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# Data Structures Notes

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[SPM (DU)]

# Computer Science Notes

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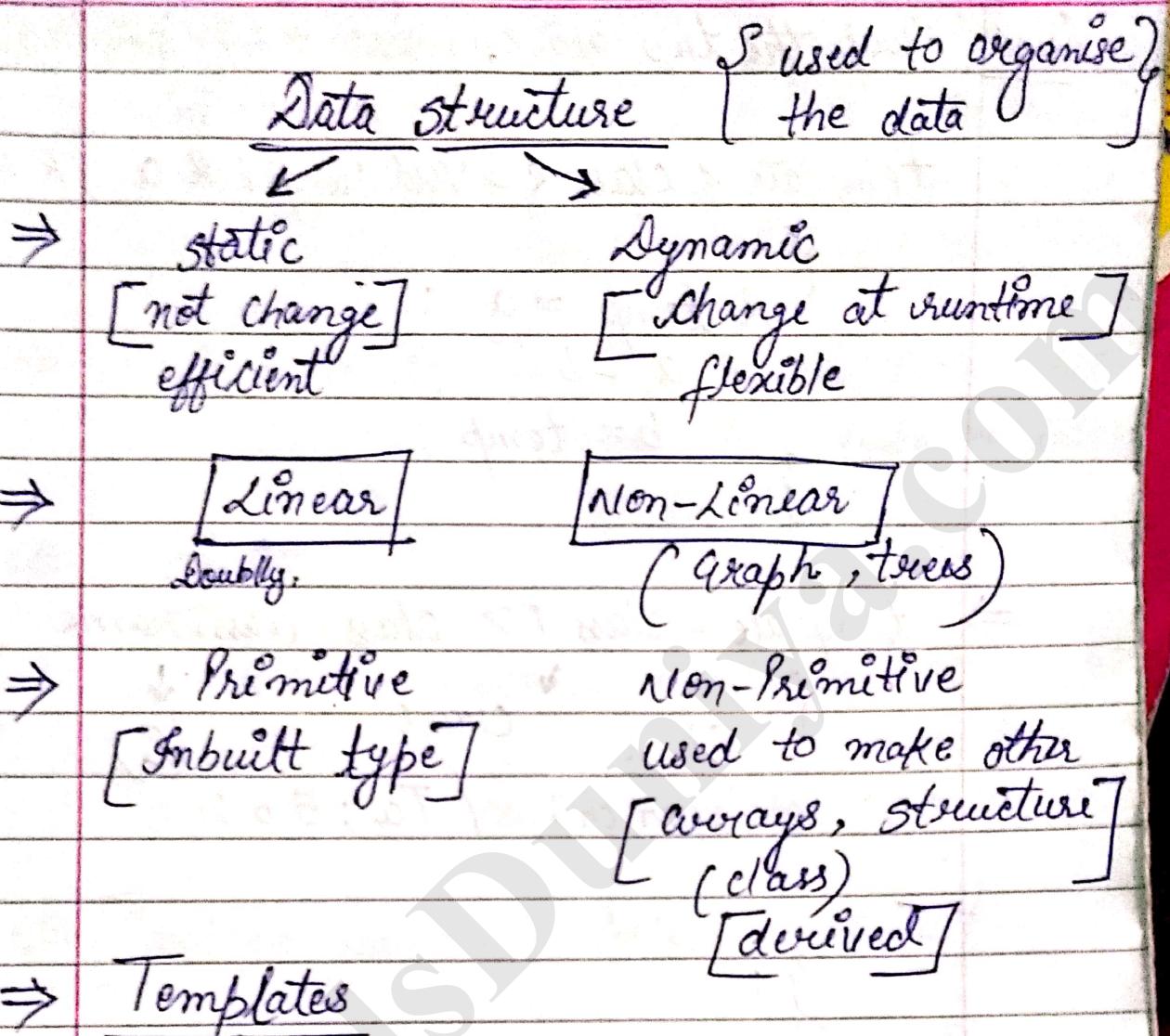
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23/3/2023



Generic code of same function with (vary) data type.

Time independent.

# template < class T > ret\_type f-name (para).

template < class T > T add ( T a, T b )  
{  
 return a+b ;

template < class A > void print ( A c )  
{  
 cout << c ;

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Ques1. Swap the two no.8.

template < class R > void swap( R a , R b )

g

R temp = a ;

a = b ;

g

b = temp ;

⇒ template < class T > class class-name

S

↓

T a ; Class E

(C)

char ch ; / Ta ; Eb ;

g ;

⇒ [for object] →

class-name & > obj ;

C < int > C1 ;

C < double > C2 ;

C < < int, char > C3 ;

⇒ Pointers

①

NULL

②

WILD

③

DANGLING

④

VOID / GENERIC

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⇒ `int *a = new int[5];`  
`int *b = a;`      { b is dangling }  
`delete a;`      Here  
 { b points the deleted a }

⇒ `void * a;`      → Generic pointers that holds any type of data type.

# `void * a;`  
`int i = 100;`  
`a = &i; cout << *(int *) a;`  
`char ch = 'a';`  
`a = &ch; cout << *(char *) a;`

# [Garbage value in void Pointers]

# `int *p;`      { Here p is a }  
`cout << *p;`      NULL pointer }

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(1)

class A

{

int i;

A()

{ i=10;

}

A f1()

{ return this;

}

A &amp; f2()

{ return \*this;

}

void set()

{ i++; }

int get()

{ return i; }

A a1, a2;

a1.f1().set();

a2.f2().set();

cout << a1.get()  $\rightarrow \boxed{10}$   
i =

cout &lt;&lt; a2.get()

 $\rightarrow \boxed{i=11}$ 

dynamic memory  
allocation is mandatory  
to create a copy  
constructor.

(2)

Class A

{ int i;

int \*a;

copy constructor

A( A &amp;a)

{ i = a.i;

A()

for( — )

{ i=10

ar = new int[5];

}

ar[i] = a.ar[i];

}

A a1;

A a2 = a1;

A()

Destructor

300

a2 { i=10 }

a = (300)

delete [] ar;

}

$$m(i,j) = 0 \text{ if } |i-j| > 1$$

upper

	1	4	0
6	2	5	
0	7	3	

⇒ no. of elements =  
 $3n - 2$ .

lower main

$$\begin{bmatrix} n^2 & 3n-2 \end{bmatrix}$$

template < class T >  
 class TD

T {

private

int size

T \* arr;

public:

TD(int n)

size = 3\*n - 2

arr = new T [size];

}

~TD()

{ delete [] arr;

}

#

1	4	0
6	2	5
0	7	3

1	4	6	2	5	7	3
---	---	---	---	---	---	---

{(i-j)}

1 →  $3*i - 1$  lower diagonal0 →  $3*i$  (main)-1 → (upper)  $3*i + 1$

voidEx 1

TM < T > & store { int i, int j, const T val. }

Switch ( $i - j$ )

Switch

equality

K level

Compare

Case

Write

Case -1 : ar [ $3*i + 1$ ] = val;

break;

Case 0 :

ar [ $3*i$ ] = val;

break;

Case 1 :

ar [ $3*i - 1$ ] = val;

break;

default :

if (val != 1) ;

cout << "Print" ;

T & retrieve (int i, int j)

1	2	3	4	5	6	7
---	---	---	---	---	---	---

0 1 2 3 4 5 6

$i - j = 0 \quad ar[i] = val;$

$i - j = -1 \quad ar[n+i] = val;$

$i - j = 1$

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Lower triangle

$$\begin{bmatrix} 1 & 0 & 0 \\ 4 & 2 & 0 \\ 6 & 8 & 3 \end{bmatrix} \quad n=3 \rightarrow 6$$

$\frac{n \times n+1}{2}$

~~2/8/2013~~Symmetric matrix

$$\Rightarrow m(i, j) = m(j, i)$$

mapping:

$$\boxed{n \times i - i \times (i+1)/2 + j}$$

template <class T> class sm

{

int size;

T\* arr;

public :

sm (int n)

{

$$\text{size} = n \times (n+1)/2 ;$$

int arr = new T[size];

{

void store (int i, j, val.)

{

if ( $i \leq j$ )

$$\text{arr}[n \times i - i \times (i+1)/2 + j] = \text{val.}$$

else .

if ( $\text{Val}! = \text{retrieve}(j, i)$ )

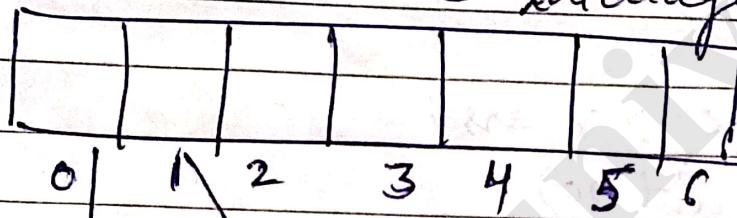
or

 $(\text{Val}! = \text{arr}[n \times j + j \times (j+1)/2 + i])$ Sparse Matrix

(Half entries are zero)

① diagonal matrix

② tridiagonal matrix



row	1	1
column	3	5
value	1	3

0	0	1	0	5	0
0	2	0	0	3	0
4	0	0	0	0	0
0	0	6	7	0	0

4x6

Ques 2

0	0	0	0	0	5	0	2	7
8	0	0	0	3	0	0	0	0
0	9	0	0	0	0	0	4	0
0	1	6	1	0	0	0	0	0

Ans

0							
0	1	2	3	4	5	6	7

Row wise

1	1	2	2	3	3	4	4
6	8	1	5	2	7	2	3
5	2	8	3	9	4	6	1

Column wise

1	2	2	3	5	6	7	8
2	3	4	4	2	1	3	1
8	9	6	1	3	5	4	2

Term1<sup>st</sup> row, col.

Term;

3

Sparse Matrix

P

Term &lt;T&gt; \* arr;

SPM (int nz)

S

arr = new Term &lt;T&gt; [nz];

y

Student [10];

# A[m][N]

Row

=

map (i, j) =

i \* N + j

Student [3]. name;

or

arr [i]. row

arr [i]. value

arr [i]. column

Column

map (i, j) = j \* M + i

# Linklist representation

Array * Static structure * Continuous * Insertion / deletion Costly * Searching easy.	linked list * dynamic structure * No continuous memory allocation. (Random) * easily * Problem in searching (Costly).
--	--

Node

┌ val / data  
 ┌ pointer to next node

Collection of nodes  
 (Scattered)

# template < class T >

class Node

{ Public :

  T data ;

  Node \*Next ;

  Node ()

{

  data = 0 ;

  Next = NULL / 0 ;

}

structure  
 of  
 nodes

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Node (T val, Node \*ptr = 0)

{

    data = value;

    next = ptr;

}

}

LinkedList

Singly

Doubly

Circular LL

[in circle]

1 pointer  
only

& pointer  
(both side)

if not last points to  
null.

Successor

[S + P]

# Singly  $\rightarrow$  template <class T> class SLL

{

    head  $\rightarrow$  first  
    tail  $\rightarrow$  last

    Node <T> \* head, \* tail;

    SLL ()

{

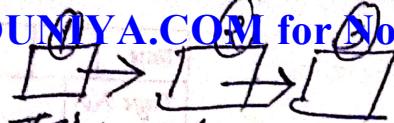
    head = tail = 0;

}

Void addAtHead (T val)

{

    Node <T> \* n1 = new Node <T>  
                        (val);



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1st points the second & second points the third node.

### Insert

head = tail = 0

① if ( head == 0 )

{  
head = n1;  
tail = n1;

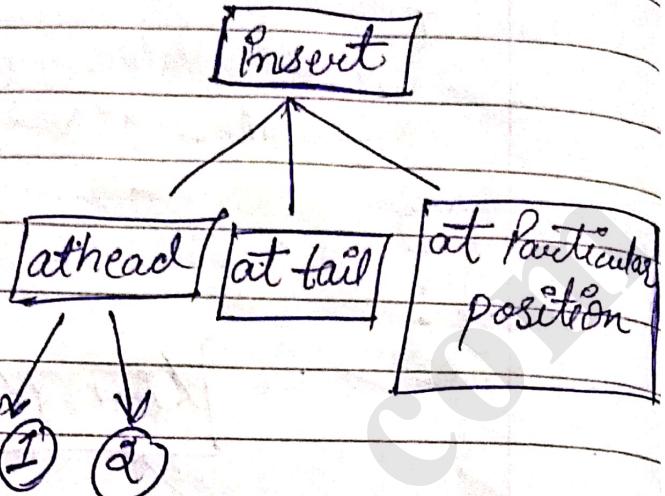
else

② {

n1 → next = head;

head = n1;

{  
}



Void addAtTail (T val)

{

Node< T > \* n1 = new Node< T >(val);

if ( tail == 0 )

{

head = tail = n1;

{

else

{  
tail → next = tail->n1;  
tail = n1;

{

```

void display()
{
    Node<T>* temp = head;
    while (temp != 0)
    {
        cout << temp->data;
        temp = temp->next;
    }
}

```

Void AddAtPos ( Tval, int pos )

```

{
    if ( pos == 1 || head == 0 )

```

addAtHead ( val );

else

```

    Node<T>* temp = head;
    int i=1;
    for ( ; i < pos-1; i++ )
    {
        temp = temp->next;
    }

```

~~Order (n) time  
Order of position~~

$n_1 \rightarrow next = tempt \rightarrow next$

$tempt \rightarrow next = n_1;$

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if ( $\text{temp} == \text{tail}$ )

$\text{tail} = \text{null}$

}

Display  $\rightarrow$

$5 \rightarrow 7 \rightarrow 10 \rightarrow 1$

6 | 8 | 2019

# bool search (T value)

if Node < T > \*temp = head;

if ( $\text{head} == \text{null}$ )

{ return false;

else

if ( $\text{head} == \text{tail}$ )

{ if ( $\text{head} \rightarrow \text{data} == \text{value}$ );

{ return true;

else

return false;

else

Node \* temp; int Pos = 1;

while ( $\text{temp} != \text{null} \& \& \text{temp} \rightarrow \text{data} != \text{value}$ )

Pos ++;

temp = temp  $\rightarrow$  next;

}

```

if (temp->data == Deleto)
else return false;
else
    return True;

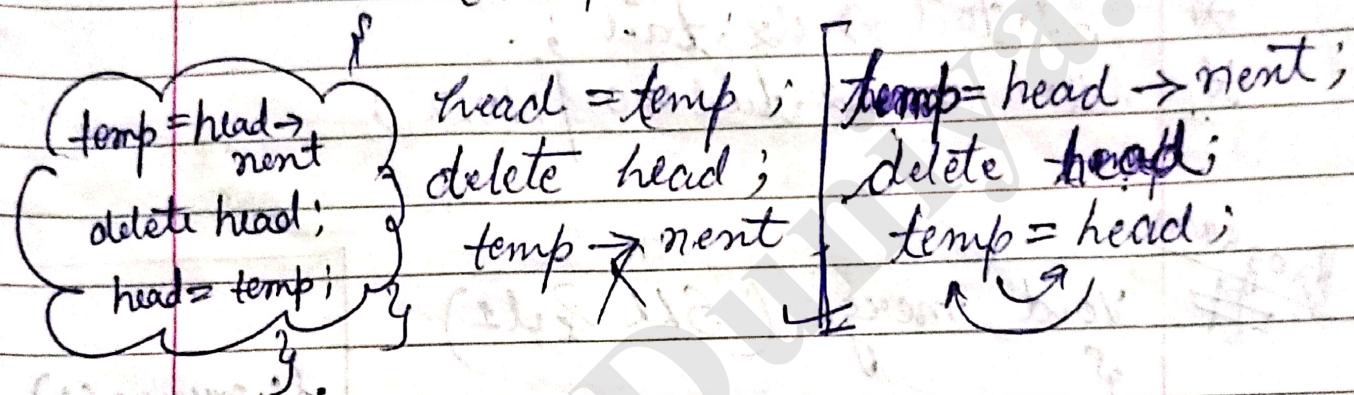
```

# ~SLL()

```

{ Node<T> *temp = head;
while (temp != 0)

```



# reverse()

```

{ Node<T> *temp = head;
curr = temp
1 -> 2 -> 3 -> NULL

```

```

* curr = head;
0 <- 1 <- 2 <- 3 ->

```

curr temp

```

* prev = 0;
1 <- 2 <- 3 -> NULL

```

= prev curr temp

```

while (curr != 0)

```

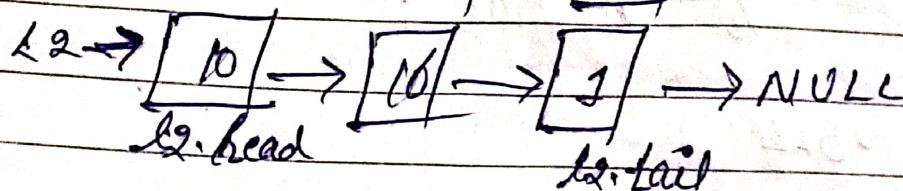
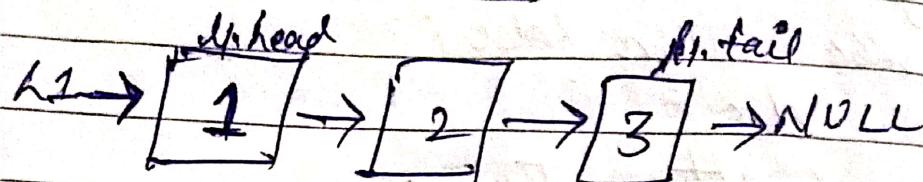
curr temp



(Merge)

Concatenate two SLL

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- \*  $l1.tail \rightarrow next = l2.head;$
- \*  $l2.tail \rightarrow l2.old\_head;$
- \*  $l2.h = l2.tail = 0 \text{ } / \text{ } \text{NULL};$

~~Program~~

Void merge (SLL &amp; l2)

{

If ( head == 0 &amp;&amp; l1.head == 0 )

{

cout &lt;&lt; "empty";

}

l1.merge(l2)



else if ( head != 0 &amp;&amp; l1.head == 0 )

{

cout &lt;&lt; "2nd list empty";

}

else if ( head == 0 &amp;&amp; l1.head != 0 )

{

head = l1.head;

tail = l1.tail;

l1.head = l1.tail = 0;

}

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else {

tail-&gt;next = dl.head;

tail = dl.tail;

dl.h = dl.t = 0;

}

Ques if (dl+dl2)

void operator+

(SLL &amp; L1).

dl.operator+(dl2);

# Deletion

from head

from tail

⇒ FROM HEAD

void deleteFromHead()

{

if (head == 0)

cout &lt;&lt; "Empty";

else if (head == tail)

cout &lt;&lt; "node passed" &lt;&lt; head-&gt;data

delete head;

head = tail = 0;

}

dangling  
Pointers

else  
{

Node<T> \*temp = head ;  
head = head → next ;  
delete temp ;  
}

⇒ FROM TAIL

# void deleteTail ()  
{

If Node<T> \*temp = head ;

while ( temp → next != tail )

{  
temp = temp → next ;

}

delete tail ;

tail = temp ;

tail → next = 0 ;

}

PRACTICE

~~11~~ ✓ void deletenode (T Val)

{ if (head == 0)

cout <<

else if (head == tail && head->data  
== Val) {

}

delete head;

head = tail = 0;

}

else {

Node<T> \* temp = head, \* prev;  
while (temp != 0 && temp->data !=  
Val) {

}

prev = temp;

temp = temp->next;

If (temp == 0)

{ cout << "No data";

}

else { prev->next = temp->next;  
delete temp;

}

Ques=1

LL(Given)

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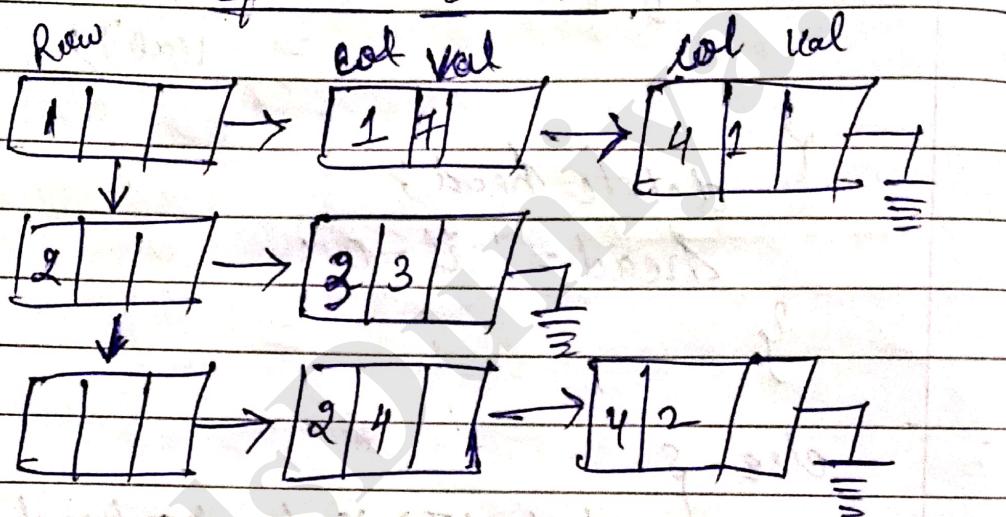
Search / find middle Node  
MAP to find a man of a link.

Ques=2Print even pos<sup>n</sup> nodes.Ques=3

Find loop node's position.

