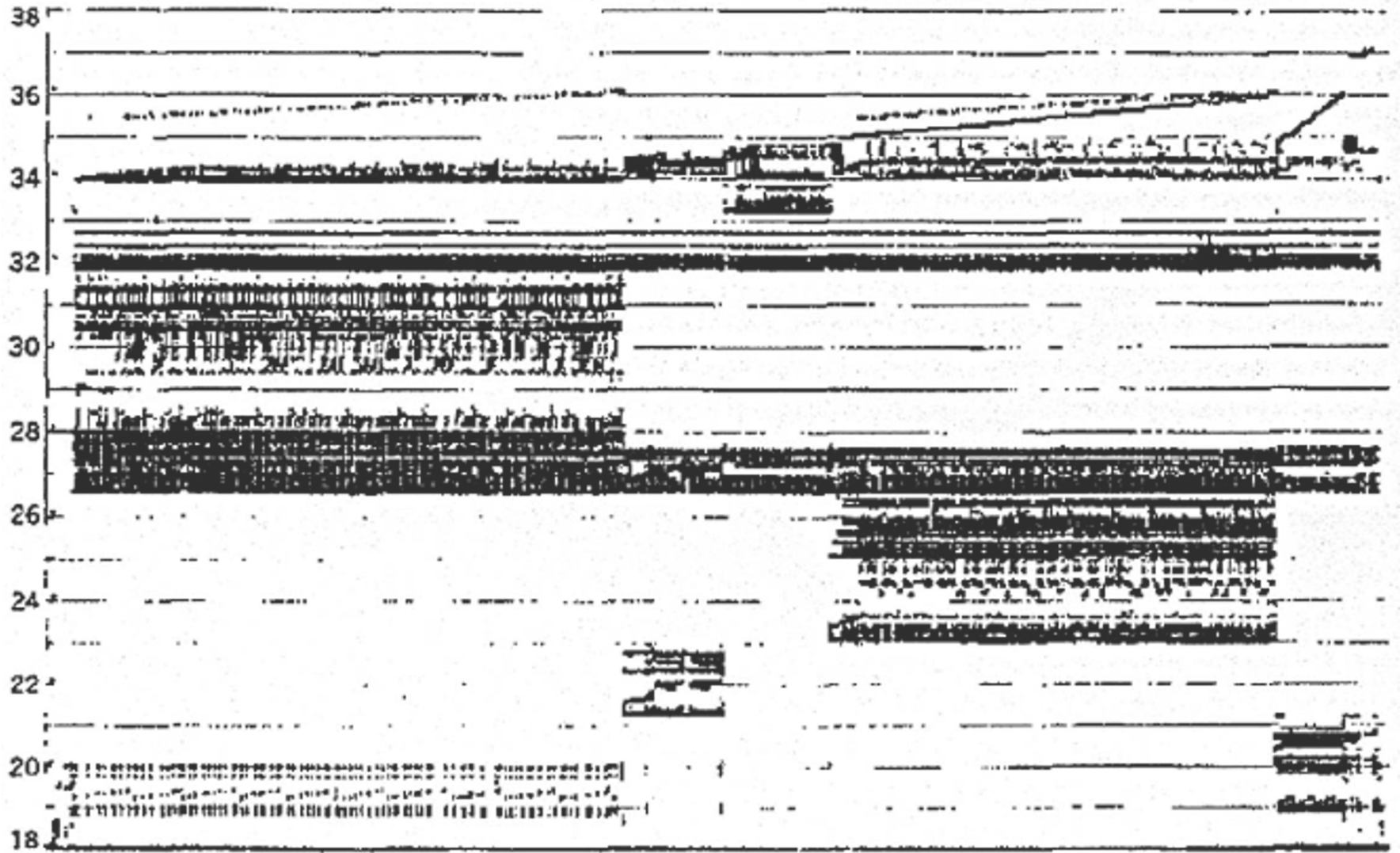
- **Spatial locality:**

- Items with nearby addresses tend to be referenced close together in time



Real Memory Reference Patterns

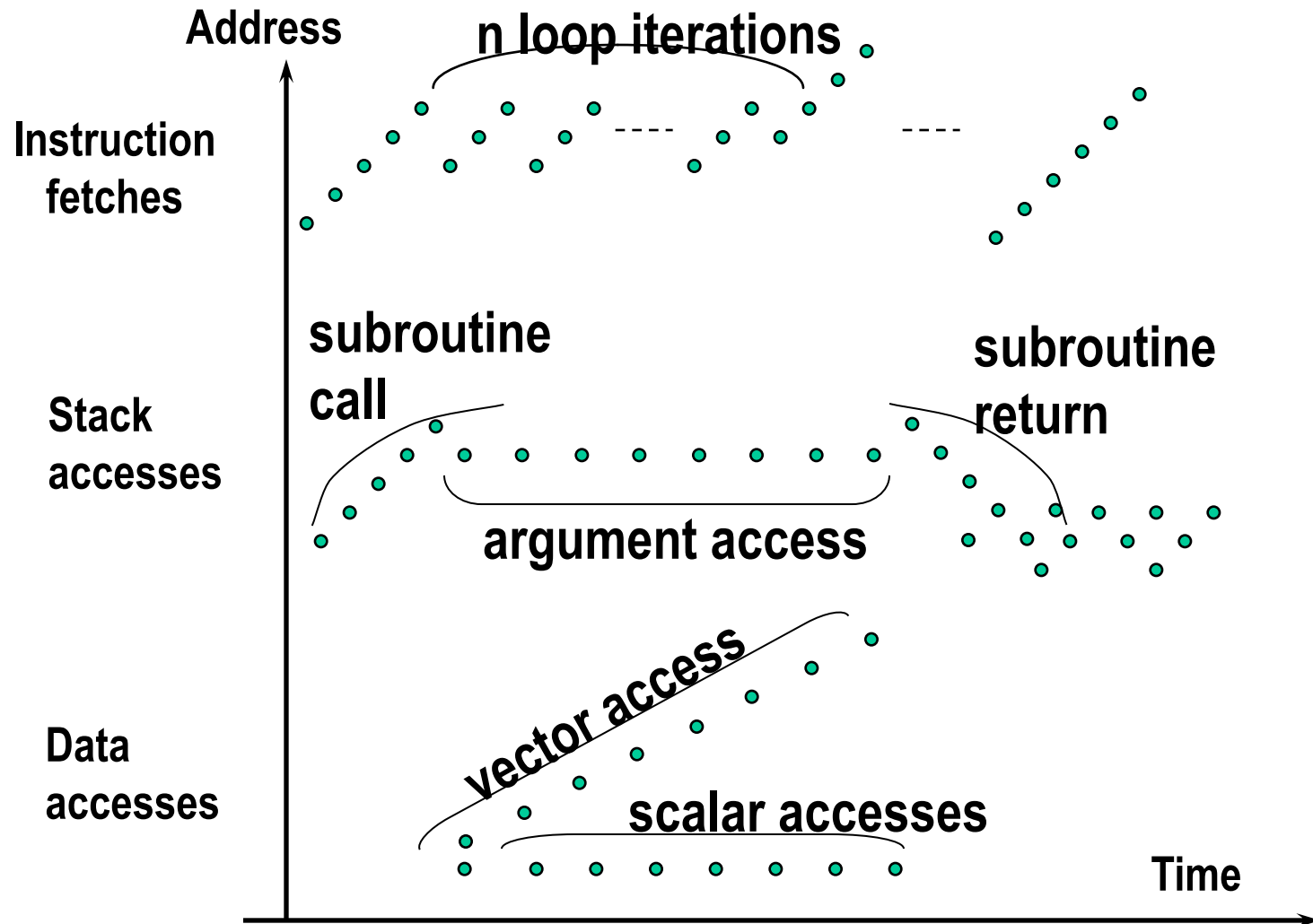
Memory Address (one dot per access)



