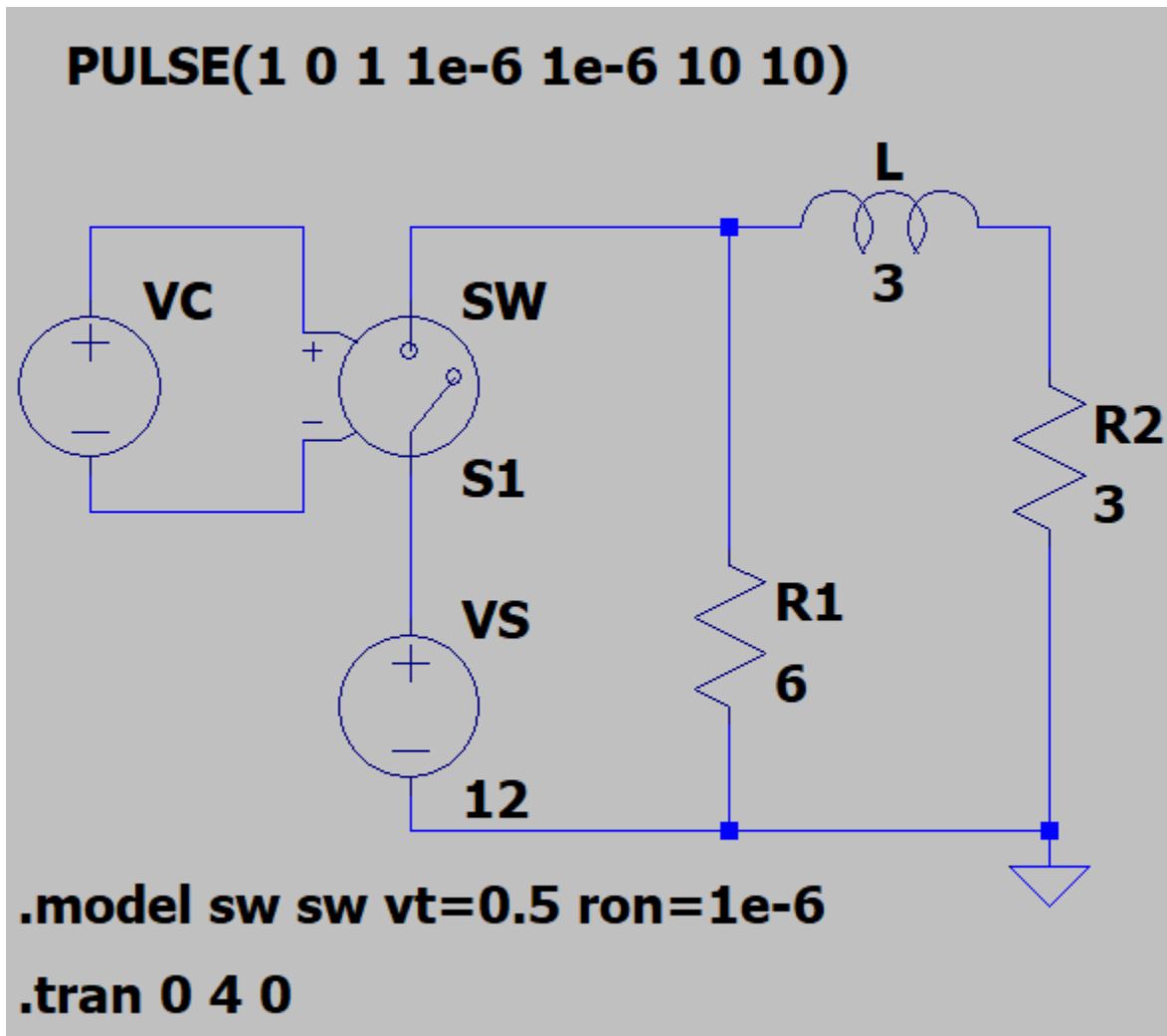


## Assignment 4: Laplace Transform in Circuit Analysis

### Exercise 1: Transient 1st Degree Circuit

Schematic:



