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## Compiler design

Lexical Analysis [ Regular Expression  
finite automata ]  
parsing [ CFN DPPA ]  
Semantic Analysis [ context sensitive grammar ]  
Intermediate code generation [ Attribute grammar ]  
Code optimization  
Code generation and Runtime Environment

## Grammars

DEF :- Set of rule used to describe string of language.

$$G = (V, T, P, S)$$

$V \Rightarrow$  Set of variable (non terminals)

$T \Rightarrow$  Set of terminal

$P \Rightarrow$  No. of production

$S \Rightarrow$  Starting symbol

- # For every language there exists a grammar and every grammar represent rules of some language.

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$$\alpha = \{a^n b^n \mid n \geq 1\}$$

{ ab, aabb, aaabb --- }  
Recursion

then grammar for this.

$$S \rightarrow a b \mid \underbrace{a S b}_{\text{recursion representation}}$$

$$\alpha = \{a^n b^n c^m \mid n, m \geq 1\}$$

{ abc, , aabbcc, , aaabbccc, }

$$\begin{array}{l} S \rightarrow \overline{AB} \\ A \rightarrow \overline{ab} \mid \overline{aAb} \\ B \rightarrow \overline{c} \mid \overline{cB} \end{array} \} \text{ production}$$

$$V = \{S, A, B\} \quad p.$$

$$T = \{a, b, c\}$$

$$\alpha = \{a^n b^m c^m d^n \mid m, n \geq 1\}$$

$$\begin{array}{l} S \rightarrow a \ A \ \overline{d} \midasd \\ A \rightarrow bc \mid bAC \quad \{b^m c^m\} \end{array}$$

$$\alpha = \{ a^m b^n \mid m > n \}$$

$\{aab, aaabb, aaaaabbb\}$

$$S \rightarrow aSb \mid aAb$$

$$A \rightarrow aA \mid a \text{ Minm String}$$

$$\alpha = \{ a^i b^j \mid i \neq j \}$$

$$S \rightarrow aSb \mid aAb \mid aBb$$

$$A \rightarrow aA \mid a$$

$$B \rightarrow bB \mid b$$

Find the grammar, that all string of a and b where each string is odd length palindrom.

$$\alpha = \{ a, b, aba, bab, aaa \dots bbb \dots \}$$

$$S \rightarrow aSa \mid bSb \mid aib$$

Find the grammar that generate odd length palindrom string of English language and how many production will be there.

$$S \rightarrow aSb \mid bSb \mid cSc \mid \dots zSz \mid aib \mid d \mid \dots$$

# Find the grammar that represent all palindromes of English language.

$$S \rightarrow aSg | bSb | cSc | \dots zSz | \underbrace{a | b | c}_{2^6} | \underbrace{aa | bb | cc}_{2^6}$$

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# Identify language generated by this grammar.

$$S \rightarrow aS | bS | a | b$$

Derivation: process of generating strings from the given grammar by replacing left hand side grammar by its corresponding right side part.

$$\Sigma = \{a, b, aa, bb, ab, ba\}$$

$$= (a+b)^+ \Sigma$$

#  $a^n b^n c^n \geq 1 \rightarrow$  it can't be generated

$$S \rightarrow aSBC \quad \text{by type 2 grammar.}$$

$$S \rightarrow abc$$

$$cB \rightarrow Bc$$

$$bb \rightarrow bb$$

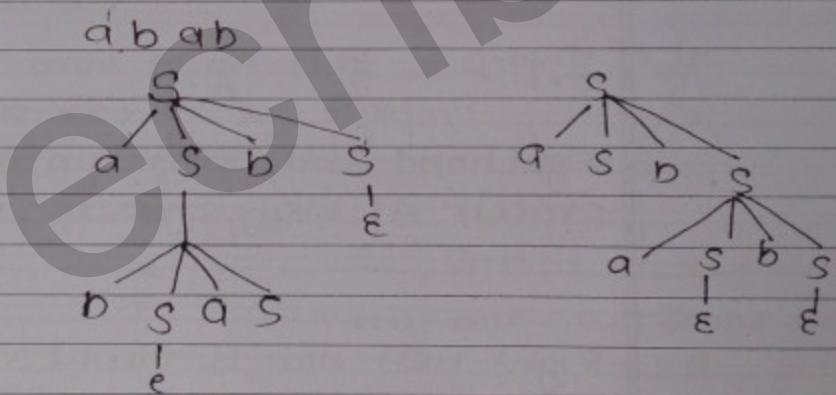
#  $S \rightarrow aSbS \mid bSaS \mid E$

$\{ \underline{E}, \underline{aa}, \underline{bb}, \underline{aa}, \underline{bb}, \underline{aa}, \underline{bb}, \underline{ab}, \underline{ba}, \underline{ab}, \underline{ba}, \underline{ab}, \underline{ba} \}$

$\Rightarrow S \rightarrow aSbS \mid bSaS \mid E$

# parse tree

The tree representation of derivation.



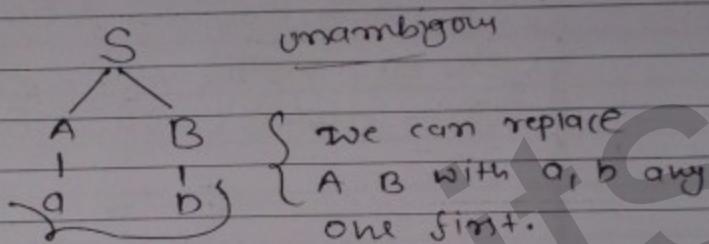
# context free grammar said to be ~~context~~ ambiguous if it contain more than 1 parse tree. More than 1 left most derivation and 1 right most derivation and 1 left most and right most derivation

Q1

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b$$



if we replace A by a first then it is called left most derivation else it is right most derivation.

+1

E·M·D :- Left most non terminal replace by its corresponding right hand side part in the derivation process. At every step is known as L·M·D

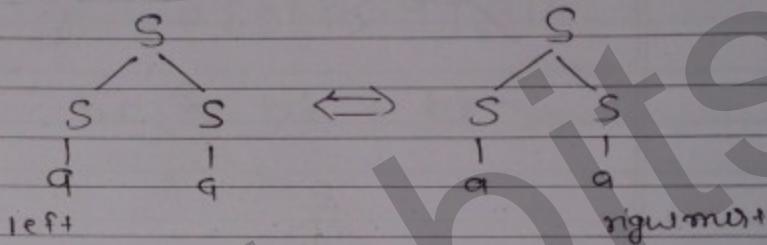
#1

Right most non terminal replace by its corresponding right hand side part at every step in derivation process is R·M·D.

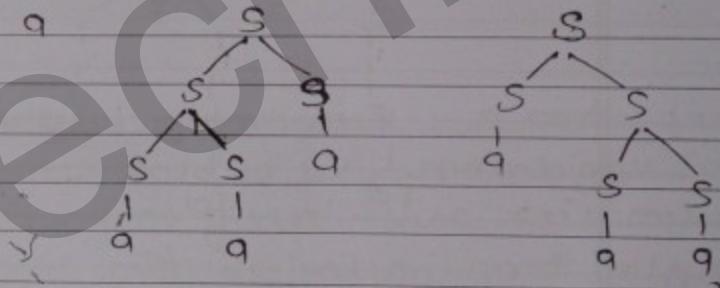
The derivation may be left most or right most derivation or random derivation.

But in parsing we will use left most derivation or right most derivation.

$$S \rightarrow SS1a \quad \text{Same: } a = \begin{array}{c} S \\ | \\ a \end{array}$$



$\Rightarrow$  ~~some~~  
 $\Rightarrow$  ~~a a a~~

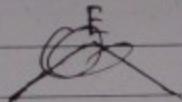


They are not same

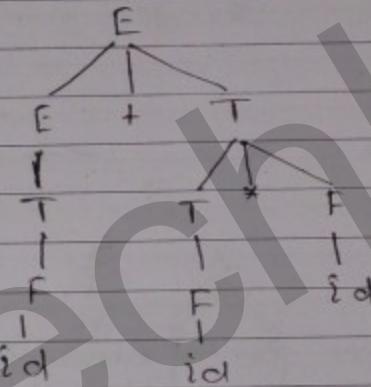
so it is unambiguous.

$$\# \quad \begin{array}{l} S \rightarrow aSb \\ S \rightarrow ab \\ S \rightarrow SS \end{array} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \text{well formed prefixes.}$$

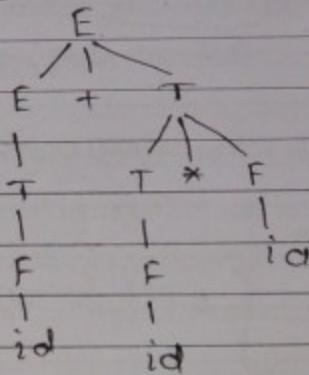
Q1

$$\begin{aligned} E \rightarrow & E + T \mid T \\ T \rightarrow & T * F \mid F \\ F \rightarrow & id \end{aligned}$$


$id + id * id$

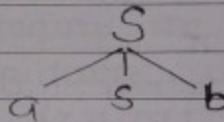


Q2



# Note :- To check the ambiguity in context free grammar there is no algorithm hence ambiguity problem is "undecidable" problem.

$$S \rightarrow a S b \mid b S a \mid a b$$



~~Small  
Small string = a~~

# unambiguous grammar :- A context free grammar said to be unambiguous for "all strings of given" there exist only one left most derivation and only one right most derivation and it produce same tree.

For one string one left most derivation and one right most derivation or it both have to produce only one parse tree.

$S \rightarrow aSb | ab$  grammar is  
ambiguous are not.

AU =) undecidable

# NOTE :- It is ~~im~~ impossible to eliminate , ambiguity from every ambiguous context free grammar because, there is no generalized algorithm hence, elimination of ambiguity problem is also undecidable problem.

# A ambiguous grammar for which, elimination of ambiguity is not possible, it called , an inherently ambiguous grammar.

$$\alpha = S a^i b^j c^k | i=j \oplus j=k \}$$

$$\alpha = \{ a^n b^n c^m | n, m \geq 1 \} \cup \{ a^n b^m c^m | n, m \geq 1 \}$$

# Fortunately No programming language are inherently ambiguous.

$$S \rightarrow S_1 | S_2$$

$$S_1 \rightarrow AB$$

$$\begin{aligned} A &\rightarrow aAb | ab \\ B &\rightarrow cBc | c \end{aligned}$$

$$S_2 \rightarrow CD$$

$$C \rightarrow cCc | c$$

$$D \rightarrow bDc | bc$$

#

Types of grammar

P-Lin

regular

(TYPE 3)

L-Lin

(TYPE 2) CFN

G

 $A \rightarrow \alpha$  $\times ((V+T)^+)$ 

(TYPE 1) CSN

Sensitive

(TYPE 0)  
unrestricted  
grammar $A \rightarrow \alpha B \beta \gamma$  $A \rightarrow B \alpha \beta$  $\alpha \rightarrow \beta$  $|\alpha| \leq |B|$  $\times B(V+T)^+$  $\alpha A \rightarrow \alpha b$ 

linear grammar:- In any grammar,

left hand side only one non terminal

right hand side at most one non terminal

if present, that is linear grammar.

- #1 Linear grammar may be left linear or right linear or middle linear.
- #1 If the linear grammar is either left linear or right linear then it is regular.
- #1 All regular grammar are linear grammar but all linear grammar need not be regular.

$S \rightarrow qSb|ab$   
linear but not regular.

CFN

e.g.  $\overline{A} \rightarrow BCD$

$S \rightarrow qSb|ab$  = linear not regular.

CSL     $qA \rightarrow bb$     LFL context  
 $S \rightarrow AB$     ]  
 $qA \rightarrow qb$     ] CSL  
 $B \rightarrow q$

regular grammar:

$$S \rightarrow aS \mid bS \mid a$$

H  $S \rightarrow lA$       } RG  
 $A \rightarrow lA \mid dA \mid e$  }

$$S \rightarrow cS \mid ss \mid \epsilon = CFG$$

H CSG

$$\textcircled{a} A(B) \rightarrow a\alpha b$$

replace A by  $\alpha$  if only it has  
 a and b as left context & right context

$$S \rightarrow asb \mid ab = CFG$$

becoz it is regular we can have either  
 $A \rightarrow \alpha B$  :

or  $A \rightarrow B\alpha$ ;

#

- 1) Regular grammars, not have enough power, to represent syntax of programming language (structure) hence to represent syntactic structure of programming languages the suitable grammar are context free grammar.
- 2) context free grammar, doesn't have enough power to represent semantic (meaning) of programming language hence to represent semantic of programming language suitable grammar are context sensitive grammar that language context sensitiv language.  
Hence C language, C++ Java this languages called as context sensitive language.

$$S \rightarrow aSb \mid aAb \\ A \rightarrow bA \mid b$$

b, bb-

a bb

$a^n$	$b^n$	$n \in \mathbb{N}$	$\emptyset$
-------	-------	--------------------	-------------

1) Checking the string is member of grammar or not. It is called as parsing.

$$S \rightarrow ABIBC$$

$$A \rightarrow BAIA$$

$$B \rightarrow CCIB$$

$$C \rightarrow ABIA$$

b

a

Ans

First calculation first (FIRST & LAST)

2) 1) The FIRST of a non-terminal, gives information regarding that non-terminal right hand side available first terminal information.

$$A \rightarrow a\alpha$$

↑ a is aw.

$$\text{first}(A) = \{a\}$$

2)

$$A \rightarrow Bd$$

$$\text{first of } (A) = \text{First of } (B)$$

$$A \rightarrow Bdy$$

$$B \rightarrow e$$

$$\text{first}(A) = \{\text{first}(B) - E\} \cup \{\text{first}(X)\}$$

#1

$$S \rightarrow aAB$$

$$A \rightarrow b$$

$$B \rightarrow c$$

calculate first of every, non terminal  
of this grammar.

S	{a}
A	{b}
B	{c}

#1

$$S \rightarrow AB$$

$$A \rightarrow a | \epsilon$$

$$B \rightarrow b$$

$$S \rightarrow A$$

$$A \rightarrow a$$

S	{a, b}
A	{a, \epsilon}
B	b

#

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b | \epsilon$$

S	{a}
A	{a}
B	{b, \epsilon}

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- # 1.  $E \rightarrow TE'$   
 $E' \rightarrow +TE' | \epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT' | \epsilon$   
 $F \rightarrow id$

$$\begin{aligned} E &= \{id\} \\ E' &= \{+, *\} \\ T &= \{id\} \\ T' &= \{*, \epsilon\} \\ F &= \{id\} \end{aligned}$$

- # 2.  $S \rightarrow A^e a A^b | B^e b B^a$   
 $A \rightarrow e$   
 $B \rightarrow e$   
 $S = \{e, a, b\}$   
 $A = \{e\}$   
 $B = \{e\}$
- $$\left( \begin{array}{l} S \rightarrow A = \{S\} = \{a\} \\ S \rightarrow B = \{e\} = \{b\} \\ S \rightarrow \{a, b\} \end{array} \right)$$

- # 3.  $S \rightarrow A^c B^a | C^b B^a | B^a \{$   
 $A \rightarrow d^a | BC = \{d^a\} \{d, a, b, h, \epsilon\}$   
 $B \rightarrow g | \epsilon = \{g, \epsilon\} \{d, a, h, \epsilon\}$   
 $C \rightarrow h | \epsilon = \{h, \epsilon\} \{$

$$S = \{d, g, h\}$$

Q1       $A \rightarrow A_1 A_2 A_3$

First of ( $A_1$ ) contain 5 elements.

First of ( $A_2$ ) contain 4 elements.

First of ( $A_3$ ) contain 3 elements.

All first set contain ( $E$ ) and all element are different. So how many element contain

$$A_1 \rightarrow 5 \quad (1 'E' \text{ then take } 4)$$

$$A_2 \rightarrow 4 \quad (3)$$

$$A_3 \rightarrow 3 \quad (2)$$

and last of  $A_3 \rightarrow E$  include  $E$

$$= 4 + 3 + 2 + 1$$

$$= 10$$

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1) follow (starting symbol) = { \$ }

2)  $A \rightarrow \alpha BB$

follow(B) = first(B)

3)  $(A) \rightarrow \alpha B$

follow(B) ~~is~~ follow(A)

$A \rightarrow \alpha BB$

$B \rightarrow \epsilon$

follow(B) = { first(B) -  $\epsilon$  }  $\cup$  follow(A)

[ NOTE:- follow set doesn't include  $\epsilon$  ]

$E \rightarrow TE$   
 $E' \rightarrow T(E')\epsilon$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT'| \epsilon$   
 $F \rightarrow id$

{ \*,  $\epsilon$  }

~~Follow~~ Follow = { \$ }

follow =  $E1 = \{ \$ \}$ ,

follow(T) = { +, \$ }

$T \rightarrow E' \rightarrow E$  generally ( $\epsilon$ )

then - take first of  $E'$

= { +,  $\epsilon$  } :

excluding  $\downarrow$  = { +, \$ }

follow(T') = { +, \$ }

follow(F) = { \*, +, \$ }

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#

$S \rightarrow AaAb \mid BbBa$

$A \rightarrow E$

$B \rightarrow E$

$S = \{ \$ \}$

$A = \{ a, b \}$

$B = \{ b, a \}$

#

$S \rightarrow AaB \mid Bb \mid Ba$

$A \rightarrow d \alpha \mid B \beta$

$B \rightarrow g \mid \epsilon$  :  $\{ g, \epsilon \}$

$C \rightarrow h \mid E$  :  $\{ h, \epsilon \}$

$S = \{ \$ \}$

$A = \{ h, g, \$ \}$

$B = \{ \$, a, h, g \}$

$C = \{ g, h \} \{ a, \$, b, h \}$

#  $S \rightarrow aA bB | bAa B| E$

$A \rightarrow S$

$B \rightarrow S$

$\text{First}(S) = \{a, b, E\}$

$\text{First}(A) = \{a, b\}$

$\text{First}(B) = \{a, b\}$

$\text{follow}(S) = \{\$ \} \cup \{a, b\}$

$\text{follow}(A) = \{a, b\}$

$\text{follow}(B) = \{\$, a, b\}$

# what is the regular expression that represent all the substring of string - delhi.

Substring of delhi	Total
$S - d, e, l, h, i, \sim$	$T_{OC}$
$4 - de, el, lh, hi, \sim$	$T_1, O, C - 3$
$3 - del, elh, lhi, \sim$	$T_0 O C - 2$
$2 - delh, elhi, \sim$	$T O C - 1$
$1 - delhi, \sim$	

$$\left[ \frac{n(n+1)}{2} + 1 \right]$$

Q1

what is regular expression that generates letter and digits and every string is starting with letter and length of string is atmost "32".

