```
In [5]: #q1
        import numpy as np
        from collections import Counter
        class DecisionTree:
             def fit(self, X, y):
                 self.tree = self.fitter(X, y)
            def fitter(self, X, y):
                 samples, features = X.shape
                 labels = len(np.unique(y))
                 max_split = None
                 max_gain = 0
                 for feature in range(features):
                     for threshold in np.unique(X[:, feature]):
                         left = y[X[:, feature] < threshold]</pre>
                         right = y[X[:, feature] >= threshold]
                         if len(left) > 0 and len(right) > 0:
                             gain = self.infogain(y,left, right)
                             if gain > max_gain:
                                 max split = (feature, threshold)
                                 max gain = gain
                 if max gain == 0:
                     return Counter(y).most_common(1)[0][0]
                 feature, threshold = max split
                 left = X[:, feature] < threshold</pre>
                 right = ~left
                 l_tree = self.fitter(X[left], y[left])
                 r tree = self.fitter(X[right], y[right])
                 return (feature, threshold, 1 tree, r tree)
            def entropy(self, y):
                 _, l = np.unique(y, return_counts=True)
                 prob = 1 / len(y)
                 entropy = -np.sum(prob * np.log2(prob))
                 return entropy
            def infogain(self, y, left, right):
                 p = len(left) / len(y)
                 q = len(right) / len(y)
                 gain = self.entropy(y) - (p * self.entropy(left) + q * self.entropy(
                 return gain
            def predict(self, X):
                 return [self.predictor(x, self.tree) for x in X]
             def predictor(self, x, tree):
                 if isinstance(tree, int) or isinstance(tree, float) or isinstance(tr
                     return tree
                 feature= tree[0]
                 threshold= tree[1]
                 left= tree[2]
                 right = tree[3]
                 if x[feature] < threshold:</pre>
                     return self.predictor(x, left)
                 else:
                     return self.predictor(x, right)
        xtrain = np.array([[1, 2], [2, 3], [3, 4], [4, 5]])
        ytrain = np.array([0, 0, 1, 1])
```

```
tree = DecisionTree()
                        tree.fit(xtrain, ytrain)
                        X_{\text{test}} = \text{np.array}([[4, 3], [1, 2]])
                        predictions = tree.predict(X_test)
                        print("Array of prediction is")
                       print(predictions)
                       Array of prediction is
                       [1, 0]
In [7]: #2.3
                        import numpy as np
                        from collections import Counter
                        data = np.loadtxt("Druns.txt")
                        X = data[:, :-1]
                        y = data[:, -1]
                        def entropy(y):
                                   _, n = np.unique(y, return_counts=True)
                                   prob = n / len(y)
                                   return -np.sum(prob * np.log2(prob + 1e-10))
                        H = entropy(y)
                        cuts = []
                        ig ratios = []
                        for feature_i in range(X.shape[1]):
                                    feature_values = X[:, feature_i]
                                   unique_values = np.unique(feature_values)
                                    for threshold in unique values:
                                               1 = np.where(feature_values < threshold)</pre>
                                               r = np.where(feature_values >= threshold)
                                               H_{eff} = entropy(y[1])
                                               H_right = entropy(y[r])
                                               Infogain = H - (len(1[0]) / len(y) * H_left + len(r[0]) / len(y) / len