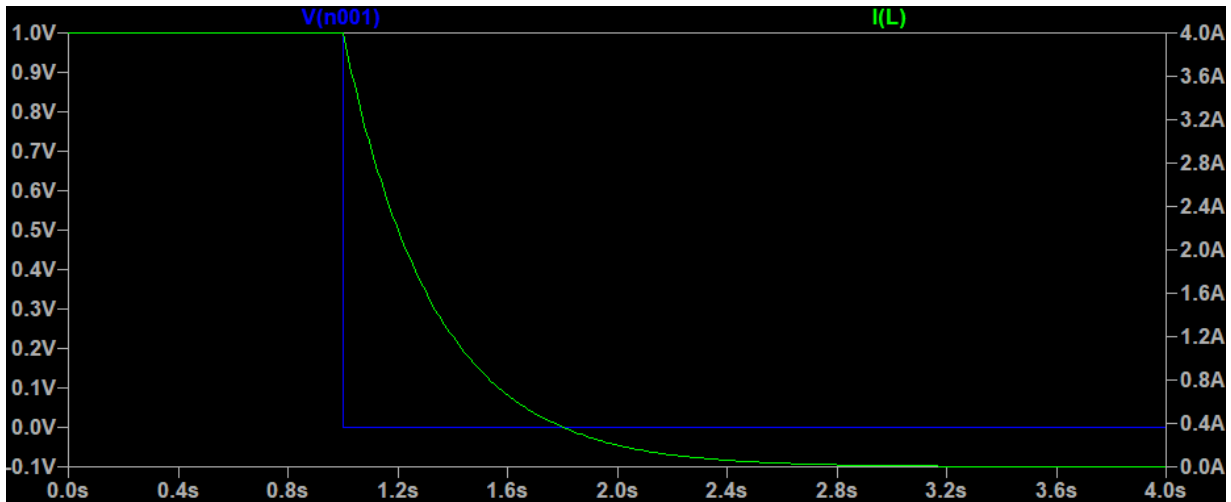
Netlist:

```
* C:\Users\gurle\Documents\LTspiceXVII\eleceng 2cf3 assignments\assignment
4\assig4_q1.asc
R2 N003 0 3
VC N001 N004 PULSE(1 0 1 1e-6 1e-6 10 10)
S1 N005 N002 N001 N004 SW
R1 N002 0 6
```

```

VS N005 0 12
L N002 N003 3
.model sw sw vt=0.5 ron=1e-6
.tran 0 4 0
.backanno
.end

```

**Plot:****Analytical Solution:**

$$V = 12 \text{ V}$$

$$i(0^-) = \frac{V_{R_2}}{R_{R_2}} = \frac{12}{3} = 4 \text{ A}$$

KVL:

$$6i(t) + 3i(t) + 3\frac{di(t)}{dt} = 0$$

$$9i(t) + 3\frac{di}{dt} = 0$$

Laplace Transform:

$$9I(s) + 3[I(s) - I(0^-)] = 0$$

$$9I(s) + 3I(s) - 3I(0^-) = 0$$

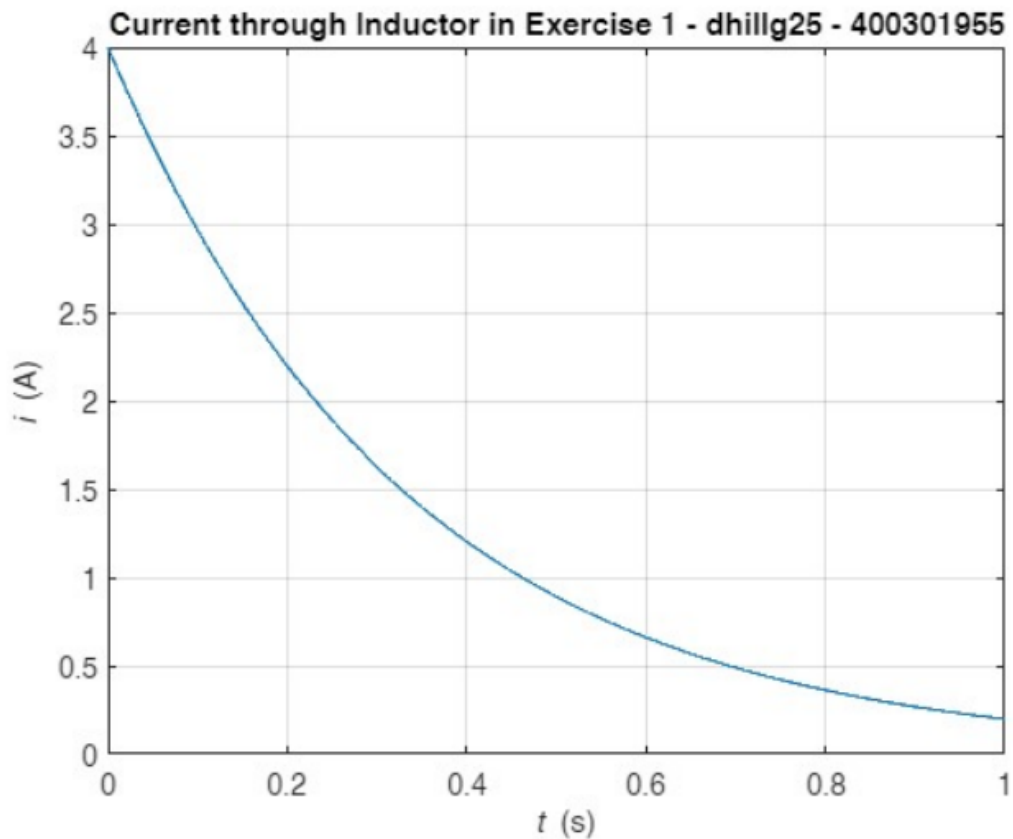
$$I(s)(s + 3) = I(0^-)$$

$$I(s) = \frac{4}{s+3}$$

$$i(t) = 4e^{-3}u(t)$$

**Matlab Source Code and Plot:**

```
clear all; close all; % clean up memory and close all open plot windows
t = linspace(0, 1, 1001); % vector of time samples where function is calculated
i = 4*exp(-3*t); % change this to the function i(t) you found from Laplace analysis
figure;
plot(t, i);
grid on;
title('Current through Inductor in Exercise 1 - dhillg25 - 400301955');
xlabel('\it t (s)');
ylabel('\it i (A)');
```