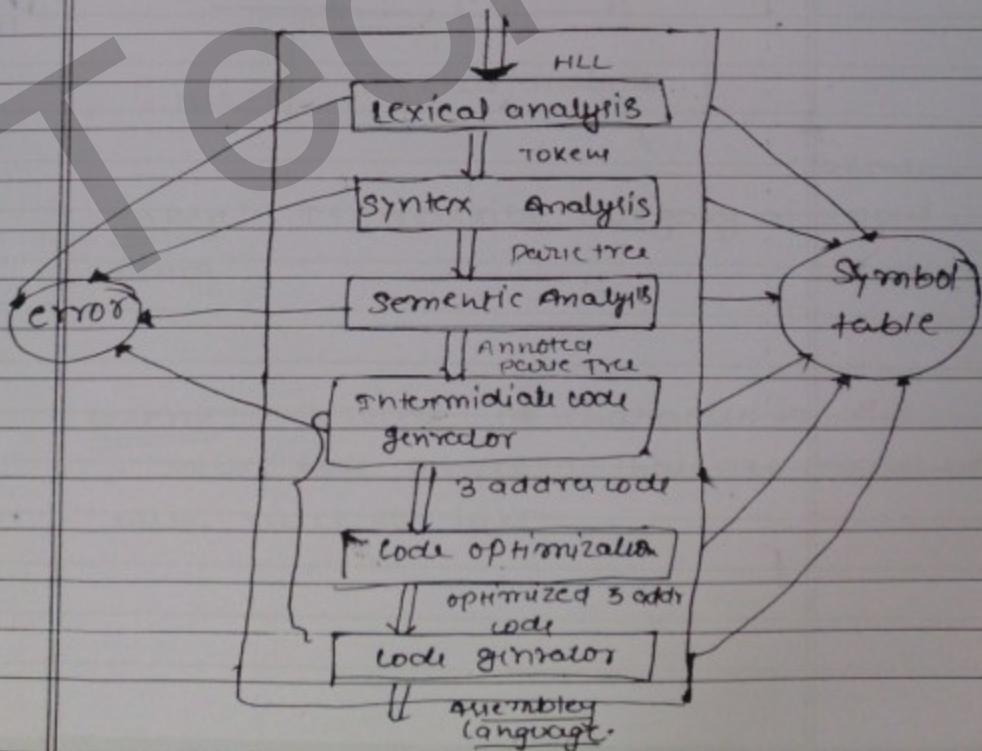
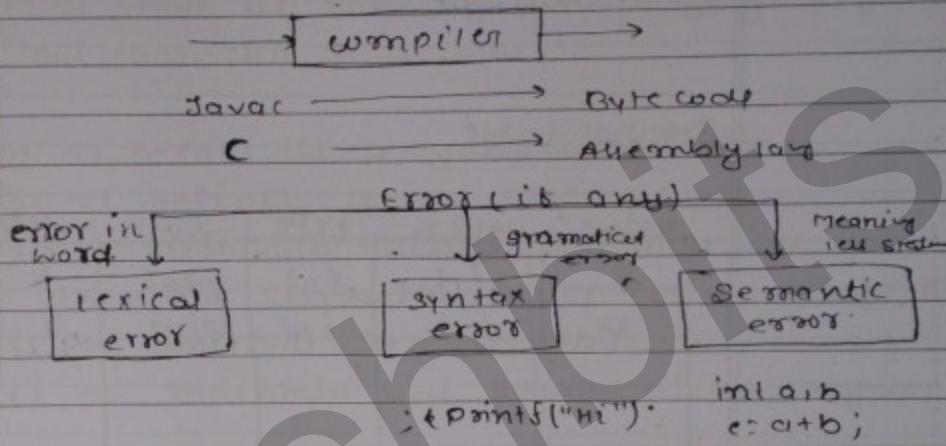
Ans

$\Sigma = \{a, b\}$  of lengths

$$(a+b)^5$$

A)  $L \cdot (1+d+\epsilon)^{31}$

# compiler :- It's a program that translates a program written in one language into an equivalent program in another language.



Symbol table is a data structure that contain information regarding variable and constants of the program along with its attribute values.

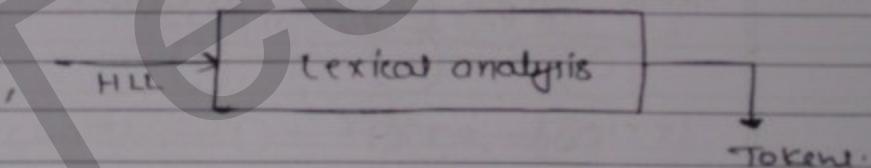
### Symbol table

value	token	TYPE	SCOPE	Memory
a	id	int	local	4
b	id	int	local	4

## lexical analysis

### functionalities

- 1) It reads the total high level language programs one character at a time.
- 2) It break the program into token.
- 3) It defines lexical error.
- 4) It eliminates blank, comment lines, new line character present in the program.
- 5) It construct symbol table.
- 6) It maintain line number of the program.



Token:- It describe category of input, String

lexeme:- Sequence of character in the source ~~code~~ program, that are matched with, rules of token.

int a, b;

↓  
Token (keyword)

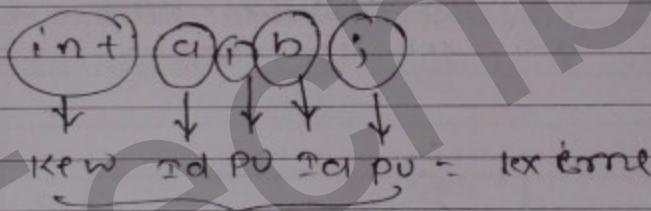
Keyword :- if, else,  
for, while.

Identifier :- xyz,  
abc

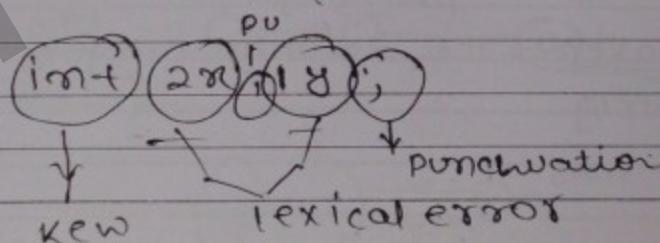
constant 20, 50.6

operator :- +, -, \*, /, %

punctuation  
;, (, ), {, }



lexical error



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# int =  $\text{--} \circ^i \circ^n \circ^+ \circ^{\text{other}} \circ$

float  $\text{--} \circ^j \circ^l \circ^o \circ^a \circ^! \circ^{\text{other}} \circ$

int  $\text{--} \circ^i \circ^f \circ^{\text{other}} \circ$

else  $\text{--} \circ^e \circ^l \circ^o \circ^s \circ^e \circ^{\text{other}} \circ$

# Identifier

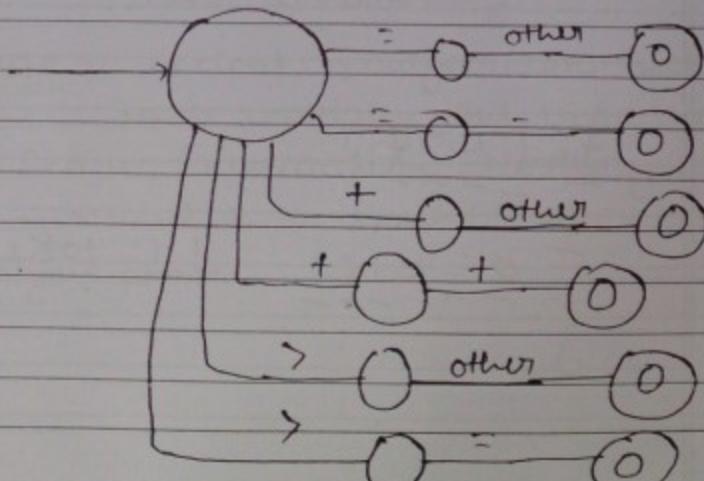
R.E  $((I+d)^*)^*$

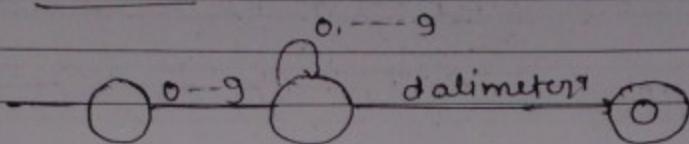
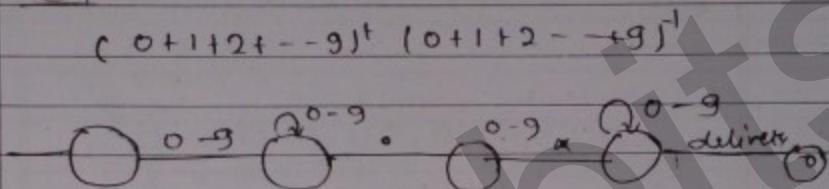
$\text{--} \circ^I \circ^d \circ^{\text{other}} \circ$

String  $\text{--} \circ^" \circ^{\text{other}} \circ^" \circ$

charct  $\text{--} \circ^' \circ^{\text{other}} \circ ^' \circ$

# operator



constantReal

int my3123;  $\frac{my}{other} \frac{3123}{other};$

for(;;) { i<10 } i++ )

= Total = 13 token.

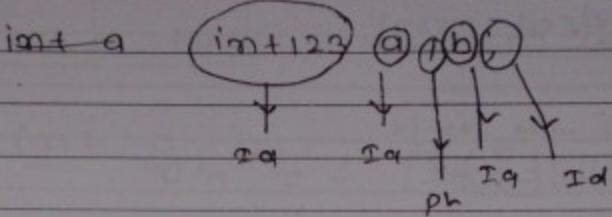
#1

f. ( a > b )

$\frac{f}{a} \frac{(}{b} \frac{>}{c})$

14 = token

}



#  
if ( $a > b$ )  
 $\frac{1}{2} \frac{2}{3} \frac{3}{4} \frac{4}{5}$

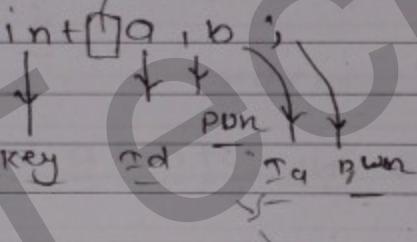
$\frac{1}{2} q = b + c ; / * \text{ addition } + /$   
 $\frac{2}{3} \frac{3}{4} \frac{4}{5} \frac{5}{6} \frac{6}{7} \frac{7}{8} \frac{8}{9} \frac{9}{10} \frac{10}{11} \frac{11}{12} \frac{12}{13}$

$\frac{3}{4}$

$\frac{1}{4}$  kept as tokens

white spaces, comments also implemented

#



Symbol table construction.

NOTE :- Lexical analyzer construct symbol table partially. The type information, scope information, memory size will be allocated to the symbol table, into semantic analysis phase.

lexical error

PU id op id op id

✓ 1) ; a E B A C = NO

✓ 2) c = a + "Hello"; NO

✓ 3) int a = 1, b = 2; NO

X 4) String S = (Hello); → No operator, not punctuation, no regno

X 5) char a = ab; character automatically gives error

X 6) char b = ab;

X 7) String J = compiler; error

✓ 8) int a = 908; NO

✓ 9) float c = 9.7; NO

X 10) float d = 9..8; lexical error

✓ 11) int a, b;

X 12) int a, b; error

(3) X 13) int a, b;

Int a, b; NO

No' ot tokew

$$1) \quad \underline{\text{int } a, b, c} \Rightarrow ?$$

2) printf ("compiler"): 5

3) printf (" %d %d ", a, b); = 9

$$4) \quad \begin{array}{l} \text{if } b \neq 0 \\ \text{then } \frac{a}{b} = \frac{a \cdot b^{-1}}{b \cdot b^{-1}} = a \cdot b^{-1} \end{array}$$

$$5) \quad ; a = b + c \quad 6 \text{ ist kein}$$

6) int findMax( int a, int b )

2 15 (9>5)

return q;      24 A (Token)

eue

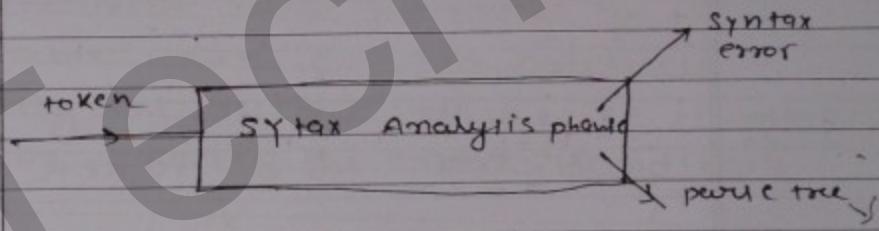
return b;

3

```
# main()
{
    for( i=0 ; i<=10 ; i++ )
}
```

compiler response for this code

- 1) lexical error : [FYO unidentified]
- 2) Syntax error
- 3) lexical and syntax
- 4) None of these



### Syntax errors

- 1) lack of tokens to frame Statement
- 2) more no of token than actually required for a statement
- 3)

#  $a = b + c * d$

$$S \rightarrow id = E$$

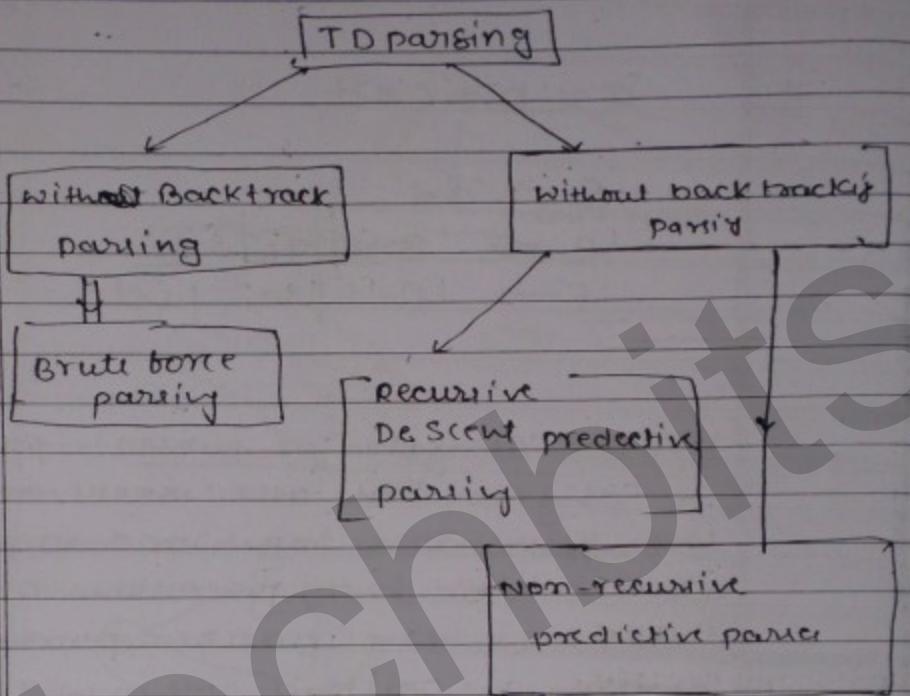
$$\begin{array}{c} E \rightarrow E+E \mid E*E \mid Id \\ E \rightarrow E+E \mid E*E \mid Id \end{array}$$

Syntax analyzer or parser :- parser is a program, that takes tokens and context free grammar as input and varieties tokens are derivable from grammar or not. If derivable, then parser produce parse tree passing as output otherwise it written Syntax errors to the error handler.

# The parsing can be done is top down, bottom up approach.

# If any parser uses top down parsing technique then it follows left most derivation in the construction of parse tree.

# If any parser uses bottom up parser technique then it uses, reverse of right most derivation in construction of parse tree.