                                               Ig ratio = Infogain / (entropy(feature values)+ 1e-10)
                                               cuts.append((feature_i, threshold))
                                               ig_ratios.append(Ig_ratio)
                                               print(f"Cut: Feature {feature_i}, Threshold {threshold}")
                                               print(f"Information Gain: {Infogain}")
                                               print(f"Information Gain Ratio: {Info_gain_ratio}")
                                               print("\n")
```

Cut: Feature 0, Threshold 0.0 Information Gain: 0.0 Information Gain Ratio: 0.05464847681701849

Cut: Feature 0, Threshold 0.1
Information Gain: 0.04417739185414593
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold -2.0 Information Gain: 0.0 Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold -1.0
Information Gain: 0.04417739185414593
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 0.0
Information Gain: 0.03827452220629268
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 1.0
Information Gain: 0.004886164091842837
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 2.0
Information Gain: 0.0010821659130776373
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 3.0
Information Gain: 0.016313165825732168
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 4.0
Information Gain: 0.04945207278939401
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 5.0
Information Gain: 0.10519553207004628
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 6.0
Information Gain: 0.19958702318968757
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 7.0
Information Gain: 0.03827452220629268
Information Gain Ratio: 0.05464847681701849

Cut: Feature 1, Threshold 8.0
Information Gain: 0.18905266852990077
Information Gain Ratio: 0.05464847681701849

```
In [8]: #2.4
        import numpy as np
        from collections import Counter
        data = np.loadtxt("D3Leaves.txt")
        # Extract features and labels
        X = data[:, :-1] # Features
        y = data[:, -1]  # Labels
        class DecisionTree:
            def fit(self, X, y):
                 self.tree = self.fitter(X, y)
            def fitter(self, X, y):
                 samples, features = X.shape
                 labels = len(np.unique(y))
                max split = None
                max gain = 0
                 for feature in range(features):
                     for threshold in np.unique(X[:, feature]):
                         left = y[X[:, feature] < threshold]</pre>
                         right = y[X[:, feature] >= threshold]
                         if len(left) > 0 and len(right) > 0:
                             gain = self.infogain(y,left, right)
                             if gain > max_gain:
                                 max split = (feature, threshold)
                                 max gain = gain
                 if max gain == 0:
                     return Counter(y).most common(1)[0][0]
                 feature, threshold = max split
                 left = X[:, feature] < threshold</pre>
                right = -left
                l_tree = self.fitter(X[left], y[left])
                r tree = self.fitter(X[right], y[right])
                return (feature, threshold, l_tree, r_tree)
            def entropy(self, y):
                 _, l = np.unique(y, return_counts=True)
                 prob = 1 / len(y)
                 entropy = -np.sum(prob * np.log2(prob))
                return entropy
            def infogain(self, y, left, right):
                 p = len(left) / len(y)
                 q = len(right) / len(y)
                 gain = self.entropy(y) - (p * self.entropy(left) + q * self.entropy(
                 return gain
            def predict(self, X):
                 return [self.predictor(x, self.tree) for x in X]
            def predictor(self, x, tree):
                 if isinstance(tree, int) or isinstance(tree, float) or isinstance(tr
                     return tree
                 feature= tree[0]
                 threshold= tree[1]
                 left= tree[2]
```

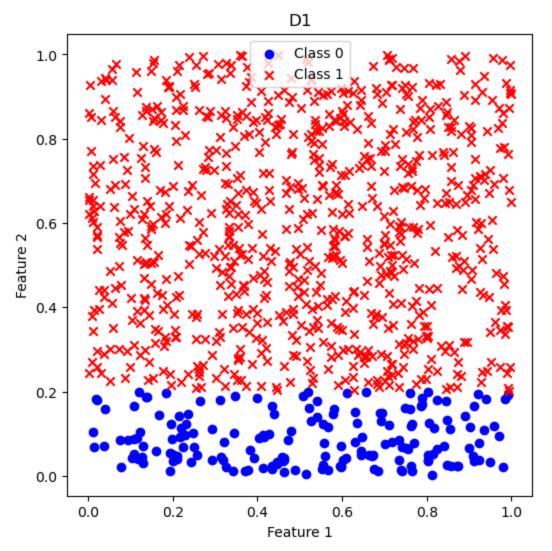