~~13/8/2019~~

Linkedlist Representation of a Sparse Matrix



7	0	0	10	7
0	0	3	0	0
0	4	0	2	0

# Doubly Linked list

template &lt;class T&gt; class Node

{

T data;

Node \*next, \*prev;

Node()

{ data = 0;

next = prev = NULL;

Node ( $T$  val, Node \* $p1 = 0$ , Node \* $p2 = 0$ )

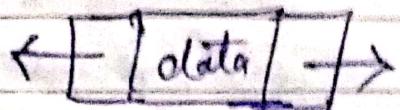
{

    data = val;

    next = p1;

    prev = p2;

{



$\Rightarrow$  template < class  $T$  > class DLL

{

    Node< $T$ > \*head, \*tail;

    DLL ()

{

        head = tail = 0;

{

#

    void AddAtHead (  $T$  val)

{

        Node< $T$ > \*n1 = new Node< $T$ >(val);

        if ( head == 0 )

            head = tail = n1;

{

        else

            n1->next = head;

            head->prev = n1;

            head = n1;

{

{

# void AddAtTail ( T val )

{

Node < T > \* n1 = new Node < T > ( val );

if ( head == 0 )

{ tail

head = tail = n1;

}

else

{

tail->next = n1;

n1->prev = tail;

tail = n1;

}

# void addAtPos ( int pos , T val )

{

if ( pos == 1 || head == 0 )

addAtHead ( val );

else

{

Node < T > \* temp = head ;

for ( int i = 0 ; i < pos - 1 && temp != 0 )

temp = temp->next ; i++ ;

} else {

Node < T > \* temp2 = temp->next ;

temp->next = n1 ;

n1->next = temp2 ;

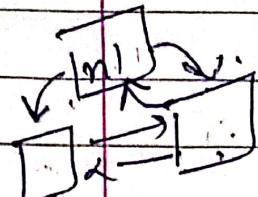
temp2->prev = n1 ;

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$n1 \rightarrow prev = temp;$

{

[OR] else



if

if ( $temp \rightarrow next$   
 $\neq 0$ )

{

$n1 \rightarrow next = temp \rightarrow next$

$n1 \rightarrow prev = temp;$

$temp \rightarrow next \rightarrow prev = n1$

$temp \rightarrow next = n1;$

}

# Void concatenate ( DLL & L1 )

{

if ( $head == 0 \&& l1.head \neq 0$ )

{

$head = l1.head$

$tail = l1.tail$

$l1.head = l1.tail = 0;$

{

else

{

$tail \rightarrow next = l1.head;$

$l1.head \rightarrow prev = tail;$

$l1.head = l1.tail = 0;$

$tail = l1.tail;$

# Void deleteFromHead()

{

if ( $head == 0$ )

cout << "empty";

else

(2) 6 7 8  
→  
3 4 5 6 7 8

~~Node 7 →~~  
if ( $\text{head} == \text{tail}$ )

{

    delete head ;

    head = tail = 0 ;

}

else

{

    head = head  $\rightarrow$  next ;

    delete head  $\rightarrow$  prev ;

    head  $\rightarrow$  prev = NULL ;

}

# void deleteFromTail()

{

~~Node 2 → 7 → 8~~

else

{

    tail  $\Rightarrow$  tail  $\rightarrow$  prev ;

    delete tail  $\rightarrow$  next ;

    tail  $\rightarrow$  next = NULL ;

}

~~at front  
const time~~

H.W! Reverse (DLL) / Delete particular Node  
(after search)

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# void reverse ()  
{

Node <T> \*curr = head, \*temp;  
while (curr != 0)

{  
temp = curr → next;  
curr → next = curr → prev;  
curr → prev = temp;  
curr → curr → prev;

}

state  
Head  
tail

3

# void deletenode (T val)

{

else

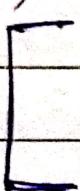
{ Node <T> \*temp = head;

while (temp != 0 && temp → data != val)

{  
temp = temp → next;

temp → prev → next = temp → next;  
temp → next → prev = temp → prev;  
delete temp;

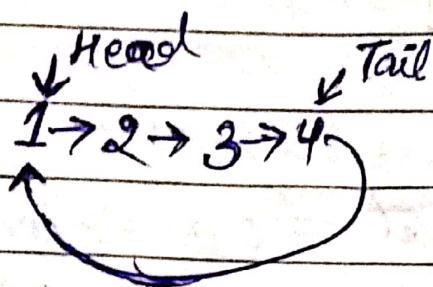
if (temp != tail)



3

3

#

Circular linkedlist

class Node

{

int data;

Node \*next;

Node()

{ data = -1;

next = 0;

}

Node( int val, Node \*p = 0)

{ data = val;

next = p;

}

class CLL

{

Node \*head, \*tail;

CLL()

{ head = tail = 0;

}

void addAtHead( int val)

{

Node \*n1 = new Node( val);

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if (head == 0)

{ }

head = tail = n1 ;

& tail → next = head ;

else

{ n1 → next = head ;

head = n1 ;

tail → next = n1 ;

}

# void addAtTail (int val)

{ }

Node \* n1 = new Node (val) ;

if (tail == 0)

{ }

head = tail = n1 ;

tail → next = head ;

}

else

{ }

tail → next = ~~tail~~ n1 ;

tail = n1 ;

n1 → next = head ;

}

{ }

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# void display()

{

    Node \*temp = head;

    do

        { cout << temp->data;

        temp = temp->next;

    }

    while (temp != head);

~~DO~~

    while (temp->next != head)

        {

            cout << temp->data;

            temp = temp->next;

        }

    cout << tail->data;

    }

# void concatenate ( CLL & l1 )

{

    if (head == 0 && l1.head == 0)

        {

            cout << "empty";

        }

    else if (head != 0 && l1.head == 0)

        {

            cout << "2<sup>nd</sup> list empty";

        }

    else if (head == 0 && l1.head != 0)

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5 6 7 8  
x temp = head.

{

 $\text{head} = l1.\text{head};$  $\text{tail} = l1.\text{tail};$  $l1.\text{tail} = l1.\text{head} = 0;$ 

{}

else

{ } tail  $\rightarrow$  next =  $l1.\text{head};$ ~~tail  $\rightarrow$  head~~ $l1.\text{tail} \rightarrow \text{next} = \text{head};$  $\text{tail} = l1.\text{tail};$ 

{}

 $l1.\text{head} = l1.\text{tail} = 0;$ 

{}

~~20/08/2019~~

# void reverse()

{}

Node \* curr = head, \* prev = tail;

\* temp;

do

{}

 $\text{temp} = \text{curr} \rightarrow \text{next};$  $\text{curr} \rightarrow \text{next} = \text{prev};$  $\text{prev} = \text{curr};$  $\text{curr} = \text{temp};$ 

{}

while ( curr != head );

~~Swap~~

{

Node \*Swap;

Swap = tail;

tail = head;

head = Swap;

3 → 4 → 5 → 6 → 8 → 9

↑

3 4 5 6 8 9

5 6 7

# deletion from Head ()

{

Node \*temp = head;

if (head == 0)

{

cout &lt;&lt; "empty";

else if (head == tail)

{

delete head;

head = tail = 0;

else

{ Node \*temp = head;

head = head → next;

tail → next = head → next;

delete temp;

{

## # Void delete fromTail ()

```

    {
        if ()
    }
}
```

```
else if ( head == tail )
```

```

    {
        cout << "node" << tail -> data;
        delete tail;
    }
```

```
    head = tail = 0;
```

```
else { for ( Node<T> *temp = head;
```

```
            temp -> next != tail;
```

```
            temp = temp -> next );
```

```
            temp -> next = head;
```

```
            delete tail;
```

```
            tail = temp;
```

```

    }
}
```

## # Void deleteFromNode (int val)

```

    {
        int res = 0; if ( head == 0 ) cout << empty
        else
```

```

        {
            Node<T> *temp = head, prev = 0;
            do
```

```

        {

```

```
            if ( temp -> data == val )
```

```

            {

```

```
                res += 1;
```

```
            if ( temp == head )
```

```
deleteFromHead();  
else if (temp == tail)  
    deleteFromTail();  
else  
{  
    prev->next = temp->next;  
    if (temp == tail)  
        tail = prev;  
    delete temp;
```

{

break;

}

prev = temp;

temp = temp-&gt;next;

{

while (temp != head);

if (res == 0)

{

cout &lt;&lt; "Value not found";

{

{

23/08/2019

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## Self organizing lists

(1) (2) (3)

(1) Move to front -

$$\Rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 0 \rightarrow 5 \rightarrow \text{NULL}$$

$$0 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow \text{NULL}$$

No Exit  
↓  
add at  
Tail

(2) Transpose Method -

$$\Rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow \text{NULL}$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow \text{NULL}$$

$$1 \rightarrow 2 \rightarrow 5 \rightarrow 3 \rightarrow 4 \rightarrow \text{NULL}$$

↓

(3) Count Method -

$$\Rightarrow 1 \overset{(0)}{\rightarrow} 2 \overset{(0)}{\rightarrow} 3 \overset{(0)}{\rightarrow} 4 \overset{(0)}{\rightarrow} \underline{\underline{5}} \quad [\text{Search } (3)]$$

$$3 \overset{(1)}{\rightarrow} 1 \overset{(0)}{\rightarrow} 2 \overset{(1)}{\rightarrow} 4 \overset{(0)}{\rightarrow} \underline{\underline{5}} \quad [\text{Search } (2)]$$

$$\Rightarrow 3 \overset{(1)}{\rightarrow} 2 \overset{(0)}{\rightarrow} 1 \overset{(0)}{\rightarrow} 4 \overset{(1)}{\rightarrow} \underline{\underline{5}} \quad [\text{Search } (1)]$$

$$2 \overset{(0)}{\rightarrow} 3 \overset{(0)}{\rightarrow} 1 \overset{(0)}{\rightarrow} 4 \overset{(0)}{\rightarrow} \underline{\underline{5}} \quad \} \text{ Any.}$$

(4) Ordering Method -

Insert at according  
to itself

$$\Rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 9 \rightarrow 13 \overset{1}{\rightarrow} \underline{\underline{5}}$$

in order

#	MTF	T	C	O
A	A	A	A A	
C	$A \rightarrow C$	AC	AC	AC
E	$A \rightarrow C \rightarrow E$	ACE	ACE	ACE
C	$C \rightarrow A \rightarrow E$	CAE	CAE	ACE
B	$C \rightarrow A \rightarrow E B$	CAEB	CAEB	ABCE
D	CAEBD	CAEBD	CAEBD	ABCDE
B	BCAED	CABED	<del>CBAED</del>	ABCDE
A	ABCD	ACBED	CABED	ABCDE
A	ABCD	ACBED	CBAED	ABCDE
E	EABCD	<del>EACBED</del>	ABCED	ABCDE

Assign:

4, 1, 0, 1, 3, 2, 2, 1, 3, 0, -1, 4

## # Ordered List

⇒ class Node

{

};

class DLL

{

Node \* head, \* tail;

DLL()

{

head = tail = 0;

{

# void insert (int val)

{ if (head == 0)

{ if (list == empty)

    h = t = n1;

}

else

    if (head -> data > val)

{ N1 -> next = head;

Date			
Page No.			

head = n1;

}

else if (tail → data < val)

{

tail → next = n1;

val);

}

tail = n1;

else

{ Node \*temp = head;

while (temp != 0 && temp → data < val)

{ temp1 = temp;

temp = temp → next;

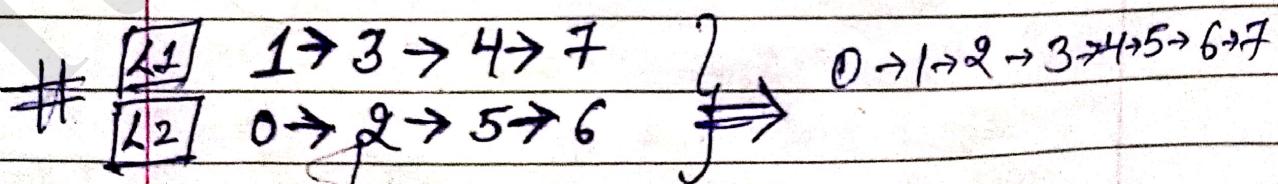
}

temp1 → next = n1;

n1 → next = temp;

}

g



⇒ Concatenate in ordered manner.

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$\text{temp1} = \text{head}, \text{temp2} = \text{l}. \text{head};$

while (  $\text{temp1} \neq 0 \& \& \text{temp2} \neq 0$  )

{ if (  $\text{temp2} \rightarrow \text{data} < \text{temp1} \rightarrow \text{data}$  )

{ if (  $\text{temp2} \rightarrow \text{next} \rightarrow \text{data} < \text{temp1} \rightarrow \text{data}$  )

{  $\text{temp} = \text{temp2} \rightarrow \text{next};$

$\text{temp2} \rightarrow \text{next} = \text{temp1};$

{  $\text{temp2} \rightarrow \text{temp};$

else

{  $\text{temp2} = \text{temp2} \rightarrow \text{next};$

}

}

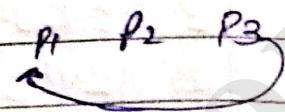
else

PRACTICE				
	Date			
	Page No.			
<del>Answers</del>	MTF	T	C	O
4	4032	4	40	4
1	41	41	41	14
0	410	410	410	014
1	140	140	140	014
3	1403	1403	1403	0134
2	14032	14032	14032	01234
2	21403	14023	12403	01234
1	12403	14023	12403	01234
3	31240	14032	13240	01234
0	03124	10432	10324	01234
-1	03124(-1)	10432(-1)	10324(-1)	(-1)01234
4	40312(-1)	14032(-1)	10432(-1)	(-1)01234

26/08/2023

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## Application of Linked list

S.L	DLL	CLL
Addition of the polynomials. $5x^2 + 3x + 5$ Coefficient, power & a pointer that points another	undo, redo back, forward In MS Word	Round Robin Scheduling Algorithm 

⇒ template < class T > class Node

class Node

```

{ int Coeff;
  int power;
  Node *next;
  Node ()
```

}

```

  Coeff = power = -1;
  next = NULL;
```

{}

```
Node ( int c, int p, Node *n = 0 )
```

```

{ power = p ;
  coeff = c ;
  next = n ; }
```

{}

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class Poly

 $3x^2$ 

Power = 2

Coeff = 3

{ node \* head, \*tail;

Poly()

{ h=t=0;

{ }

} void input ( int p, int c )

{ node \* n = new Node ( c, p );

if ( h == 0 )

{ h=t=n;

{ }

If ( head-&gt;power == p )

{ head-&gt;coeff += c;

{ OR  
in TAIL }

else if ( head-&gt;power &lt; p )

{ }

n-&gt;next = head;

head = n;

{ }

else if ( tail-&gt;power &gt; p )

{ }

tail-&gt;next = n;

tail = n;

{ }

else

{ }

node \* temp = head;

\*pre;

while ( temp-&gt;power &gt; p &amp;&amp; temp != tail )

$\{$   
 $\text{pre} = \text{temp};$

$\text{temp} = \text{temp} \rightarrow \text{next};$

$\{$   
 $\text{if } \text{pre} \rightarrow \text{next} = n;$

$\{$   
 $n \rightarrow \text{next} = \text{temp};$

$\{$   
 $\text{if } (\text{temp} \rightarrow \text{power} < p)$

$\{$   
 $\text{else} .$

$\{$

$\text{temp} \rightarrow \text{coeff} + = c;$

$\text{delete } n;$

$\{$

$\{$

$\{$

$\Rightarrow \text{void display}()$

$\{$

$\text{Node} * \text{temp} = \text{head};$

$\text{while } (\text{temp} \neq 0)$

$\{$

$\text{cout} \ll \text{temp} \rightarrow \text{coeff} \ll "x"$

$\ll \text{temp} \rightarrow \text{power};$

$\text{if } (\text{temp} \neq \text{tail})$

$\{$

$\} \text{ cout} \ll "+";$

$\{ \text{temp} \Rightarrow \text{temp} \rightarrow \text{next};$

$\{$

$\{$

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Ques=1

$$P_1 \Rightarrow 5x^4 + x^3 + 3x^2$$

$$P_2 \Rightarrow 4x^4 + 7x^3 + 5x^2 + 2x^1$$

Add them.

$$\Rightarrow P_3 = 4x^4 + 12x^3 + 7x^2 + 5x + 5.$$

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$\Rightarrow$  void Concatenate(const Poly & P2) const  
Add / Sum

{

Poly P3 ;

if ( head == 0 &amp;&amp; P2.head == 0 )

{

cout &lt;&lt; "empty structure" ;

{

else if ( head != 0 &amp;&amp; P2.h == 0 )

{

P3.head = head ;

{

else if ( head == 0 &amp;&amp; P2.h != 0 )

{

P2.h = P2.head ;

{

else

{

Node \*t1 = head , \*t2 = P2.head ;

while ( t1 != 0 &amp;&amp; t2 != 0 )

{

if ( t1-&gt;power == t2-&gt;power )

Page No. \_\_\_\_\_

P3. input ( $t1 \rightarrow \text{power}, t1 \rightarrow \text{coeff} + t2 \rightarrow \text{coeff}$ )  
 {  
 }  $t1 = t2 \rightarrow \text{next};$   
 }  $t2 = t2 \rightarrow \text{next};$

else if ( $t1 \rightarrow \text{power} > t2 \rightarrow \text{power}$ )

{ P3. input ( $t1 \rightarrow \text{power}, t1 \rightarrow \text{coeff}$ );  
 }  $t1 = t1 \rightarrow \text{next};$

else if ( $t1 \rightarrow \text{power} < t2 \rightarrow \text{power}$ )

{ P3. input ( $t2 \rightarrow \text{power}, t2 \rightarrow \text{coeff}$ );  
 }  $t2 = t2 \rightarrow \text{next};$

} }

else

{ while ( $t1 != 0 \&\& t2 == 0$ )

{ P3. input ( $t1 \rightarrow \text{power}, t1 \rightarrow \text{coeff}$ );  
 }  $t1 = t1 \rightarrow \text{next};$

}

while ( $t2 != 0 \&\& t1 == 0$ )

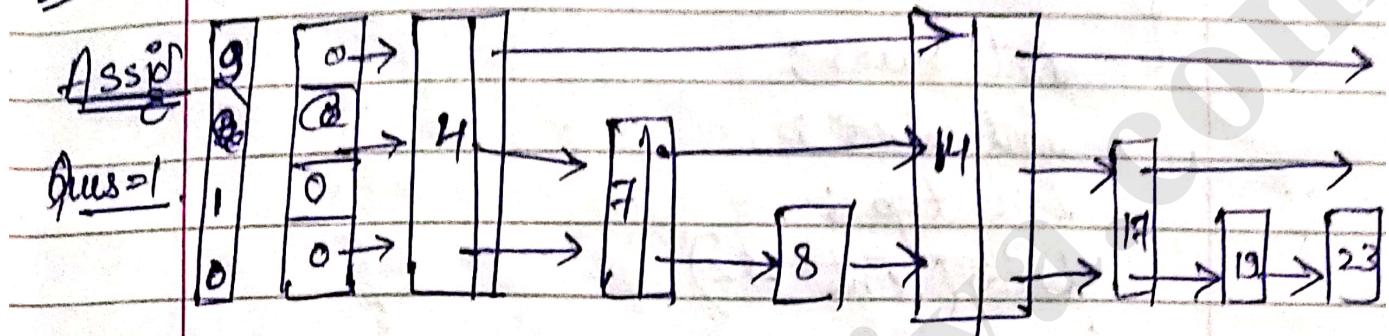
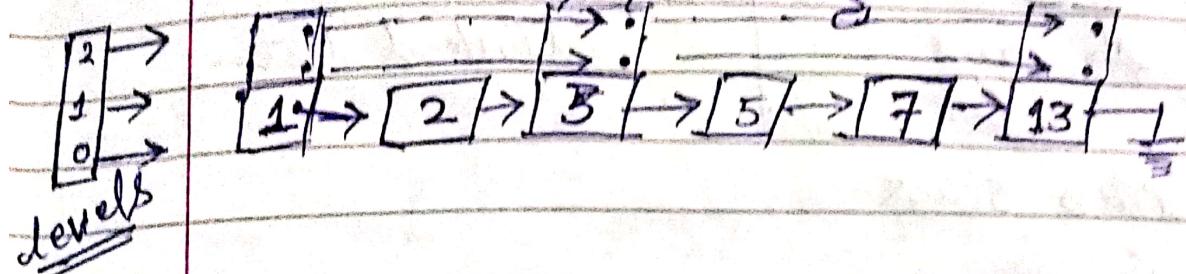
{

{ P3. input ( $t2 \rightarrow \text{power}, t2 \rightarrow \text{coeff}$ );  
 }  $t2 = t2 \rightarrow \text{next};$

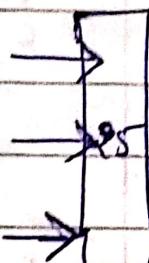
}

$\Rightarrow$  Skip Lists

Searching



Search [20, 1, 7, 9]



Level 1  $\rightarrow$  3 Compare

27/08/2019

Stack & Queue

Stack  $\rightarrow$  LIFO  
 $\rightarrow$  FILO

Queue  $\rightarrow$  FIFO

Stack.