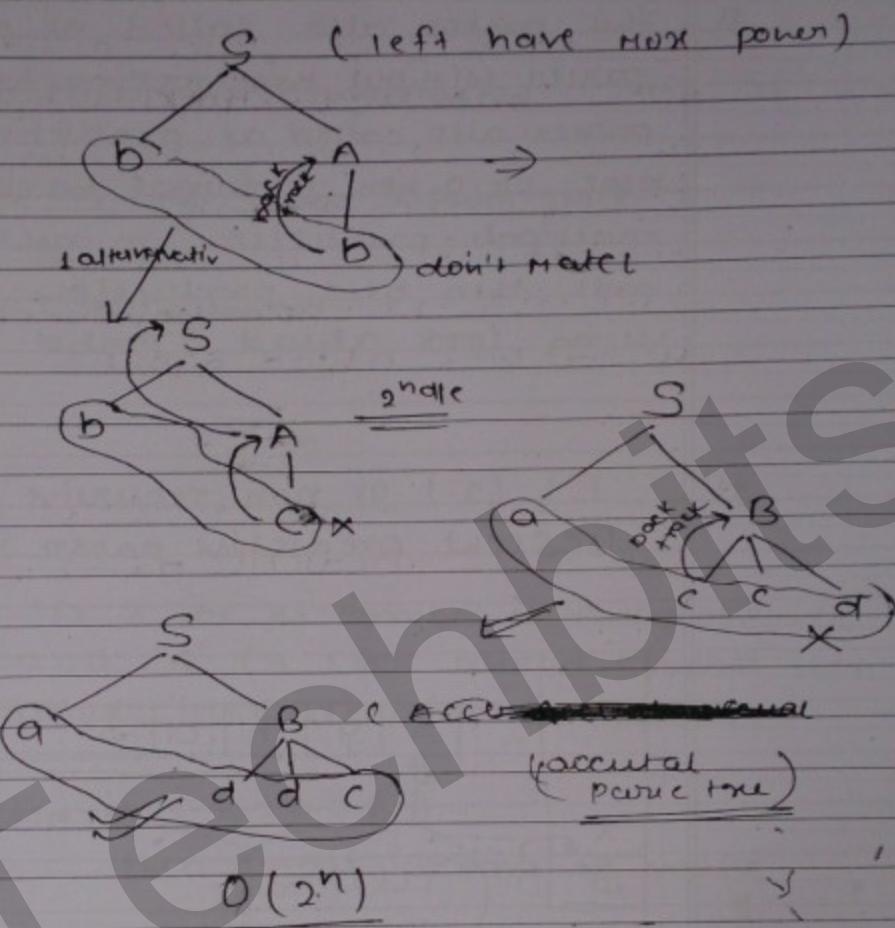
01

add c

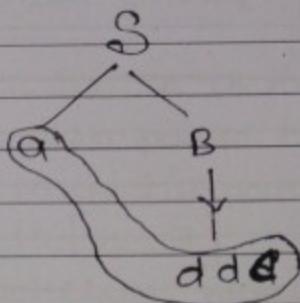
$S \rightarrow bA|aB$

$A \rightarrow b|c$

$B \rightarrow cc|dd|cc|dd$



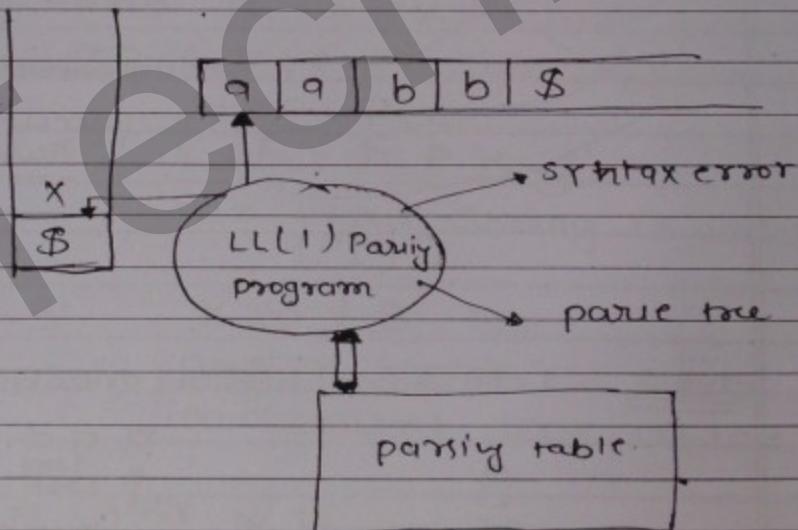
NOTE Left have higher priority



a d d c  
↑  
1st 2nd  
look ahead  
we check,  
which side give  
a sim +

1) This parser also called as predictive parser without backtracking topdown parser also called as predictive parser bcoz it's a non terminal having multiple production on right hand part then best production is selected using look ahead symbol.

2) LL(1) or non recursive descent predictive parser



ib

1)  $x = a = \$ \} \text{ input valid}$

2)  $x = a \neq \$ \} \text{ pop } x \text{ from stack}$

3)  $X$  is non terminal

let  $x$  be the symbol at the top of stack  
and ' $a$ ' is look ahead symbol then  
parser take decision as follows.

1) if ( $x = a = \$$ )

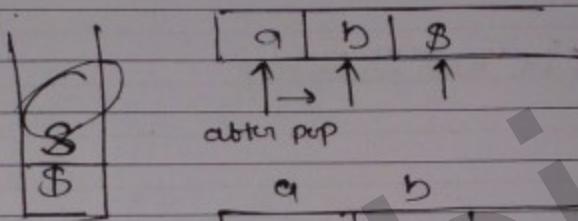
then input string is valid

2)  $x = a \neq \$$  then

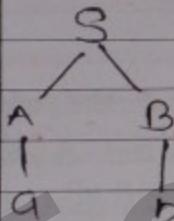
pop  $x$  from the stack  
increment look ahead.

3) If  $x$  is non terminal on the stack  
then parser take decision from -  
predictive parsing table. In the table  
if  $[x, a] : X \rightarrow u, v, w$   $x = u$   
production such as ~~u~~  $v$   $w$  present at then  
replace  $x$  such the  $u$  appear at the  
top of stack.

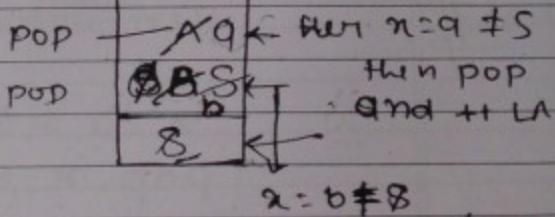
$[x, q]$  = blank entry in the table  
 Then there is syntax error, and  
 written it do error handler.

algo

⇒ Making with S



S	S → A B		
a	A → a		
b	B → b		



n

OK

all

# construction of LL(1) parsing table for the following grammar. And verify grammar is LL(1) grammar or not. also check whether it is ambiguous or not

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' | \epsilon$$

$$T \rightarrow F T'$$

$$T' \rightarrow * F T' | \epsilon$$

$$F \rightarrow id$$

Size of table = (No. of non-terminals)  $\times$  (Terminal + non-terminal)

First and Follow

$$F = \{ id \}$$

$$T' = \{ *, +, \epsilon \}$$

$$T = \{ id \}$$

$$F = \{ id \}$$

$$E' = \{ +, \epsilon \}$$

Follow E

$$E = \{ \$ \}$$

$$E' = \{ \$ \}$$

$$T' = \{ +, \$ \}$$

$$\begin{matrix} T \\ F \end{matrix}$$

	$i d$	$\oplus +$	$*$	$\vee$	$S$
$F$	$E \rightarrow T E'$				
$E'$		$E' \rightarrow + T E'$			$E' \rightarrow E$
$T$	$T \rightarrow F T'$				
$T'$		$T' \rightarrow E$	$T' \rightarrow * F T'$	$T' \rightarrow E$	
$F$	$F \rightarrow i d$				

## All LL(1) grammars are unambiguous grammars. But all unambiguous grammars need not be LL(1)

FOLLOW =  $S = a$

$A = a$

$B = \{a, E\}$

$C = \{b, E\}$

$$S \rightarrow a \textcircled{A} \textcircled{B} c$$

$$A \rightarrow a/bb$$

$$B \rightarrow a/E = \{a, E\}$$

$$C \rightarrow b/E = \{b, E\}$$

First

 $S = \{a\}$  $A = \{a, b\}$  $B = \{a, E\}$  $C = \{b, E\}$ 

Follow

 $S = \{\$\}$  $A = \{a, b\}$  $B = \$$ 

#

construct LL(1) parsing table for the following grammar

 $S \rightarrow aABC$  [For, E calculate follow then

 $A \rightarrow a/bb$  choose position where to place.]

 $B \rightarrow a/E$ 
 $C \rightarrow b/E$ 

	a	b	E
S	$S \rightarrow aABC$		
A	$A \rightarrow a$	$A \rightarrow bb$	
B	$B \rightarrow a$	$B \rightarrow E$	
C		$C \rightarrow b$	$C \rightarrow E$

$$S \rightarrow a \underline{A B E}$$

$$A \rightarrow A b c / b$$

$$B \rightarrow d$$

first

$$S = \{a\}$$

$$A = \{b\}$$

$$B = \{d\}$$

follow

$$S = \{\$\}$$

$$A = \{d\} b \}$$

$$B =$$

	a	b	c	d	e	\$
S	$S \rightarrow a A B E$					
A		$A \rightarrow A B C$				
B					$B \rightarrow d$	

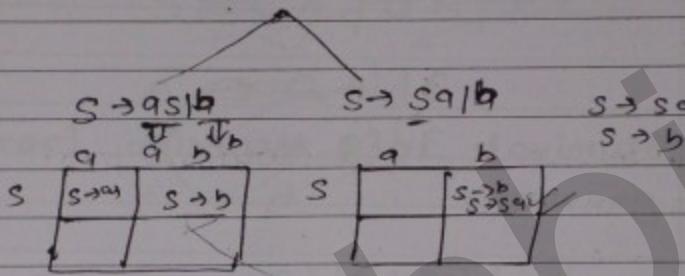
## NOTE

#

If grammar contain Left recursion  
then there is multiple entry in table.

NOTE

power of parser :- The number of grammar handed by a particular parser, is known as power of that parser.



NOTE :- If a grammar contain left recursion then its predictive parsing table contain multiple entries. Hence left recursive grammar are not LLL.

- # we can make this grammar are LLL by removing left recursion for that.

Removing of left recursion

$S \rightarrow Sq/b$ ,  
generated string =  $b a^*$   
Removed

$\Rightarrow S \rightarrow bS' = b$  } there is  
 $S' \rightarrow qS' | \epsilon = a^*$  } no more  
 $- ba^*$  } left recursive

$$\# \quad A \rightarrow A\alpha_1 | A\alpha_2 \dots \left. \begin{array}{|c|c|c|} \hline B_1 & B_2 & B_3 \\ \hline \end{array} \right| \dots$$

$$A \rightarrow B_1 A' | B_2 A' | B_3 A' \dots$$

$$A' \rightarrow \alpha_1 A' | \alpha_2 A' \dots \alpha_n A' \dots$$

$\#$  Eliminate left recursion from grammar.

$$E \rightarrow E + T | T$$

$$T \rightarrow T * F | F$$

$$F \rightarrow id$$

$$\begin{aligned} \# \quad E &\rightarrow T A' \\ A' &\rightarrow \cancel{E} + ET | E \\ T &\rightarrow F B' \\ B' &\rightarrow * FT | \epsilon \end{aligned} \quad \left. \begin{array}{l} \text{Removed} \\ \text{left recursion} \end{array} \right\}$$

$$F \rightarrow id$$

Eliminate left recursion form following grammar

$$S \rightarrow S_a | S_b | c | d | e$$

~~$$S \rightarrow c A' + d B' + e C'$$~~

$$\begin{array}{l} A' \rightarrow a A' | \epsilon \\ B' \rightarrow d B' | \epsilon \\ C' \rightarrow e \end{array}$$

$$S \rightarrow c S' | d S' | e S'$$

$$S' \rightarrow a S' | b S' | \epsilon$$

More Problem

$$\begin{array}{l} S \rightarrow a B | a A_2 \\ A \rightarrow a | b \\ B \rightarrow d | c \end{array} \quad \left. \begin{array}{l} \text{String } ab \\ \text{ambiguous this problem} \end{array} \right\}$$

creates problem for LL(1)

↑

Soln :- using left factoring we remove ambiguity problem.

$$\begin{array}{l} S \rightarrow a B A \\ A \rightarrow a | b \\ B \rightarrow d | c \end{array} \quad \Rightarrow$$

$$\begin{array}{l} S \rightarrow a(B+A) \Rightarrow S \rightarrow aZ' \\ \downarrow Z' \\ Z' \rightarrow B | A \\ A \rightarrow a | b \\ B \rightarrow d | c \end{array} \quad \left. \begin{array}{l} \text{Removed} \\ \text{ambiguity.} \end{array} \right\}$$

#  $A \rightarrow \alpha B_1 | \alpha B_2 | \alpha B_3 | \dots | \alpha B_n$

$A \rightarrow \alpha B$

$B \rightarrow B_1 | B_2 | \dots | B_n$

left factor the grammar

$S \rightarrow i E t S | i E t S e S | q$

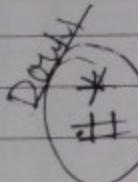
$E \rightarrow b$

∴  $S \rightarrow i E t S ( E t e S ) | q$

$S \rightarrow i E t S z' | q$

$z' \rightarrow E t e S$

$E \rightarrow b$



NOTE GATE prob

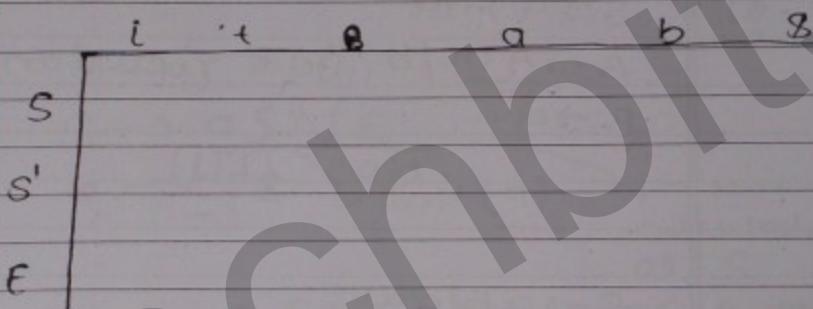
If it is impossible to convert into  
into LL(1) grammar

check whether this grammar LL(1) or not.

$$S \rightarrow iE + Sz' | A$$

$$z' \rightarrow \epsilon | es$$

$$E \rightarrow b$$



Q1 →  $S \rightarrow aS A^+ E \quad \left\{ \begin{array}{l} \text{create table} \\ A \rightarrow C | \epsilon \end{array} \right.$   
condition check (LL(1))

- 1) Single production is LL(1)
- 2) Left recursion gram not LL(1)
- 3) Non left factoring gram not LL(1)
- 4)  $A \rightarrow \alpha_1 | \alpha_2 | \dots | \alpha_n$   
 $\text{First}(\alpha_1) \cap \text{First}(\alpha_2) \cap \dots \cap \text{First}(\alpha_n) = \emptyset \quad \text{LL}(1)$

5)  $A \rightarrow \alpha | \epsilon \quad \left\{ \begin{array}{l} \text{LL}(1) \\ \text{First}(\alpha) \cap \text{First}(\epsilon) \neq \emptyset \\ \text{Follow}(A) \end{array} \right.$

$S \rightarrow AB \vee \left\{ \begin{array}{l} A \rightarrow a \\ B \rightarrow b \end{array} \right. \text{ single production} \right. \text{ LL(1)}$

Q)  $S \rightarrow a ABe$   
 $A \rightarrow \underline{ABC}/b$  (Left recursion)  
 $B \rightarrow d$   
 Not LL(1)

H)  $S \rightarrow ab/a^a$   
 common prefix so Not LL(1).

H)  $\checkmark S \rightarrow AB$   
 $\checkmark A \rightarrow a/b$  [can't find out a, b]  
 $\checkmark B \rightarrow b/c$  i.e. a, b  
 and a is  $\neq$  so Not LL(1)

$E \rightarrow TE' \quad S.P$   
 $E' \rightarrow +TE' | id \quad \{ \text{fix } +TE' \text{ if } id \}$   
 $T \rightarrow FT' \sim S.P$   
 $T' \rightarrow *FT' | \epsilon \Rightarrow \text{calculate follow } T'$   
 $F \rightarrow id \quad S.P$  ie.

#

$S \rightarrow qSAE$

$A \rightarrow C | E \rightarrow \underline{\text{first}(q)}$  for this calculate follow of S

$S \Rightarrow \text{fix } A \{ C, \epsilon \} \text{ then remove } A \Rightarrow \{ C, \$ \} \cap \text{first}(qSA) = \emptyset$

$\text{first}(C) = C \cap \neq \emptyset \text{ the follow}(A) = \{ C, \$ \}$   
Not LL(1)

#

$E \rightarrow TE'$

$E' \rightarrow +T$

#

$$S \rightarrow q S A | \epsilon \quad \{c, \epsilon, \$\}$$

$$A \rightarrow C | \epsilon$$

S

Q1

$$S \rightarrow q \underline{S} b S | b \underline{S} q S | \epsilon$$

→)

$$[S, q] \Rightarrow$$

$$\text{follow } S = (b, q, \$)$$

NOT LL(1) = ↗

$$[S, q] \Rightarrow S \rightarrow q S b S$$

$$[S, q] \Rightarrow S \rightarrow \epsilon$$

$$[S, b] \Rightarrow S \rightarrow b S q S$$

$$[S, b] \Rightarrow S \rightarrow \epsilon$$

$$\begin{array}{ll} \#1 & S \rightarrow A \mid q \quad [S;q] = S \rightarrow q \\ & \qquad [S,q] = S \rightarrow A \quad \left. \right\} \text{multiple} \\ & A \rightarrow q \quad \left. \right\} \text{NOT LLL(1)} \end{array}$$

$$\begin{array}{l}
 9) \quad S \rightarrow 1 \ A B b \mid \varepsilon \\
 A \rightarrow L \overset{1}{A} D \mid b \overset{c}{c} \\
 B \rightarrow \overset{a}{a} B \mid \overset{b}{b} \\
 C \rightarrow q
 \end{array}$$

$$S \rightarrow \frac{AaAB}{\alpha} \mid \frac{BbBq}{\beta} \quad \text{and } \sin \varphi = \phi$$

$\sim A \rightarrow E_a$   
 $\sim B \rightarrow E_b$

$L L(1) \frac{A}{\alpha}$

$$Q1 \quad E \rightarrow E + n | n \quad \text{Not LLLij}$$

which of the following condition sufficient to convert CFN with LL(1)

- 1) Removing left recursion above
  - 2)

Consider the following grammar.

$$\begin{array}{l} S \rightarrow i \underset{i}{\cancel{E}} + \underset{\cancel{S}}{S} ) q \\ S' \rightarrow e \underset{e}{\cancel{S}} E \\ E \rightarrow b \end{array}$$

Predictive Parsing Table entries ( $S'$ ,  $E$ )  
 $(S', e)$

Follow

- Q1 Consider following grammar and predictive parsing table.