```
right = tree[3]
                  if x[feature] < threshold:</pre>
                      return self.predictor(x, left)
                  else:
                      return self.predictor(x, right)
          xtrain = X
         ytrain = y
         tree = DecisionTree()
         tree.fit(xtrain, ytrain)
         X_{\text{test}} = \text{np.array}([[4, 3], [1, 2]])
         predictions = tree.predict(X test)
         print("Array of prediction is")
         print(predictions)
         #The tree will have following set of logic rules:
          # If Feature 1 <= 5.5 and Feature 2 <= 2 then class 0
          # If Feature 1 <= 5.5 and Feature 2 > 2 then class 1
          # If Feature 1 > 5.5 then class 1
         Array of prediction is
         [1.0, 0.0]
In [25]: #2.5
         import numpy as np
         from collections import Counter
         data = np.loadtxt("D1.txt")
         X = data[:, :-1]
          y = data[:, -1]
          class DecisionTree:
              def fit(self, X, y):
                  self.tree = self.fitter(X, y)
              def fitter(self, X, y):
                  samples, features = X.shape
                  labels = len(np.unique(y))
                  max_split = None
                  max_gain = 0
                  for feature in range(features):
                      for threshold in np.unique(X[:, feature]):
                          left = y[X[:, feature] < threshold]</pre>
                          right = y[X[:, feature] >= threshold]
                          if len(left) > 0 and len(right) > 0:
                               gain = self.infogain(y,left, right)
                               if gain > max gain:
                                  max_split = (feature, threshold)
                                  max_gain = gain
                  if max_gain == 0:
                      return Counter(y).most_common(1)[0][0]
                  feature, threshold = max_split
                  left = X[:, feature] < threshold</pre>
                  right = ~left
                  l_tree = self.fitter(X[left], y[left])
                  r_tree = self.fitter(X[right], y[right])
                  return (feature, threshold, l_tree, r_tree)
              def entropy(self, y):
                  _, l = np.unique(y, return_counts=True)
                  prob = 1 / len(y)
```

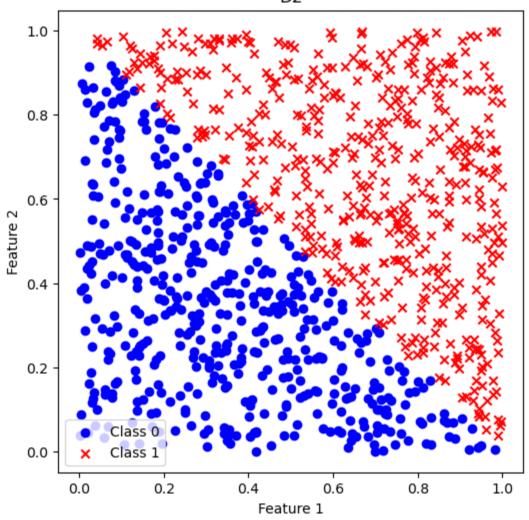
```
entropy = -np.sum(prob * np.log2(prob))
        return entropy
    def infogain(self, y, left, right):
        p = len(left) / len(y)
        q = len(right) / len(y)
        gain = self.entropy(y) - (p * self.entropy(left) + q * self.entropy(
        return gain
    def predict(self, X):
        return [self.predictor(x, self.tree) for x in X]
    def predictor(self, x, tree):
        if isinstance(tree, int) or isinstance(tree, float) or isinstance(tr
            return tree
        feature= tree[0]
        threshold= tree[1]
        left= tree[2]
        right = tree[3]
        if x[feature] < threshold:</pre>
            return self.predictor(x, left)
        else:
            return self.predictor(x, right)
    def print_tree(self, node,features=None,classes=None, space=""):
        if isinstance(node, int) or isinstance(node, float):
            classname = classes[node] if classes else node
            print(space + "Predict", classes)
            return
        if features is None:
            feature = f"Feature {node[0]}"
            feature = features[node[0]]
        print(space + f"[{feature} < {node[1]}]")</pre>
        print(space + '--> True:')
        self.print_tree(node[2], features,classes, space+ " ")
        print(space + '--> False:')
        self.print_tree(node[3], features,classes, space+ " ")
X train = X
y train = y
tree = DecisionTree()
tree.fit(X train, y train)
feature_names=["Feature 1", "Feature 2"]
print("Tree for D!")
tree.print_tree(tree.tree, feature_names)
data = np.loadtxt("D2.txt")
X = data[:, :-1]
y = data[:, -1]
X_{train} = X
y_train = y
print("\n\n")
tree = DecisionTree()
tree.fit(X_train, y_train)
feature_names=["Feature 1", "Feature 2"]
print("Tree for D2")
tree.print_tree(tree.tree, feature_names)
```

```
Tree for D!