- $\rightarrow$  # Push()
- $\rightarrow$  # Pop()
- $\rightarrow$  # del()
- $\rightarrow$  # IsEmpty()
- $\rightarrow$  # Clear()

Static



Arrays

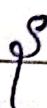
Dynamic



Linked list.



class stack



int \*arr;

int size;

int top;

stack ( int sz )



top = -1;

size = sz;

arr = new int [sz];



void push ( int el )



if ( top == ( size - 1 ) )



cout &lt;&lt; " overflow " ;



else



top = top + 1

arr [ ++ top ] = el ;

] any



By using L.L

class Node

{

int data;

=

Node \* next;

Node (int e, Node \* p1 = 0)

{

data = e;

next = p1;

}, }

}, class Stack

{

Node \* top;

Stack ()

{

top = 0;

{

void push (int el)

{ Node \* n1 = new Node (el);

if (top == 20)

{

top = n1;

}

else

{

n1 → next = top;

top = n1;

}

```

int
void pop (int el)
{
    if (top == 0)
    {
        cout << "empty";
        return -1;
    }
    else
    {
        Node *temp = top;
        top = top->next;
        int v = temp->data;
        delete temp;
        return v;
    }
}

```

## # Stack Application

- ① Checking for balanced parenthesis
- ② Express<sup>n</sup> evaluation
- ③ Infix to postfix

30/08/2019

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→ `bool checkBalanceExpr (char *s)`

{ stack <char> s1;

for ( i=0 ; i < strlen(s) ; i++ )

{ if ( s[i] == '(' || s[i] == '[' || s[i] == '{' )

s1.push ( s[i] )

else if ( s[i] == ')' || s[i] == ']' || s[i] == '}' )

{ ~~s1.pop ( s[i] )~~

if ( s1.pop () != s[i] )

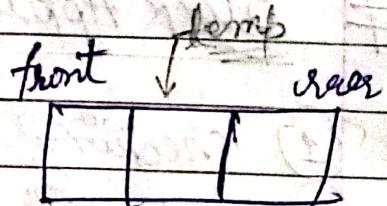
return false;

} else if {

} else if ]

} }

Queue



Class Node

{

int val;

Node \*next;

Node ( int e, Node \*p1 = 0 )

{

val = e;

next = p1;

}

{

In Queue New Node  
at the end & delete  
at Head.

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------------	----------------

Ques 1

class Queue

{  
    Node \*Front \* rear ;

    Queue ()

    {  
        Front = rear = 0 ;

}

    ⇒ void enqueue ( int el )

    {  
        Node \* n1 = new Node ( el );

        if ( Front == 0 )

            {  
                Front << "empty" ;  
                Front = rear = n1 ;

            else if {

                rear → next = n1 ;

                rear = n1 ;

}  
    }

    ⇒ void dequeue ( int el )

    {  
        Node \* n1 = new Node ( el );

        if ( front == 0 )

            {  
                cout << "empty" ;

            else if ( f == r )

                delete f ;

            {  
                f = r = 0 ;

else

```

    { temp = front->next;
      f = f->next;
      delete temp;
    }
  }
}

```

# class Queue

```

{ int *arr;
  int size;
  int *f, *r;
  Queue (int sz)
  {
    size = sz;
    arr = new int [sz];
    f = r = -1;
  }
}

```

void enqueue (int el)

```

{ if ( r == (size - 1) && f == 0 )
    {
      overflow;
      f = r + 1;
    }
}

```

else

```

{ arr [++r] = el;
  arr [(r + 1) % size] = el;
}
}

```

Order (3)  
due to  
Priority  
Current / future

void degreae (int &f)

{  
if ( front == -1 )

{ cout << " underflow";

else if ( f == r )

{ f = r = -1 ;

else

{ set front;  
front = (f+1) % size ;

}

# Postfix expression evaluated

Add two large no.

Convert infix  $\Rightarrow$  postfix

5|4|+|3|\*

$\Rightarrow (\text{expr}[i] \geq '0' \& \& '9')$

(5+4)\*3  
27

st.push (expr[i] - '0')

[  
 $\Rightarrow$  num = 0;

$\Rightarrow \text{if} (\text{expr}[i] \geq '0' \& \& '9')$

{ while ( expr[i] != '.' )

{ num = num \* 10 + (expr[i] - '0');

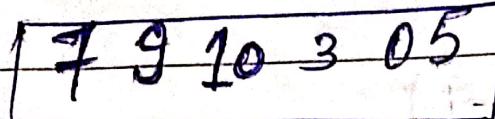
}; i++;

2/9/2013

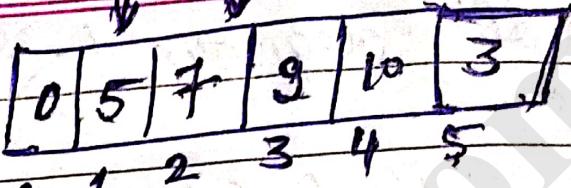
Queue.

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display as

Ques 21

rear front

 $\Rightarrow i^{\circ} = \text{front};$ while ( $\text{front} \neq \text{rear}$ )

{

cout << arr [ $i^{\circ}$ ]; $i^{\circ} = (i^{\circ} + 1) \% \text{size};$ 

}

cout << arr [ $i^{\circ}$ ] / rear;for ( $i^{\circ} = \text{top}; i^{\circ} \geq 0; i^{\circ}--$ 

for stack.

display

Ques 22Add two no. using  
stack.

Void

$\Rightarrow \{$  while ( $s1.top! = -1 \& \& s2.top! = -1$ )

 $\}$ 

int  $n1 = s1.pop();$

int  $n2 = s2.pop();$

Sum =  $n1 + n2 + c;$

If (Sum  $\leq 9$ )

 $\}$ 

$s3.push(Sum);$

$c = 0;$

else

$\{ c = Sum / 10;$

Sum =  $Sum \% 10;$

$s3.push(Sum);$

 $\}$ 

if ( $c > 0$ )

$s3.push(c);$

 $\}$

while ( s1.top != -1 && s2.top != -1 )

{  
int n1 = s1.pop();

sum = n1 + c;

if ( sum <= 9 )

{  
s3.push( sum );

c = 0;

else

{

sum = sum % 10;

c = sum / 10;

}

{

if ( c > 0 )

{  
s3.push( c );

}

while ( s1.top == -1 && s2.top != -1 )

{

{

y

## Infix to Postfix Conversion

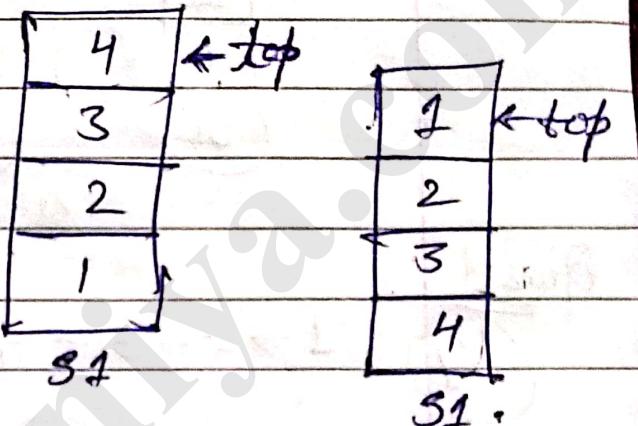
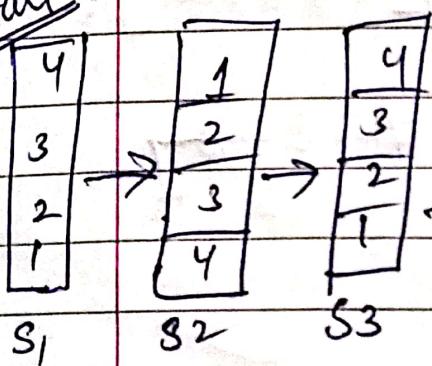
(Q)

$$5 + 4 * 3 \\ \Rightarrow 54 + 3 *$$

[Stack application]

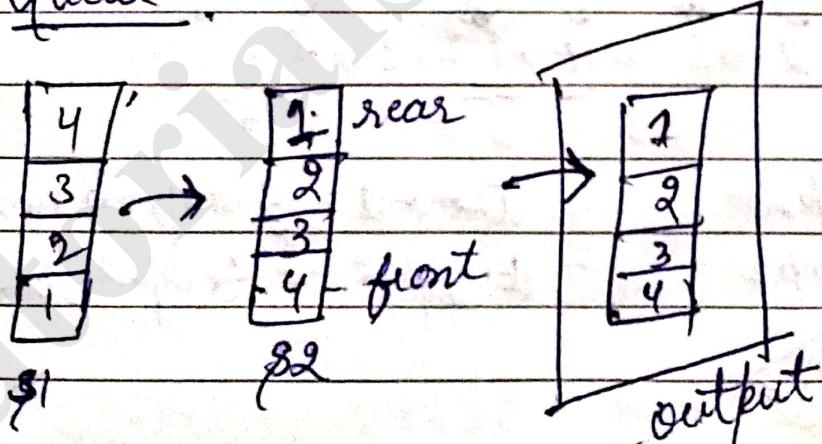
$\Rightarrow$  Reverse elements of Stack

using additional  
stack.

~~Stack~~.

again  
push in S1.

## Queue



Ques=1. using one stack + auxiliary var.

Ques=2 L1 1  $\rightarrow$  2  $\rightarrow$  3  $\rightarrow$  4  $\rightarrow$  5  $\rightarrow$  NULL

L2 0  $\rightarrow$  4  $\rightarrow$  5  $\rightarrow$  NULL

Common

$\rightarrow$  1  $\rightarrow$  2  $\rightarrow$  3  $\rightarrow$  4  $\rightarrow$  5  $\rightarrow$  NULL

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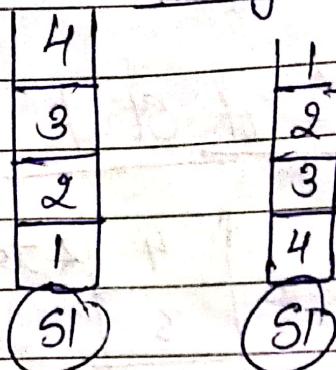
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Find first intersection / common node.

6/9/2019

using one stack + auxiliary var.



$\text{temp} = \text{S1.pop}();$

Count

[2 variable].

Ques-1

Q1

$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 9$

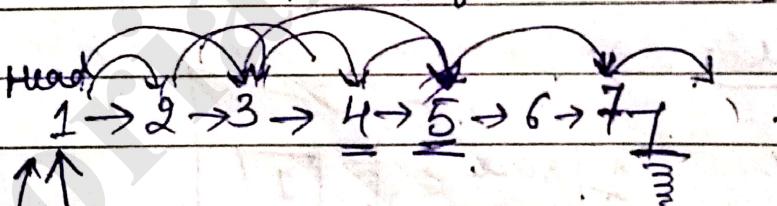
L2

10

Skip 4 nodes from L1.

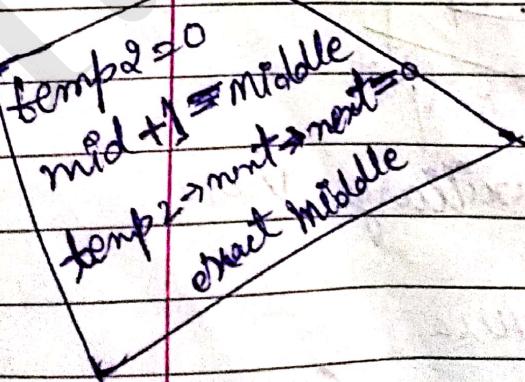
Then for loop for both list [m, N].

Ans=2



$\text{temp1} = \text{temp1} \rightarrow \text{next}$

$\text{temp2} = \text{temp2} \rightarrow \text{next} \rightarrow \text{next}$



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6/9/2018 Recursion (chapter)

## Activation Frame / Stack Frame [use in ds]

### Factorial

$\Rightarrow$  int Fact (int num)

Non  
Tail

{ if (num == 0 || num == 1)  
    { return 1; }

else [return num \* fact (num - 1)];

}

}

### Types of Recursion

Tail

call only

Simple recursion.

$\boxed{\text{return } (n-1);}$

Non-Tail

Complete.

when +

call.

[Ex :-  
above

factorial  
function]

Indirect

void f()

{

g();

}

void g()

{

f();

}

when a function  
call directly or  
indirectly call itself  
is called Indirect  
Recursion.

1	2	3	4
1	2	3	4

Date			
Page No.			

of  $\Rightarrow$  int array ( int a[8], int index, int size )

```

    {
        if ( index >= size )
            return a[index];
        else
            cout << a[index];
            array ( a, index + 1, size );
    }

```

*Tail*

# Fibonacci.

~~0 1 1 2 3 5 8~~

num = 4

int fibonacci ( int num )

```

    {
        int x = 0;
        int y = 1;
        if ( n == 0 || n == 1 )
            return n;
        else
            return fib(n-1) + fib(n-2);
    }

```

*fib(4)*

*fib(3): fib(2)*

*fib(2): fib(1) fib(0)*

*fib(1): fib(0)*

*Excessive Recursion*

Hashing

Date			
Page No.			

(Optimize Searching)

2	0	1	3	5
---	---	---	---	---

-1	0	2	3	5
----	---	---	---	---

Linear  $\Rightarrow O(n)$ Binary Search  $\Rightarrow O[\log(n)]$ 

(Element % arr-size)

$$h(0 \% 5) = 5$$

no. of collisions  
should be minimumTypes of Hash function(1) division  $\Rightarrow h(k) \Rightarrow (k \% \text{size})$ 

11, 23, 27, 54, 35, 86, 60

$$h(11) = 11 \% 10 = 1$$

Array-size = 10

$$h(23) = 23 \% 10 = 3$$

$$h(27) = 7$$

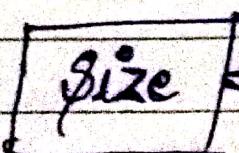
$$h(54) = 4$$

$$h(35) = 5$$

$$h(86) = 6$$

$$h(60) = 0$$

60	11	23	54	35	86	27			
0	1	2	3	4	5	6	7	8	9



Prime

Non-Prime

(2)

Folding

Shift

Boundary

1234

→ Shift 3

 $\frac{12}{+34}$  $\underline{46 \% / 10} = 6$ 

12

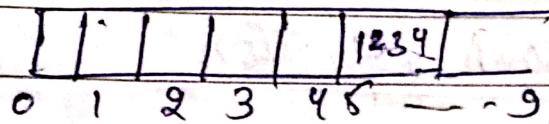
3

4

 $\underline{19 \% / 10} = 9$ 

→ Boundary

3

 $\frac{12}{+43}$  $\underline{55 \% / 10} = 5$ 

(3)

Mid Square  $\vdash (1234)$ Square (Suppose)  $\vdash 1522756$ 
 $1522756$   
 □ ↓ □      key size = 1

middle

⇒ 2% Tsize

⇒ 227% avg-size

 $1522756$   
 □ ↴ □

key size = 3

(4)

Extraction  $\vdash$ 

Extract random digit.

123456

⇒ choose 123 % Tsize

196 % "

146 % "

## # Radix transformation

$$(11)_2 \rightarrow (1011)_2$$

$$\frac{27}{(23)_{10}} = (27)_{\text{8}}$$

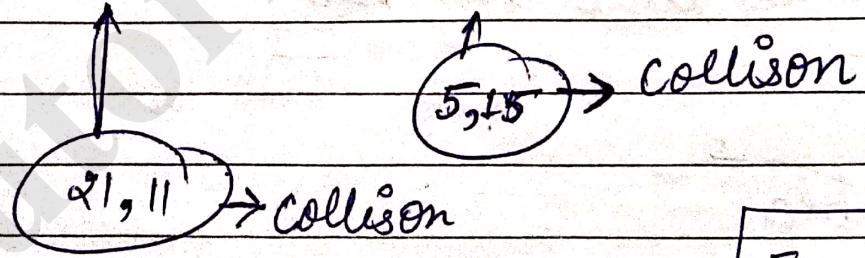
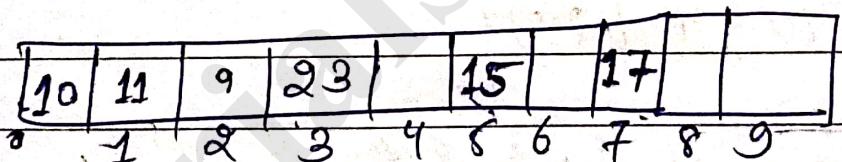
$$(23)_{10} = (17)_{16} \quad \left[ \begin{array}{c} 00010111 \\ \hline 1 \quad 7 \end{array} \right]$$

## # Collision

$$(2) \quad 15, 5, 10, 23, 11, 17, 21$$

hash table size = 10

hash fun<sup>n</sup> - k mod size



## Open Addressing

→ Linear Probing

$\Rightarrow$  Quadratic 11

→ Double

For Overflow  
Rehashing  
allocate a new  
array

Linear Probing

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\* clusters of  $(15, 5)$   $\{25, 35\}$  के साथ आए  
रखे Array में.

10	11	21	23	45	15	5	17	25	35
----	----	----	----	----	----	---	----	----	----

Quadratic

$\Rightarrow \{15, 5, 25, 10, 23, 11, 17, 21, 23, 35\}$

1	1	1	1	25	15	5	1	1	35
0	1	2	3	4	5	6	7	8	9

$$h(k) + 1 = 16$$

$$h(k) - 1 = 24$$

$$h(k) + 4 = 35 + 4 = 39$$

$$h(k) - 4 =$$

$$16 \% . 10 = 6 (5) \quad \text{value}$$

$$24 \% . 10 = 4 (25)$$

[Remove clustering here]

Double

$$h(k) = k \bmod \text{Array size}$$

$\Rightarrow$  next  $\{ (i \cdot h(k) + 1) \% \text{ size} \}$

$\Rightarrow (i \cdot h(k) + 1) \% \text{ Prime No}$

$\Rightarrow$

$$i^2 + 1 \leq 2$$

10, 30, 21, 27, 25, 3.

10 19

10	30	21			25	27	19
0	1	2	3	4	5	6	7

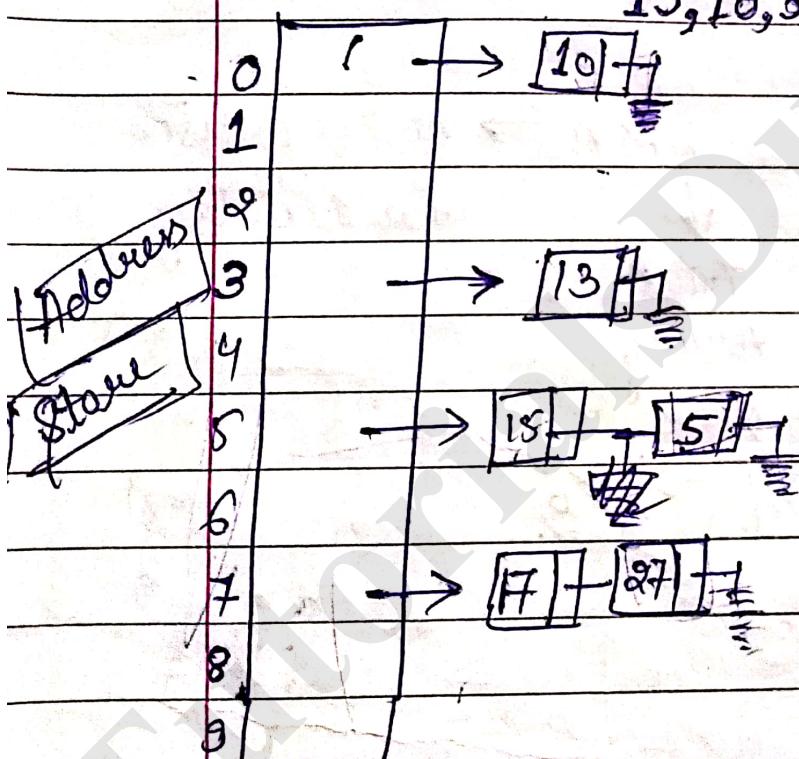
9

if size smaller  $\Rightarrow$  no. of collision more  
(depend upon entry, clustering).

~~②~~ChainingAnother type of  
collision

15, 10, 5, 17, 13, 27

Tsize - 10

 $h(K) \bmod Tsize$ ③ Coalesced chaining↓  
Linear + chaining

0	21			
1	13	6		15, 10, 5, 16, 17, 13, 27, 25
2	31	0		31, 61
3	15	7		
4	10	9	free slots	Array size = 0-5 (6)
5	5	88		
6	25	8	Cellar area	
7	23			$\left\lfloor h(k) \bmod 6 \right\rfloor$
8	17			
9	16			

(4)

Bucket Addressing

0	.	.		mxn → no. of collision
1	13	25		↓ in 1 entry
2				Total
3	15	27		Array
4	10	16	→ Array size	
5	5	17		$\equiv (0-5) = 6$

#

Deletion

Specify any default value (-1, NULL, 10)  
 at the place of value because we can  
 not delete the value from array or  
 shifting is also difficult.

Trees

Date			
Page No.			