$$S \rightarrow a \underset{q}{\cancel{A}} b B | b A a B | E$$

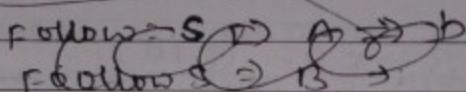
$$A \rightarrow \underset{b}{\cancel{S}}$$

$$B \rightarrow \underset{b}{\cancel{S}}$$

	a	b	\$
S	$S \rightarrow E$ $S \rightarrow a A B$	$S \rightarrow E$ $S \rightarrow b A B$	$S \rightarrow E$
A	$A \rightarrow S$	$A \rightarrow S$	
B	$B \rightarrow S$	$B \rightarrow S$	$B \rightarrow S$

FIRST =

$$\text{FIRST} = S \{ a, b, \epsilon \}$$



$$\text{FIRST}(S) = \{ a, b, \epsilon \} \quad | \quad \text{FOLLOW}(S) = \{ a, b, \$ \}$$

$$\text{FIRST}(A) \rightarrow \text{FIRST}(S) \Rightarrow (\check{a}, \check{b}, \epsilon) \Rightarrow \text{for } \epsilon$$

$$\text{FOLLOW}(A) \Rightarrow \{ b, a \} \quad \checkmark$$

$$\text{FIRST}(B) \Rightarrow (a, b, \epsilon)$$

$$\text{FOLLOW}(B) \Rightarrow \{ a, b, \$ \} \quad \checkmark$$

#

$$S \rightarrow AB$$

$$\begin{aligned} A &\rightarrow aa | ab \\ B &\rightarrow ba | bb \end{aligned}$$

#

$$S \rightarrow AB$$

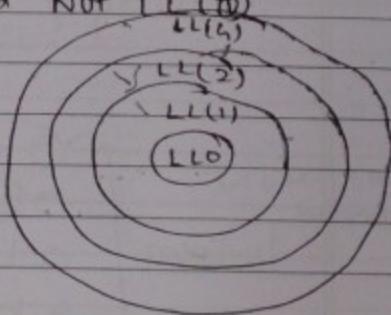
$$\begin{aligned} A &\rightarrow a | b \\ B &\rightarrow b | a \end{aligned}$$

#

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b$$



NOTE: All LL(k) grammars are unambiguous  
but all unambiguous grammars need not be  
LL(k) where k is the length of look ahead

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Q1)

Consider the following grammar

$$S \rightarrow FR^- (S, id)$$

$$R \rightarrow *S | E (*; $)$$

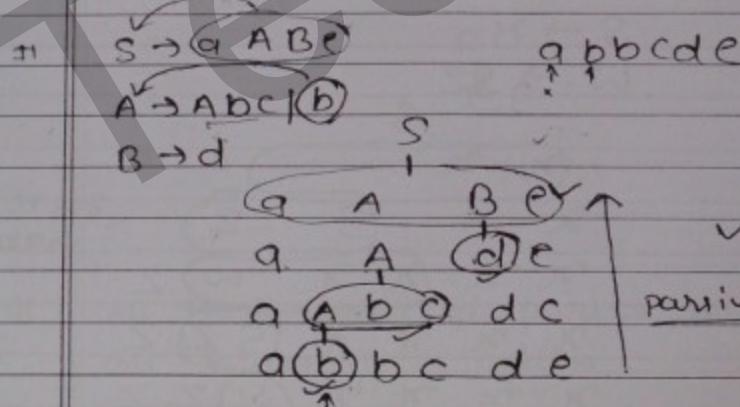
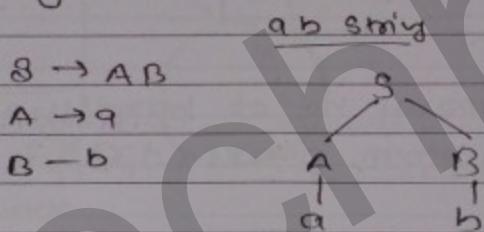
$$F \rightarrow id$$

in predictive parsing table to enter

$$\begin{array}{cc} [S, id] & [R, S] \checkmark \\ \Downarrow & [R, \\ (FR) & (R \rightarrow E) \checkmark \end{array}$$

NOTE

Top down parser can't work for, left recursive grammar and non deterministic grammar. Even it eliminates the left recursion from the grammar loses precedence, and associativity rules and readability also. Hence we need a parsing technique that can for "left recursive grammar" i.e bottom up parsing.



NOTE Bottom up parser construct the parse tree starting from giving string and proceeds until starting symbol of grammar.

Bottom up parser uses reverse of right most derivation, in construction of parse tree.

MATE = 2008

Handle - Handle is substring in the sentential form i.e. it is matching with complete right hand side part of given grammar

- Q1 How many no. of handle are detected by bottom parser + tree?

$$S \rightarrow x \pi w$$

xxxxyyzz

$$S \rightarrow R$$

$$W \rightarrow SZ$$

S

x x w

x x S Z

x x x x w z

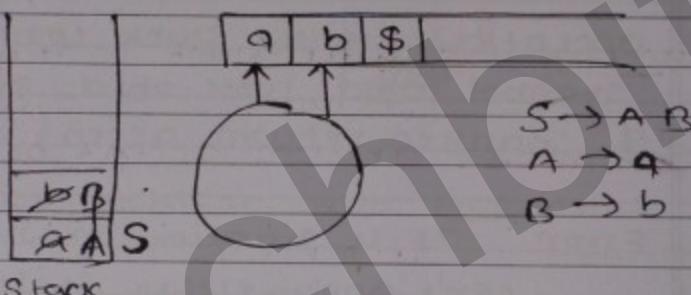
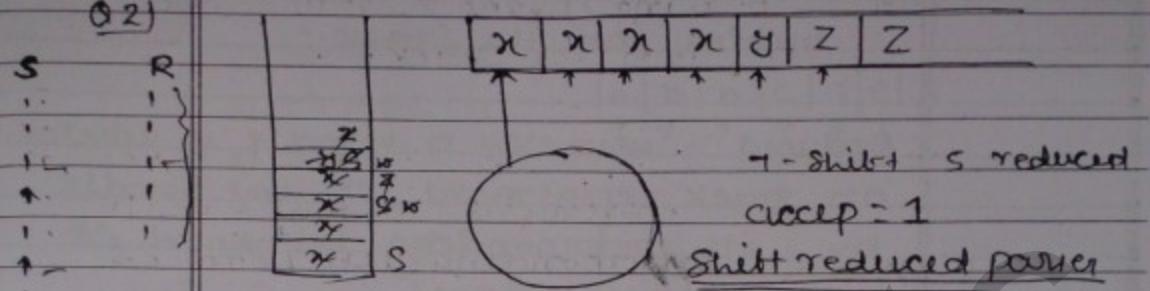
x x x x S Z z

x x x x y z z

there are  
handles

5 No. of handles are done.

021



$$\frac{S}{I} \quad \frac{R}{I}$$

- # All the bottom up parser will work based  
on following 4 action

  - 1) Shift.
  - 2) Reduce.
  - 3) accept.
  - 4) error.

Shift :- pushing symbol from input buffer into the stack.

Reduced :- whenever a handle is detected on stack replacement of that handle by its corresponding left hand is non-terminal done.

accept :- with the stack contain starting symbol and lookahead symbol is "S" parser return accept action.

Error :- It is situation in which parser can't apply either Shift action or reduced action not even accept also.

- Q1 How many shift action  
reduced action How many total action taken  
by shift reduced parser to parse

$$\begin{aligned} \text{Shift} &= 7 \\ \text{Reduced} &= 5 \\ \text{Accept} &= 1 \end{aligned} \quad \left. \begin{array}{l} \text{Total} \\ = 13 \end{array} \right\} \quad Q2A$$

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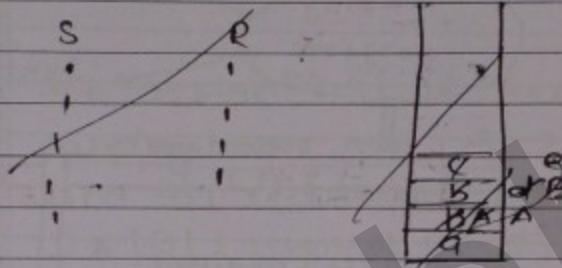
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$S \rightarrow a A B e$

$A \rightarrow A D C / b$

$B \rightarrow d$

$a | b | b | c | d | e | s$

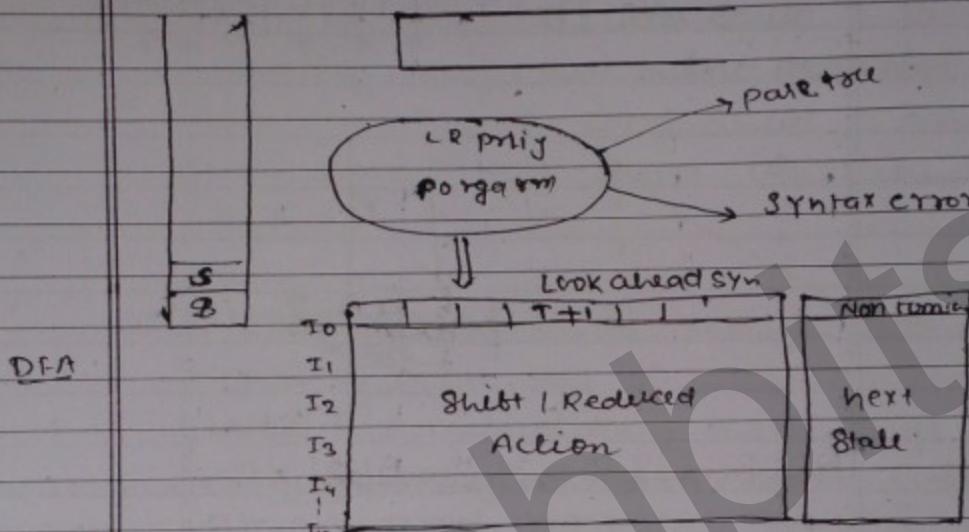


# Two problem with SLR

1) Reduced Reduced  $\Rightarrow$  conflict

2) When to do reduced and shift

## LR parsing



- 1) Let S be the State on the top of stack "a" is the look ahead symbol then parser take decision regarding Shift reduced action from the parsing table.
- ⇒ following are the possible action in the parsing table

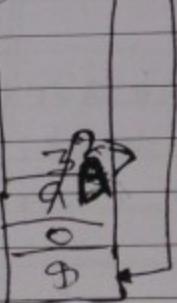
- # If Action [s,q] is shift j in the parsing table, then shift ~~s~~ "a" into the stack and shift j on the top onto Stack and increment look ahead symbol
- # If action [s,q] is reduce in the parsing table and  $A \rightarrow B$  is the product used for reduction, then pop  $2 \times |B|$  (length of B) symbols from the stack and push 'A' onto the stack and then push goto(i,A) onto the top of stack where 'i' is previous state onto the stack.
- # If action [s,q] is accept and stop parser halt and announce success.
- # If action [s,q] is error (black in the table entry) parser halt, return syntax error to the error handler.
- # Time complexity = O(n) where n is length of input string.

	<u>ACTION</u>	a	b	\$	S	goto A	goto B
T <sub>0</sub>	S <sub>3</sub>				1	2	
T <sub>1</sub>				accept			
T <sub>2</sub>		S <sub>5</sub>					4
T <sub>3</sub>			r <sub>2</sub>				
T <sub>4</sub>				r <sub>1</sub>			
T <sub>5</sub>				r <sub>3</sub>			
T <sub>6</sub>							
T <sub>7</sub>							

$$\begin{array}{l} S \rightarrow AB \\ A \rightarrow a \\ B \rightarrow b \end{array} \quad \left. \begin{array}{c} q \\ b \end{array} \right\}$$

q b \$

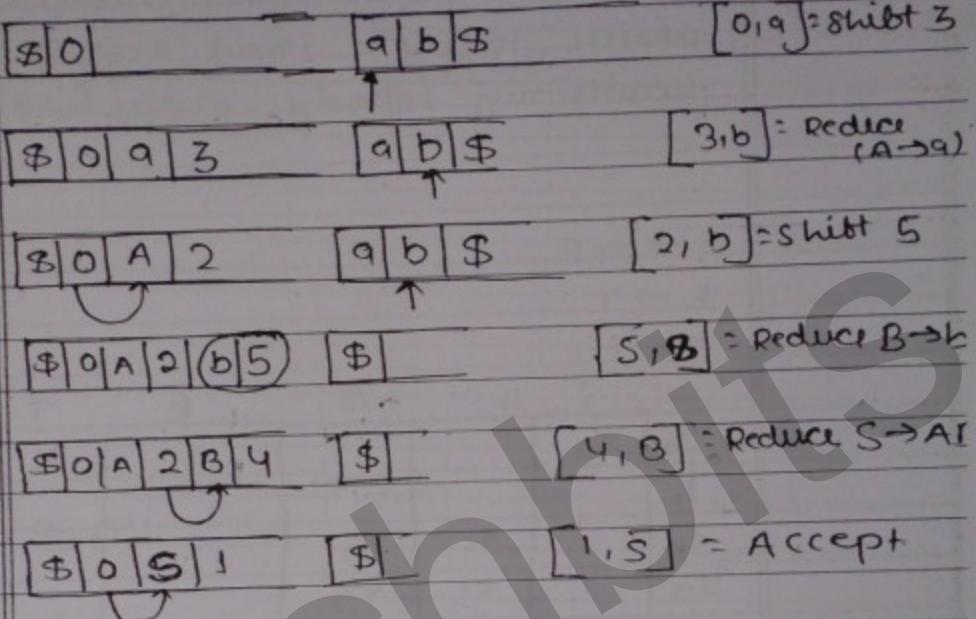
LR parsing



Stack

input buffer

Action



- # Note any parity done on table known as table driven parser.  
hence LLL(1) and LR(1) parsing are examples
- # Recursive decent parser is not table driven.

# How many reduced action how many shift and total action taken by LR process to parse input string( $i$ ) by considering following parser table.

$$E \rightarrow T+E$$

$$E \rightarrow T$$

$$T \rightarrow i$$

	$i$	+	\$	E	T
$I_0$	$S_3$			1	2
$I_1$			accept		
$I_2$		$S_4$	$r_2$		
$I_3$		$r_3$	$r_3$		
$I_4$	$S_3$			5	2
$I_5$			$r_1$		

O
\$

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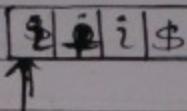
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Stack

Input buffer

Action

\$	0	
\$	0	i 3



Stack:  
+ i 8  
↑ ↑ ↑  
8 0  
8 0 i 3  
8 0 i 3 T  
8 0 i T 2 + 4  
8 0 i T 2 + 4  
8 0 i T 2 + 4 (i 3)  
8 0 i T 2 + 4 T 2  
8 0 i T 2 + 4 E 5  
8 0 i T 2 +  
8 0 i

Input buffer:  
[0, i] = S<sub>3</sub>  
[3, +] = R<sub>3</sub> ( $T \rightarrow i$ )  
[2, T] = S<sub>4</sub>  
[4, i] = S<sub>3</sub>  
[3, \$] = R<sub>3</sub> ( $T \rightarrow i$ )  
[2, \$] = R<sub>2</sub> ( $E \rightarrow T$ )  
[5, \$] = R<sub>1</sub> ( $E \rightarrow T+E$ )

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Stack

input buffer

\$ | 0      i + i \$       $[0, i] = S_3$

\$ | 0 | i | 3      i + i \$       $[3, i] = R_3 (T \rightarrow i)$

\$ | 0 | T | 2      i + i \$       $[2, i] = S_4$

\$ | 0 | T | 2 | 4 | i | 3      i + i \$       $[3, i] = R_3 (T \rightarrow i)$

\$ | 0 | T | 2 | 4 | T | 2      i + i \$       $[2, i] = R_2 (\Sigma \rightarrow T)$

\$ | 0 | T | 2 | 4 | E | 5      i + i \$       $[5, i] = R_1 (E \rightarrow T+E)$

\$ | 0 | E | 1      i + i \$       $[1, i] = \text{Accept}$

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### construction of LR(0) parsing table

- 1) Augmented grammar:- Adding a New production

$S' \rightarrow S$  to the original grammar.

- 2) This augmented production helps the parser to show accept action i.e whenever parser tries to reduce  $S$  by  $S'$  it lead to accept action.

- 3) Compute LR(0) item :-

LR(0) item is nothing but a context free grammar production having a " $\cdot$ " on ~~RHS~~ RHS part.

$A \rightarrow \cdot XYZ$  parser has seen 'x'

$A \rightarrow X \cdot YZ$  and ready to see "YZ".

$A \rightarrow XY \cdot Z$

$A \rightarrow X Y \cdot Z$

$S' \rightarrow \cdot S$  (parser ready to see right hand side part)

closure 's'  $\rightarrow \cdot s$   
 $s \rightarrow \cdot AB$   
 $A \rightarrow \cdot a$

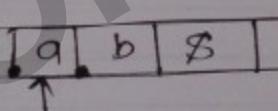
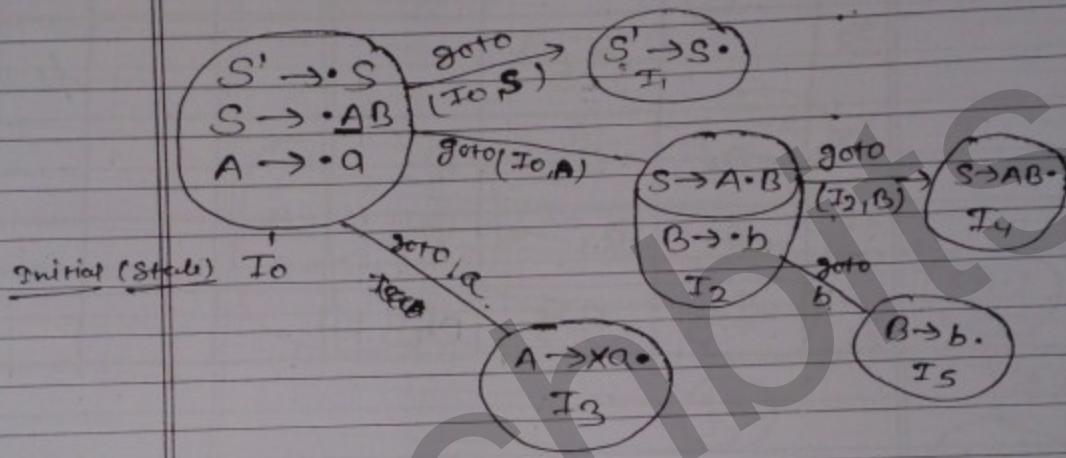
it means move " $\cdot$ " 1 more right place.

closure :- closure function add non terminal ~~to~~ production and it will put " $\cdot$ " on right hand point of the production.

note :- create function move " $\cdot$ " 1 position ahead.

a) construct LR(0) parsing table, for the following grammar. And verify grammar is LR(0) or not. Check if it is ambiguous or, unambiguous.