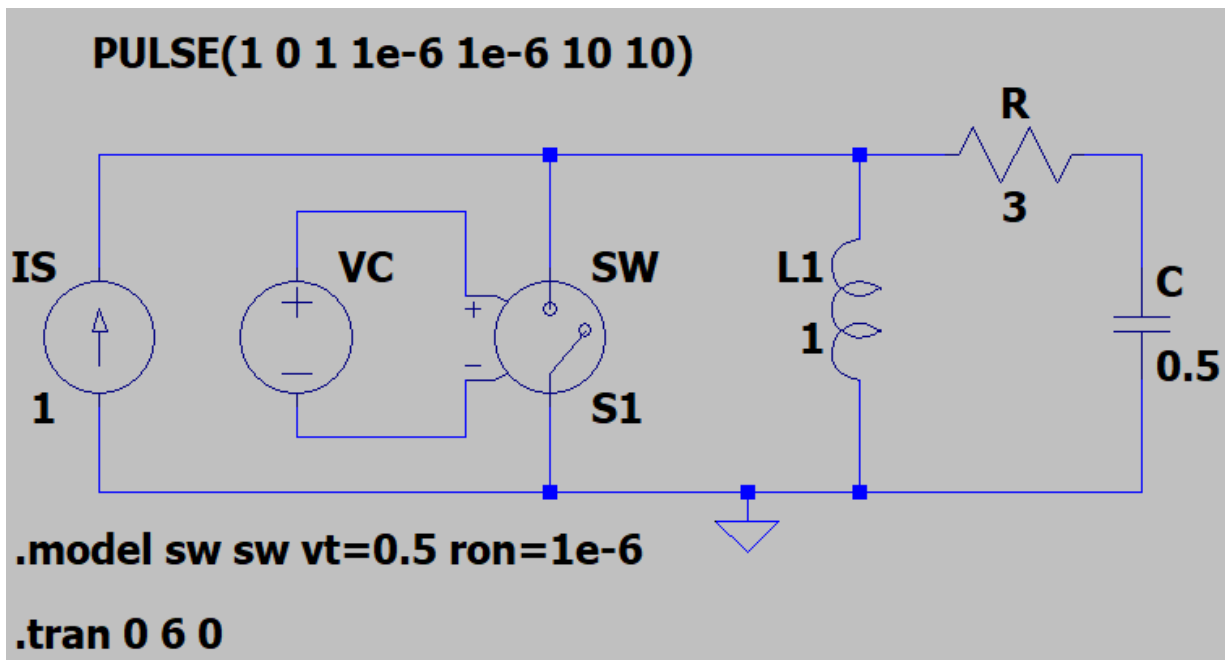


**Does the LTspice simulation result agree with the MATLAB plot of theoretical result? Justify your answers.**

The LTspice simulation results agree with the MATLAB plot. This can be seen as the MATLAB graph matches up with the  $I(L)$  from LTspice.

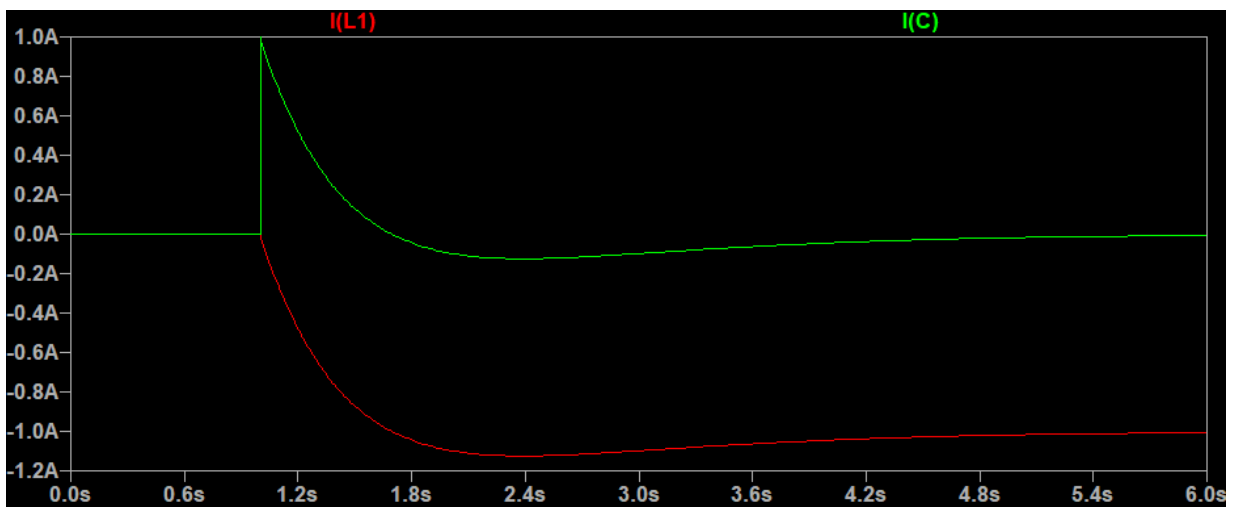
## Exercise 2: Transient 2nd Degree Circuit

**Schematic:**

**Netlist:**

```
* C:\Users\gurle\Documents\LTspiceXVII\eleceng 2cf3 assignments\assignment
4\assig4_q2.asc
R N002 N001 3
VC N003 N004 PULSE(1 0 1 1e-6 1e-6 10 10)
L1 0 N001 1
C N002 0 0.5
S1 0 N001 N003 N004 SW
IS 0 N001 1
.model sw sw vt=0.5 ron=1e-6
.tran 0 6 0
.backanno
.end
```