HW  
①

	12	13	2	3	23	15	18	15
0	1	2	3	4	5	6	7	8

②

$$h(12) = 12 \bmod 10 = 2$$

$$13 = 3$$

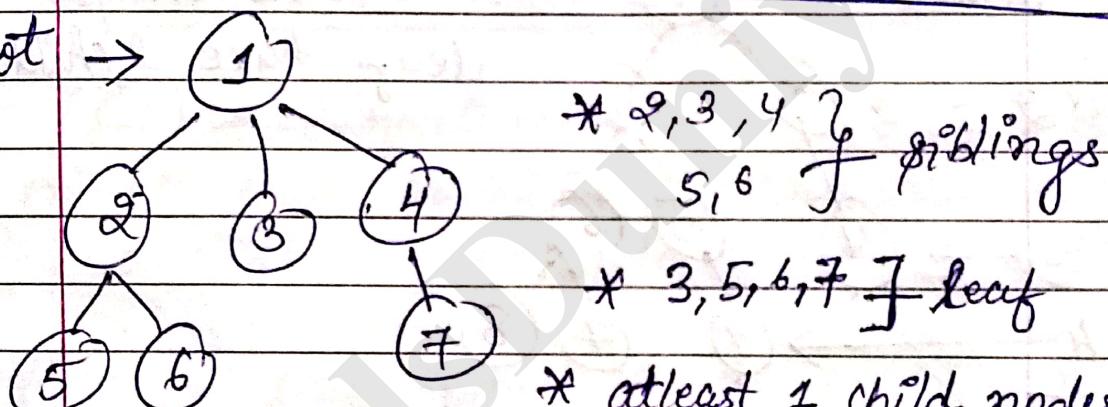
$$2 = 2 \quad 4$$

$$3 = 5$$

③

$$h(k) = k \bmod 8$$

root

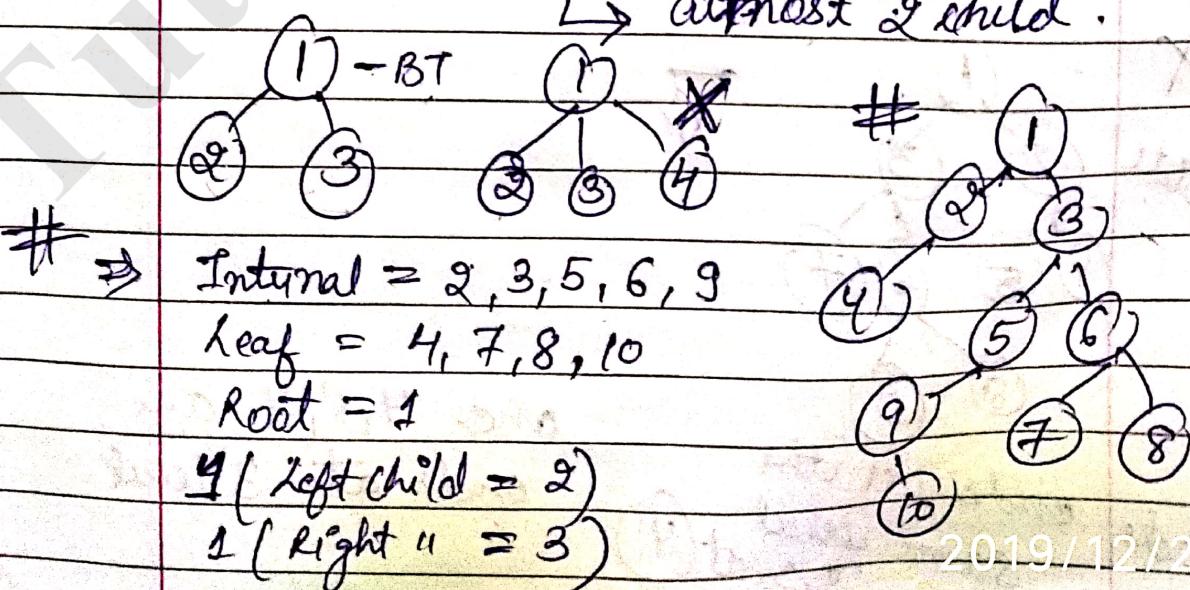


\* atleast 1 child nodes  
except root are called internal

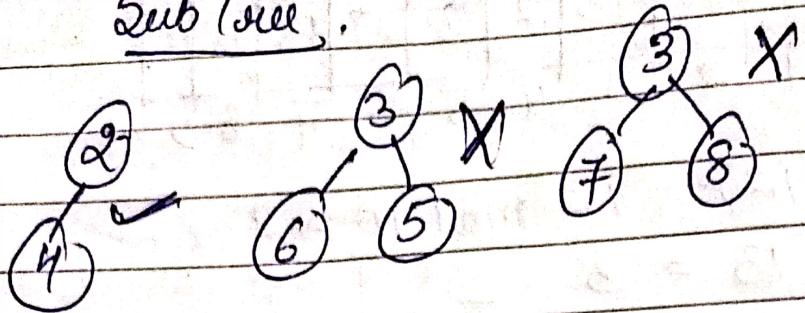
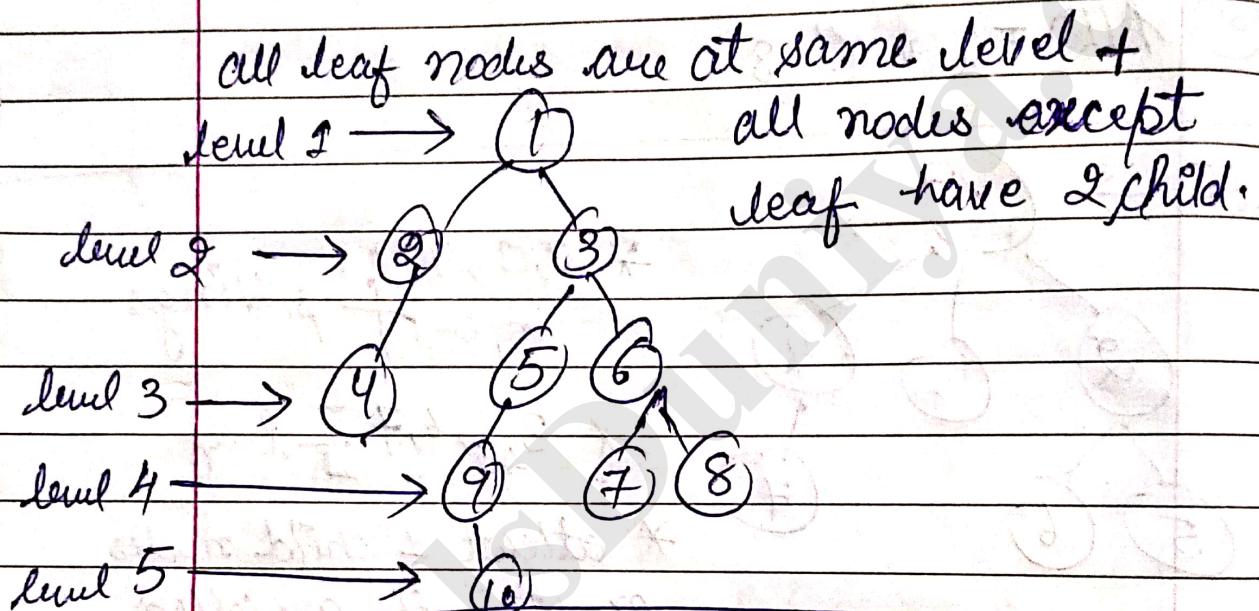
\* External = Leaf      Internal . [2, 4]

Binary Tree

↳ atleast 2 child .

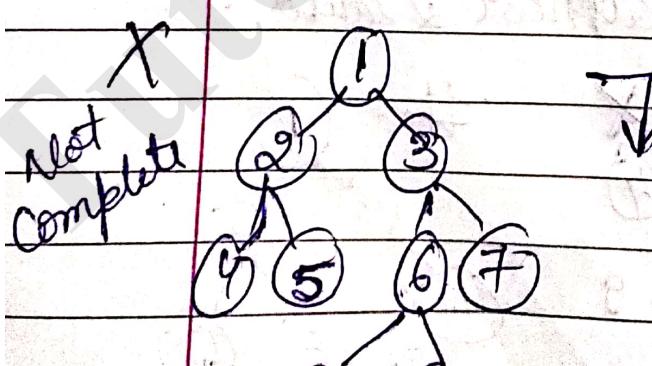


2019/12/20 11:18

Sub Tree.Complete BT

$$\text{Height} = \text{no. of edges} + 1$$

(in longest path)



node ends at the same level 8, 9 at (4) and 4, 5, 7 are ends at 3 level

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if  $i^{th}$  level

$\lceil \text{total nodes} = (2^{i-1}) \rceil \rightarrow \text{at last level for complete tree (BT)} .$

$\lceil \text{Total no. of nodes} = (2^p - 1) \rceil \leftarrow \boxed{\text{level } i}$

if from  $[0^{th}$  level [root]  
 $\lceil \text{total nodes} = 2^i$   
 $\lceil \text{leaf nodes} = (2^{i+1} - 1)$

Almost Complete BT

$\lceil (p-1) \rightarrow \text{Complete BT}$   
 $\text{on } p^{th} \text{ level collect } \text{III} \text{ and then insert value from Left Side.}$

\* every leaf nodes will be at either level  $i$  or  $(i-1)$ . All nodes are left justified.

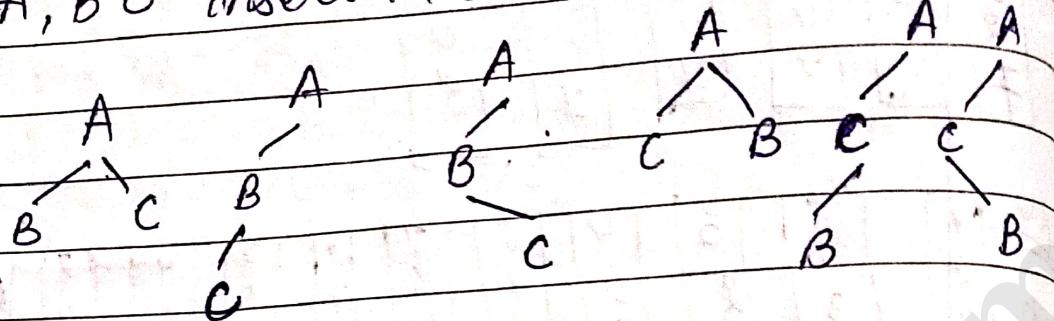
\* Degree of a node [total no. of child exist]  
 $1 \text{ degree} \Rightarrow 11$

24/3/2019

Data Structure

Date \_\_\_\_\_  
Page No. \_\_\_\_\_Ques 1

A, B, C insert in tree

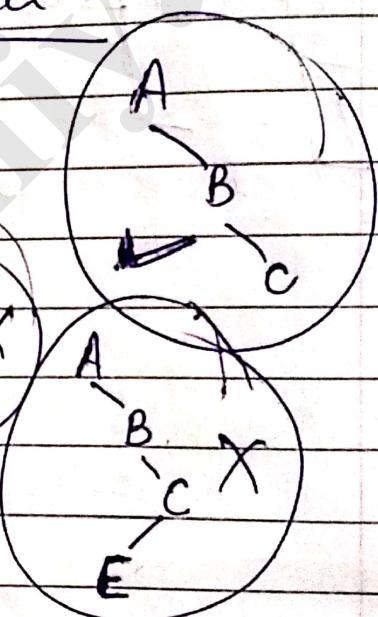
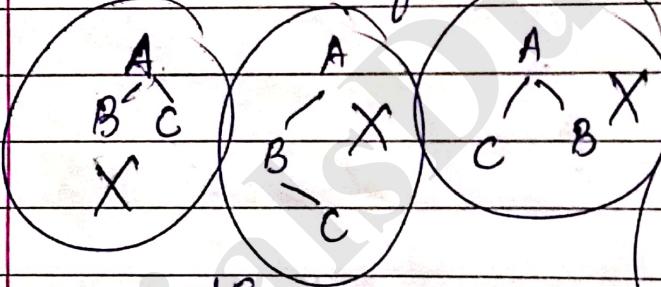
Sol

3 nodes = 6 Combinations

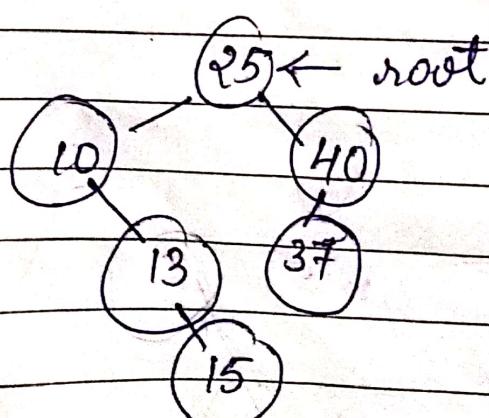
Find  $n=4$ , no. of unique trees (Formula).Binary Search Tree

Parent &lt; Right side

Parent &gt; Left side

Insertion. $O(\log n)$ time  $\nwarrow$   
 $\Omega(n^2)$ 

25, 10, 13, 40, 15, 37

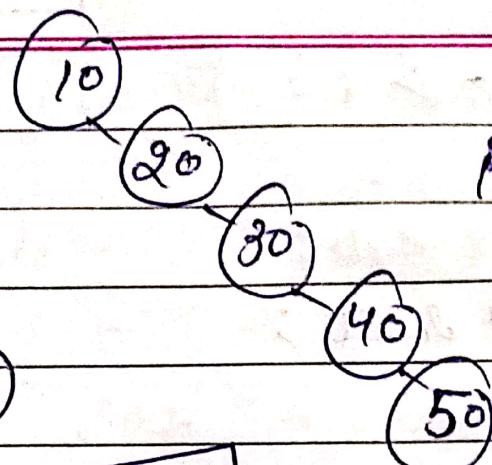
Ans  $\Rightarrow$ final Binary search Tree

~~Ques 2~~ 10, 20, 30, 40, 50

Date			
Page No.			

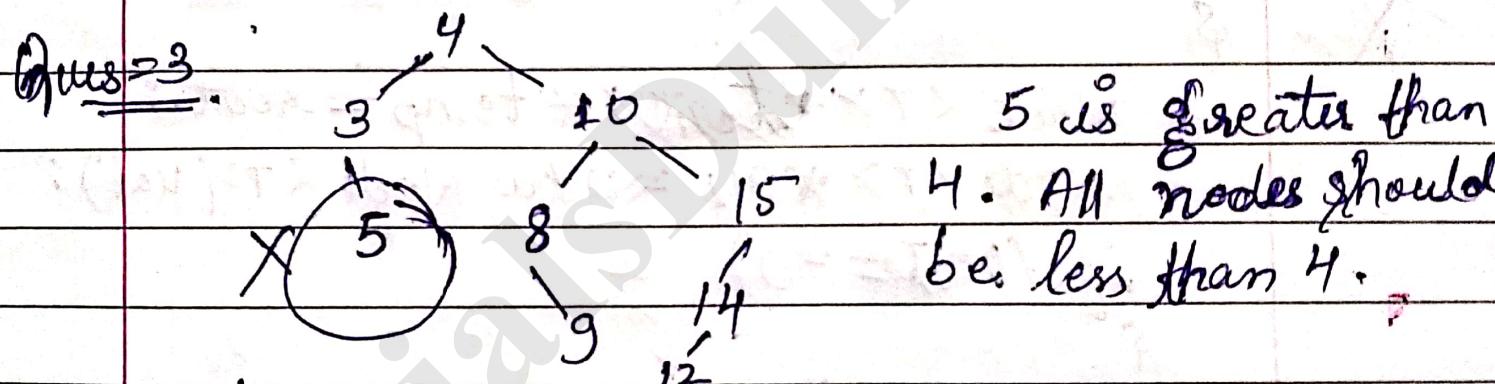
~~searching  
n times~~

order =  $O(n)$



Right skewed Tree

for half Search  
 $(O[\log(n)])$



Not a Binary Search Tree.

template < class T >

→ class Node

\$

~~int data;~~

~~int right;~~

~~Node \* right, \* left;~~

~~Node ()~~

T data;

Node \* right,

\* left;

Node()

\$ ~~left = right = 0; data~~ \$

~~right = new Node();~~

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23, 30, 10, 15, 27

Date			
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void insert ( T val )

{

Node &lt; T &gt; \* n1 = new Node &lt; T &gt; ( val );

if ( root == 0 )

root = n1;

else

Node \* temp = root ; \* prev = 0 ;

while ( temp != 0 )

{

if ( temp -&gt; data &gt; val )

{

prev = temp ;

temp = temp -&gt; left ;

}

}

else {

prev = temp ;

temp = temp -&gt; right ;

}

}

If previous  
use

if ( prev -&gt; data &gt; val )

{

prev -&gt; left = n1 ;

}

else

{ prev -&gt; right = n1 ;

}

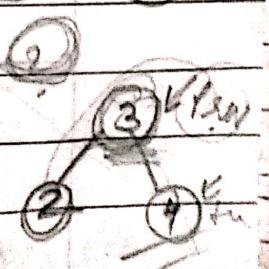
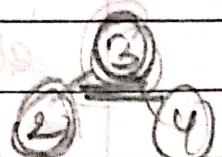
}

}

}

}

}



if ( $\text{temp} \rightarrow \text{left} == 0$ )

{

$\text{left} \rightarrow \text{left} = \text{nil}$ ;

break;

else

{

$\text{temp} = \text{temp} \rightarrow \text{left}$ ;

}

$\Rightarrow$  bool search (T val)

{

~~Node~~

if ( $\text{root} == \text{NULL}$ )

{

return False;

}

else ( $\text{root} \rightarrow \text{data} == \text{val}$ )

{ Node \* temp = root;

while ( $\text{temp} != 0$ )

{ if ( $\text{temp} \rightarrow \text{data} == \text{val}$ );

return true;

else

{ if ( $\text{temp} \rightarrow \text{data} > \text{val}$ )

{

$\text{temp} = \text{temp} \rightarrow \text{left}$ ;

else

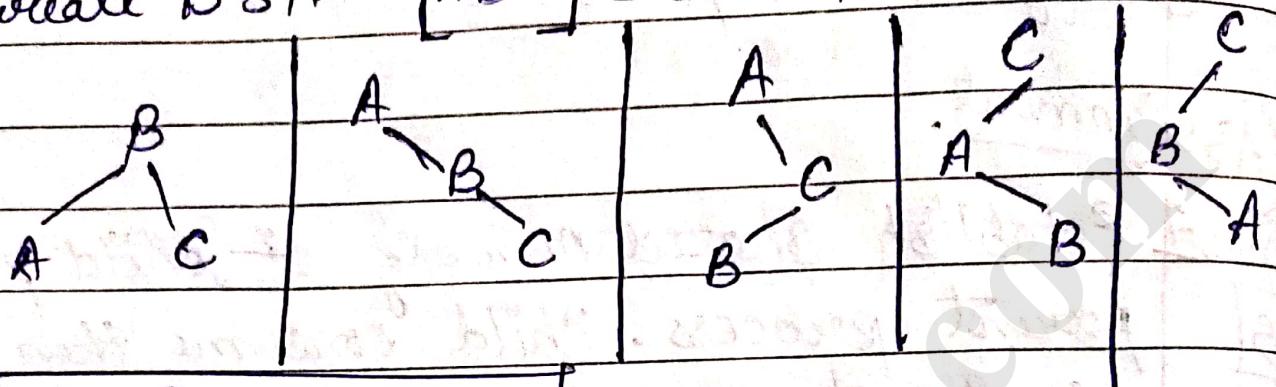
{  $\text{temp} = \text{temp} \rightarrow \text{right}$ ;

return false; (while k bad)

27/09/2019

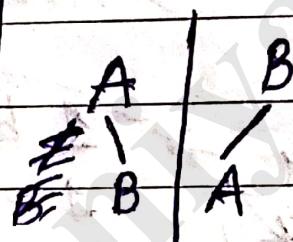
Data Structure

⇒ Create BST. [ABC] otherwise.