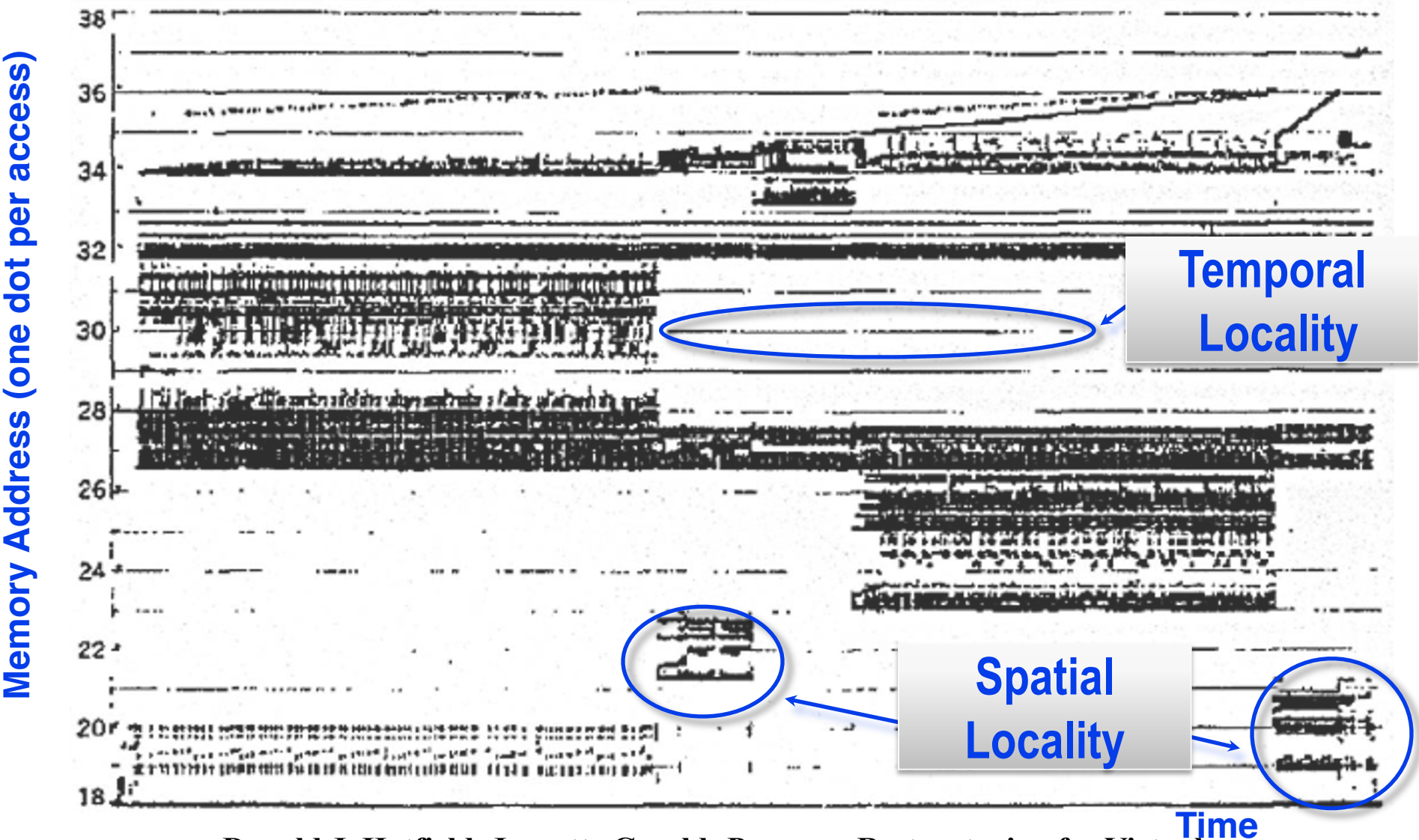
Time

Donald J. Hatfield, Jeanette Gerald: Program Restructuring for Virtual Memory. IBM Systems Journal 10(3): 168-192 (1971)

Typical Memory Reference Patterns



Memory Reference Patterns



Donald J. Hatfield, Jeanette Gerald: Program Restructuring for Virtual Memory. IBM Systems Journal 10(3): 168-192 (1971)

Locality Example

```
sum = 0;  
for (i = 0; i < n; i++)  
    sum += a[i];  
return sum;
```

■ Data references

- Reference array elements in succession (stride-1 reference pattern).
- Reference variable `sum` each iteration.

Spatial locality

Temporal locality

■ Instruction references

- Reference instructions in sequence.
- Cycle through loop repeatedly.

Spatial locality

Temporal locality

Locality Example

- **Question:** Does this function have good locality with respect to array `a`?

```
int sum_array_cols(int a[M][N])
{
    int i, j, sum = 0;

    for (j = 0; j < N; j++)
        for (i = 0; i < M; i++)
            sum += a[i][j];
    return sum;
}
```

Locality Example

- **Question:** Can you permute the loops so that the function scans the 3-d array `a` with a stride-1 reference pattern (and thus has good spatial locality)?

```
int sum_array_3d(int a[M][N][N])
{
    int i, j, k, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            for (k = 0; k < N; k++)
                sum += a[k][i][j];

    return sum;
}
```

Qualitative Estimates of Locality

- **Claim:** Being able to look at code and get a qualitative sense of its locality is a key skill for a professional programmer.
- **Question:** Does this function have good locality with respect to array *a*?

```
int sum_array_rows(int a[M][N])
{
    int i, j, sum = 0;

    for (i = 0; i < M; i++)
        for (j = 0; j < N; j++)
            sum += a[i][j];
    return sum;
}
```

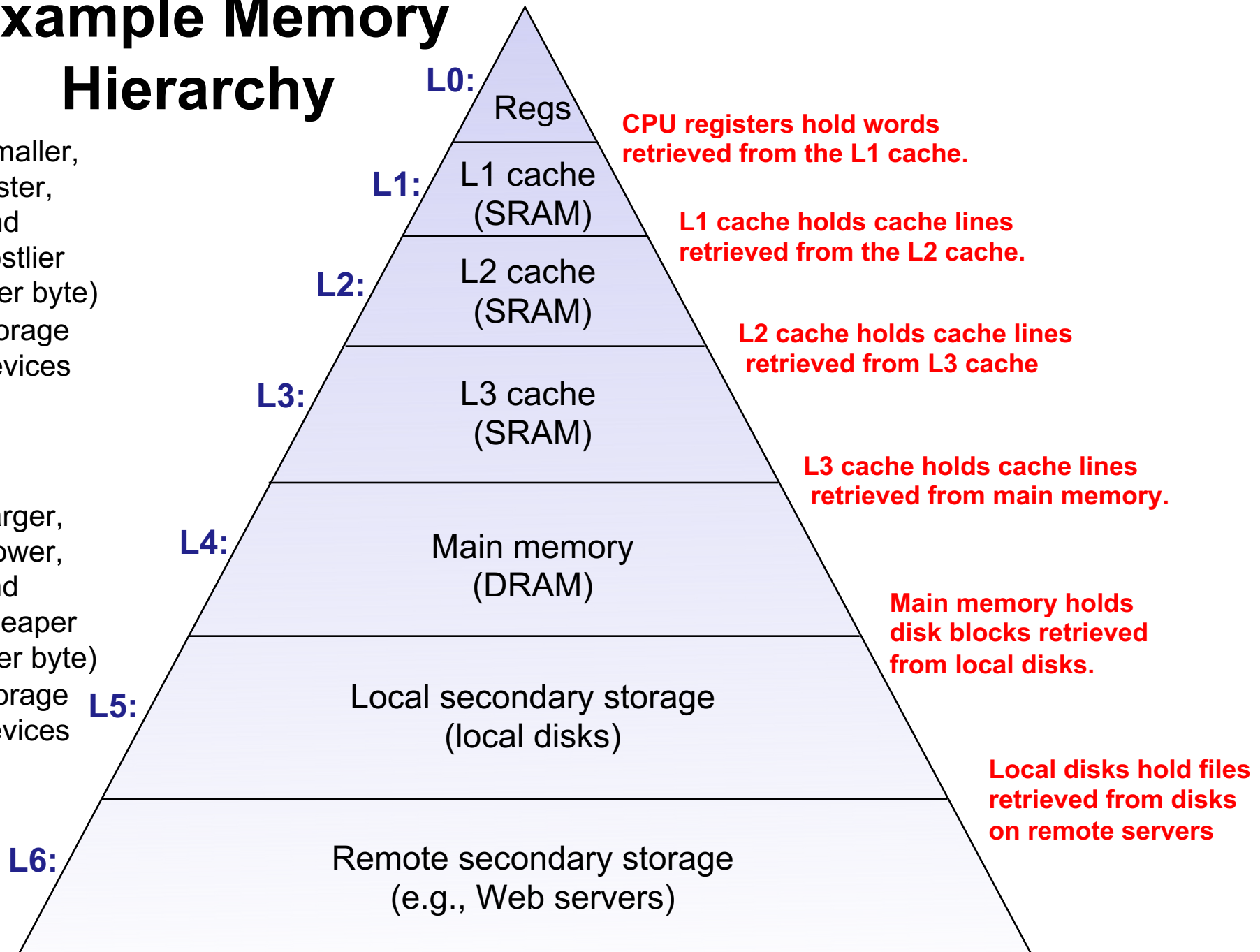
Memory Hierarchies

- **Some fundamental and enduring properties of hardware and software:**
 - Fast storage technologies cost more per byte, have less capacity, and require more power (heat!).
 - The gap between CPU and main memory speed is widening.
 - Well-written programs tend to exhibit good locality.
- **These fundamental properties complement each other beautifully.**
- **They suggest an approach for organizing memory and storage systems known as a **memory hierarchy**.**

Example Memory Hierarchy

↑
Smaller,
faster,
and
costlier
(per byte)
storage
devices

↓
Larger,
slower,
and
cheaper
(per byte)
storage
devices



Management of Memory Hierarchy

■ Small/fast storage, e.g., registers

- Address usually specified in instruction
- Generally implemented directly as a register file
 - but hardware might do things behind software's back, e.g., stack management, register renaming

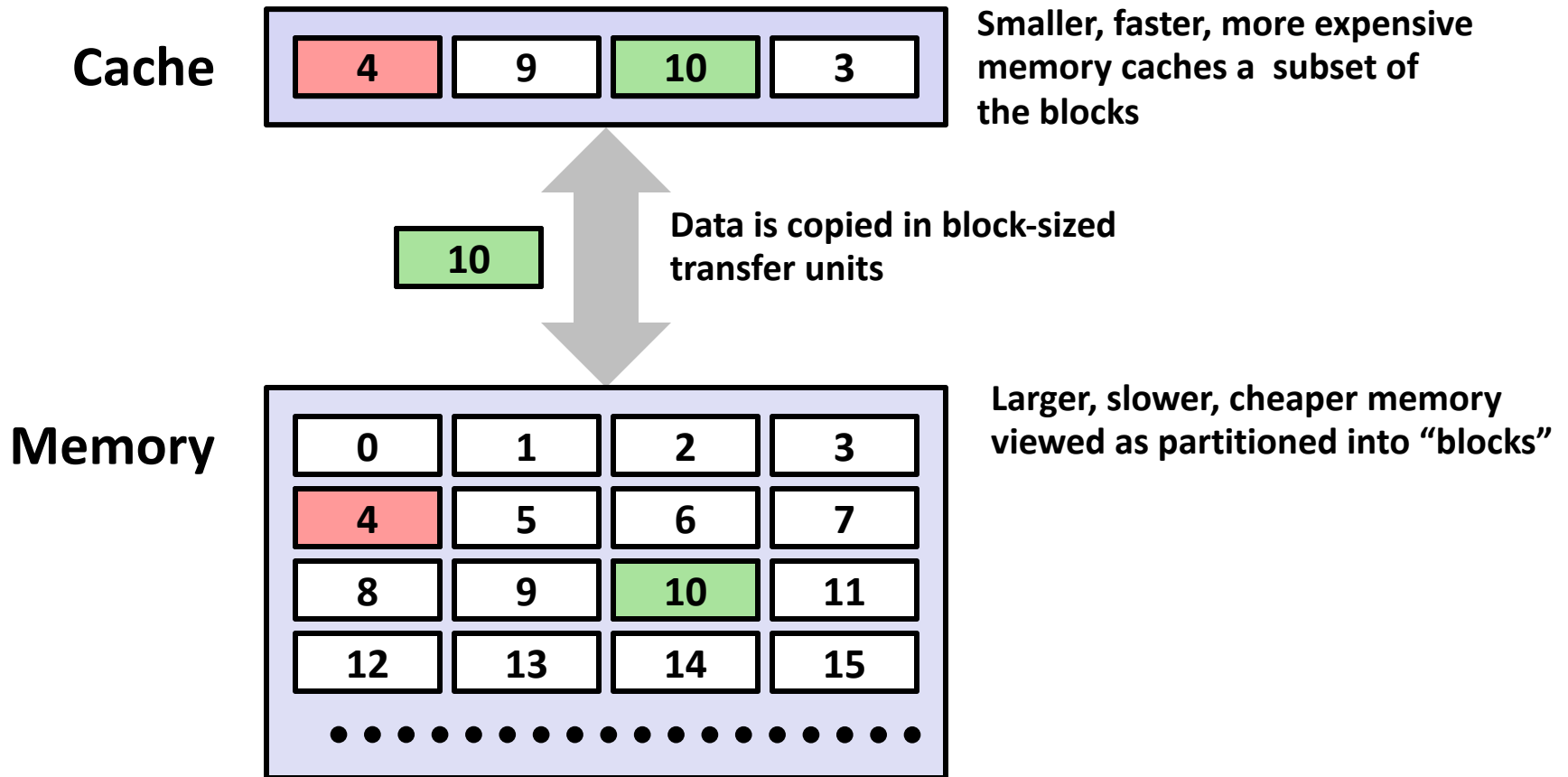
■ Larger/slower storage, e.g., main memory