Ay

$$\begin{array}{l}
 S \rightarrow AB \\
 A \rightarrow a \\
 B \rightarrow b
 \end{array}
 \xrightarrow{\text{construct argument grammar}}
 \begin{array}{l}
 S' \rightarrow S \\
 R_1: S' \rightarrow AB \\
 R_2: A \rightarrow a \\
 R_3: B \rightarrow b
 \end{array}$$


3
a
0
\$

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shift

	a	b	c	S	A	B
I <sub>0</sub>	S <sub>3</sub>				1	2
I <sub>1</sub>				Accept		
I <sub>2</sub>		S <sub>5</sub>				4
I <sub>3</sub>	R <sub>2</sub>	R <sub>2</sub>	R <sub>2</sub>			
I <sub>4</sub>	R <sub>1</sub>	R <sub>1</sub>	R <sub>1</sub>			
I <sub>5</sub>	R <sub>3</sub>	R <sub>3</sub>	R <sub>3</sub>			

Note

All LR(0) are unambiguous grammars  
but all unambiguous grammar need not be LR(0)

Q1

$$A \rightarrow (A)$$

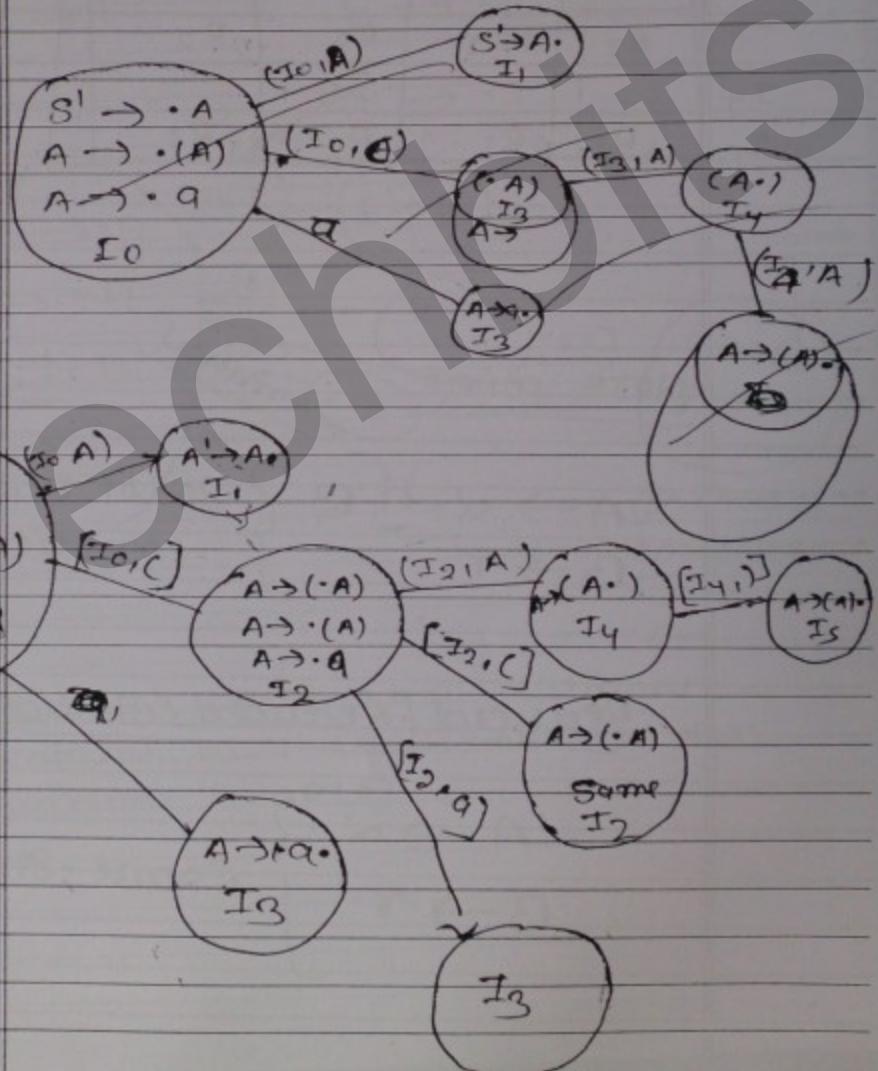
$$A \rightarrow q$$

$$\begin{matrix} S \rightarrow S' \\ S' \rightarrow \end{matrix}$$

$$S' \rightarrow A$$

$$A \rightarrow (A)$$

$$A \rightarrow \cdot q$$



	a	c	)	\$	A
I <sub>0</sub>	S <sub>3</sub>	S <sub>2</sub>			I
I <sub>1</sub>					
I <sub>2</sub>	S <sub>3</sub>	S <sub>2</sub>			4
I <sub>3</sub>	R <sub>2</sub>	R <sub>2</sub>	R <sub>2</sub>	R <sub>2</sub>	
I <sub>4</sub>			S <sub>5</sub>		
I <sub>5</sub>	R <sub>1</sub>	R <sub>1</sub>	R <sub>1</sub>	R <sub>1</sub>	

NOTE pointterminalLR(0)

$A \rightarrow \alpha \cdot \underset{\text{terminal}}{\underline{\alpha}} B$  } Shift reduced  
 $B \rightarrow \gamma \cdot$  } conflict

Reduced / Reduced conflict

$A \rightarrow \alpha \cdot \underset{\text{Same state}}{\underbrace{B \rightarrow \gamma \cdot}}$

$E' \rightarrow E$ 

$$E \rightarrow T + E$$

$$E \rightarrow T \Rightarrow$$

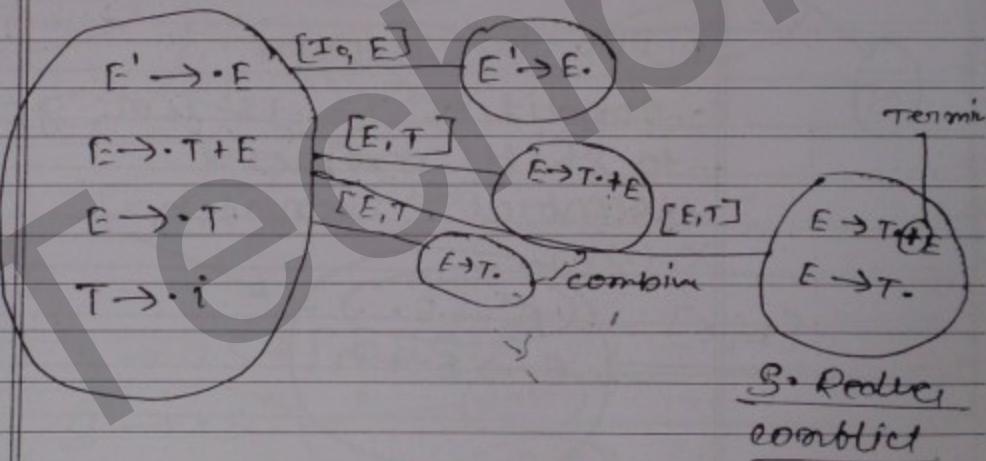
$$T \rightarrow i$$

$$E' \rightarrow \cdot E$$

$$E \rightarrow \cdot T + E$$

$$E \rightarrow \cdot T$$

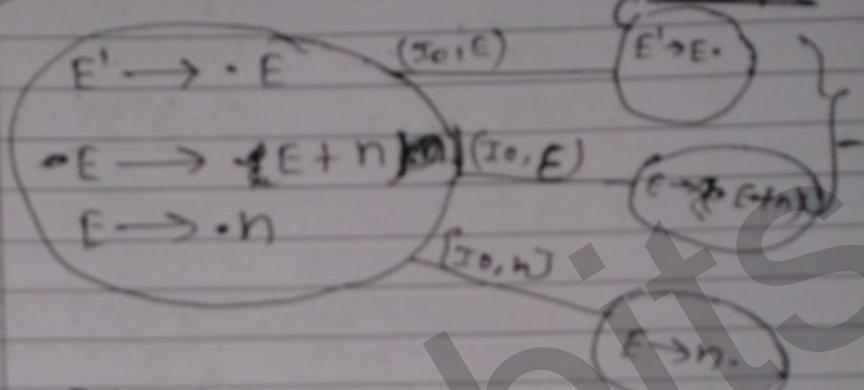
$$T \rightarrow \cdot i$$



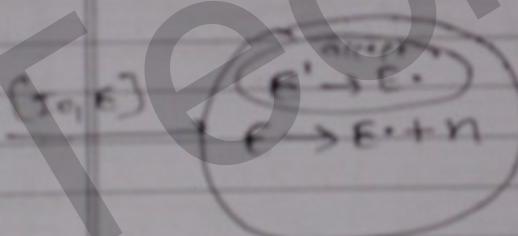
Note:- If LR(0) item automata contains atleast one conflict then grammar is not LR(0).

~~gate~~

$$E \rightarrow E + n \mid n$$



DUE to accept condition it is not going to shift reduced conflict even it has



Q1

check whether following grammar is LR(0) or not.

$$E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow i$$

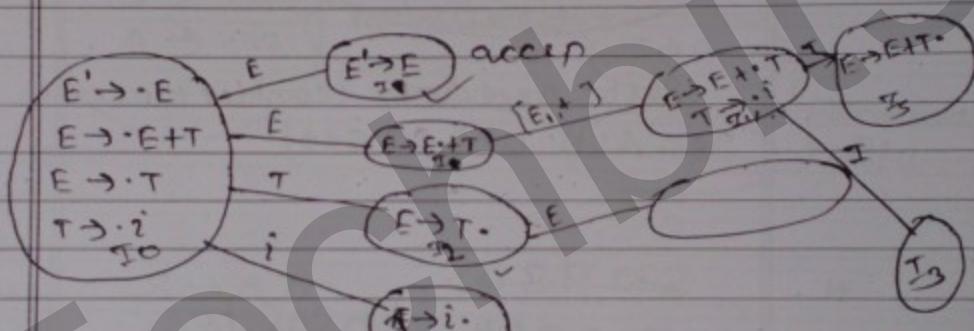
$$E' \rightarrow \cdot E$$

⇒

$$E \rightarrow \cdot E + T$$

$$E \rightarrow \cdot T$$

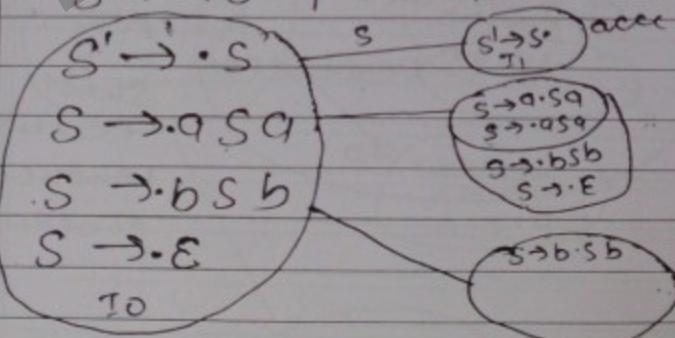
$$T \rightarrow \cdot i$$



LR(0) ✓  
LR(1) ✗

H

$$S \rightarrow aSb \mid bSb \mid E$$



#

 $S \rightarrow aSa \mid bSb \mid E$ 

$$\begin{aligned} S' &\rightarrow \cdot S \\ S &\rightarrow \cdot aSa \\ S &\rightarrow \cdot bSb \\ S &\rightarrow E \end{aligned} \quad \text{Reduce}$$

To

Shift reduced conflict occur.  
so it is not LR(0)

#

$$\begin{aligned} S &\rightarrow aSbS \\ S &\rightarrow aSbS \mid bSaS \mid E \end{aligned}$$

$$\begin{aligned} S' &\rightarrow \cdot S \\ S &\rightarrow \cdot aSbS \\ S &\rightarrow \cdot bSaS \\ S &\rightarrow \cdot E \end{aligned} \quad \text{Reduce}$$

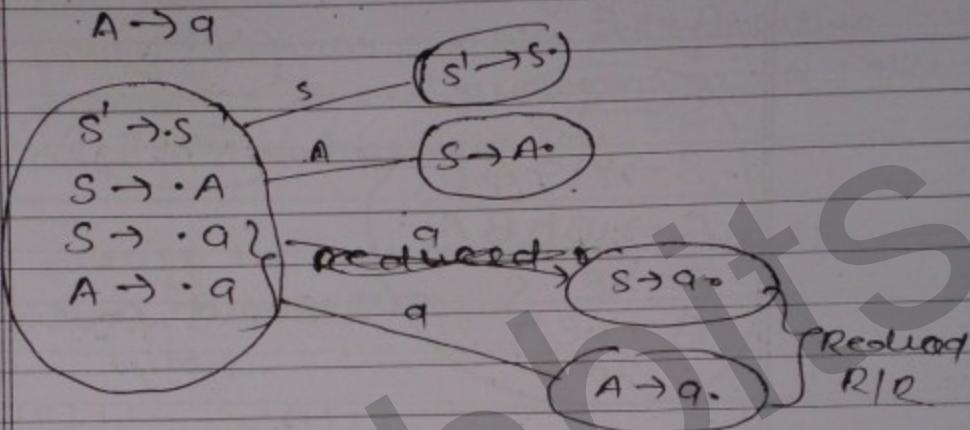
To

(not LR(0))  
shift  
reduced  
conflict  
occur.

11

$$S \rightarrow A/q$$

$$A \rightarrow q$$



Q1

$$S \rightarrow A A$$

$$A \rightarrow q A$$

$$A \rightarrow q$$

$$S' \rightarrow S$$

$$S \rightarrow \cdot A A$$

$$A \rightarrow \cdot q A$$

$$A \rightarrow \cdot q$$

$$S' \rightarrow S$$

$$S \rightarrow A \cdot A$$

$$A \rightarrow \cdot q A$$

$$A \rightarrow \cdot q$$

$$A \rightarrow q \cdot A$$

$$A \rightarrow \cdot q A$$

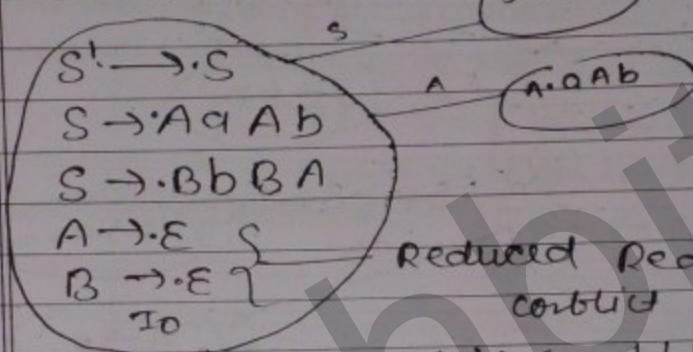
$$A \rightarrow \cdot q$$

$$A \rightarrow q \cdot$$

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow E$$

$$B \rightarrow E$$



LL(1) ✓    LL(0) ✗

NOTE :- In LR(0) "0" indicate no look ahead concept is used to place the reduced action. Hence there may be chance of having unnecessary reduced action in the parsing table. To avoid this drawback we will use SLR(1) parsing table.

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SLR(1) = simple LR(1)

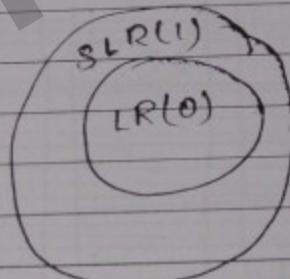
construct SLR(1) parsing table for the following grammar and also verify whether grammar is SLR(1) grammar or not. Also check it ambiguous or not.

As

placing the reduced entry base on below calculation.