$$n = 2$$

$$\# \text{Combination} = 2$$



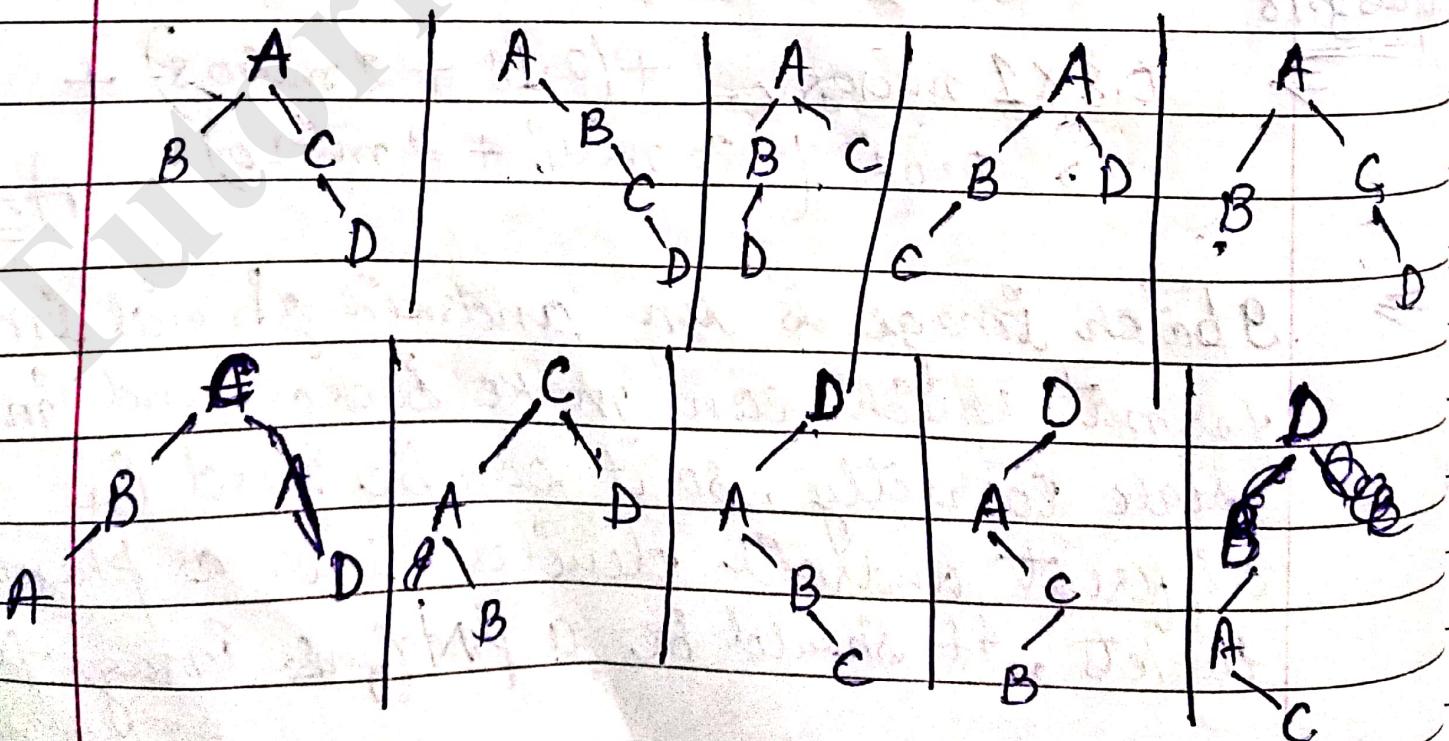
$$n = 3$$

$$\# \text{Combi.} = 5$$

$$n = 4$$

$$\# \text{Combi} = 14$$

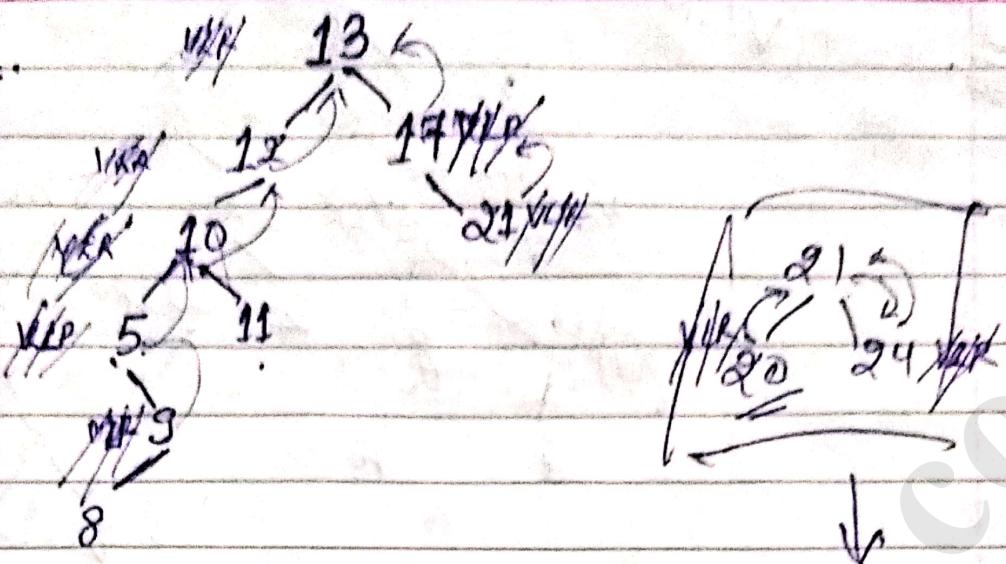
$$2^n - n$$



Tour 3 Binary Search Tree (Accord 8)

13, 12, 10, 17, 11, 5, 9, 8, 21

Date			
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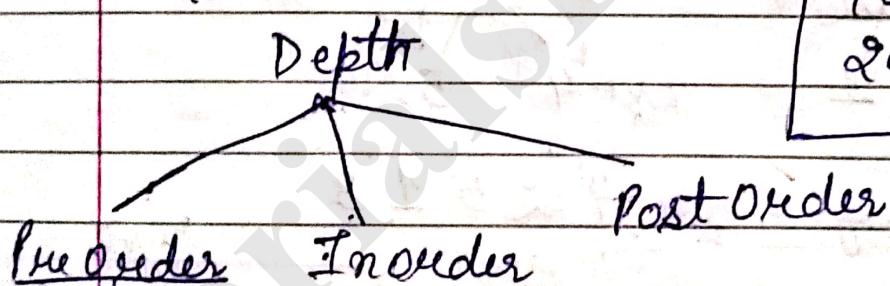
Sol.2 types traversed

⇒ Breadth First Traversal

⇒ Depth " "

Point some level

13	12	17
10	21	5 11
20	24	9 8



$$(ab) \xrightarrow{a+b} a \begin{smallmatrix} + \\ / \end{smallmatrix} b \quad \begin{array}{l} VLR \\ Visit \end{array}$$

13 12 10 5 9 8 11 14  
- 21 20 24

VLR

visit  
node  
traverse  
left subtree  
traverse  
subtree in  
in pre-order

PreorderQues 1LVRNLRakmNLR bNLR cNLR dNLR eNLR fNLR gNLR hNLR iNLR jNLR kNLR lNLR mNLR nNLR oNLR pNLR qNLR rNLR sNLR tNLR uNLR vNLR wNLR xNLR yNLR z

Ans. a b d e f i j g h k l z w y m n p q r

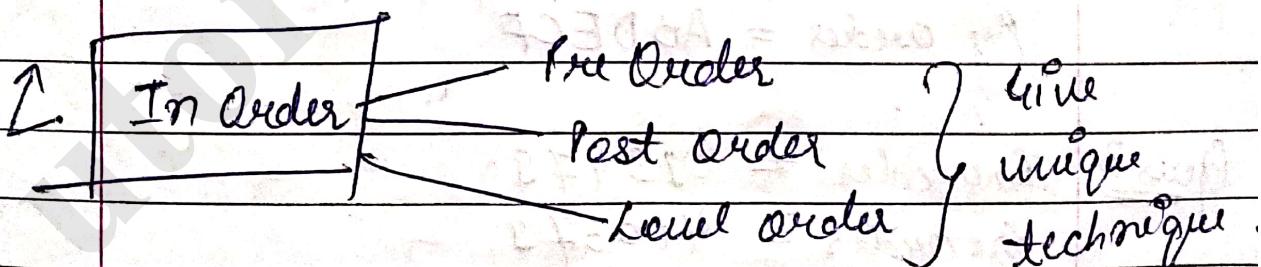
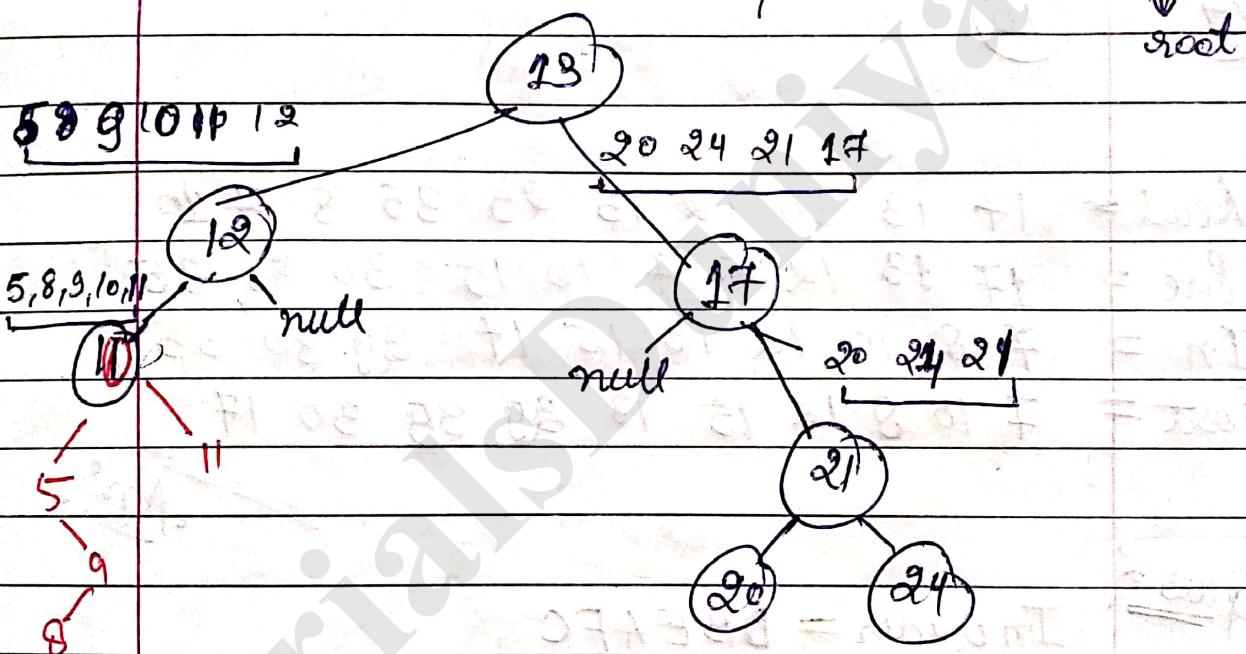
InorderLVR(a+b)I II IIIKVR 123LVR 45 KVRAns.bleft4 2 5 1 3rootrightd f i e g haz l w y km q p r nLVRAns.bad f i e g hz l w y km q p r nLVRAns.b

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$\Rightarrow$  diff of height b/w L & R is 2  
 q. 2. p.n.m.R(a)  
 root  $\xrightarrow{\text{Ans.}}$

Inorder in BST apply then should be in ascending order.

Post  $\leftarrow$  8 9 5 11 10 12 20 24 21 17 13



Post = 8 9 5 11 10 12 20 24 21 17 13

In = 5 8 9 10 11 12 13 17 20 21 24

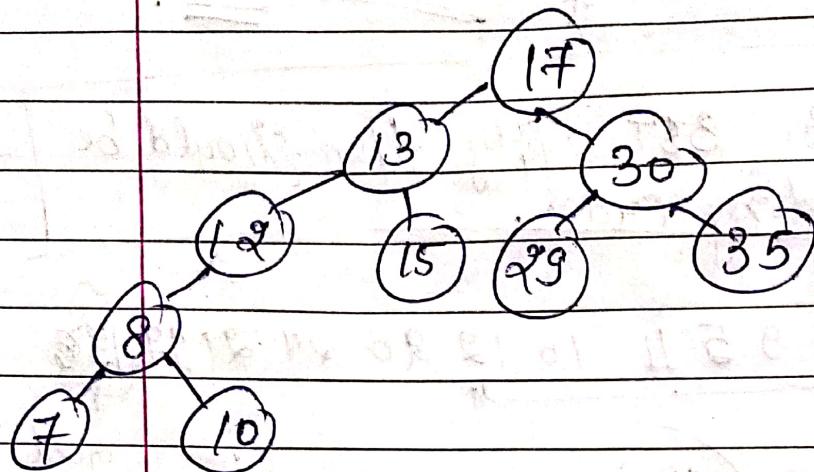
Left

Right

Ques 1

BST

17 30 35 29 13 15 12 8 7 10



Level = 17 13 30 12 15 29 35 8 7 10

Pre = 17 13 12 8 7 10 15 30 29 35

In = 7 8 10 12 13 15 17 29 30 35

Post = 7 10 8 12 15 13 29 35 30 17

Ans.Ques 2

In Order = DBE AFC

Pre Order = ABDEC F

Ques 3

In Order = 013479

Pre Order = 410379

Ques 4

In Order = g b h e d i a f j m c k

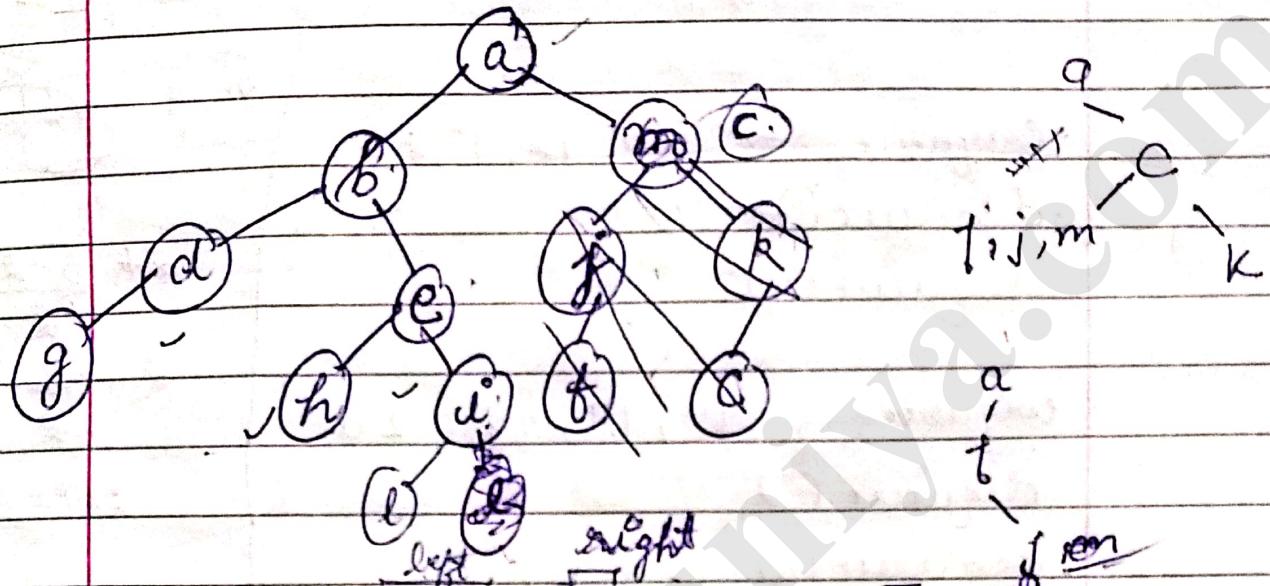
Post = g a h d i e b m j f k c a

30/3/2019

Q5.

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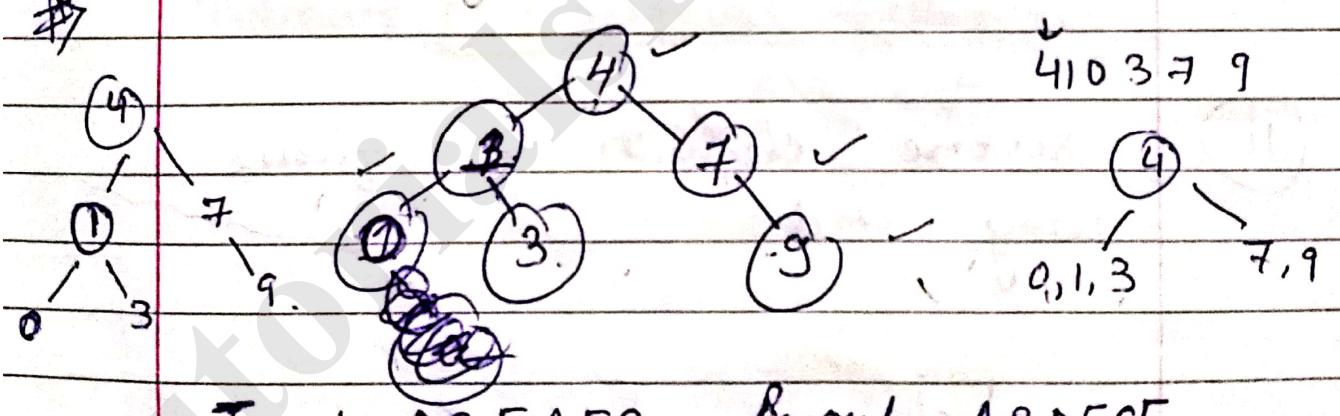
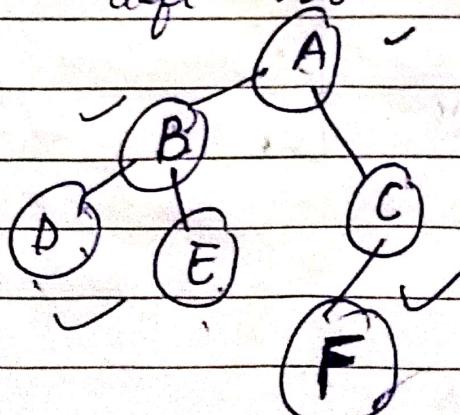
left right

Ans 4 Inorder = g d b h e i a f j m c k FLRPost = g d h d i e b m i f k c a FLRAns 3. Inorder 0 1 3 4 7 9.

F L R m

Preorder 4 1 0 3 7 9

F VLR

Ans 2Inorder D B E A F C  
left rightPreorder A B D E C F

In	LVR
Pre	VLR
Post	LRV

Date \_\_\_\_\_  
Page No. \_\_\_\_\_

Pre-Order Recursive Code

~~PRACTICE~~

int RecurPre ( int v )

{

cout << " enter value of V " ;

cin >> v ;

if ( v == NULL )

{

cout << " empty structure " ;

return 1 ;

}

else

{ return RecurPre (

)



Void preOrder ( Node \* &temp )

{

if ( temp == 0 )

{

return ;

}

else

{

cout << temp -> data ;

preOrder ( temp -> left ) ;

preOrder ( temp -> right ) ;

}

}

VLR

~~Void Inorder (Node <temp)~~

Date			
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if (temp == 0)

{

return ;

}

else

{

cout &lt;&lt; Inorder ( temp -&gt; left );

cout &lt;&lt; temp -&gt; data ;

Inorder ( temp -&gt; right );

{ }  
3

Void Postorder ( Node &lt;temp )

{

if ( temp == 0 )

return ;

else

{

Inorder ( temp -&gt; left );

Inorder ( temp -&gt; right );

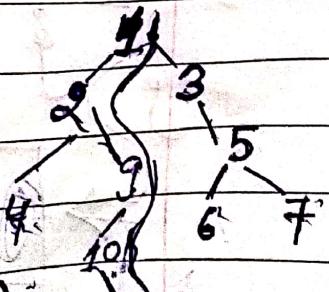
cout &lt;&lt; temp -&gt; data ;

3

3

① To find the height of a tree.

Longest path :-



int height ( Node &lt;temp )

{

if ( temp == 0 )

```
    return 0;
```

```
else
```

```
{
```

```
    int l = height (temp->left);
```

```
    int r = height (temp->right);
```

```
    if (l > r)
```

```
        return l+1;
```

```
}
```

{ if (l > r) l++ } else r++

```
}
```

② To find the no. of leaf nodes.

```
int leafNode (Node *temp)
```

```
{ if (temp == 0) return 0;
```

```
else if (temp->left == 0 && temp->right == 0)
```

```
    return 1;
```

```
else
```

```
{
```

```
    int l = leafNode (temp->left);
```

```
    int r = leafNode (temp->right);
```

```
    return (l+r);
```

```
    }
```

```
    }
```

```
return leaf (temp->left) +  
leaf (temp->right);
```

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③ print leafnode (Node  $\leftarrow$  temp)

$\oint \text{Left } (\text{temp} = \infty)$

return 0;

g

i else if ( temp > left == 0 && temp > right == 0)

5

return 0;

3

else { return(1 + leaf(temp>left) + leaf(temp>right))}

→ Mirror Image

4) ~~function~~ void mirror( Node L > \* temp )

S

If  $\int \text{temp} = 0$ )

return May

else

else  
if (temp > left == 0 && temp > right == 0)

return 1;

3

else

mirror (temp  $\rightarrow$  left);

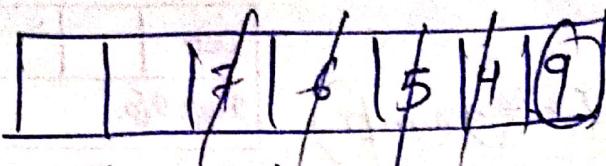
mirror (temp → right);

Node <?> \*temp1;

$\text{temp}1 = \text{temp} \rightarrow \text{left}'$

$\text{temp} \rightarrow \text{left} = \text{temp} \rightarrow \text{right};$

$$\text{temp}_{\text{right}} = \text{temp}_{\text{left}}$$

Ques 1.

Date		
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~~Traverse it~~~~dequeue~~

Node Address part ↴

→ Queue < Node < T > \* > q, 1 ;

Used BFS()

{

if (root == 0)

return;

else

{

Queue &lt; Node &lt; T &gt; \* &gt; q, 1 ;

Node &lt; T &gt; \* temp = root ;

q, 1 . enqueue ( temp );

{ temp = q, 1 . dequeue ();

cout &lt;&lt; temp -&gt; data ;

if ( temp -&gt; left != 0 )

q, 1 . enqueue ( temp -&gt; left );

if ( temp -&gt; right != 0 )

q, 1 . enqueue ( temp -&gt; right );

→ while ( ! q, 1 . isEmpty () )

1/10/2019

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Q6 WAP to check whether BT is Complete or not.

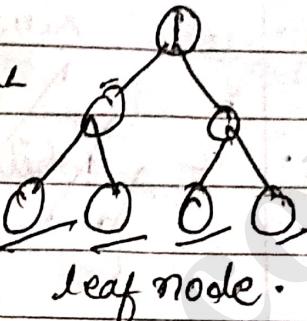
Check  $\Rightarrow$  level for nodes  
And leaf nodes has  $2^h$  child.

If a single leaf node is NULL  
then its not a BT complete.

Ans 1.