- Address usually computed from values in register
- Generally implemented as a hardware-managed cache hierarchy
 - hardware decides what is kept in fast memory
 - but software may provide “hints”, e.g., don't cache or prefetch

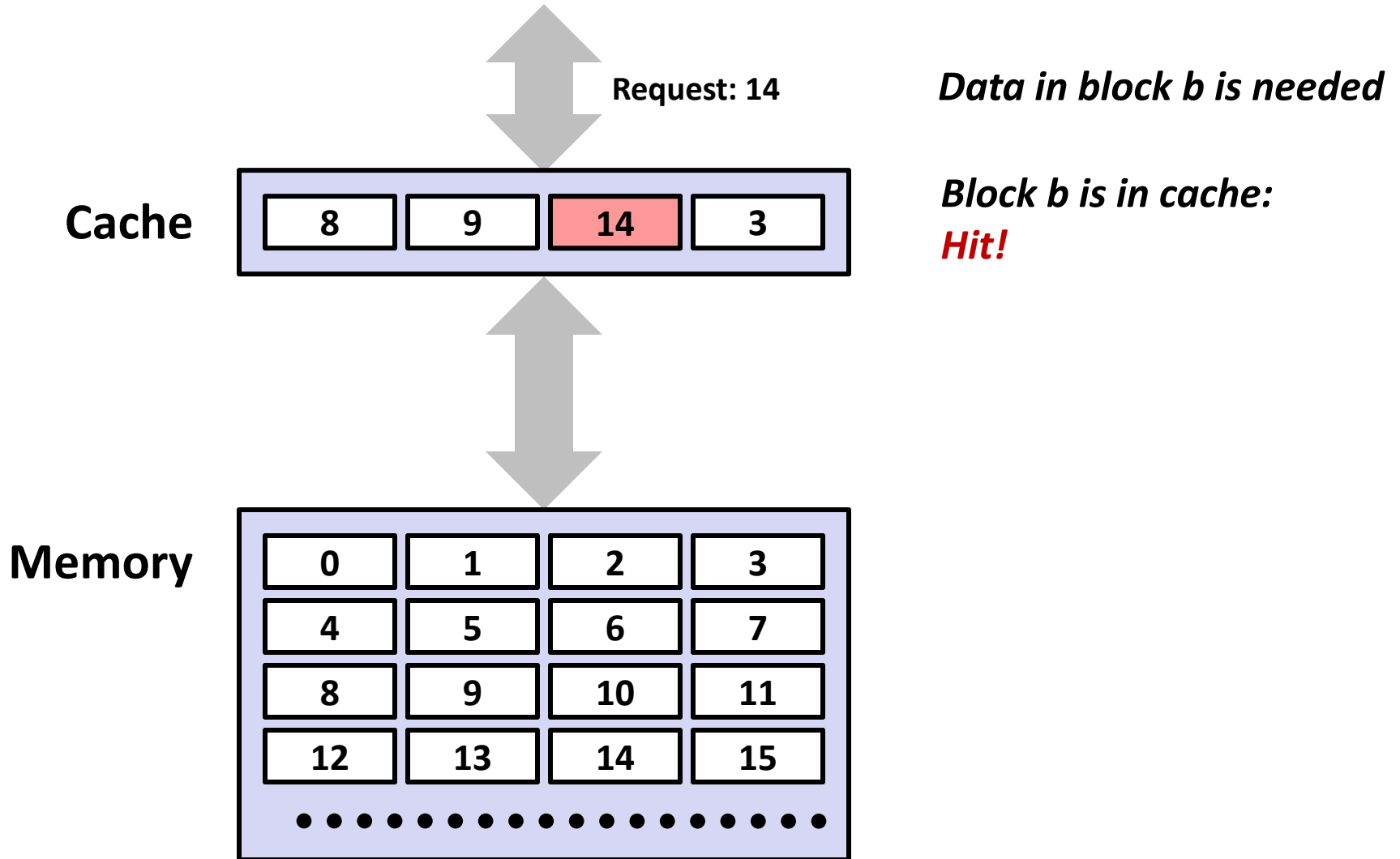
Caches

- **Cache:** A smaller, faster storage device that acts as a staging area for a subset of the data in a larger, slower device.
- **Fundamental idea of a memory hierarchy:**
 - For each k , the faster, smaller device at level k serves as a cache for the larger, slower device at level $k+1$.
- **Why do memory hierarchies work?**
 - Because of locality, programs tend to access the data at level k more often than they access the data at level $k+1$.
 - Thus, the storage at level $k+1$ can be slower, and thus larger and cheaper per bit.
- **Big Idea:** The memory hierarchy creates a large pool of storage that costs as much as the cheap storage near the bottom, but that serves data to programs at the rate of the fast storage near the top.

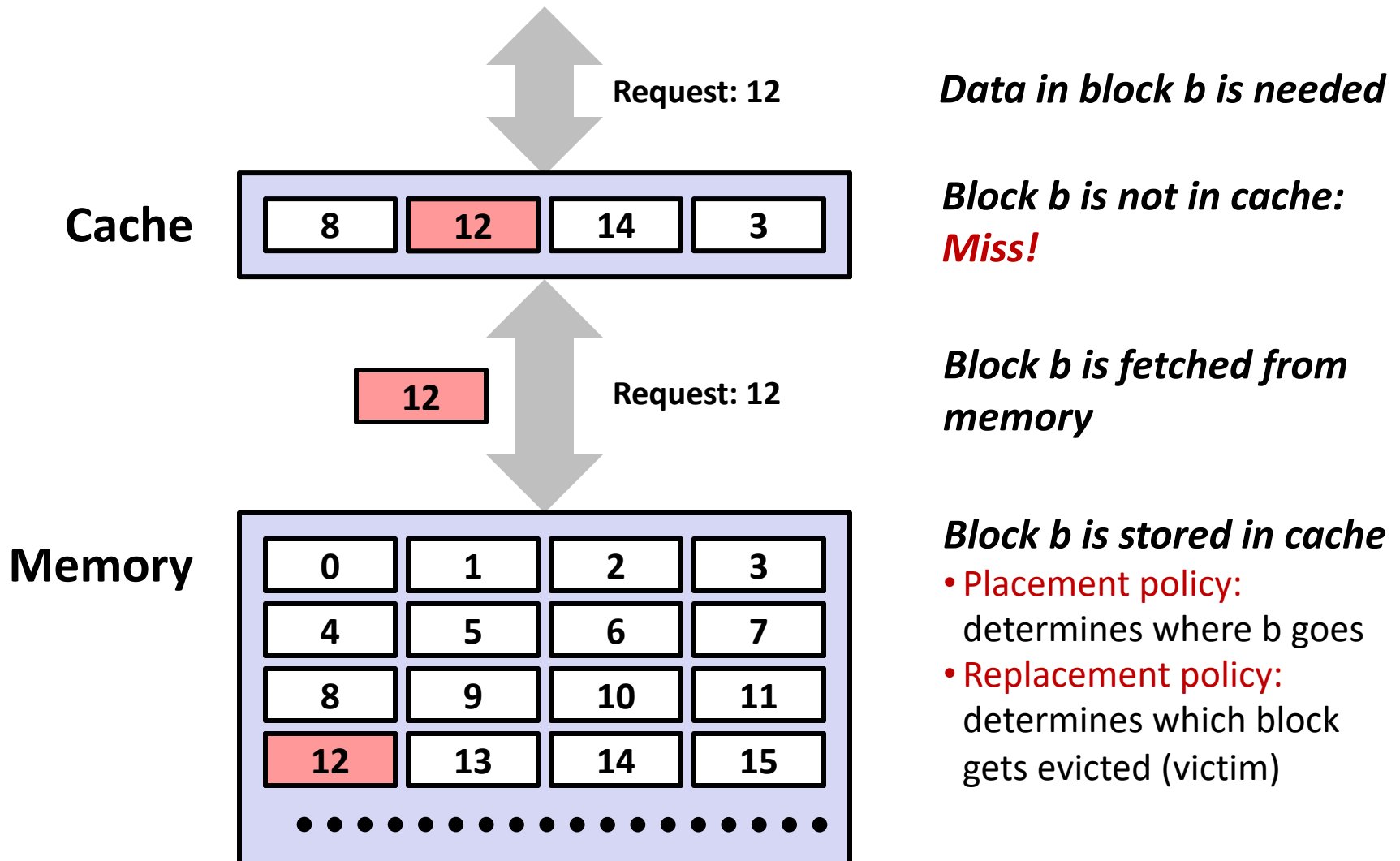
General Cache Concepts



General Cache Concepts: Hit



General Cache Concepts: Miss



General Caching Concepts:

Types of Cache Misses

■ Cold (compulsory) miss

- Cold misses occur because the cache is empty.