I<sub>0</sub>  
I<sub>1</sub>  
I<sub>2</sub>  
T<sub>3</sub>  
I<sub>4</sub>  
T<sub>5</sub>


#



power SLR(1) > power LR(0)

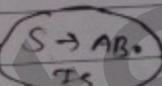
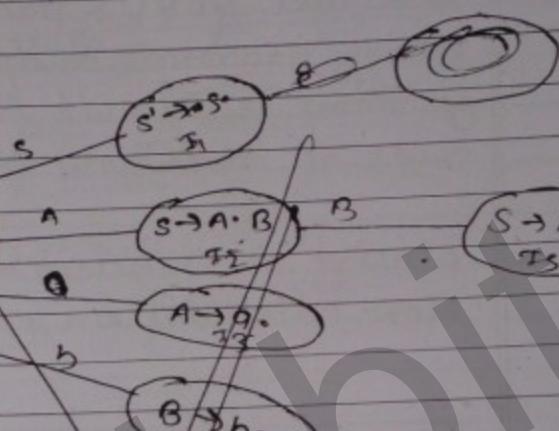
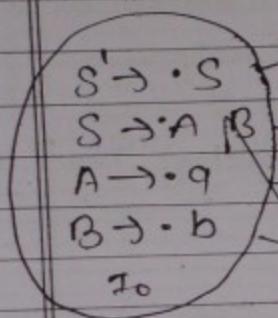
and it is unambiguous grammar:

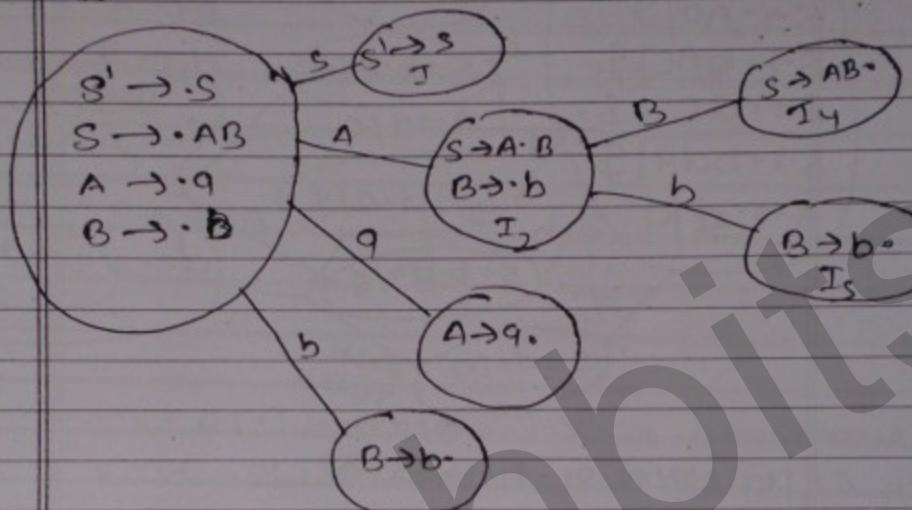
Q) Check whether grammar is SLR(0)

$$S \rightarrow AB$$

$$A \rightarrow a$$

$$B \rightarrow b$$



$S \rightarrow AB$  $A \rightarrow a$  $B \rightarrow b$ 

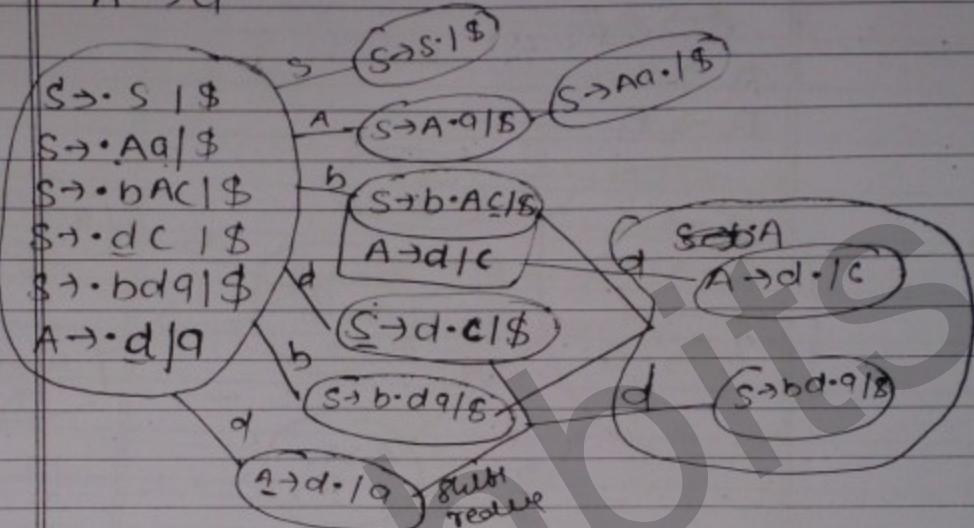
	a	b	\$	A	B	.
$I_0$	$S_B$					
$I_1$						
$I_2$		$S_S$				$\downarrow$
$I_3$			$\gamma_2$			
$I_4$				$\gamma_4$		
$I_5$					$\gamma_3$	

NOTE:- context free are ~~not regular~~ but  
 Set of all LR(0) item  
 are regular.

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$$0) \quad S \rightarrow Aa \mid bAc \mid dc \mid bdq \\ A \rightarrow d$$

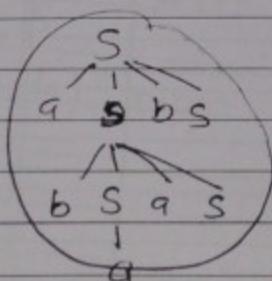


for 1 (0) shift reduce

for SLR(1) X

so

$$\# \quad S \rightarrow aSbS \mid bSaS \mid E \quad (abab)$$



ambiguous grammar

Not LR(0) &  
 LL(1) &  
 SLR(1) &  
 CLA(1) &  
 LALR(1) &

Q)

$$S \rightarrow AqAb$$

$$S \rightarrow BbBq$$

$$A \rightarrow q$$

$B \rightarrow b$  check for LR(0), \*#

#)

$$S \rightarrow A1q$$

$$A \rightarrow q$$

$$\begin{array}{c} S \\ \Rightarrow \\ \begin{array}{c} 1 \\ q \end{array} \end{array} \Rightarrow \begin{array}{c} S \\ \mid \\ \begin{array}{c} A \\ q \end{array} \end{array}$$

(i) LALR(1) parser, for a grammar have shift reduce conflict, it is an only.

1) LR(0) grammar reduce reduce conflict

2) LR(1) grammar have reduce reduce conflict

3) LR(1) have shift reduce

4) Non of this

Q) consider the following grammar and following

LR(0) item

$$S \rightarrow S^* E$$

$$1) S \rightarrow S^* E$$

$$S \rightarrow E$$

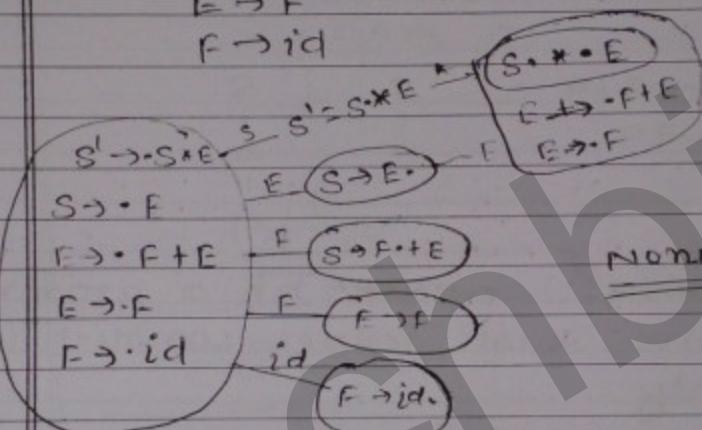
$$2) E \rightarrow \text{F+F+E}$$

$$E \rightarrow F+E$$

$$3) E \rightarrow F+F$$

$$E \rightarrow F$$

$$F \rightarrow id$$



None of them

Q) consider the following grammar which of following is true

$$S \rightarrow CC$$

$$C \rightarrow cC/a$$

1) This is LL(1)

2) This is LR(1) but not LL(1)

3) This is LL(1) but not LALR(1)

4) This is neither

Q1 conclude the following grammar

$$E \rightarrow E + n \mid E * n \mid n$$

which of the following are the handle in the right sentential form.

$$n + n * n$$

$$\begin{array}{ll} \overbrace{E}^{\text{handle}} & \text{handle} \\ \overbrace{E + n}^{\text{E}} \times n & E, E+n, E*xn \\ \overbrace{E + n}^{\text{E}} \times n & \\ \overbrace{n + n}^{\text{E}} \times n & \end{array}$$

LR(0)	SLR(1)	CLR(1) and LALR(1)
shift reduce	$A \rightarrow \alpha \# B$ $B \rightarrow \gamma$ $\text{follow}(B) = \{\gamma\}$	$A \rightarrow \alpha \# B$ $B \rightarrow \gamma$ $\text{follow}(B) = \{\gamma\}$
Reduce Reduce	$A \rightarrow \alpha$ $A \rightarrow \gamma$ $A \rightarrow B \cdot$ $\text{follow}(A) \cap \text{follow}(B) = \emptyset$	$A \rightarrow \alpha, \$ \in \{$ $B \rightarrow \gamma \$ \in \}$ $\text{follow}(A) \cap \text{follow}(B) = \emptyset$

# LR(1) by default CLR(1)

NOTE:- If we remove the ambiguity from the grammar loses readability.

# Removal of ambiguity is not advisable.  
Hence to handle ambiguous grammar,  
the suitable parsing technique is  
operator parsing.

## Operator precedence parsing

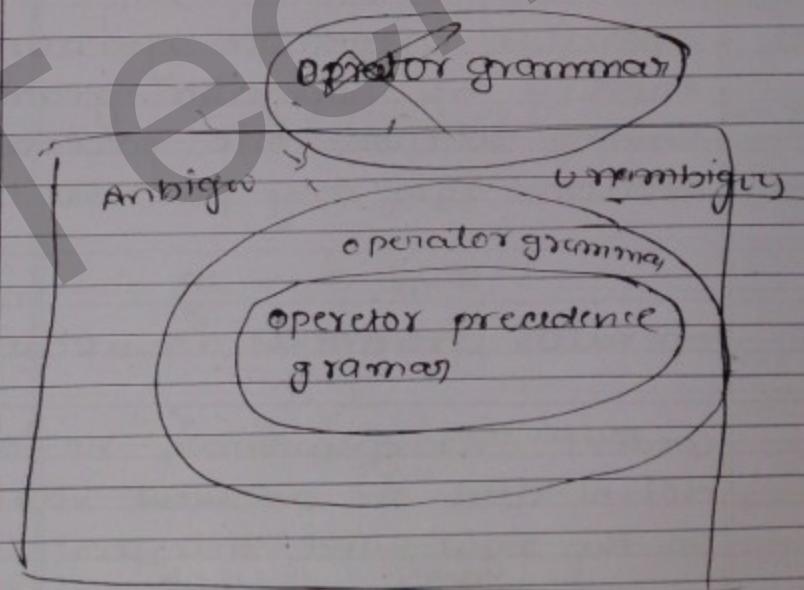
- 1) Ambiguous grammar and unambiguity
- 2) Simple to design.
- 3) We can construct operator precedence parser for the operator precedence grammar
- 4) Operator precedence grammar is nothing but operator grammar having almost one precedence relation b/w any pair of terminals.
- 5) Operator grammar is nothing but context free grammar, no "e" rule define and no adjacent variable on the right hand side part.

Q1 Which the following two rule violates the requirement of operator grammar.

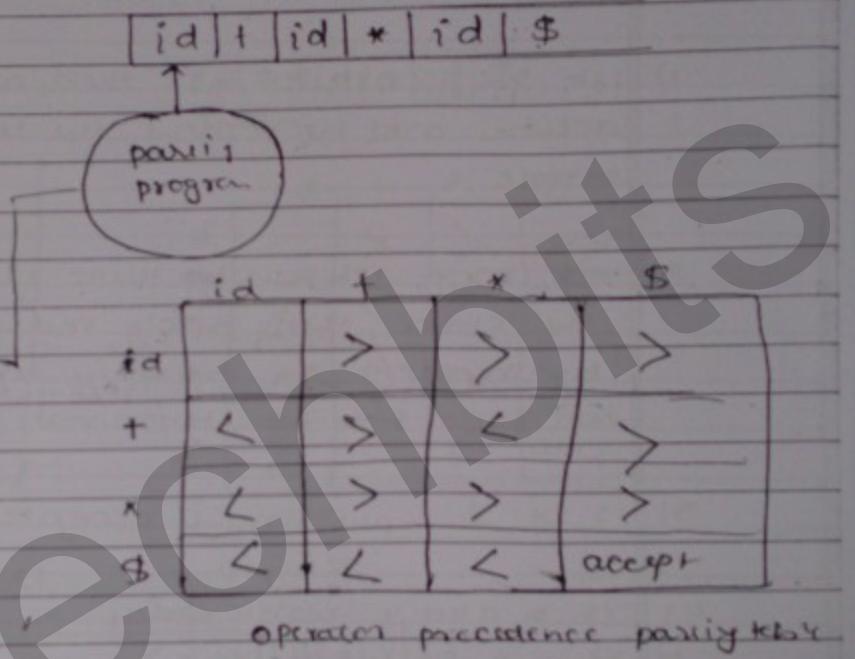
- 1)  $P \rightarrow C_a R$
- 2)  $P \rightarrow \epsilon X$
- 3)  $P \rightarrow C_b R q$
- 4)  $P \rightarrow CRX$

#

~~Ans~~  
Every operator precedence grammar is operator grammar but, operator grammar need not be operator precedence grammar



operator precedence pariy algo.



$x < y \} \text{ shift}$   
 $x = y \}$

$x > y \} \text{ reduce action}$

$x = y = \$ \text{ accept } \}$   
 $[x, y] = \text{blank} = \text{error}$

# Let 'x' is the topmost, terminal on the stack, and 'y' is current look ahead symbol. Then, parser will take action based on the parsing table.

- 1) if  $x=y$  or  $x=Y$  then, apply shift action and increment the look ahead single.
- 2) if  $x \neq y$ , then ~~as~~ there is handle in the stack, then apply reduced action by replacing the handle by corresponding left hand side non-terminal.
- 3)  $x=y=\$$  input string is accepted
- 4) if  $x \neq y$  blank entry in parsing table then there is syntax error written into error handle.

Q1 How many shift action, reduce action and how many total action taken by parser.

$id + id * id$

$id + id * id \$$				
		↑	↓	
$id$	.	$>$	$>$	$\geq$
$+$	$<$	$>$	$<$	$>$
$*$	$<$	$>$	$>$	$>$
$id$	$<$	$<$	$<$	acc
$\$$				

Stack                  Input Stream                  Action.

$\$$                    $id + id * id$                   Shift

$\$ id$                    $id + id * id$                   Ready

$\$ E$                    $id + id$                   Shift  
Non-terminal

$\$ E +$                    $id + id * id$                   Shift

+	
$id$	E
\$	

construction of table:

Ambiguous:

+ < \*

\* = /

- < \*

↑ > \*

unambiguous grammar

1)  $a = b$

$S \rightarrow \alpha a A b \beta$

2)  $S \rightarrow \alpha a A B \Rightarrow A < b$

$A \rightarrow r b S$

3)  $a > b$

$S \rightarrow \alpha A b B$

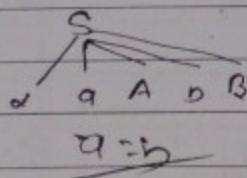
$A \rightarrow r a S$

Note:-

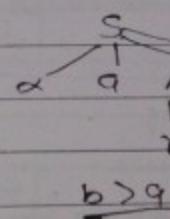
Dotter (\$) :- indicates precedence.

Parse tree

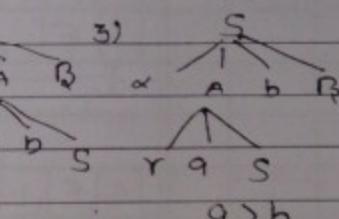
1)



2)



3)



#

If any operator grammar constraint, both left recursion or right recursion - it is ambiguous.

If operator grammars contain either left recursion or right recursion every operator present at one non-terminal only the grammar is unambiguous.

Grammar is unambiguous, parsing table is constructed based on the given grammar.

If the grammar is ambiguous, general programming language precedence rule to construct parsing table.

Q1

construct operator precedence table

$$A \rightarrow A * A / A + A / \text{id}$$

### Note

1) Identifier is always higher precedence than the other operator

2) \$ is always lower precedence.

3) Identifier, identifier up precedence available  
 $\text{[id, id]} \rightarrow \text{no}$

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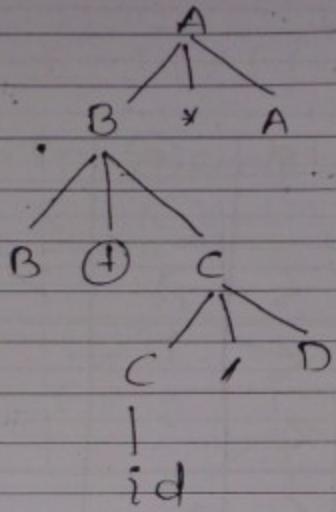
(i)  $\{ \$, \$ \}$  is accept.

id	+	*	/	\$
id	>	>	>	>
+	>	>	<	>
*	>	>	>	>
B	>	<	<	accept

(ii)

$$\begin{aligned} A &\rightarrow B * A | B \\ B &\rightarrow B + C | C \\ C &\rightarrow D | C \\ D &\rightarrow id \end{aligned}$$

id	+	*	/	\$
id	>	>	>	>
+	<	>	>	>
*	<	<	<	>
/	<	>	>	>
\$	<	<	<	accept



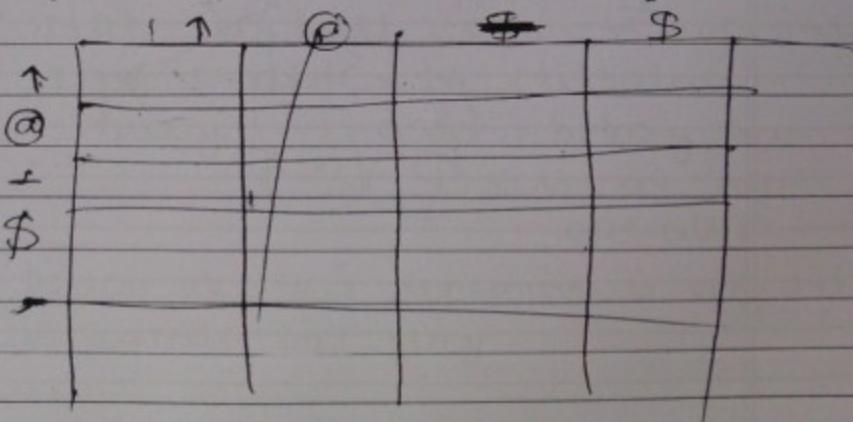
→  
# A → B ↑ T/B

B → B @ C / C

C → D \$ C / D

D → E - D / E

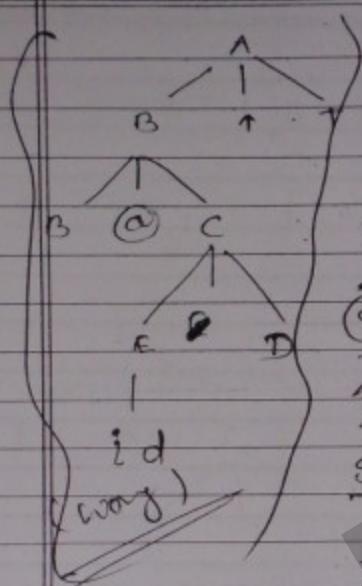
E → id



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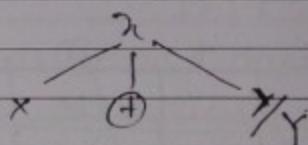
id	id	@	1	↑	8	1	\$
id	id	@	1	>	>	>	>
id	id	@	1	>	>	>	>
id	id	1	↑	<	<	<	>
id	id	1	↑	<	<	<	>
id	id	1	↑	<	<	<	>
id	id	1	↑	<	<	<	>
id	id	1	↑	<	<	<	>

o)

$$x \rightarrow x \oplus yy$$

$$y \rightarrow z^* v/z$$

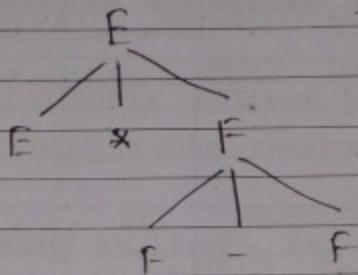
$$z \rightarrow id$$



Q1

$$E \rightarrow E * F \mid F + E \mid F$$

$$F \rightarrow F - F \mid id$$



"-" has highest precedence than + and \*

Q2

It will not work for some compilers.