[Feature 2 < 0.201829]
--> True:
 Predict None
--> False:
 Predict None
Tree for D2
[Feature 1 < 0.533076]
--> True:
 [Feature 2 < 0.639018]
  --> True:
    [Feature 2 < 0.534979]
    --> True:
      Predict None
    --> False:
     [Feature 1 < 0.409972]
      --> True:
       Predict None
      --> False:
        [Feature 1 < 0.426073]
        --> True:
         [Feature 1 < 0.417579]
          --> True:
           Predict None
          --> False:
           Predict None
        --> False:
          Predict None
  --> False:
    [Feature 1 < 0.111076]
    --> True:
     [Feature 2 < 0.964767]
      --> True:
       Predict None
      --> False:
       Predict None
    --> False:
      [Feature 2 < 0.861]
      --> True:
        [Feature 1 < 0.33046]
        --> True:
          [Feature 2 < 0.745406]
          --> True:
           Predict None
          --> False:
            [Feature 1 < 0.254049]
            --> True:
              [Feature 1 < 0.191915]
              --> True:
                Predict None
              --> False:
                [Feature 2 < 0.792752]
                --> True:
                 Predict None
                --> False:
                  Predict None
            --> False:
              Predict None
        --> False:
          Predict None
      --> False:
```

```
Predict None
         --> False:
           [Feature 2 < 0.383738]
           --> True:
             [Feature 1 < 0.761423]
             --> True:
               [Feature 2 < 0.301105]
               --> True:
                Predict None
               --> False:
                 [Feature 1 < 0.66337]
                 --> True:
                   Predict None
                 --> False:
                   Predict None
             --> False:
               [Feature 2 < 0.191206]
               --> True:
                 [Feature 1 < 0.90482]
                 --> True:
                   [Feature 2 < 0.169053]
                   --> True:
                     Predict None
                   --> False:
                     [Feature 1 < 0.850316]
                     --> True:
                       Predict None
                     --> False:
                       Predict None
                 --> False:
                   [Feature 2 < 0.037708]
                   --> True:
                     Predict None
                   --> False:
                     [Feature 1 < 0.930371]
                     --> True:
                       [Feature 1 < 0.927522]
                       --> True:
                        Predict None
                       --> False:
                         Predict None
                      --> False:
                       Predict None
               --> False:
                 Predict None
           --> False:
             [Feature 1 < 0.550364]
             --> True:
               [Feature 2 < 0.474971]
               --> True:
                Predict None
               --> False:
                 Predict None
             --> False:
               Predict None
In [35]: #2.6
         import numpy as np
         import matplotlib.pyplot as plt
         d1 = np.loadtxt("D1.txt")
         d2 = np.loadtxt("D2.txt")
         X_d1, y_d1 = d1[:, :-1], d1[:, -1]
```

```
X_d2, y_d2 = d2[:, :-1], d2[:, -1]
plt.figure(figsize=(6, 6))
plt.scatter(X_d1[y_d1 == 0, 0], X_d1[y_d1 == 0, 1], label="Class 0", c="blue"
plt.scatter(X_d1[y_d1 == 1, 0], X_d1[y_d1 == 1, 1], label="Class 1", c="red"
plt.title("D1")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.show()
plt.figure(figsize=(6, 6))
plt.scatter(X_d2[y_d2 == 0, 0], X_d2[y_d2 == 0, 1], label="Class 0", c="blue"
plt.scatter(X_d2[y_d2 == 1, 0], X_d2[y_d2 == 1, 1], label="Class 1", c="red"
plt.title("D2")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.show()
#The decision tree is complex for D2 than D1 because there is a easy split t
#straight line with slope=0, which can easily represent something above Feat
#But if we look at D2 the line has some slope, at every Feature 2 there is \epsilon
#tree to become complex.
```



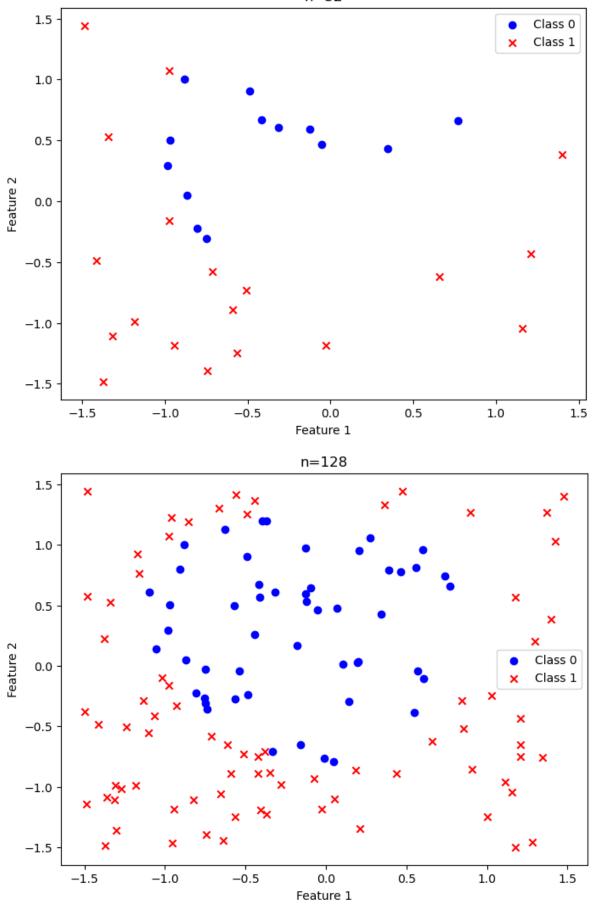


```
In [104...