■ Conflict miss

- Most caches limit blocks at level $k+1$ to a small subset (sometimes a singleton) of the block positions at level k .
 - E.g. Block i at level $k+1$ must be placed in block $(i \bmod 4)$ at level k .
- Conflict misses occur when the level k cache is large enough, but multiple data objects all map to the same level k block.
 - E.g. Referencing blocks 0, 8, 0, 8, 0, 8, ... would miss every time.

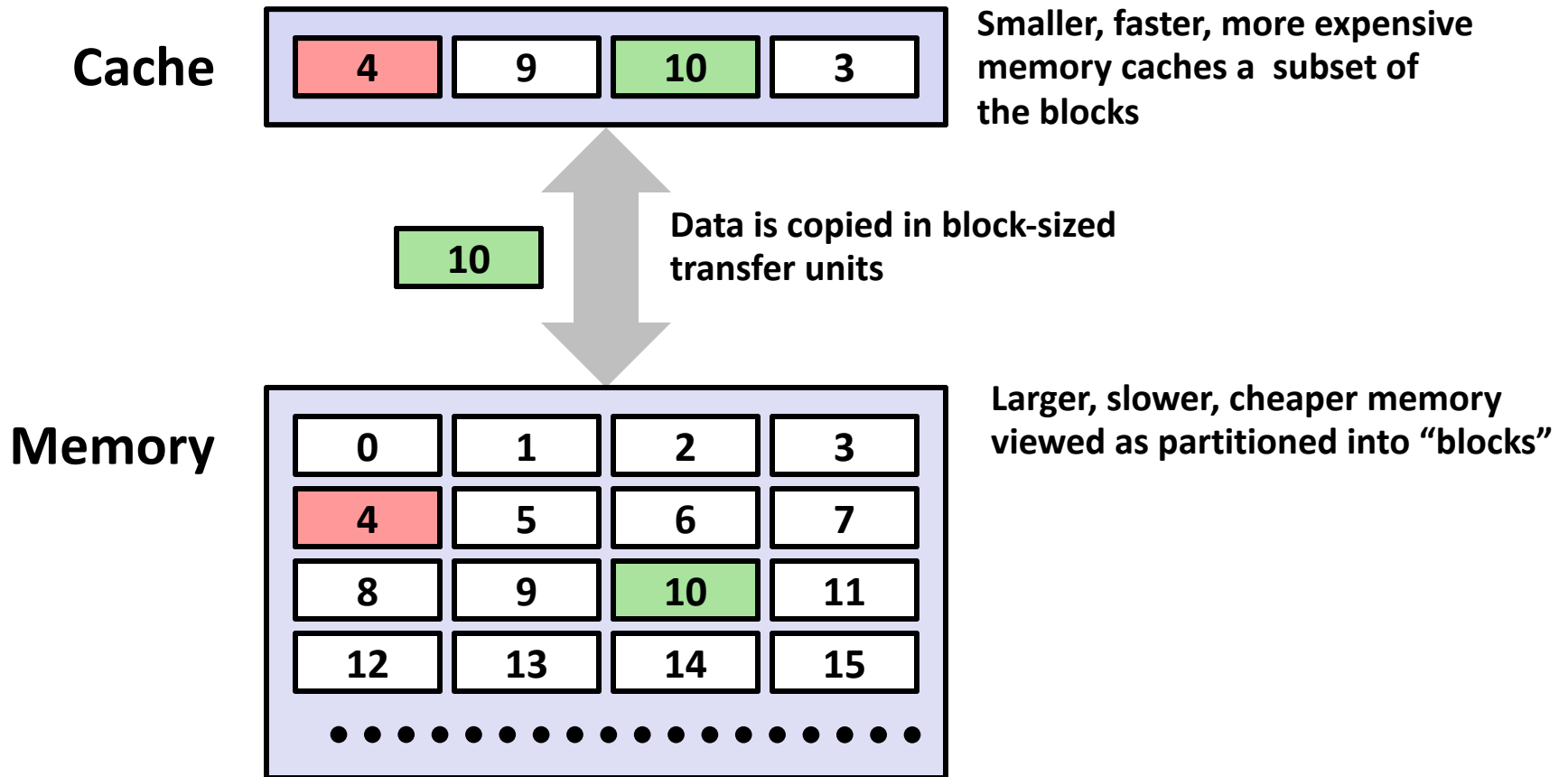
■ Capacity miss

- Occurs when the set of active cache blocks (**working set**) is larger than the cache.

Examples of Caching in the Mem. Hierarchy

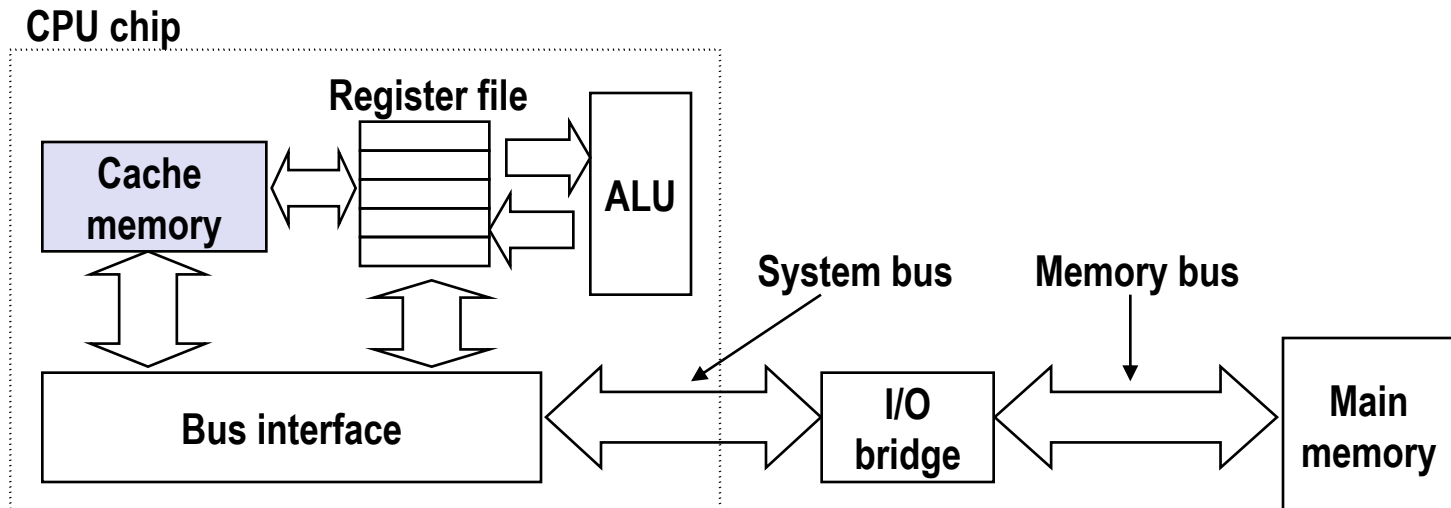
Cache Type	What is Cached?	Where is it Cached?	Latency (cycles)	Managed By
Registers	4-8 bytes words	CPU core	0	Compiler
TLB	Address translations	On-Chip TLB	0	Hardware MMU
L1 cache	64-byte blocks	On-Chip L1	4	Hardware
L2 cache	64-byte blocks	On-Chip L2	10	Hardware
Virtual Memory	4-KB pages	Main memory	100	Hardware + OS
Buffer cache	Parts of files	Main memory	100	OS
Disk cache	Disk sectors	Disk controller	100,000	Disk firmware
Network buffer cache	Parts of files	Local disk	10,000,000	NFS client
Browser cache	Web pages	Local disk	10,000,000	Web browser
Web cache	Web pages	Remote server disks	1,000,000,000	Web proxy server

General Cache Concept



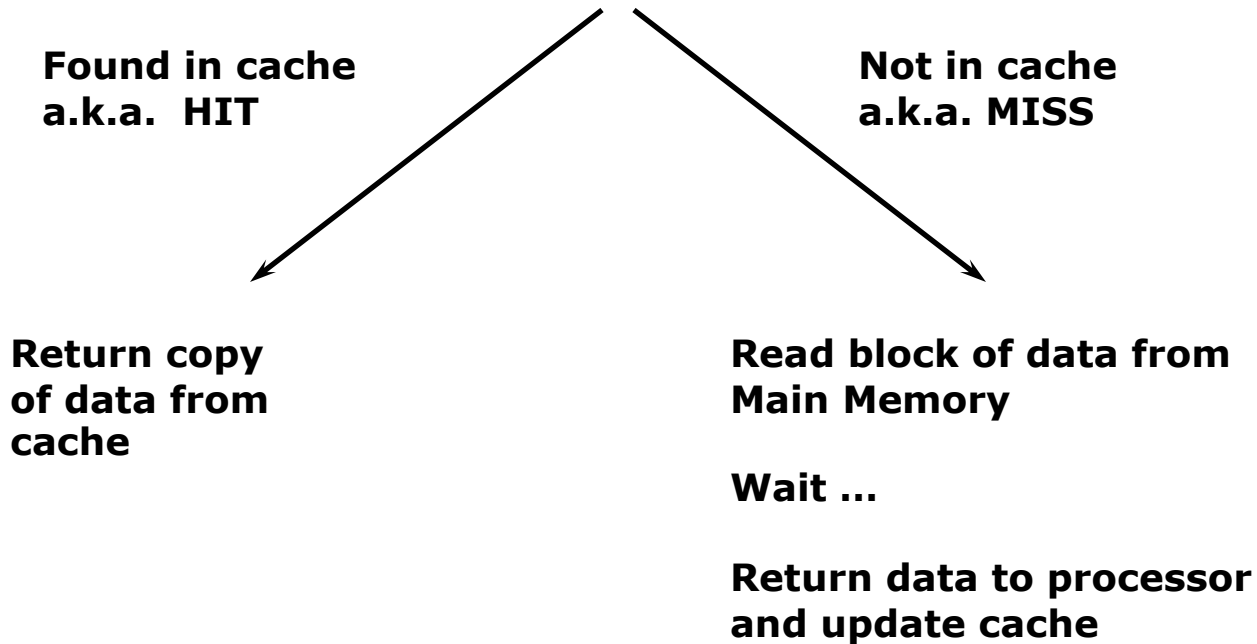
Cache Memories

- **Cache memories** are small, fast SRAM-based memories managed automatically in hardware
 - Hold frequently accessed blocks of main memory
- CPU looks first for data in cache, then in main memory
- Typical system structure:



Cache Algorithm (Read)

Look at Processor Address, search cache tags to find match. Then either



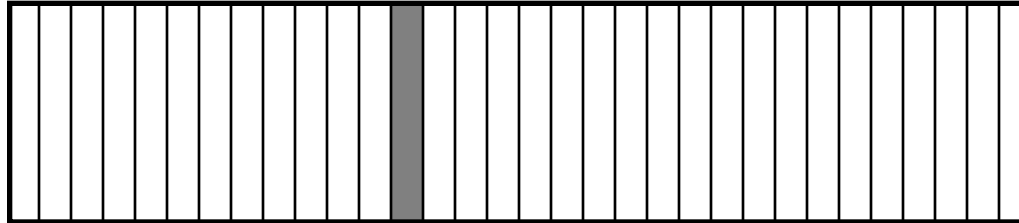
Q: Which line do we replace?

Placement Policy

Block Number

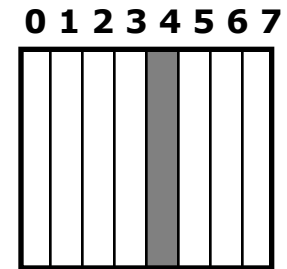
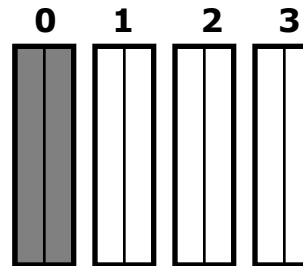
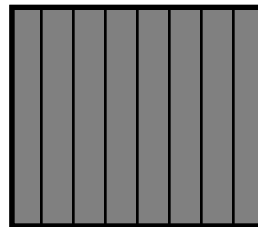
0 1 2 12 31