### Drawback

- # NOT suitable for (-ve) operator  
was unable to distribute  
unary (-) and binary (-)
- (-3)(-4) assume NO.  
operator.

- # power of this technique is very less.  
it suitable for very

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$$E \rightarrow E+E \mid E*E \mid id$$

Note: LALR(1) parser tool, handle the ambiguous grammar by resolving the conflict in the following manner,

In case of shift-reduce conflict, priority is given to shift action over reduce action.

In case of reduce-reduce conflict, priority is given for first reduce production over other reduce production.

(c)

Consider the following grammar.

$E \rightarrow E+E$  on is the above grammar

$E \rightarrow E*E$  fed to, LALR(1) parser

$E \rightarrow id$  tool, then which one of the following is true about the action taken by the parser

1) it detect recursion and eliminate recursive

it detect reduce-reduce conflict, and resolve the conflict by reducing the first production over other production.

3) if detect shift reduce conflict and resolve the conflict, in favour of - reduce over, shift action

~~✓~~ if detect shift reduce conflict and resolve the conflict in favour of shift action over reduce action.

(Q2) assume the conflict are resolved in above manner, then what precedence and associativity rules parser realize and what is the value of the expression to be eval.

$$3 * 2 + 1$$

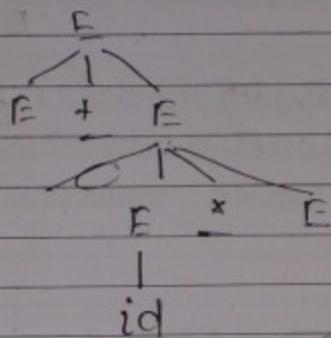
1) both + and \* are same precedence and left associative expression value is '7'

2) both + and \* are same precedence and expression value is '8' right associative '9'.

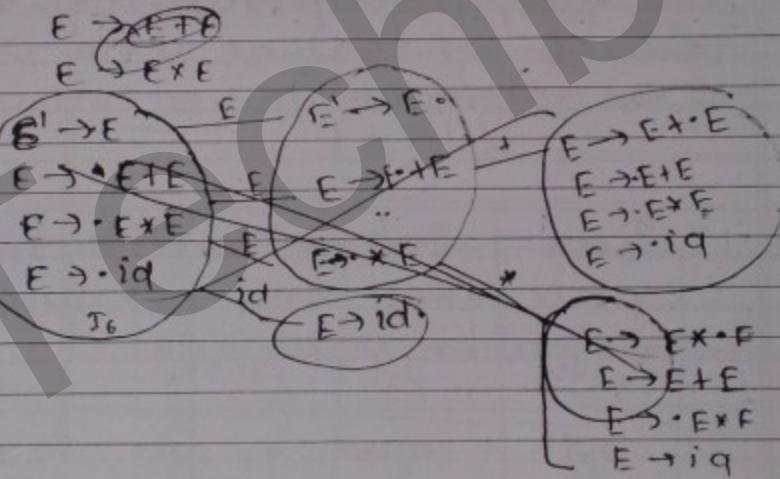
3) precedence of '\*' is higher than '+' both are left associative value is '7'.

4) +, higher precedence than '\*' and

operator are left associative expression  
value is '9'.



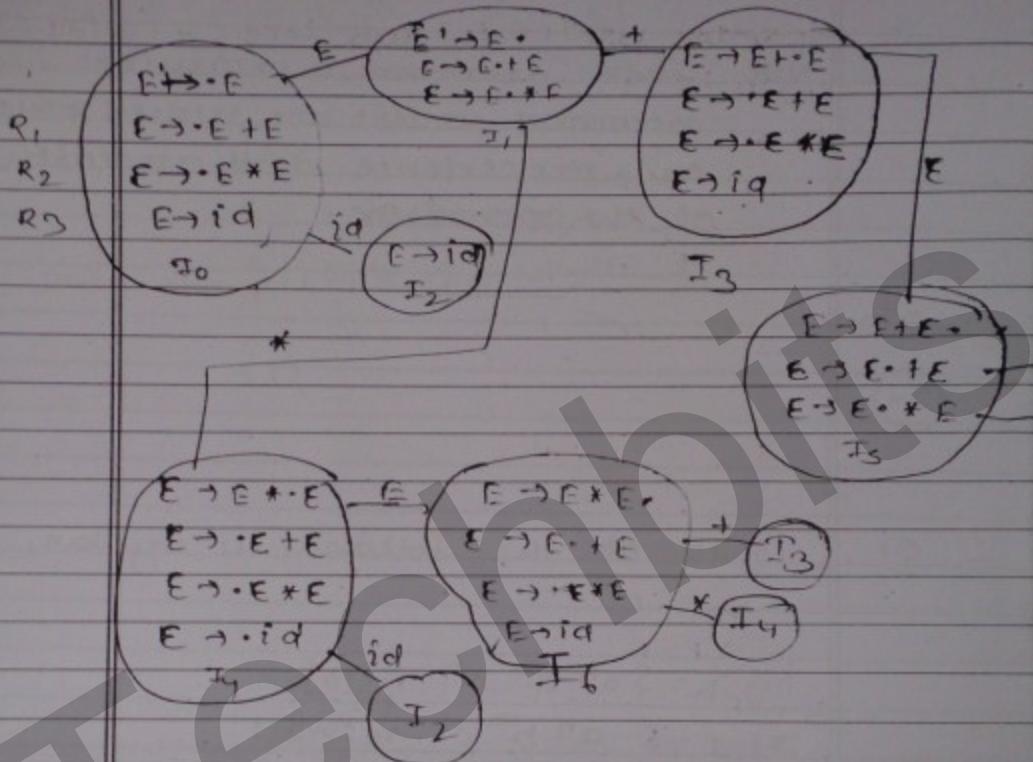
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	$id$	$+$	$*$	$$$	$E$
$I_0$	$S_2$				
$I_1$		$S_3$	$S_4$	accept	
$I_2$		$r_3$	$r_3$	$r_3$	
$I_3$	$S_2$				5
$I_4$	$S_2$	.			6
$I_5$	$r_1$	$r_1$	$r_1$	$r_1$	
$I_6$					

Note given grammar is expression grammar which are studied based on , precedence and associativity of the operators -

+ → II  
\* (I)

Q1 which of the following is regular,

- 1)  $L = \{a^n b^n c^n \mid n \leq 10\}$
- 2)  $L = \{a^n b^m c^n \mid m, n \geq 1\}$
- 3)  $L = \{a^n b^n \mid n-m=4\}$
- 4)  $L = \{a^n b^m \mid n+m \text{ is odd}\}$
- 5)  $L = \{a^n b^m \mid n \neq m\}$
- 6)  $L = \{a^n b^m \mid n|m=4\}$
- 7)  $L = \{a^{2^n} \mid n \geq 1\}$
- 8)  $L = \{a^{n^2} \mid n \geq 1\}$
- 9)  $L = \{a^k \mid k \text{ is odd no}\}$
- 10)  $L = \{a^p \mid p \text{ is even number}\}$
- 11)  $L = \{w \times w^R \mid w \in \{a, b\}^*\}$   
 $\times \in \{a, b\}^*$
- 12)  $L = \{w \times w^R \mid w \in \{a, b\}^*\}$   
 $\times \in \{a, b\}^*$

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13)  $L = \{ww^R \mid w \in \{a, b\}^*\}$

14)  $L = \{wx$

20)  $L = \{1, 2, 4, 8, \dots, 2^n, \dots\}$

all

# Every finite language are regular.

Any infinite language contain comparison b/w symbol ~~is~~ non regular

In any language symbol power not in "a.p" non regular.

```
#include <stdio.h>
```

```
# main()
```

```
{
```

```
    printf("compiler");
```

```
}
```

**preprocessor**

used for support the Macro

**compiler**

Assembly language

**Assembler**

**Linker**

[All modules] are combine

**Loader**

**preprocessor** :- preprocessor take high level  
code as input, and it evaluate all  
the macro present in the program . which  
include `#include`, `#define` in-  
c language and input statement in java  
language

**compiler** :- compiler take preprocessor  
high level language and produce  
assembly language as output.

Assembler:- Assembler take assembly language as input and produce relocatable machine code (for machine, code which can be moved in different place in memory).

# Linker:- All the different modules of program are compiled separately since to get output of our program. All different modules can be made into single module. This task is done by the linker. Hence Linker is a program, that resolve all external references required for the program to execute. which include machine code of predefined function (printf, scanf)

# loader:- Loader is a program that loads executable machine code from secondary memory into main memory.

#

```
Main() {  
    printf("Hello");  
}
```

### DIF] compile

C compiler is a translator i.e it translates one kind of language into another type of language

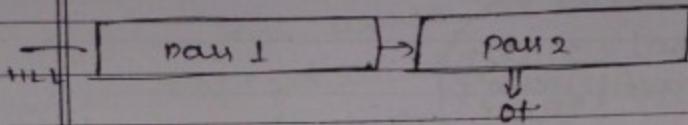
I interpreter is a language processor hence, take the language as input and execution done directly.

'C' total program is translate at a time in compiler.

line by line execution will be done in interpreter.

compiler takes less time in compilation of program. compare to interpreter.

whereas interpreter take more time, in the interpretation of language bcoz line by line execution done.



- # i) pass :- one complete scan of the given -  
high high level language called pass.
- # ii) All modern compilers are multipass compilers  
because in multipass optimization of  
program perform.
- # iii) phase :- The sub modules of each pass  
is known as phase.

# front end:- The phase of compiler which depend on source language and independent on target machine.

# Backend:- The phase of compiler depend on target machine or independent on source.

parts= code optimization , code generation

front :- lexical, syntax, semantic, intermediate

7.2)

7) b) , 8) b) 9) b) , 10) a) 12) b)

13) b) , 14) b) , 15) c) , 16) b) , 17) a)

#  $S \rightarrow aABe$

$A \rightarrow Abc/b$

$B \rightarrow d$

a A B e

$\epsilon, a, A, a, A, b, e$  a A B e

$\epsilon, a, a b c d e$  a A b c d e

$\overbrace{viable}^{\epsilon} \quad \overbrace{prefix}^{ab} \quad a b c d e$

$\overbrace{prefix}^{\epsilon, a, a b} \quad \epsilon, a, a b$

The prefix of handle left hand side in right sentential form are called as "viable prefix".

#

$S \rightarrow AB$

$S \rightarrow CA$

$B \rightarrow BC$

$B \rightarrow AB$

$A \rightarrow a$

#

### NOTE

⇒ In SLR(1), LALR shifted entries are same.

⇒ no to part is same and

Reduced entries may be different

#

the following are the semantic errors

1) Using variable, without declaration

2) Re-declaration of multiple variable

3) Scope variable rule.

4) In compatible type expression

5) Mismatch of formal actual parameter.

6) Type mismatch in formal and actual parameter.

Context Sensitive grammar

↳ Attribute grammar will used.

CFG + {Semantic rule}

used to handle the semantic analyzer.

Syntax directed translation is formalization in which each grammar production is associated with set of semantic rules.

### H functionality of (SDT)

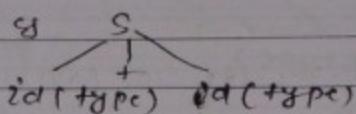
- 1) It identifies all semantic errors and error messages to error handlers
- 2) It helps ~~the construction~~ in construction of intermediate table
- 3) Symbol table construction

#### 4) Construction of syntax ~~state~~ tree.

### Designing SDT

- 1) construct parse tree
- 2) construct annotated parse tree
- 3) compute attribute values in annotated parse tree
- 4) ~~compute annotated value~~ tree.
  - 1) The generalize rules of attribute computation attached to grammar production which known as semantic rule.

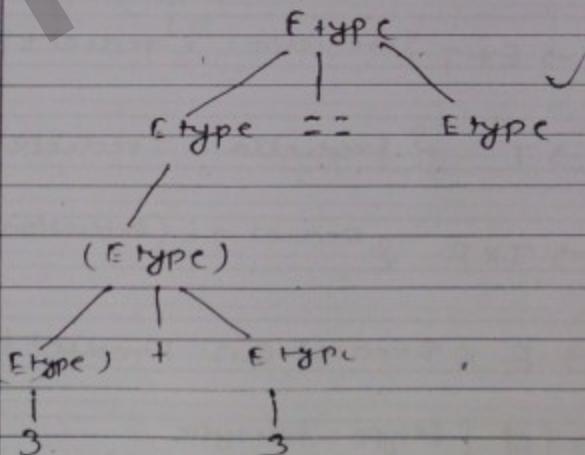
# Annotated parse tree:- Decorate parse tree.



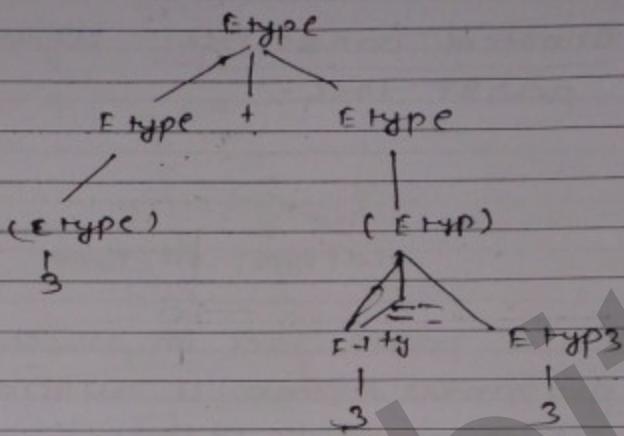
⇒ It is a parse tree in which each grammar symbol is associated with set of attribute values.

$E \rightarrow E + E$	$[ib(E_1 \cdot \text{TYPE} = E_2 \cdot \text{TYPE}) \& B(E_1 \cdot \text{TYPE} = \text{int})]$ + TYPE = int else others
$E \rightarrow X(E)$	$[E \cdot \text{TYPE} = E_1 \cdot \text{TYPE}]$
$E \rightarrow E == E$	$[ib(E \cdot \text{TYPE} = E_2 \cdot \text{TYPE}) \& B(E \cdot \text{TYPE} = \text{int/boden})]$ == TYPE = both
$E \rightarrow \text{NUM}$	$[E \cdot \text{TYPE} = \text{num type}]$
$E \rightarrow \text{true}$	$[E \cdot \text{TYPE} = \text{boolean}]$
$E \rightarrow \text{false}$	$[E \cdot \text{TYPE} = \text{boolean}]$

#  $(3 + 3) == 6$



Q1

 $3 + (3 \cdot 3) \quad K$ 

H

construct the SDT that would give total no. of reduction take by bottom up parser, in construction of parse tree.

red is attribute and  $E \cdot \text{red} = \text{total no. of reduction take by the parser}$ . To construct SDT by follow grammar.