Sum of Nodes.

$$\begin{aligned} \text{height} &= h \\ \text{nodes} &= 2^h - 1 \end{aligned}$$



$\Rightarrow$  int SumNodes(Node < T > \*temp)

{

if ( $temp == 0$ )

{

return 0;

}

else if ( $temp \rightarrow left == 0 \& temp \rightarrow right == 0$ )

{

return  $temp \rightarrow data$ ;

}

else

{

SumNode

int l = data ( $temp \rightarrow left$ );int r = <sup>SumNode</sup> data ( $temp \rightarrow right$ );return  $[l+r] + \text{Sum}(temp \rightarrow data)$ ;

}

Ans 2

{

$\Rightarrow$  Iterative method [Tree Traversal]

void IfPre()

[VLR]

{

if ( $root == 0$ )

{

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14/10/2018

Depth First Search

Inorder  $\rightarrow$  Stack  
Preorder  $\rightarrow$  Stack

Date			
Page No.			

else

{

Stack & Node  $\leftarrow T \rightarrow * \rightarrow g_1;$ Node  $\leftarrow T \rightarrow * \rightarrow \text{temp} = \text{root};$ 

S1.push(temp);

while ( $\text{temp} \rightarrow \text{left} != \text{NULL}$ )

{

S1.push( $\text{temp} \rightarrow \text{left}$ );cout  $\ll \text{temp} \rightarrow \text{left} \rightarrow \text{data};$ cout  $\ll \text{temp} \rightarrow \text{data};$ if ( $\text{temp} \rightarrow \text{right} != \text{NULL}$ )

S1.push

while ( $(S1.isEmpy())$ )while ( $\text{temp} != 0$ )

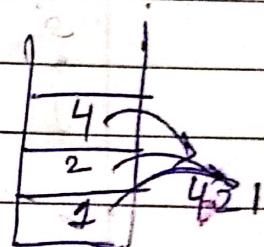
{

S1.push(temp);

temp = temp  $\rightarrow$  left;

g1

g2



temp = S1.pop(); temp = S1.pop();

cout  $\ll \text{temp} \rightarrow \text{data};$ temp = temp  $\rightarrow$  right;

2

3

4526731

Ques 1

void postorder()

{

Stack S;

temp1 = root;

S.push(root);

while ( $(S.isEmpy())$ ) {

while (!S. isEmpty())

    while (temp1->l != 0)

        f

            S.push (temp1);

            temp1 = temp1->left;

    g

    while [(temp1 != 0) && (temp1->r == 0)]  
        temp1->r == temp2]

    g     cout << temp1->data;

        temp2 = temp1;

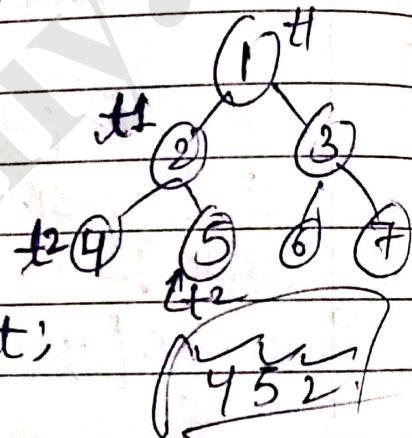
        temp1 = S.pop();

    g

        S.push (temp1);

        temp1 = temp1->right;

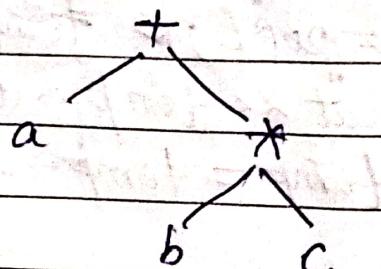
g



### Expression Tree

(1)

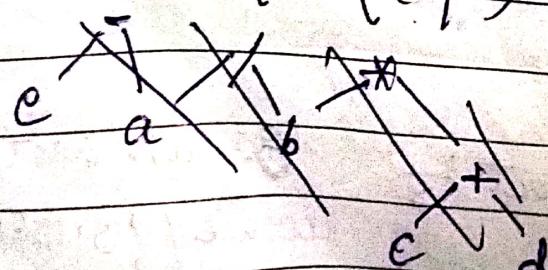
$(a + (b * c))$



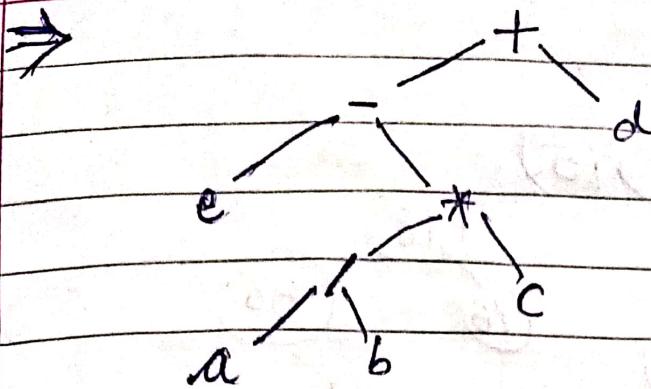
(2)

$e - a / (b * c) + d$

$(e - ((a / b) * c)) + d$



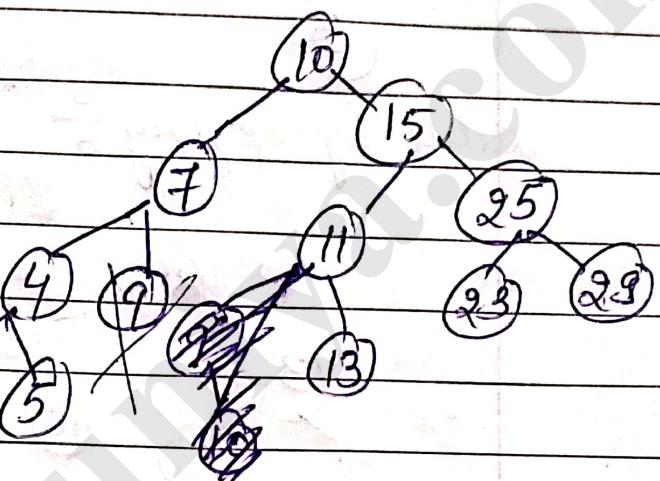
2019/12/20



## Deletion

(i)  $q = \text{leaf node}$

Search then delete



(ii) node has 1 child

(iii) A node has 2 children

Deletion  
by Merging

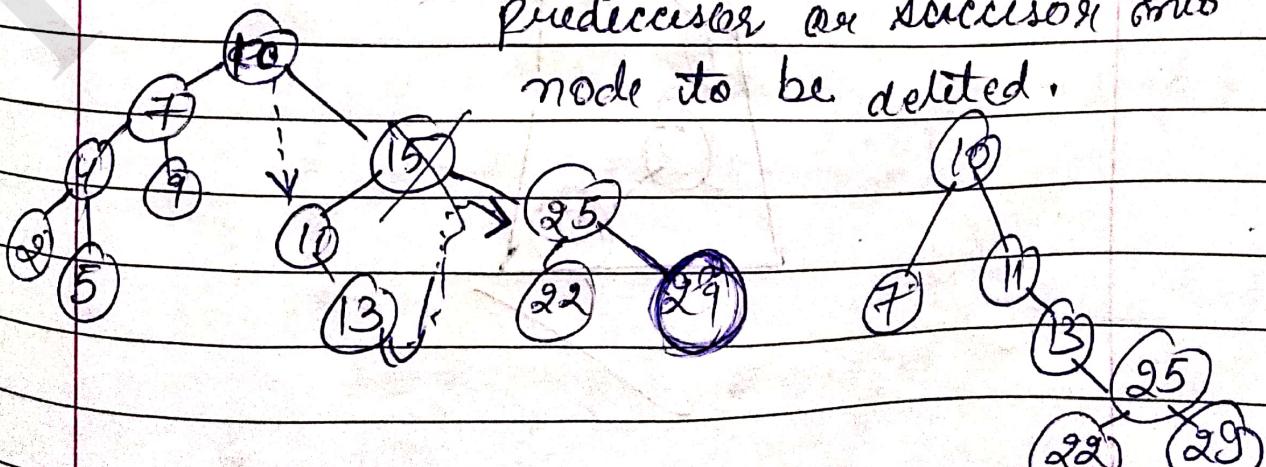
Deletion  
by Copying

[ Immediate  
Predecessor or  
Successor ]

(1) Immediate Predecessor      (1) Find  $\rightarrow P = \text{left subtree rightmost}$   
 $S = \text{right } \& \text{ leftmost}$

$P \rightarrow r(\text{node} \rightarrow rs)$

(2) Copy data of immediate  
predecessor or successor onto  
node to be deleted.

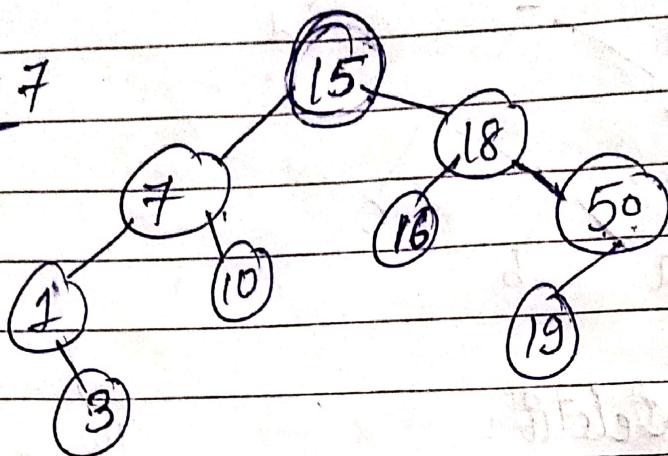


Merging = height increase  
 Copying = same (decrease)

Date		
Page No.		

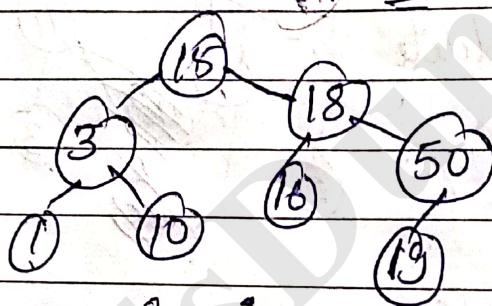
Ques 1

delete 7



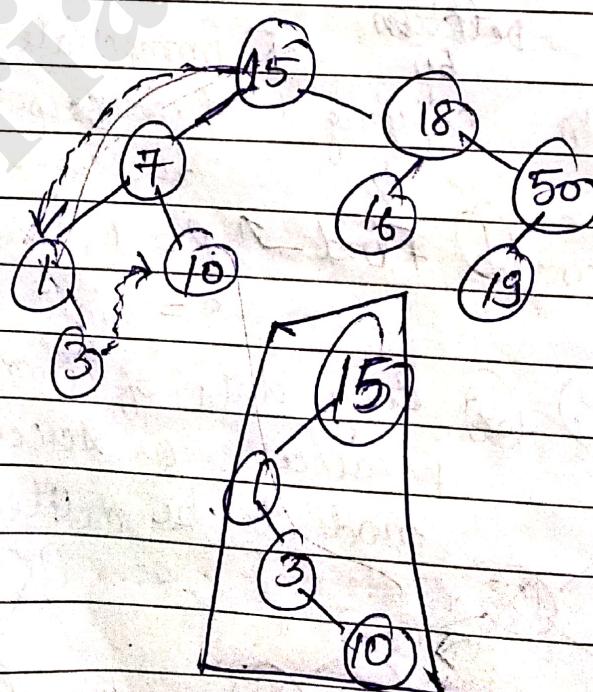
delete by copying

IP = 3



del by merging

IP = 3



15/10/2019

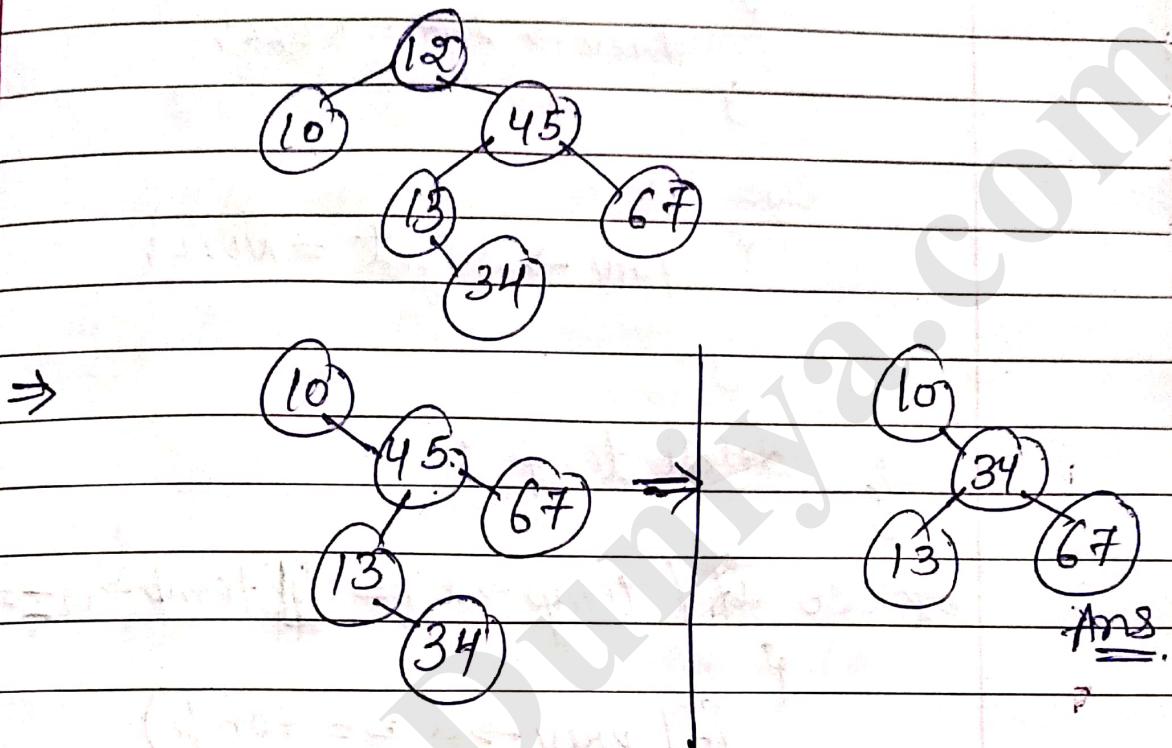
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Ques 2

12, 45, 13, 67, 10, 34

D 12 by merging

D 45 by copying of tree after 12 D2



void find( T el)

{  
Base cases : =

# temp = root , pcur = 0 ;

while (temp != 0)

{ if ( temp-&gt;data == el )

break;

else

if ( temp-&gt;data &gt; el ) → pcur = temp ;

{ temp = temp → left ; }

y

else

pcur = temp ;

{ temp = temp → right ; }

x

~~Page No.~~  
~~if ( temp → l == 0 & temp → r == 0 )~~

{ if ( prev → left == temp )

{ prev → left = NULL;

else

{ prev → right = NULL;

}

} delete temp ;

if else if ( temp → l != 0 & temp → r != 0 )

{ if ( prev → l == temp )

{

prev → l == temp → l;

}

} else ( prev → r == temp → l );

else if ( temp → l == 0 & temp → r != 0 )

{ if ( prev → r == temp )

{

prev → r == temp → r;

else

{ prev → l == temp → r;

}

}

Date			
Page No.			

~~delByMerge ( del , pprev )~~

S

temp = del  $\rightarrow$  left ;

while ( temp  $\rightarrow$  right != 0 )

S

temp = temp  $\rightarrow$  right ;

g

temp  $\rightarrow$  right = del  $\rightarrow$  right ;

If ( pprev  $\rightarrow$  left == del )

S

pprev  $\rightarrow$  left = del  $\rightarrow$  left ;

g

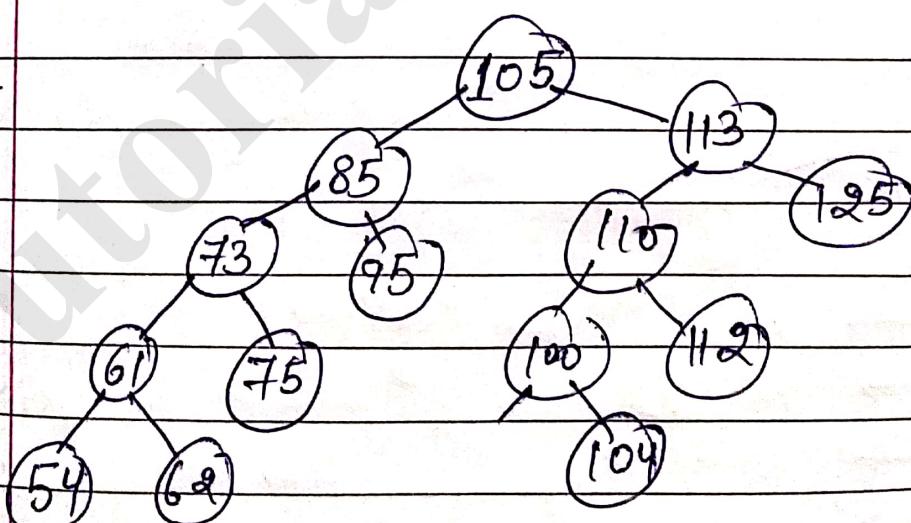
else

pprev  $\rightarrow$  right = del  $\rightarrow$  left ;

g delete del ;

g

b1



delete 105

delete 73

delete 110

on resultant .

(

21 | 10 | 20 | 21 | 9 | 3

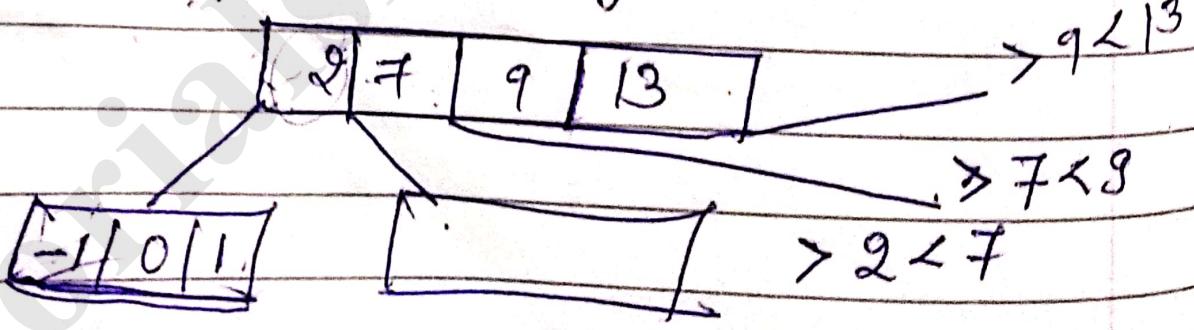
m-ary tree

- m children (allow)
- m children / Pointers
- (m-1) Keys / values
- Keys in ascending order

2-ary

-1	0	3
----	---	---

Not allow X



Date			
Page No.			

## m-way /ary tree

- (1) Each node has  $m$  children &  $(m-1)$  keys
- (2) Keys are in ascending order
- (3) Keys in first ' $i$ ' children are  $<$  than  $i^{th}$  key
- (4) Keys in last ' $m-i$ ' children are  $>$  than  $i^{th}$  key.

access time = seek time + rotational delay  
+ transfer time.

$\Rightarrow$  B Tree (height balanced) —  $\left\{ \begin{array}{l} \text{height of left \& right are same} \\ \text{height of left \& right are same} \end{array} \right\}$

$\downarrow$  BST + m-way tree

Properties :-

$\Rightarrow$  B tree of order  $m$  contains following property

- (1) Root has atleast 2 children unless it is a leaf node.
- (2) Each internal node holds  $(k-1)$  keys &  $k$  pointers to subtree  $\lceil \frac{m}{2} \rceil \leq k \leq m$ .

No leaf  
No root  
internal  
node

- (3) Each leaf node holds  $(k-1)$  keys.  
 $\lceil \frac{m}{2} \rceil \leq k \leq (m)$ ,

- (4) All leaf nodes are at same level.