Memory



Set Number

Cache



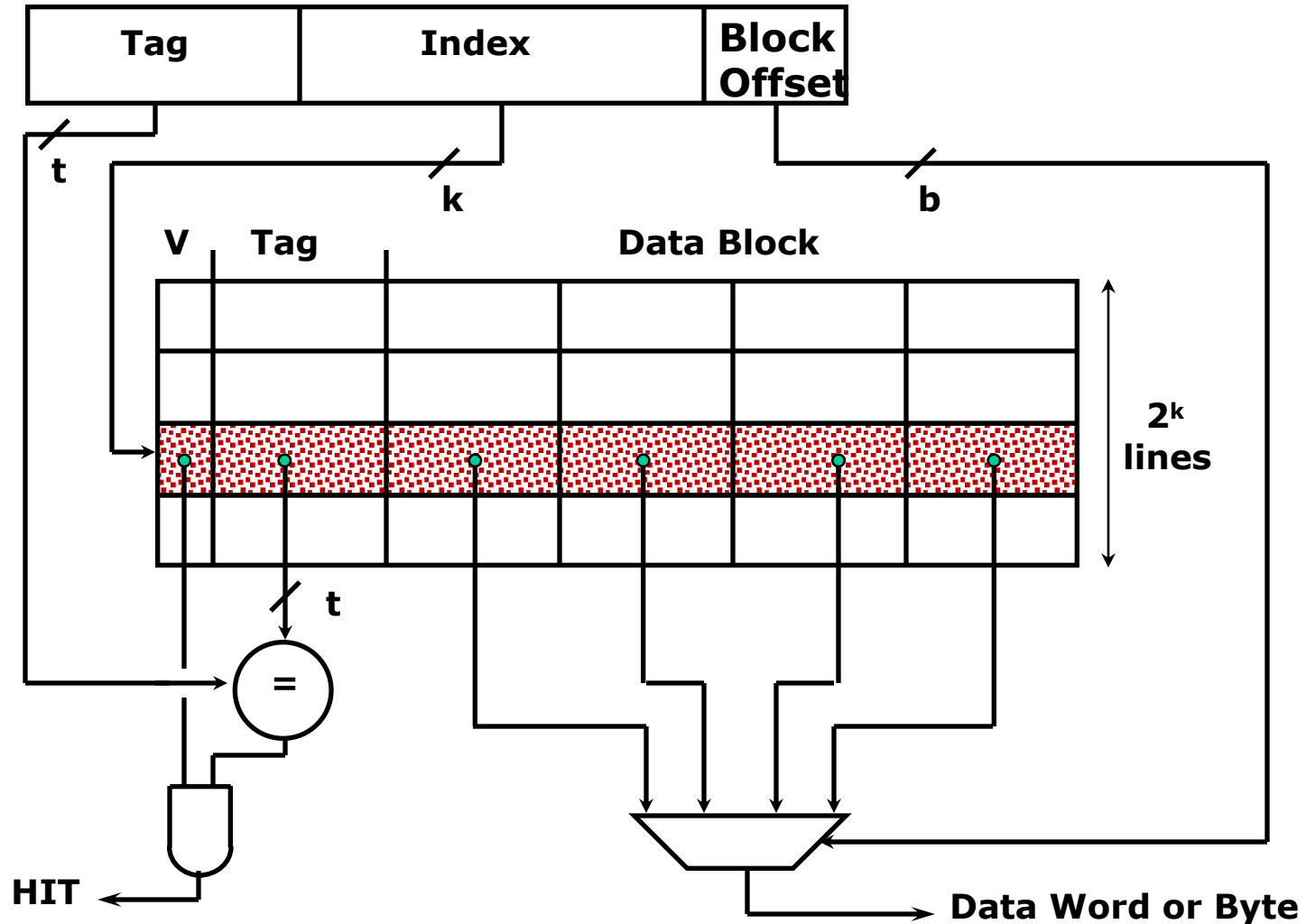
**Fully
Associative
anywhere**

**(2-way) Set
Associative
anywhere in
set 0
(12 mod 4)**

**Direct
Mapped
only into
block 4
(12 mod 8)**

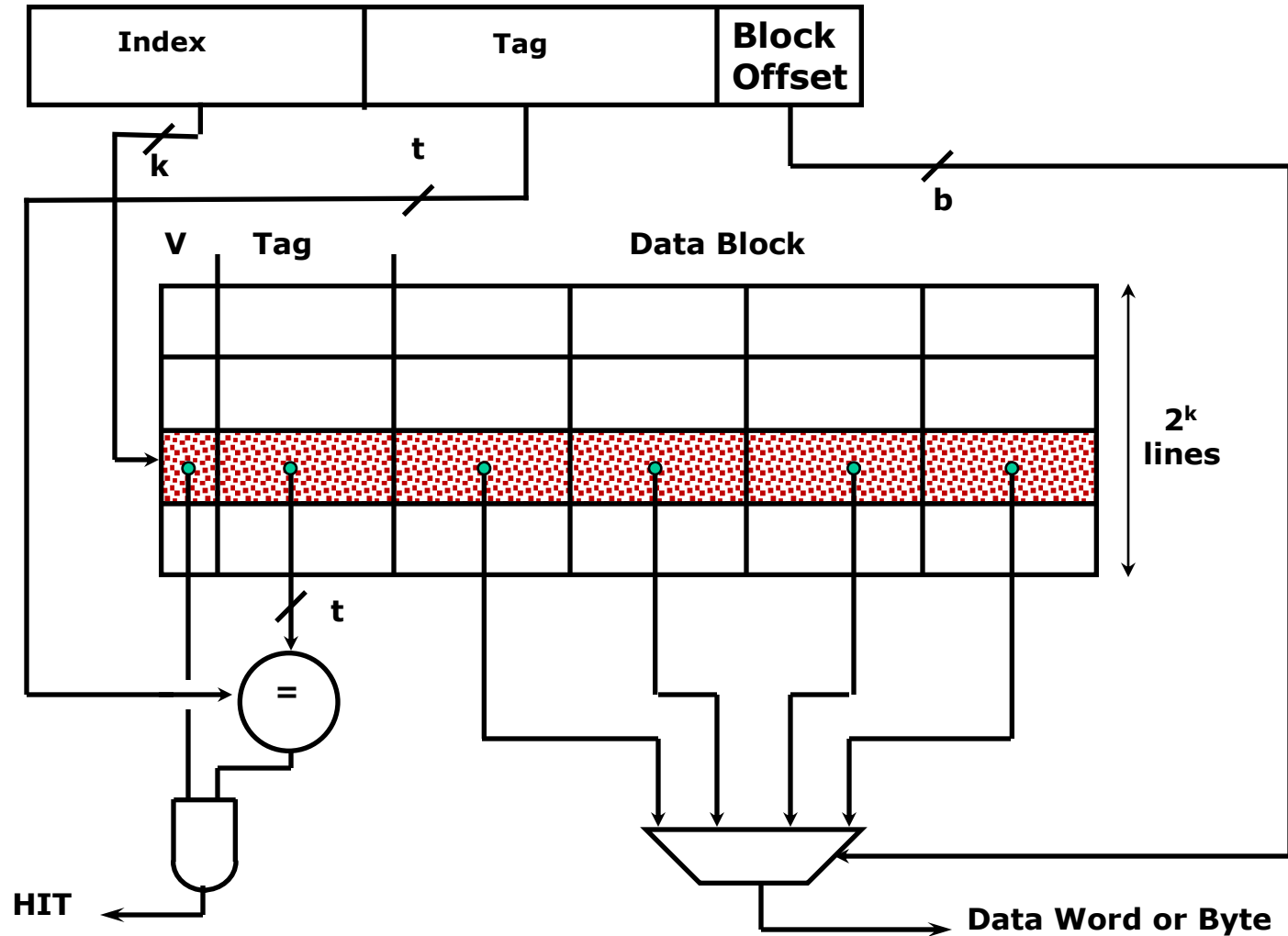
block 12
can be placed

Direct-Mapped Cache

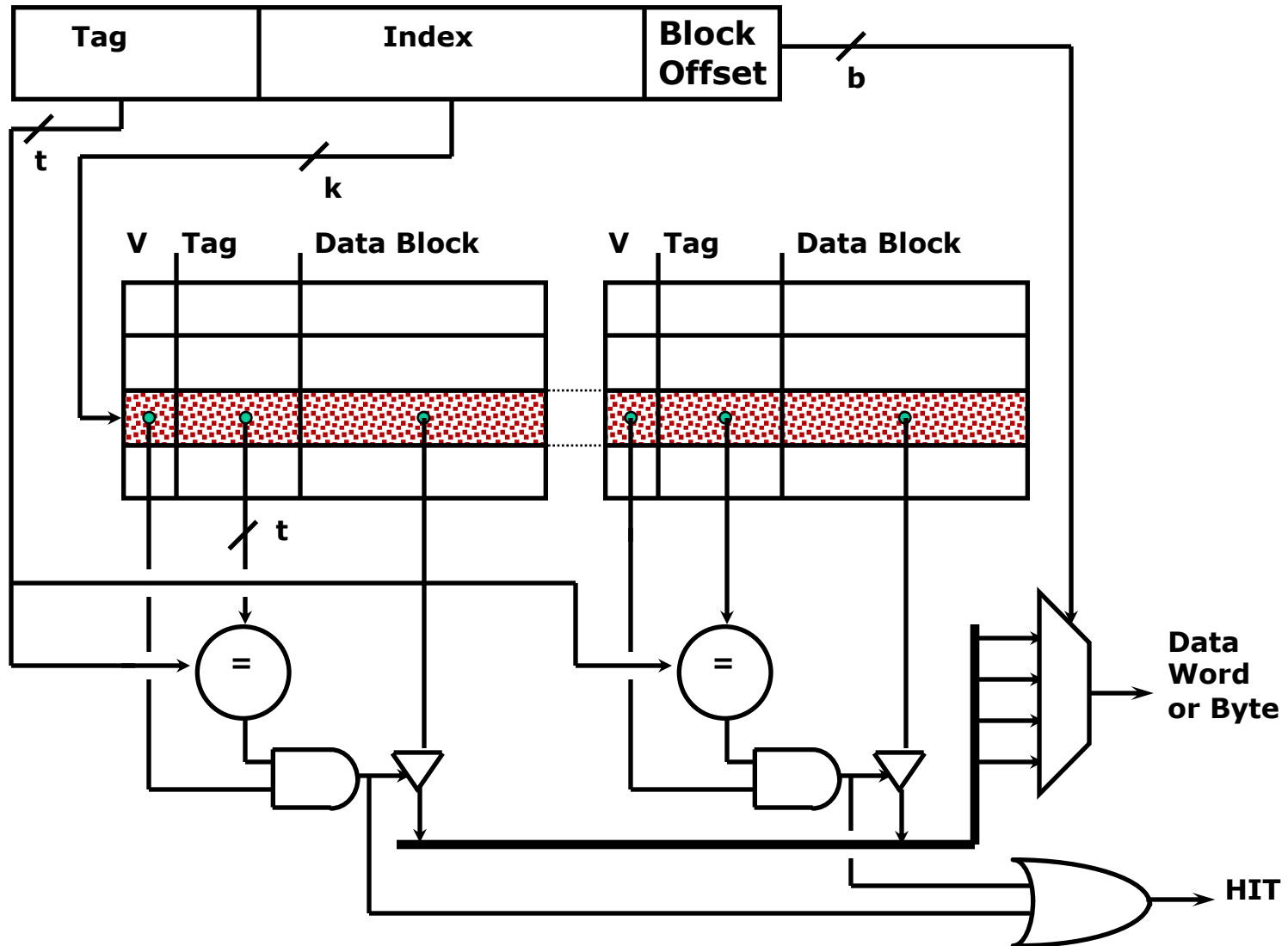


Direct Map Address Selection

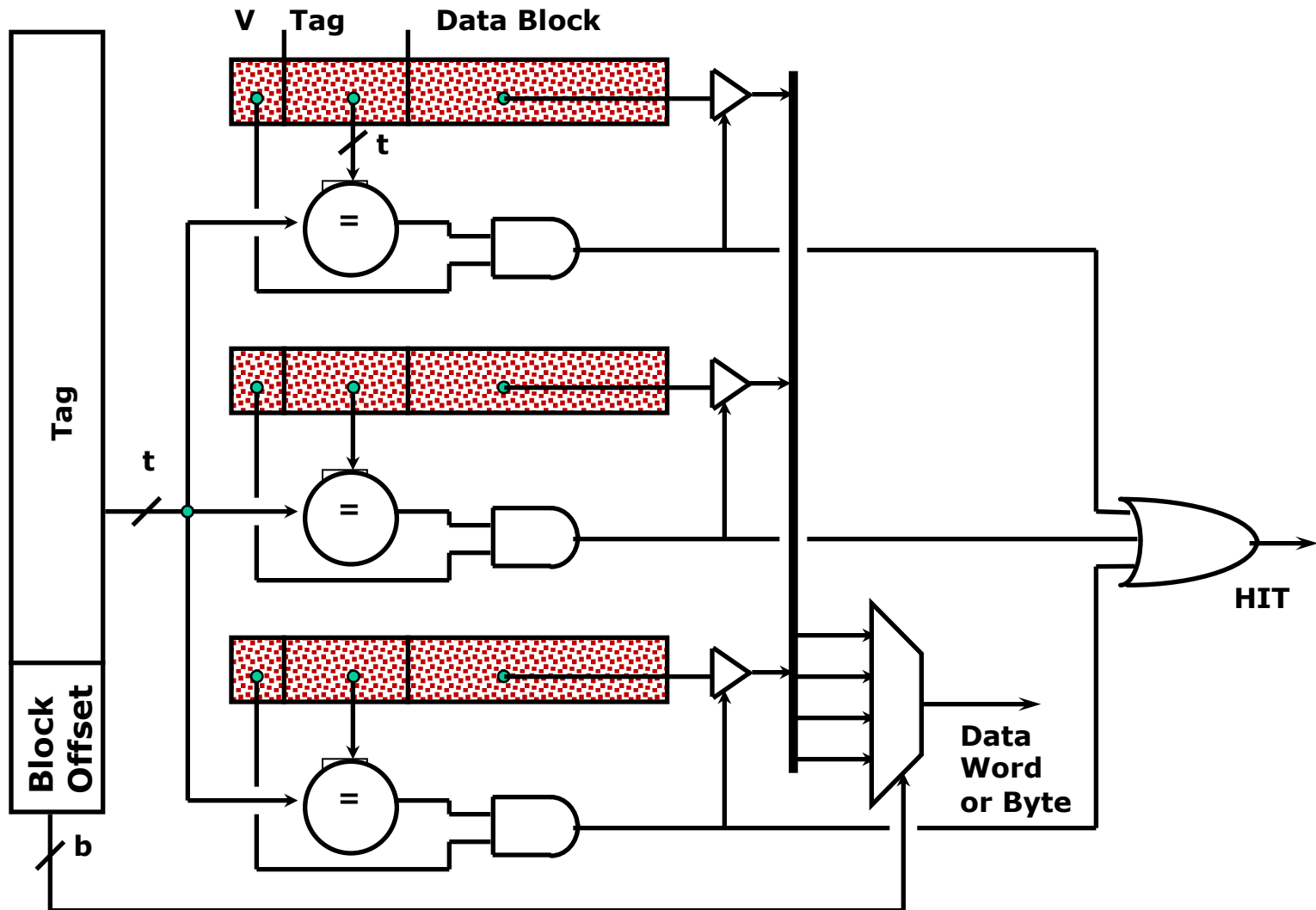
higher-order vs. lower-order address bits



2-Way Set-Associative Cache



Fully Associative Cache



Replacement Policy

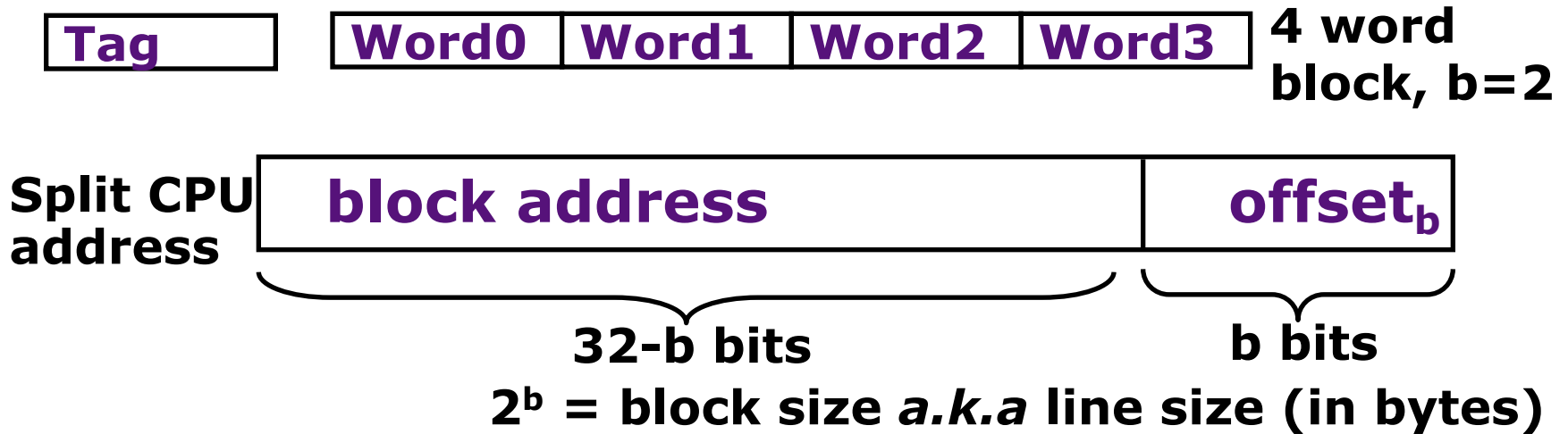
In an associative cache, which block from a set should be evicted when the set becomes full?