**Plot:**

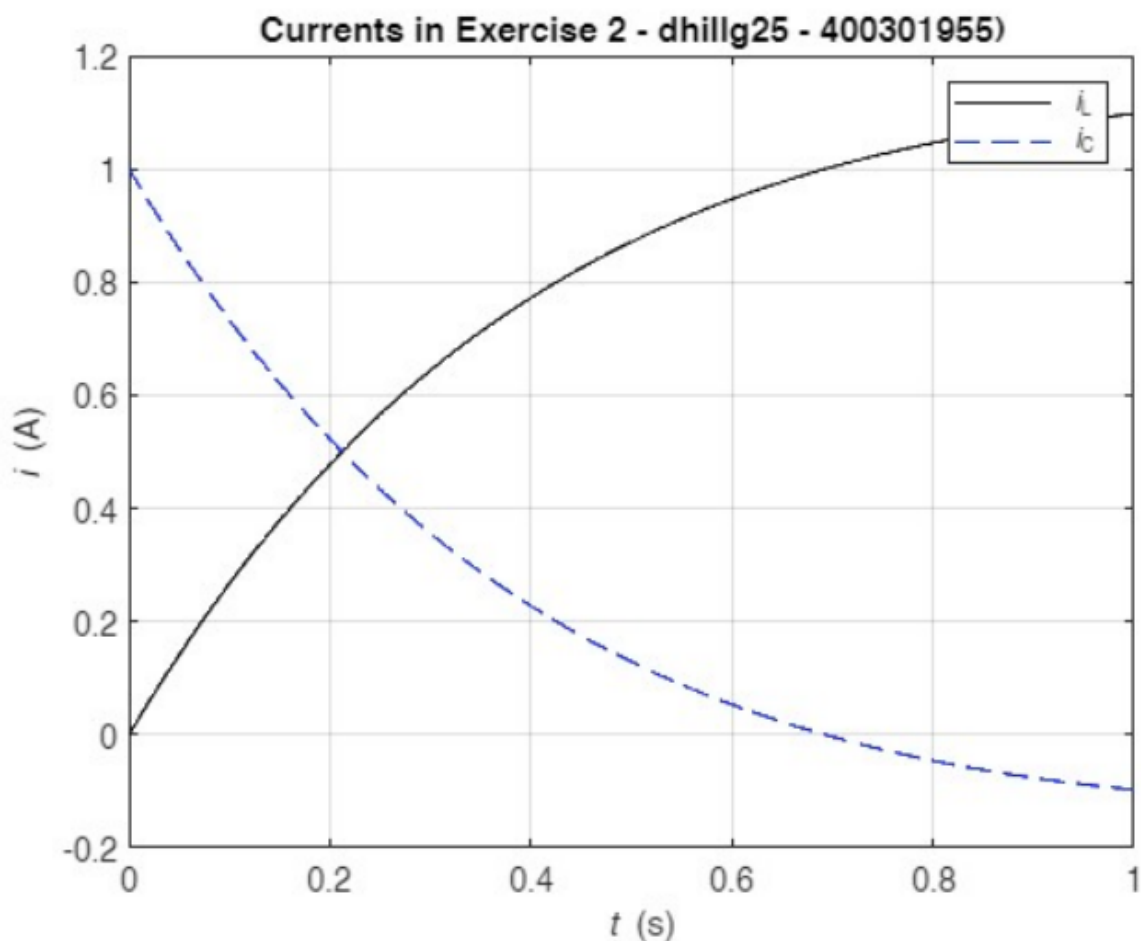


**Matlab Source Code and Plot:**

```

clear all; close all;
t = linspace(0, 1, 1001);
iC = -1*exp(-t) + 2*exp(-2*t); % change this to the function iC(t) you found from Laplace analysis
iL = 1 - iC; % change this to the function iL(t) you found from Laplace analysis
figure;
plot(t, iL, '-k') % plot curve in solid black line
hold on;
plot(t, iC, '--b') % plot curve in dash blue line
hold off;
grid on;
legend({'\it i}_L', '\it i}_C')
title('Currents in Exercise 2 - dhillg25 - 400301955')
xlabel('\it t} (s)');
ylabel('\it i} (A)');

```



**Does the LTspice simulation result agree with the MATLAB plot of the theoretical result? Justify your answers.**

The LTspice simulation results agree with the MATLAB plot. This can be seen as the curve for  $i_C$  approaches 0.