~~Order 5~~Order 5

(Not a

5/15

30 37 49 61

100 120 125 130

140 43 47

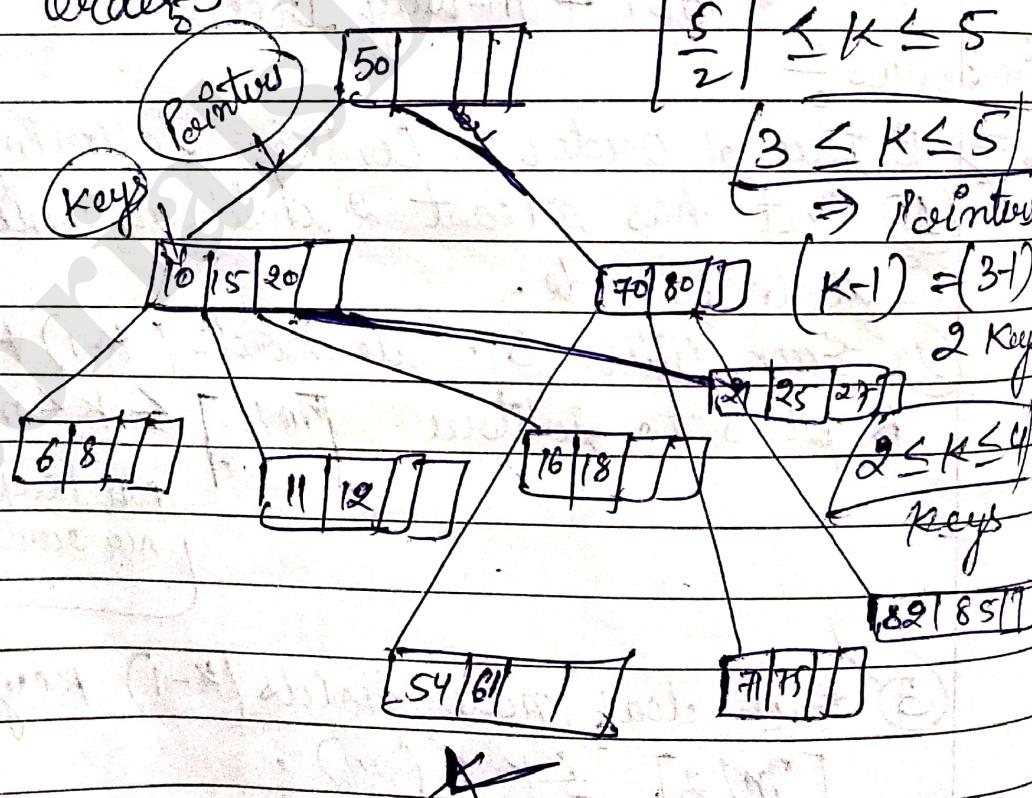
45 60 33

&gt; 30 &lt; 37

~~Q2~~

Order 5

Key



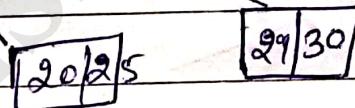
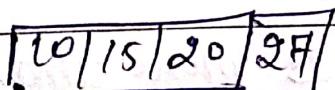
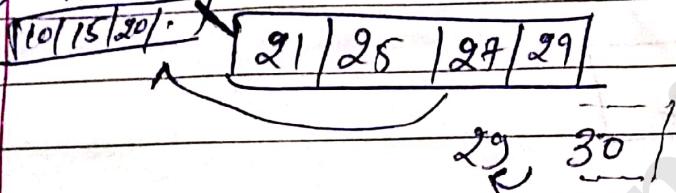
Inserion (D) at leaf nodes) B Way tree

Date	
Page No.	

- ⇒ Node is not full
- ⇒ Node is full.

- Step 1 \* Insert node and split it into two nodes.
- Step 2 \* Choose middle node & make it parent of splitted nodes.
- Step 3 \* Separated node is inserted into node's parent and then repeat Step 2.

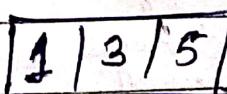
→ Insert 30



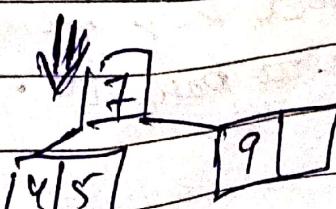
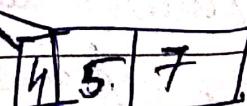
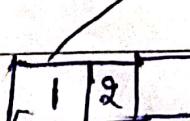
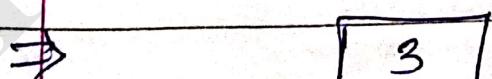
Ques 2. Order 4. → Pointer 3 keys.

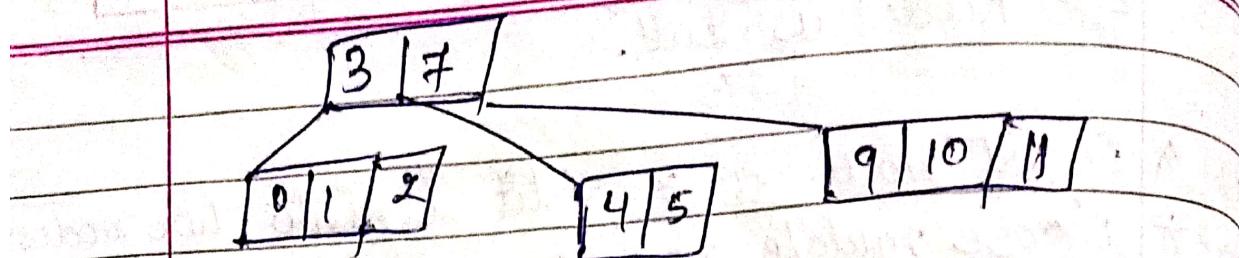
3, 1, 0, 5, 2, 7, 4, 9, 10, 0, 11

$g \leq 4$  pointer



$1 \leq < 3$  Keys



Ques 3

Order 3

- (1) 5, 3, 10, 9, 1, 14, 2, 7, 12, 19  
 (2) 1, 2, 3, 4, 5, 6, 7, 8, 9

### Deletion

deletion from leaf.

(1) No underflow, leaf is more than half full.

(2) Underflow

If there is a merge keys from left or right sibling leaf, parent sibling

more than  $\lceil \frac{m}{2} \rceil - 1$  keys

then redistribute keys from leaf & siblings

by moving separator

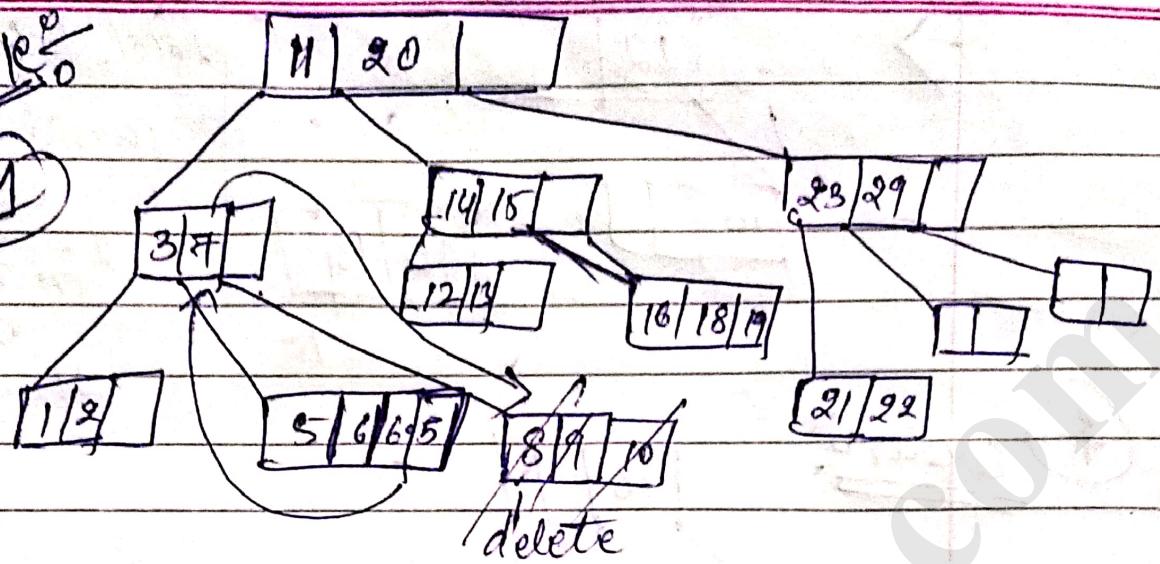
key from parent to leaf & moving left most

rightmost key from

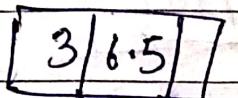
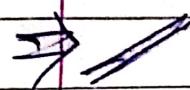
sibling to parent.

example 10<sup>2</sup>

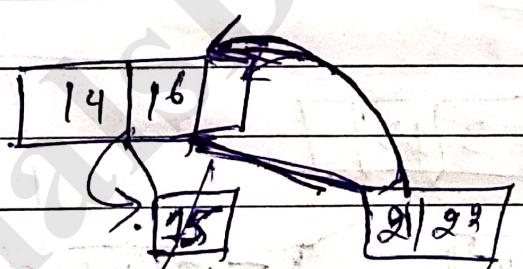
(1)



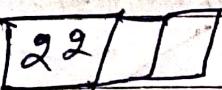
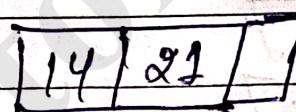
delete



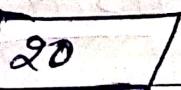
(2)



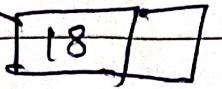
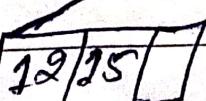
delete 15 then

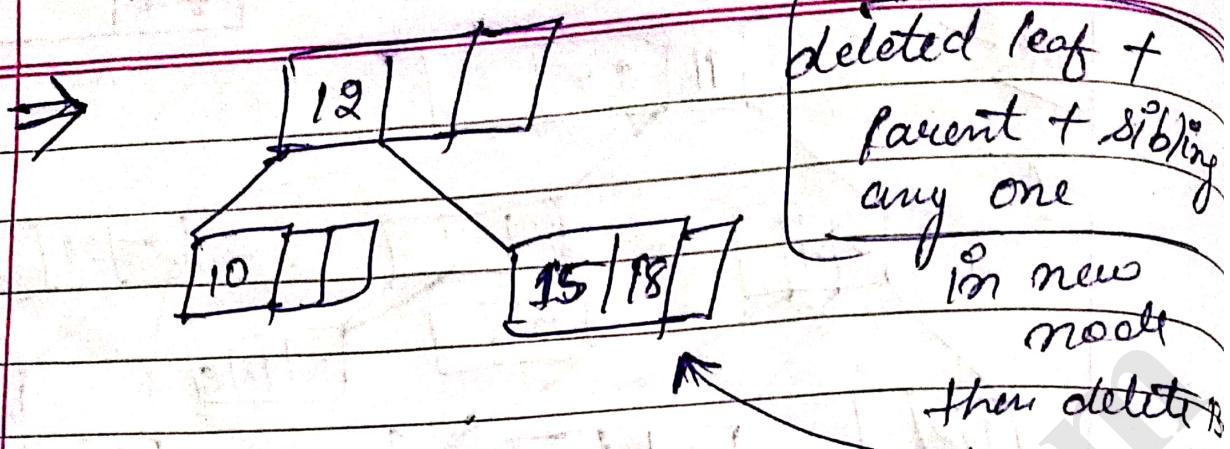


(3)

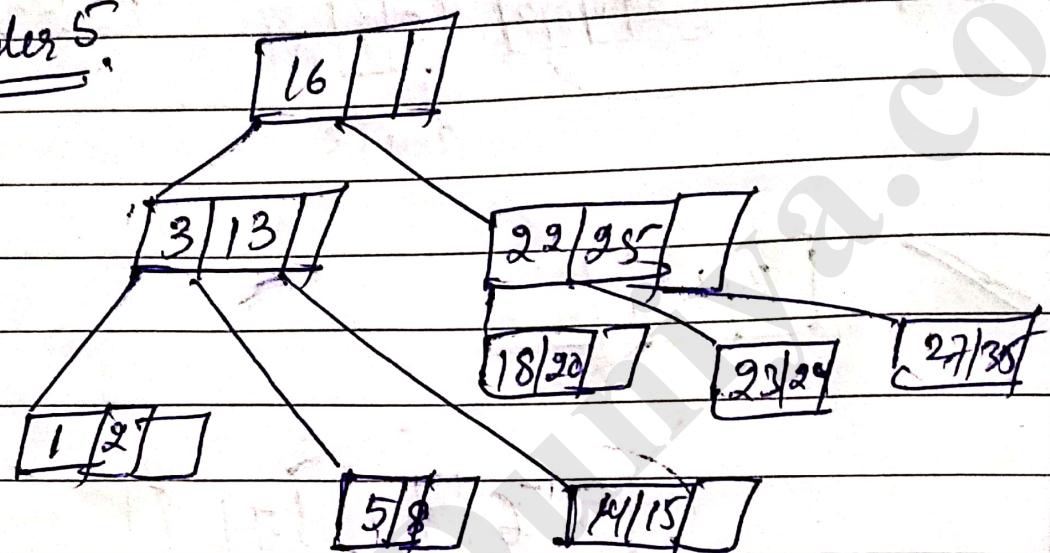


delete 13 .

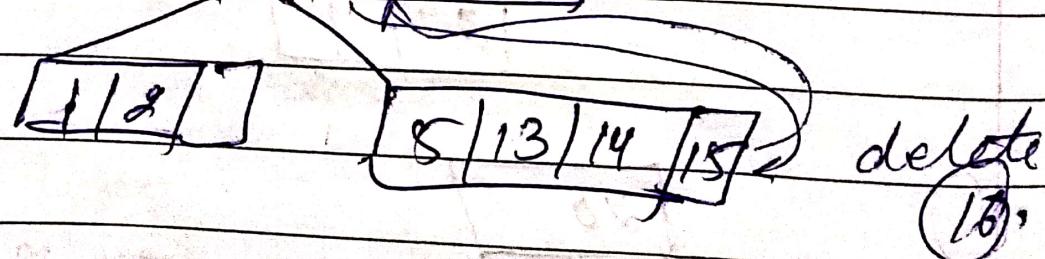
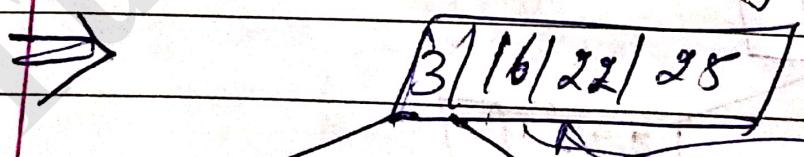
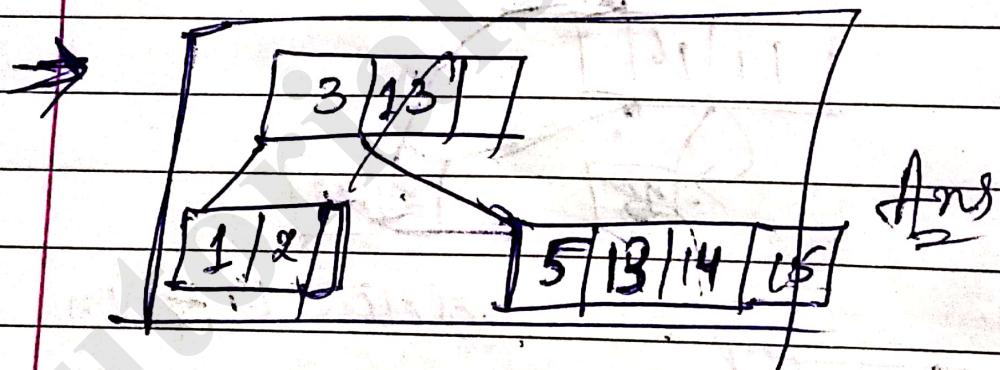




④ Order 5.



~~→ delete 8~~



Ques=1	(b) Arrays	Linked list
Ques=2	An Array is the data structure that contains a collection of similar type data elements.	It is considered as non-primitive data structure. Contains a collection of unordered linked elements (nodes).
②	It is of fixed size.	It is dynamic and flexible and can expand & contract in size.
③	Memory assigned during compile time.	it is allocated during execution or runtime.
④	Insertion & deletion consume a lot of time.	The performance of these operations are fast, efficient.
⑤	Binary & linear search	Linear Search

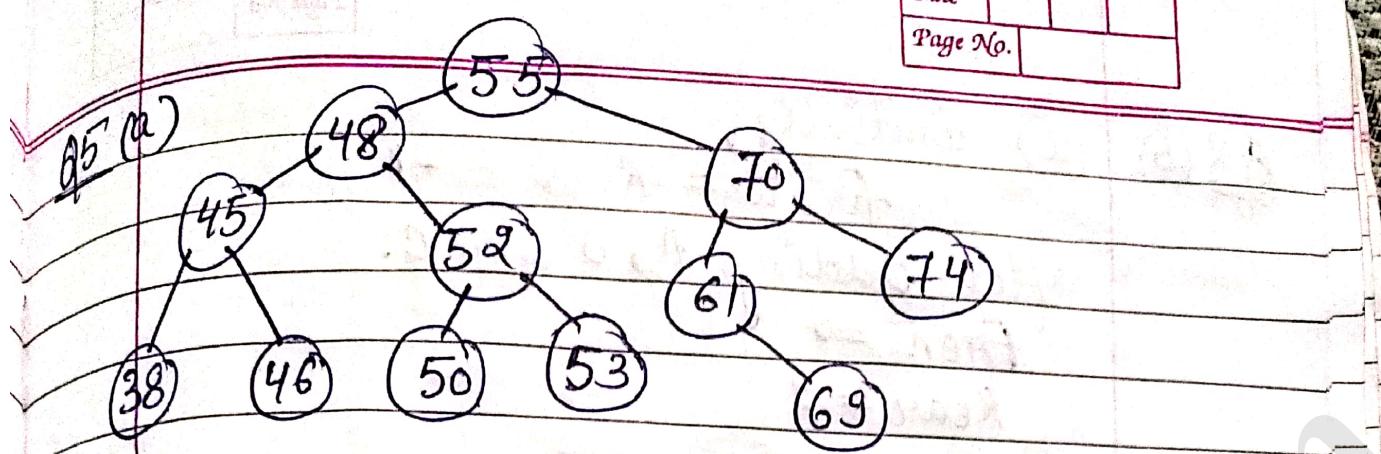
Q2 (a) To find and return length of L.L.

```

int LengthL.L (Node L.T > *temp)
{
    if (temp == head)
        count = 0;
    else
        count = lengthL.L (temp);
    return count + 1;
}

```

~~while (temp != null)~~



(ii) Breadth First  $\rightarrow$  55, 48, 70, 45, 52, 61, 74,  
38, 46, 50, 53, 69

Preorder  $\rightarrow$  55, 48, 45, 38, 46, 52, 50, 53,  
70, 61, 69, 74.

Inorder  $\rightarrow$  38, 45, 46, 48, 50, 52, 53, 55,  
61, 69, 70, 74

Postorder  $\rightarrow$  38, 46, 45, 50, 53, 52, 48, 69,  
61, 74, 70, 55

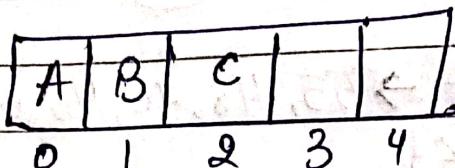
Q7 (a)	MoveToFront	Transpose
Given $\rightarrow$	EFGH -	EFGH
G	(EFGH) GEFH	EGFH -
E	GEFH	EGFH
H	GEHF	EGHF
E	EGHF	EGHF
F	EGFH	EGFH
H	EGHF	EGHF
G	GEHF	GEHF
E	EGHF	EGHP

Q2(b) (i) Initially,  
 $\text{front} = \text{Rear} = -1$

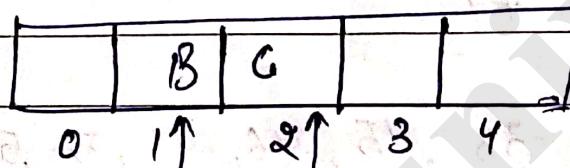
after adding A, B and C.