- **Random**
- **Least-Recently Used (LRU)**
 - LRU cache state must be updated on every access
 - true implementation only feasible for small sets (2-way)
 - pseudo-LRU binary tree often used for 4-8 way
- **First-In, First-Out (FIFO) a.k.a. Round-Robin**
 - used in highly associative caches
- **Not-Most-Recently Used (NMRU)**
 - FIFO with exception for most-recently used block or blocks
- **Most Recently Used (?)** *Replacement only happens on misses*

This is a second-order effect. Why?

Block Size and Spatial Locality

Block is unit of transfer between the cache and memory



Larger block size has distinct hardware advantages

- less tag overhead
- exploit fast burst transfers from DRAM
- exploit fast burst transfers over wide busses

What are the disadvantages of increasing block size?

Fewer blocks => more conflicts. Can waste bandwidth.

What about writes?

■ Multiple copies of data exist:

- L1, L2, L3, Main Memory, Disk

■ What to do on a write-hit?

- **Write-through** (write immediately to memory)
- **Write-back** (defer write to memory until replacement of line)
 - Need a dirty bit (line different from memory or not)

■ What to do on a write-miss?

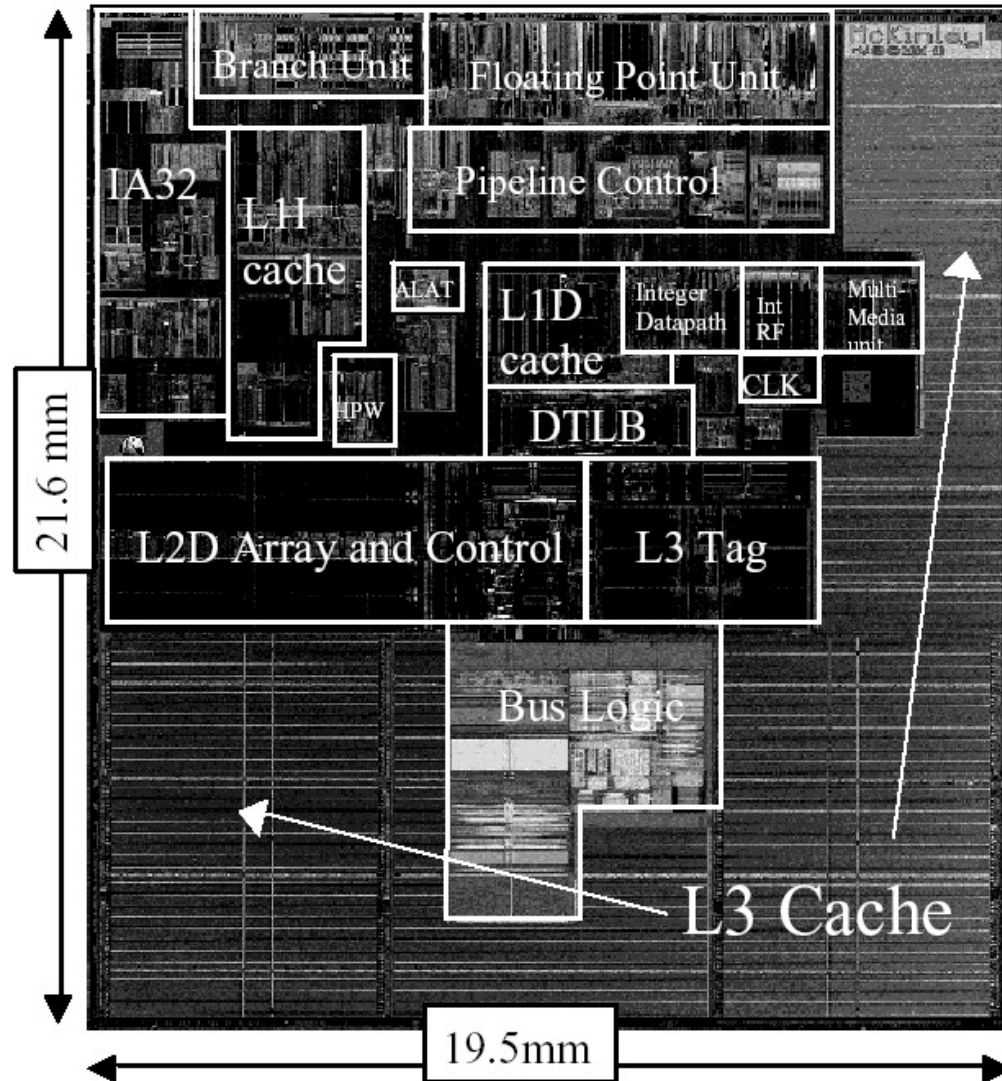
- **Write-allocate** (load into cache, update line in cache)
 - Good if more writes to the location follow
- **No-write-allocate** (writes straight to memory, does not load into cache)

■ Typical

- Write-through + No-write-allocate
- **Write-back + Write-allocate**

Itanium-2 On-Chip Caches

(Intel/HP, 2002)



Level 1: 16KB, 4-way s.a., 64B line, quad-port (2 load+2 store), single cycle latency

Level 2: 256KB, 4-way s.a., 128B line, quad-port (4 load or 4 store), five cycle latency

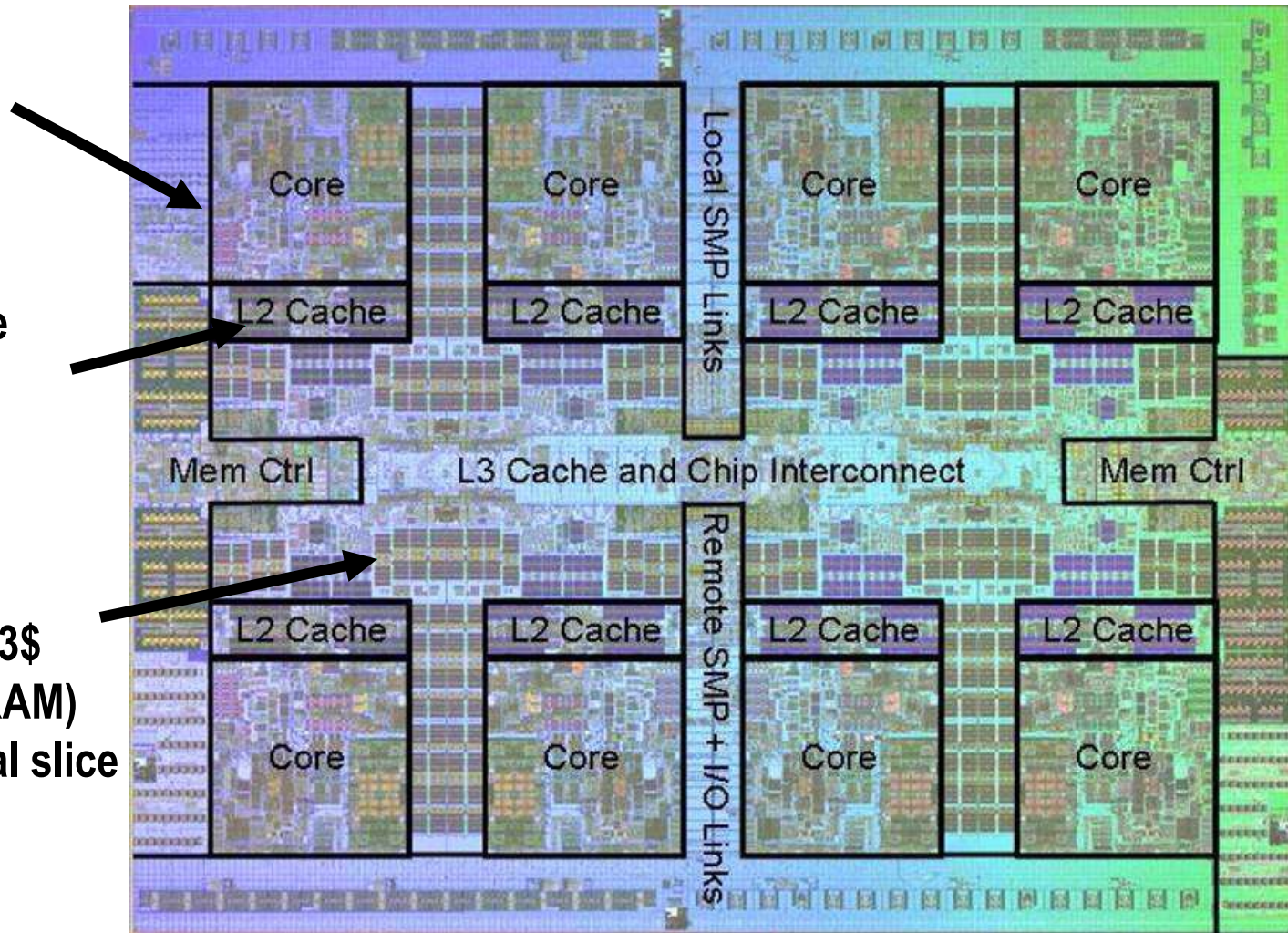
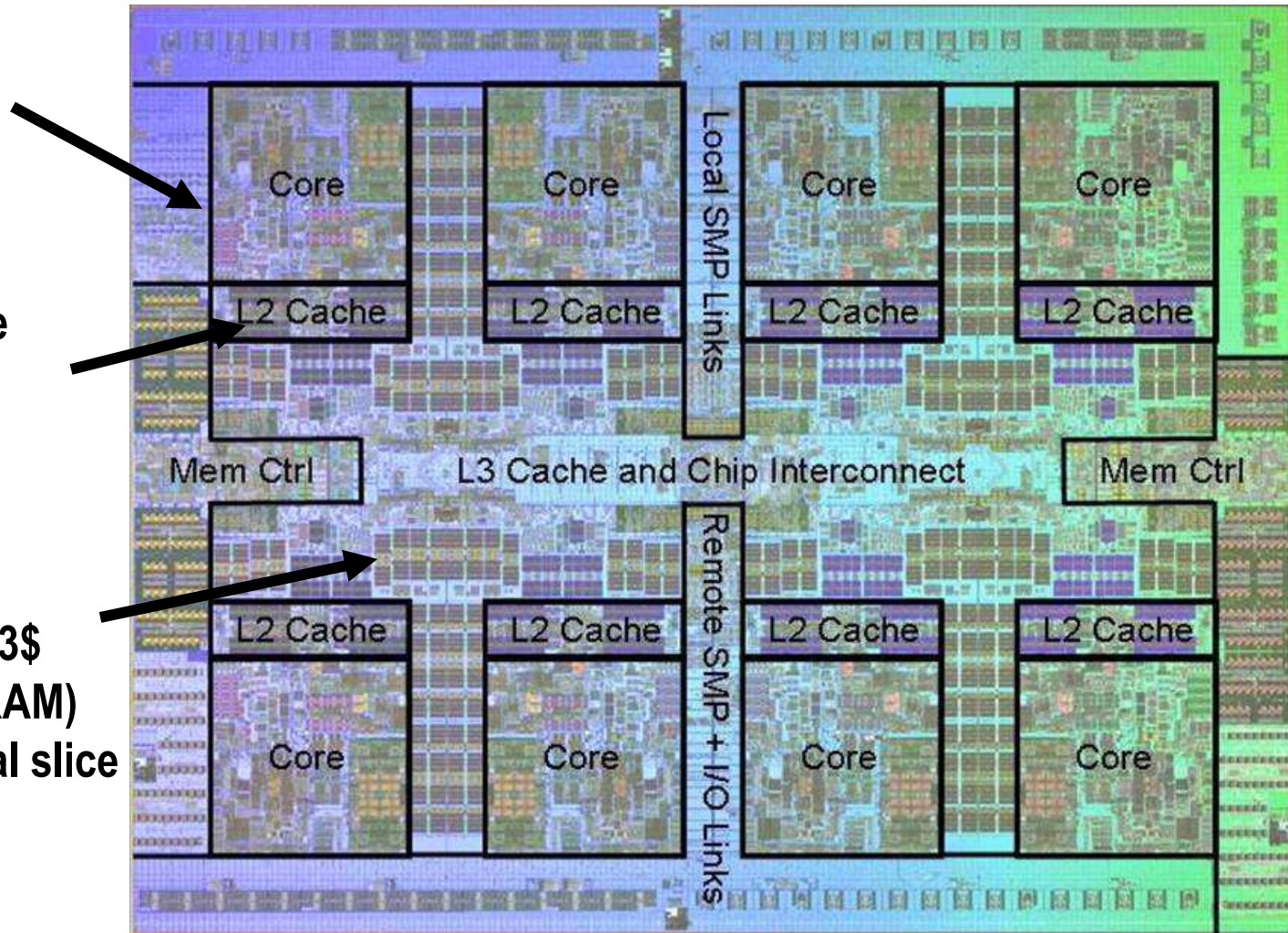
Level 3: 3MB, 12-way s.a., 128B line, single 32B port, twelve cycle latency