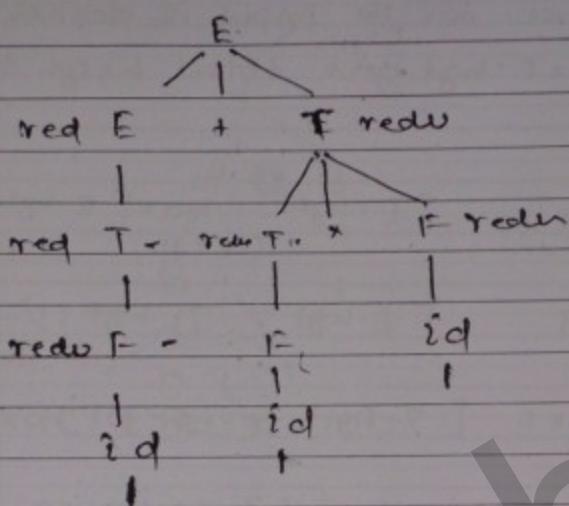
$$E \rightarrow E + T \quad \{ \text{Reduction: } E \cdot \text{reduct} + T \cdot \text{reduct} + 1 \}$$

$$E \rightarrow T \quad \{ \text{Reduction: } T \cdot \text{reduction} + 1 \}$$

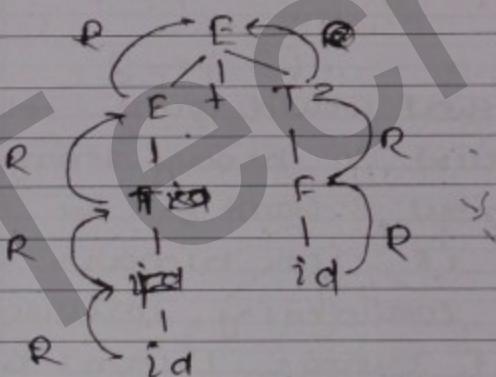
$$T \rightarrow T * F \quad \{ \text{Reduct } T = (\text{reduction } T + \text{reduction } F) + 1 \}$$

$$T \rightarrow F \quad \{ \text{Reduction: } F \cdot \text{reduct} + 1 \}$$

$$F \rightarrow id \quad [ \begin{array}{l} \text{E-type} = id \cdot \text{type} \\ - F \cdot \text{reduction} = 1 \end{array} ]$$



#1 Reduct to  $a + b$



H) construct SDT that would calculate height of parse tree. for the input is derive where S.Hgt, E.hgt give total height of parse tree

$$E \rightarrow F + T \quad [E.hgt = \max[E.hgt, T.hgt] + 1]$$

$$F \rightarrow T \quad [E.hgt = T.hgt + 1]$$

$$T \rightarrow T \times F \quad [T.hgt = \max[T.hgt, E.hgt] + 1]$$

$$T \rightarrow F \quad [T.hgt = F.hgt + 1]$$

$$F \rightarrow id \quad [F.hgt = 1]$$

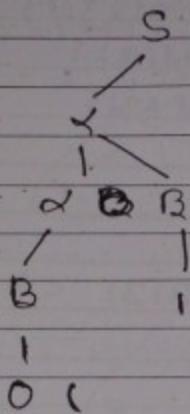
O) construct that would count, total no. of 1's present in binary string. where count is attribute S.count give the total no. of 1's. construct S-dfa to count 1's in binary string by considering following grammar

$$\alpha \rightarrow \alpha B \quad [L.count = L.count + B.count]$$

$$\alpha \rightarrow B \quad [L.count = B.count + 1]$$

$$B \rightarrow 1 \quad [B.count = 1]$$

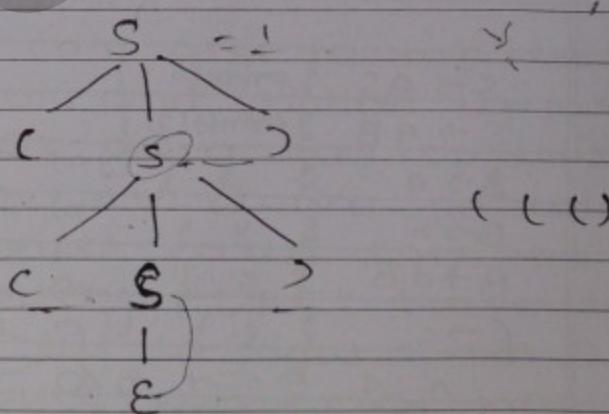
$$B \rightarrow 0 \quad [B.count = 0]$$



- Q1) Construct SDT that would give total no. of balanced parentheses possible in input string

$S \rightarrow (S)$  :  $S\text{-count} = S\text{-count} + 1$

$S \rightarrow \epsilon$  :  $S\text{-count} = 0$



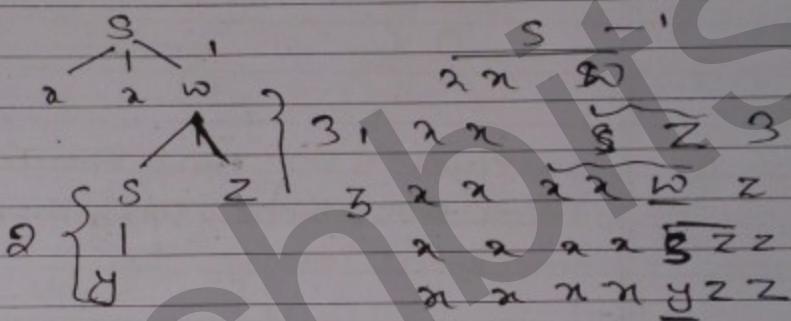
# S → now 5 points (11)

$S \rightarrow Y \in \text{pmnf}(\mathbb{Z})$

$w \rightarrow sz$  & printf(3) \$

max yzz

- 9) 12313 ✓ 23131 c) 13112 d) none



(1)  $S \rightarrow AS \quad \$ \text{ print}(.) \}$

$S \rightarrow AB$  8 points(2)}

A → 9 2 3 ? 9) 666 453211

b) 33364521

B → dβ    861    c) 333 (4125)

6-Sub 2,3, d) now

C → C      ?      J

A A A d b a a g d b c

$$\underline{a \ A \ a} \quad d \ b \ c = 3$$

$$A \neq a \neq d \neq b \neq c = 3$$

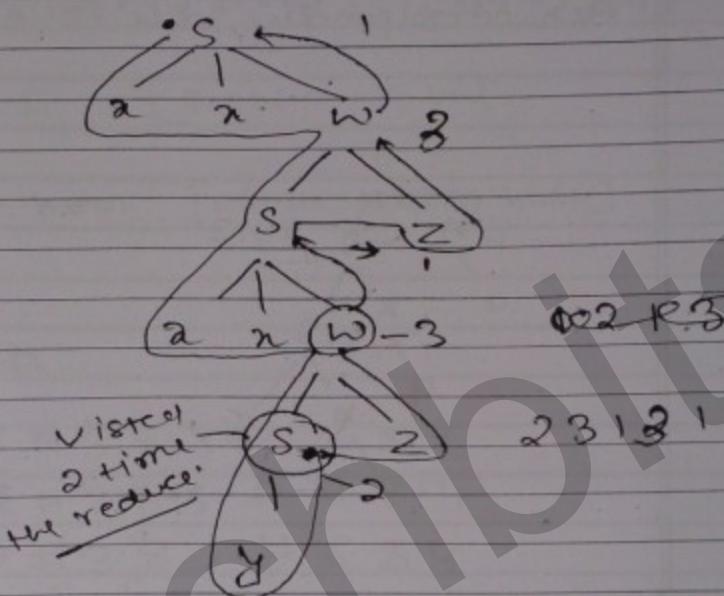
q q q d h c

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top down pars ( leftmost )



parse tree creat-

NOTE  
SDT can give to top down parser and bottom up parser  
if SDT given to top down parser, top down parser  
construct parse tree by -  
traversing "DFS" traversal  
from left to right - In DFS  
traversal when ever node is  
visited two time correspondingly  
rule is executed .

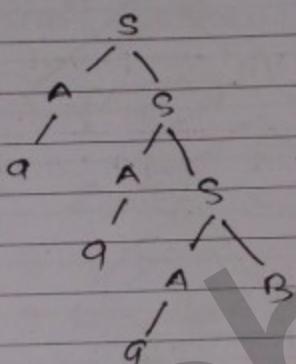
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If SDT is given to bottom up parser,  
then even reduced action it ~~the~~ happy  
then corresponding rule is executed.



Q)  $E \rightarrow E, \# T \quad \{E\text{-val} = E_1\text{-val} + T\text{-val}\}$

$E \rightarrow T \quad \{E\text{-val} = T\text{-val}\}$

$T \rightarrow T_1, 8 F \quad \{T\text{-val} = T_1\text{-val} * F\text{-val}\}$

2  $T \rightarrow F \quad \{T\text{-val} = F\text{-val}\}$

2  $F \rightarrow \text{num} \quad \{F\text{-val} = \text{num}'\text{-val}\}$

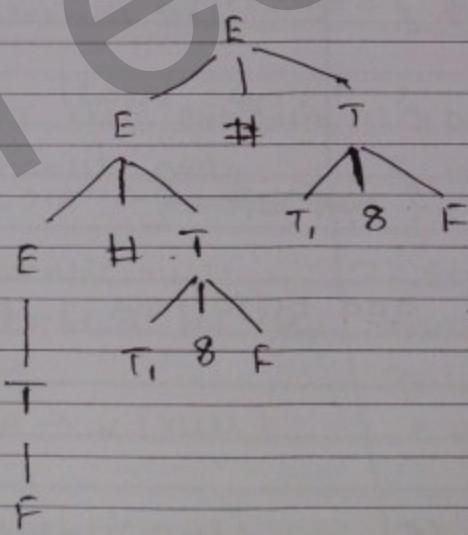
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~~T # 3 8 S # 6 8 4~~

~~E # 3 8 S # 6 8 4~~

~~2 # 3 8 S # 6 8 4~~

2



- # Synthesized attribute :- The attribute value at a node is computed in terms of its children in the annotated parse tree such type of attribute known as synthesized attribute  
(well suitable for = bottom up)
- # Inherited attribute :- The attribute value at a node in the annotated parse tree is computed either from parent, or from the left sibling. It is known as inherited attribute  
(suitable = parent down)

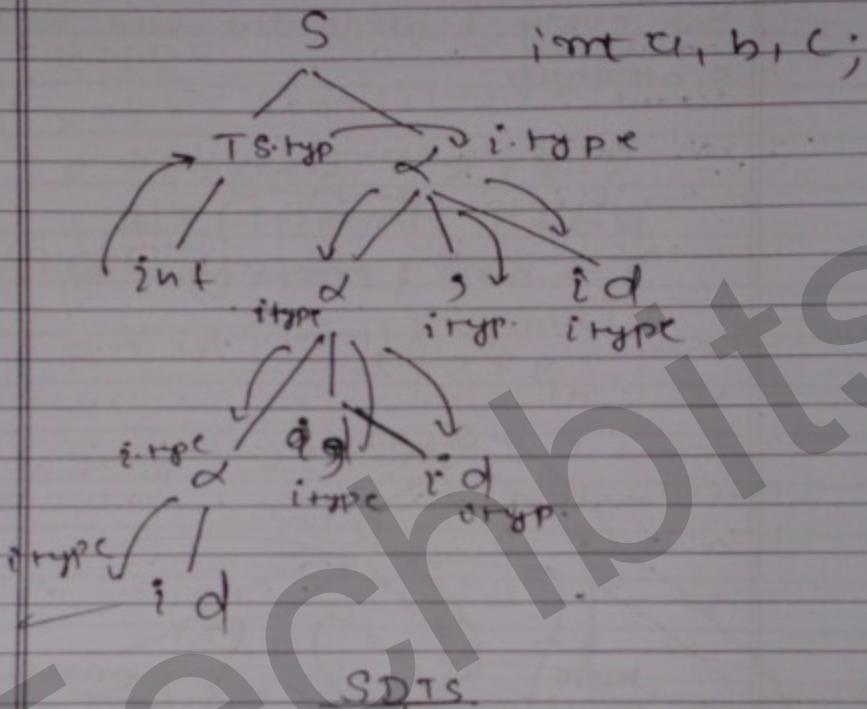
$S \rightarrow T \& S \& i\text{type} = T \cdot \text{stype}$

 $T \rightarrow \text{int} \& \{ \xrightarrow{\text{stype}=\text{int}} \}$ 

$T \rightarrow \text{float} \& \{ \text{stype} = \text{float} \}$

$\& \rightarrow \text{id} \& \{ \text{stype} = \{ \text{id}, \text{int}, \text{float} \}, \text{i.e. } i\text{type} = \{ \text{id}, \text{int}, \text{float} \}$

$\& \rightarrow \text{id} \& \{ \text{add_ty(id, name, L, idtype)}$



Q1

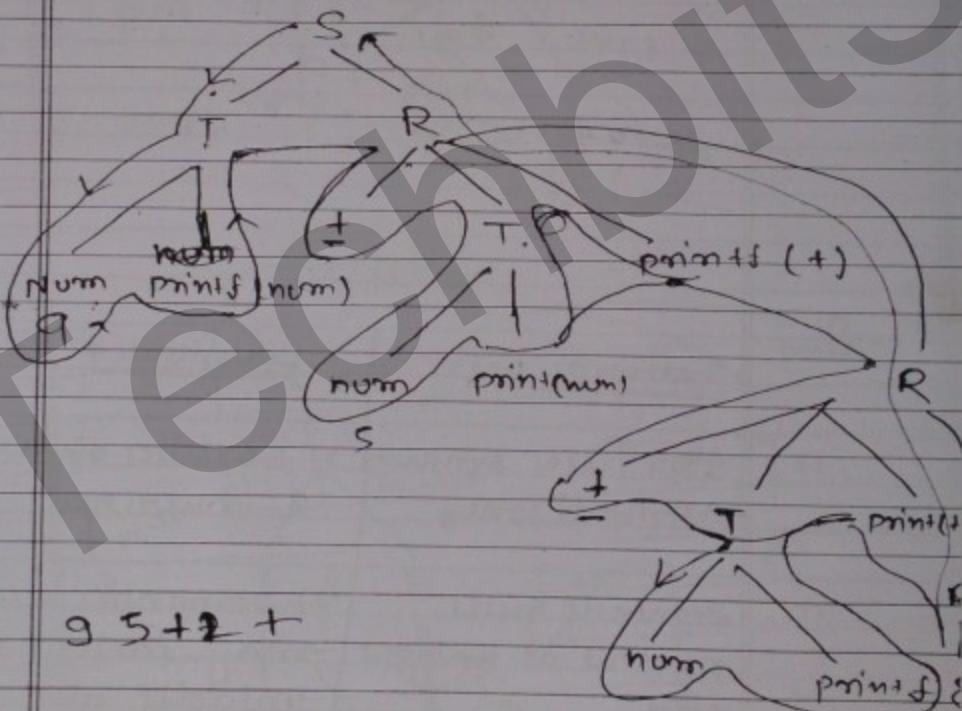
S-attribute DefL-attribute

- |  |   |
|--|---|
| 1) SDT will synthesize attributes only   | 2) SDT will synthesize attributes inherited.  |
| 2) Semantic rules present at the right end<br>$A \rightarrow \alpha \{ \text{rule} \}$ | 2) Semantic rules may present in the middle also.<br>$A \Rightarrow \alpha \{ \text{rule} \} B$ |
| 3) Semantic rules evaluate in bottom-up manner   | 3) Rules are evaluated in DFS.  |

Q1

Every S-attributed def is L-attributed def  
 but every L-attributed need not to be  
 S attribute.

 $S \rightarrow TR$  L-attributed.

 $R \rightarrow + T \{ \text{print}(+) \} R/E$ 
 $T \rightarrow \text{num} \{ \text{printf(num value)} \}$ 
 $9 + 5 + 2$ 


Consider the following SMT

$$S \rightarrow E R$$

$$R \rightarrow * E \{ \text{print}(*\}) \quad R | E$$

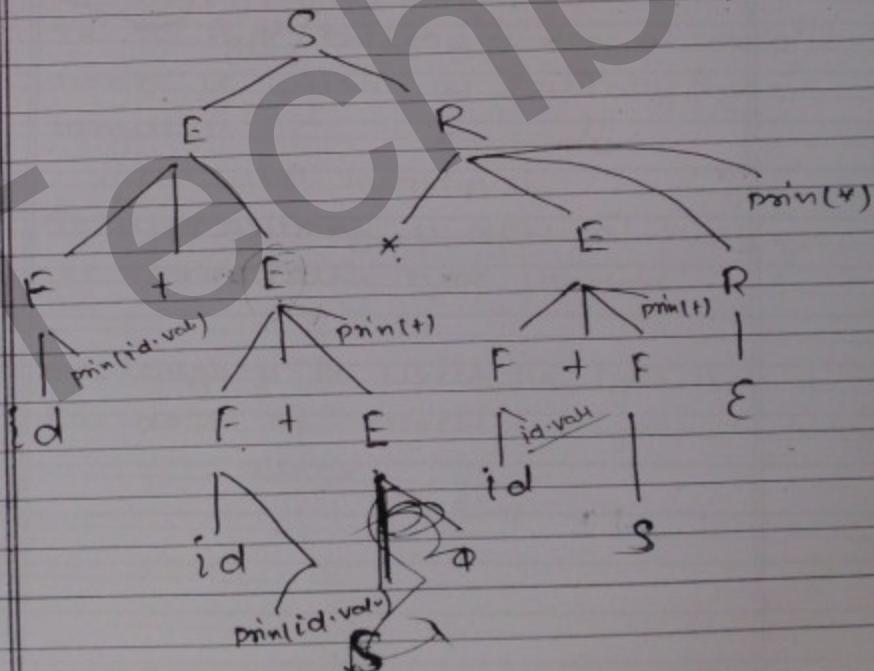
$$E \rightarrow F + E \{ \text{print}(+)\}$$

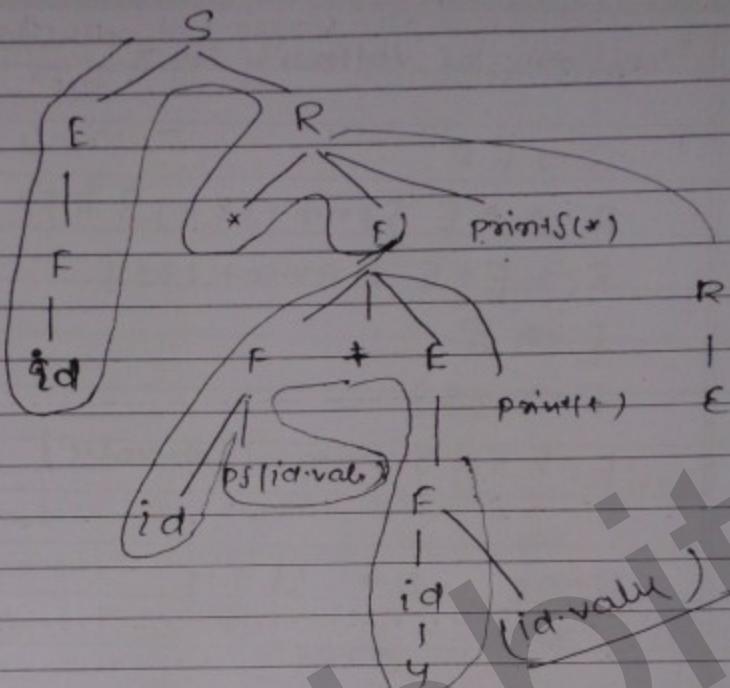
$$E \rightarrow F$$

$$E \rightarrow (S)$$

$$F \rightarrow \text{id} \{ \text{print}(\text{id.value}) \}$$

String 2 \* 3 + 4





# construct the SFD that perform type conversion by consider type conversion done in integer and real value.

$E \rightarrow ETT$

$E \rightarrow T$

# Statically type checking will done at compile time and runtime.

eg C language

# In the type checking is done at compile time ie known as statically type language.

eg LISP language

# Type checking is done at runtime, ie dynamically type language.

# The language in which no type checking will done. eg = Machine language, Assembly language