$\text{Front} = 0$

$\text{Rear} = 2$

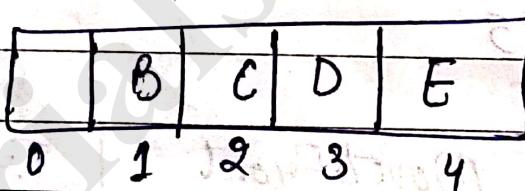


(ii)  $\text{Front} = 1$ ,  $\text{Rear} = 2$

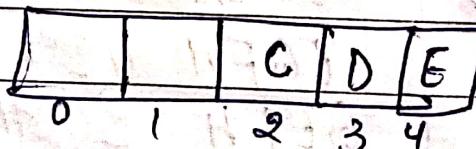


Front      Rear

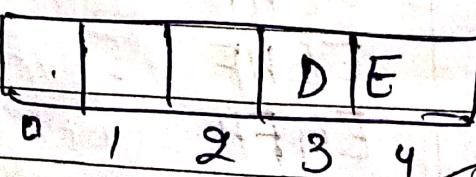
(iii)  $\text{front} = 1$ ,  $\text{Rear} = 4$



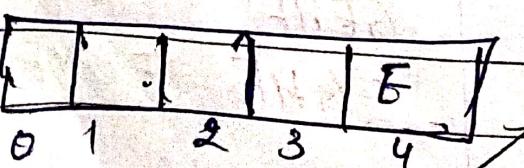
(iv) delete(1)



delete(2)



delete(3)



$\text{front} = 4$

$\text{Rear} = 4$

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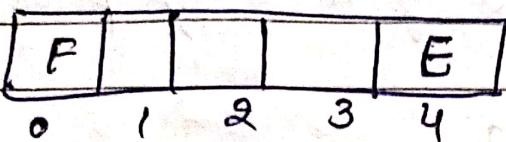
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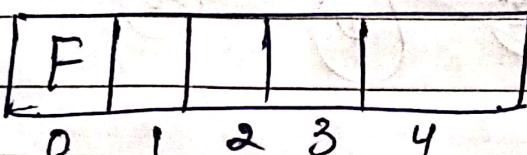
**Telegram** 

(iv) Insert F

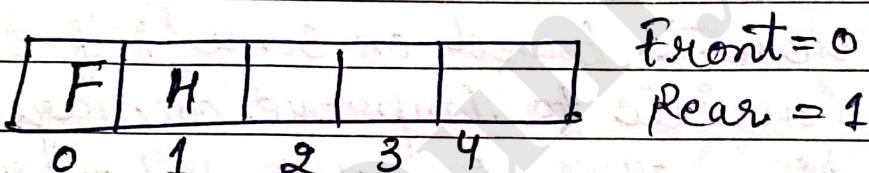
front = 4 rear = 0



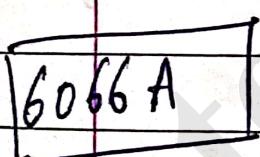
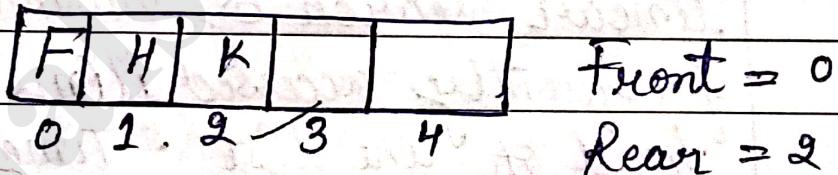
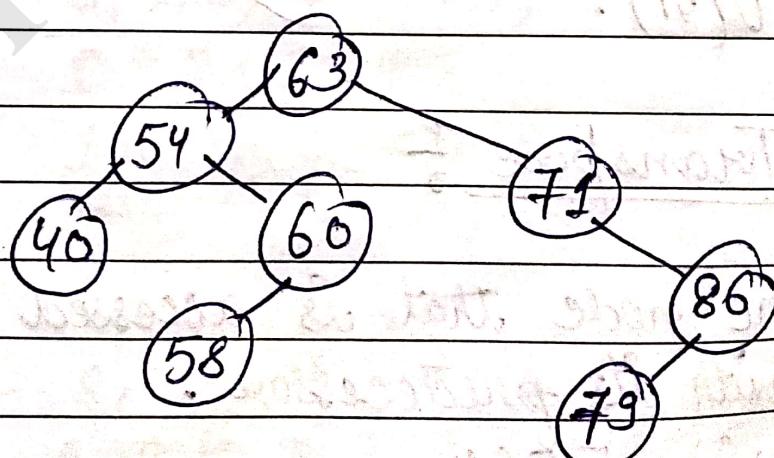
(v) delete E, Front = Rear = 0



(vi) insert H



Insert K

Q1 (g)Preorder  $\rightarrow$  63, 54, 40, 60, 58, 71, 86, 79Postorder  $\rightarrow$  40, 58, 60, 54, 79, 86, 71, 63

(f)  $\text{int func(int } m, \text{int } n)$

$\text{if } (m < n)$   
return 0;

else  
return

$1 + \text{func}(m-n, n);$

g

$\text{func}(6, 3) = 2$

$1 + \text{func}(6-3, 3)$

$1 + \text{func}(3, 3);$

$1+1=2$

$1 + \text{func}(3-3, 3)$

$1+0=1$

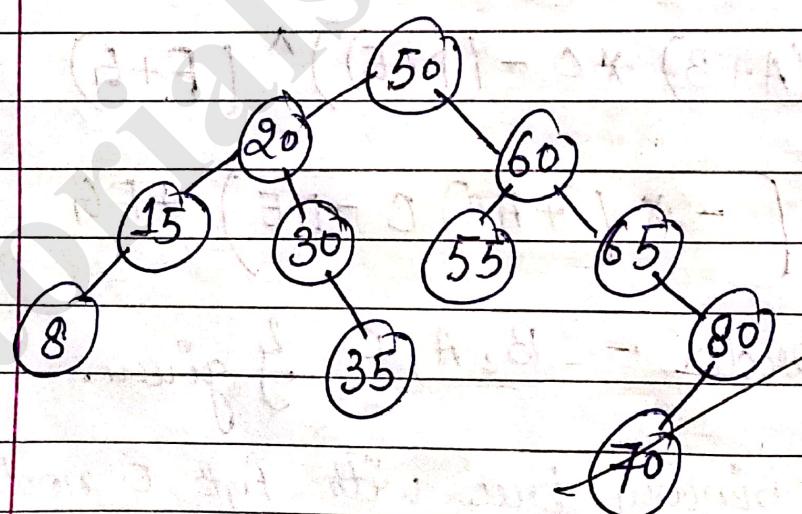
$1 + \text{func}(0, 3)$

$1+0=1$

$\Rightarrow \text{find func}(6, 3)$

∴ value of  $\text{func}(6, 3)$  is 2.

(h) 50 20 30 60 65 55 80 15 8 35 70



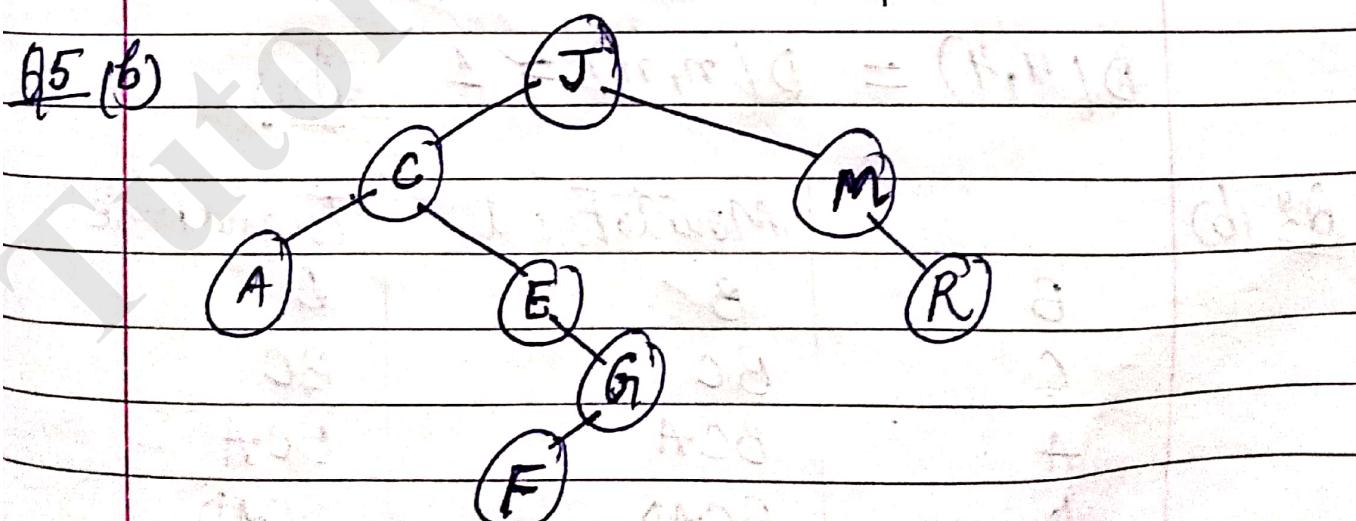
Q2(b)  $BAC + * CAB - + * [B = 5, A = 6 \& C = 4]$

$C$	$A$	$B$	$AFC = 10$	$10 \times 5 = 50$	$B$	$A$	$C$	$50$
-----	-----	-----	------------	--------------------	-----	-----	-----	------

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1			
c	$\frac{1+4}{50} = 5$		
50	50	$5 \times 50 = 250$	
-	+	*	<u>250 Ans</u>

<u>Q4 (a)</u>	moveToFront	Transpose
A	A	A
B	AB	AB
C	ABC	ABC
D	ABCD	ABCD
B	BACD	BACD
B	BACD	BACD
C	CBAD	BCAD
A	ACBD	BACD
D	DACB	BADC
D	DACB.	BDAC



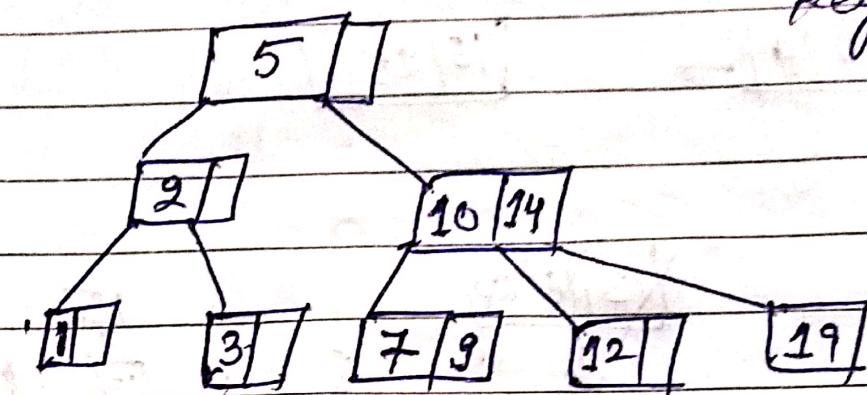
Preorder - JCAEGFMR

Inorder - ACEFGJMR

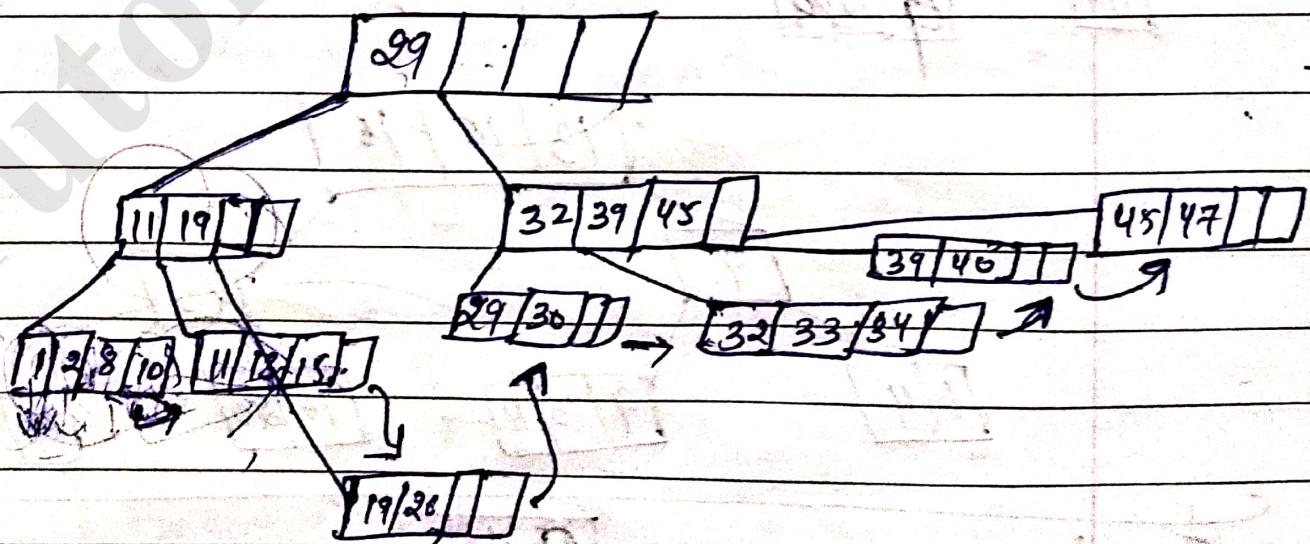
4/11/2019

DS

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Q1. 5, 3, 10, 9, 1, 14, 2, 7, 12, 19order = 3  
keys = 2B<sup>+</sup> Tree

- \* Internal nodes stores keys and pointer to child
- \* Leaf nodes stores keys, ptr. to data file and ptr to next leaf.
- \* All references to data pointers, will be stored at leaf



Searching $\beta^+$  Tree

delete 7, 9

B Tree

~~boolean Linear\_Search (int a[], int el, int sz)~~ int n;

{

n

for (int i = 0; i < n; i++)

{

if (el == a[i])

{ return true;

{

Search &  
Insert

else if (n != sz)

a[n + 1] = el;

{

else return false;

{

{

Time

Best =  $O(1)$   
 Worst =  $O(n)$

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Average =  $O(\frac{n+1}{2}) \approx O(n)$ .

Ans:

$\Rightarrow$  void binary-search (int a[], int el)

Time  
 $O(\log n)$

int sz)

int l=0, r=sz-1;

int m =  $\frac{l+r}{2}$ ;

$m = \frac{sz}{2}$

while ( $l \leq r$ )

{

  if ( $a[m] == el$ )

{

    return true;

}

  else if ( $a[m] > el$ )

{

    r = m-1;

}

  else

{

    l = m+1;

}

}

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# SORTING.

- ① Bubble
- ② Selection
- ③ merge
- ④ Quick

$$a \rightarrow [5 | 9 | 4 | 2 | 3 | 1 ]$$

0 1 2 3 4 5



void bubblesort ( int arr[], int len )

{

for ( int i = 0; i < n - 1; i++ )

{

n - i

for ( int j = 0; j < n - i; j++ )

{

if ( arr[j] > arr[j + 1] )

{

int temp = arr[j];

arr[j] = arr[j + 1];

arr[j + 1] = temp;

j

j

If sorted array

Best Case = n

Worst =  $\Theta(n^2)$

bubble-sort ( → )

{ for ( → i → ) → flag = false;

for ( j = → )

# In-place

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if ( $a[i][j] > a[i][j+1]$ )

{

flag = true;

— ;

{ — ;

{ — .

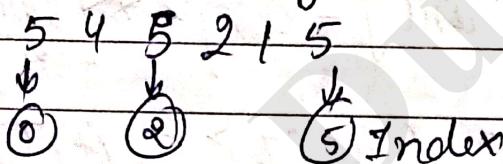
if (flag == false)

{

break;

cout &lt;&lt; "sorted array" ;

{

} # Constant memory space  $\rightarrow$  Inplace bubble sort?

$\Rightarrow$  1 2 4 5 5 5  $\rightarrow$  This is called  
stable.

of bubble sort

# If we use (=) in loop [if ( $a[i][j] > a[i][j+1]$ )] then  
it is called unstable.

SELECTION-SORT

[Inplace +

void Selection-Sort (int a[], int len)

{ for (i=0 ; i&lt;n ; i++)

{

min = index = i ;

for (j=i+1 ; j&lt;n-1 ; j++)

{

if ( $a[j] < a[min]$ )  
 min =  $j$ ;      Running Time  $O(n^2)$ .

$\left\{ \begin{array}{l} \text{if } (i^{\circ}) = \min\_index \\ \text{int temp} = a[\min\_index]; \\ a[\min\_index] = a[i^{\circ}]; \\ a[i^{\circ}] = \underline{\text{temp}}; \end{array} \right.$

Quick-SORT → PARTITION EXCHANGE SORT

Q1. 70 95 34 86 110 54 69

## Bubble, Selection, Quicksort

7/11/2019

25.

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~~Quick sort.~~

~~partition~~  
~~exchange part~~  
~~Also name~~

int partition ( int a[], int low, int high )

```
{
    int l = low, r = high, pivot = a[low];
    while ( l < r )
        {
            while ( a[l] < = pivot )
                l++;
            while ( a[r] > pivot )
                r--;
            if ( l < r )
                {
                    temp = a[l];
                    a[l] = a[r];
                    a[r] = temp;
                }
        }
}
```

UNSTABLE

```
a[low] = a[r];
a[r] = pivot;
return r;
```

~~Merge Sort~~

void MS ( int a[], int l, int h )

```
{
    if ( l < h )
        {
            int mid = (l+h)/2;
            MS ( a, l, mid );
            MS ( a, mid+1, h );
            Merge ( a, l, h );
        }
}
```

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void merge (int a[], int low, int high)

{

    int i = low, j = mid + 1;

    int \*b = new int [h - l + 1];

    int k = 0, while ( i ≤ mid && j ≤ high )

{

        if ( a[i] < a[j] )

{

            b[k++] = a[i++];

}

        else

            b[k++] = a[j++];

}

    while ( i <= mid )

{

        b[k++] = a[i++];

}

    for ( int i = 0; i < h - l; i++ )

{

        a[low + i] = b[i];

}

}

~~insertion sort~~

insertion\_sort ( int a[], int n )

{

    for ( i = 1; i < n - 1; i++ )

,

        int key = a[i];

for( $j = i - 1$ ;  $j \geq 0$  &&  $a[j] > key$ ;  $j--$ ).  
g.  
 $a[j+1] = a[j];$   
g  
 $a[j+1] = key;$

8 | 11 | 2019

~~8 11 20~~  
Let in Nables, [m]  
2

Ques 1 order - [6].

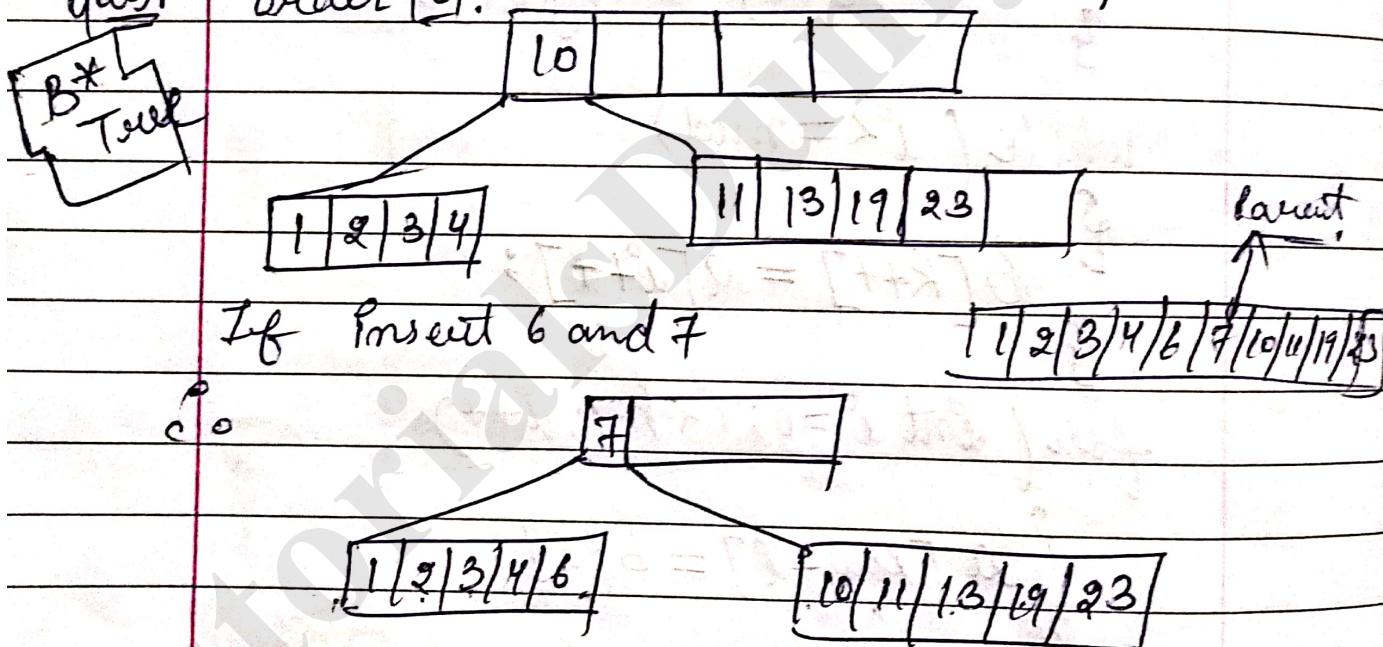
B Tree - order = 4

$1 \leq \text{values} \leq 3$

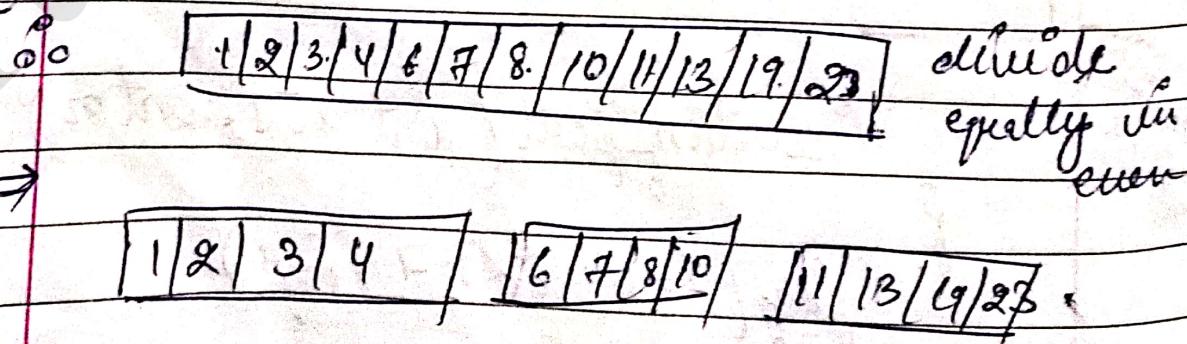
$$2 \leq \text{keys} \leq 4$$

Pauter

painter



If insert 8



Ques 2 Order 5

Page No.
----------

9 14 3 16 4 1 17 6 5 28

⇒ 3 | 9 | 14 | 16 |

⇒ (3 | 4) | 9 | 14 | 16 |

⇒ 9  
|  
[3 | 4] [14 | 16]

⇒ 9  
|  
[1 | 3 | 4] [14 | 16] ⇒ 9  
|  
[1 | 3 | 4] [14 | 16 | 17]

⇒ 9  
|  
[1 | 3 | 4 | 6] [14 | 16 | 17]

⇒ 9  
|  
[1 | 3 | 4 | 5 | 6] [14 | 16 | 17]

⇒ 4 | 9  
|  
[1 | 3] [5 | 6] [14 | 16 | 17]

⇒ 4 | 9  
|  
[1 | 3] [5 | 6] [14 | 16 | 17 | 28]

Ans

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