Power 7 On-Chip Caches [IBM 2009]

32KB L1 I\$/core
32KB L1 D\$/core
3-cycle latency

256KB Unified L2\$/core
8-cycle latency

**32MB Unified Shared L3\$
Embedded DRAM (eDRAM)
25-cycle latency to local slice**

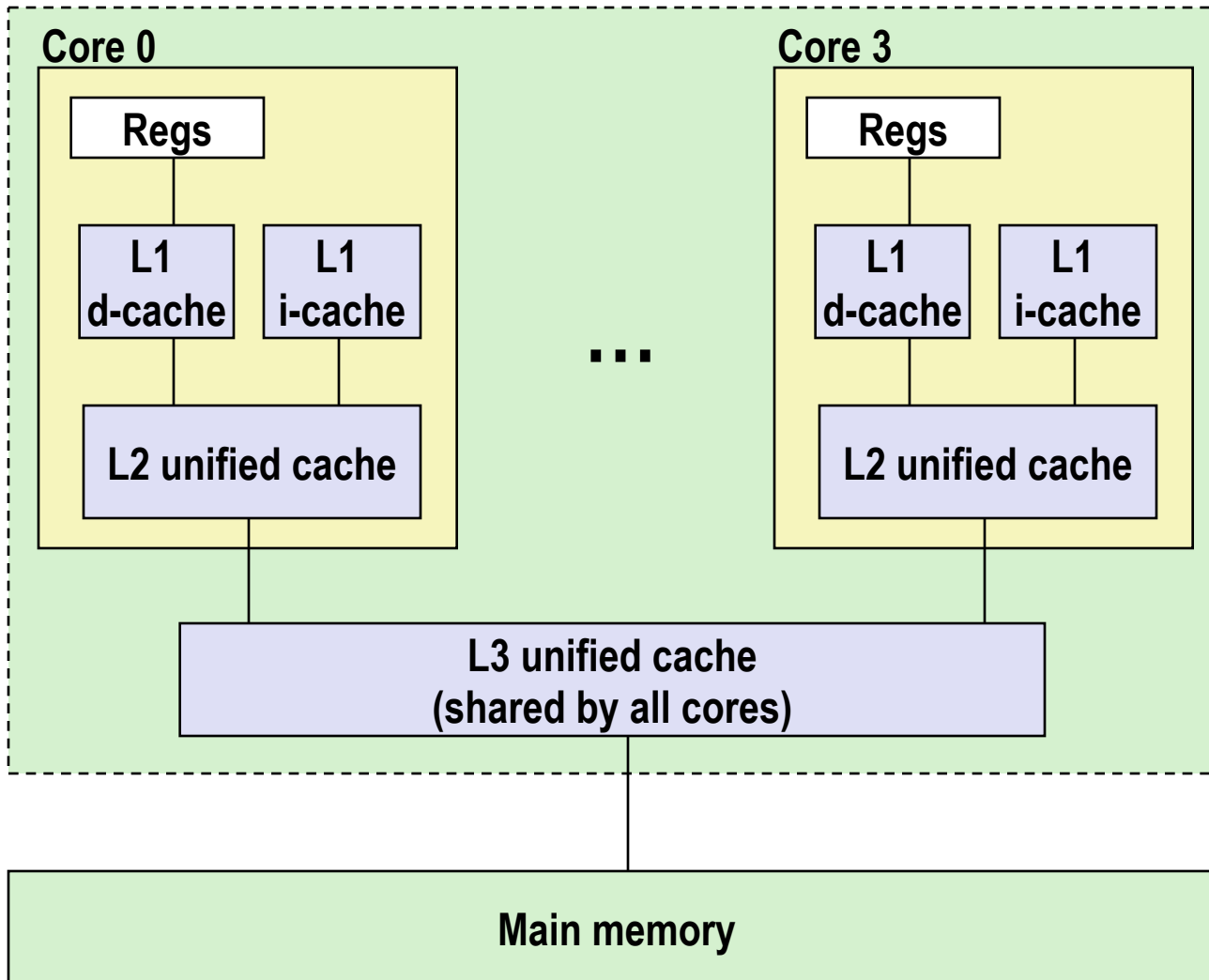


IBM z196 Mainframe Caches 2010

- **96 cores (4 cores/chip, 24 chips/system)**
 - Out-of-order, 3-way superscalar @ 5.2GHz
- **L1: 64KB I-\$/core + 128KB D-\$/core**
- **L2: 1.5MB private/core (144MB total)**
- **L3: 24MB shared/chip (eDRAM) (576MB total)**
- **L4: 768MB shared/system (eDRAM)**

Intel Core i7 Cache Hierarchy

Processor package



L1 i-cache and d-cache:

32 KB, 8-way,
Access: 4 cycles

L2 unified cache:

256 KB, 8-way,
Access: 10 cycles

L3 unified cache:

8 MB, 16-way,
Access: 40-75 cycles

Block size: 64 bytes for
all caches.

Cache Performance Metrics

■ Miss Rate

- Fraction of memory references not found in cache (misses / accesses)
= $1 - \text{hit rate}$
- Typical numbers (in percentages):
 - 3-10% for L1
 - can be quite small (e.g., < 1%) for L2, depending on size, etc.

■ Hit Time

- Time to deliver a line in the cache to the processor
 - includes time to determine whether the line is in the cache
- Typical numbers:
 - 4 clock cycle for L1
 - 10 clock cycles for L2

■ Miss Penalty

- Additional time required because of a miss
 - typically 50-200 cycles for main memory (Trend: increasing!)

Let's think about those numbers

- **Huge difference between a hit and a miss**
 - Could be 100x, if just L1 and main memory
- **Would you believe 99% hits is twice as good as 97%?**
 - Consider:
cache hit time of 1 cycle
miss penalty of 100 cycles
 - Average access time:
97% hits: $1 \text{ cycle} + 0.03 * 100 \text{ cycles} = 4 \text{ cycles}$
99% hits: $1 \text{ cycle} + 0.01 * 100 \text{ cycles} = 2 \text{ cycles}$
- **This is why “miss rate” is used instead of “hit rate”**

Writing Cache Friendly Code

- **Make the common case go fast**
 - Focus on the inner loops of the core functions
- **Minimize the misses in the inner loops**
 - Repeated references to variables are good (**temporal locality**)
 - Stride-1 reference patterns are good (**spatial locality**)

Key idea: Our qualitative notion of locality is quantified through our understanding of cache memories

Acknowledgements

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