         #2.7
          import numpy as np
          from collections import Counter
          data = np.loadtxt("Dbig.txt")
          np.random.seed(7)
          np.random.shuffle(data)
          train_size = 8192
          train set = data[:train size]
          test_set = data[train_size:]
          class DecisionTree:
              def fit(self, X, y):
                  self.tree = self.fitter(X, y)
              def fitter(self, X, y):
                  samples, features = X.shape
                  labels = len(np.unique(y))
                  max_split = None
                  max_gain = 0
                  for feature in range(features):
                      for threshold in np.unique(X[:, feature]):
                          left = y[X[:, feature] < threshold]</pre>
                          right = y[X[:, feature] >= threshold]
                          if len(left) > 0 and len(right) > 0:
                              gain = self.infogain(y,left, right)
                              if gain > max_gain:
```

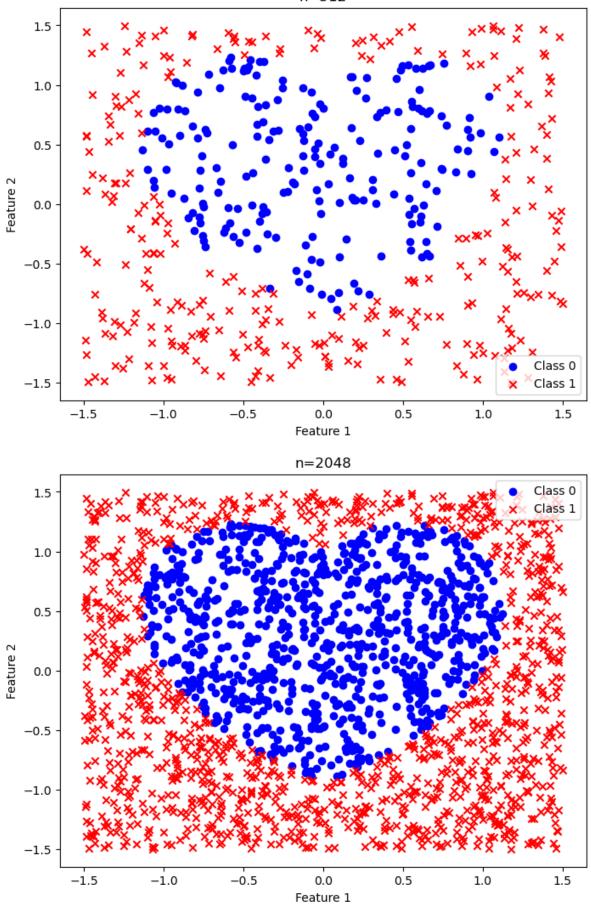
```
max_split = (feature, threshold)
                        max_gain = gain
        if max_gain == 0:
            return Counter(y).most common(1)[0][0]
        feature, threshold = max split
        left = X[:, feature] < threshold</pre>
        right = ~left
        l_tree = self.fitter(X[left], y[left])
        r_tree = self.fitter(X[right], y[right])
        return (feature, threshold, l_tree, r_tree)
    def entropy(self, y):
        _, l = np.unique(y, return_counts=True)
        prob = 1 / len(y)
        entropy = -np.sum(prob * np.log2(prob))
        return entropy
    def infogain(self, y, left, right):
        p = len(left) / len(y)
        q = len(right) / len(y)
        gain = self.entropy(y) - (p * self.entropy(left) + q * self.entropy(
        return gain
    def predict(self, X):
        return [self.predictor(x, self.tree) for x in X]
    def predictor(self, x, tree):
        if isinstance(tree, int) or isinstance(tree, float) or isinstance(tr
            return tree
        feature= tree[0]
        threshold= tree[1]
        left= tree[2]
        right = tree[3]
        if x[feature] < threshold:</pre>
            return self.predictor(x, left)
        else:
            return self.predictor(x, right)
    def print_tree(self, node,features=None,classes=None, space=""):
        if isinstance(node, int) or isinstance(node, float):
            classname = classes[node] if classes else node
            print(space + "Predict", classes)
            return
        if features is None:
            feature = f"Feature {node[0]}"
        else:
            feature = features[node[0]]
        print(space + f"[{feature} < {node[1]}]")</pre>
        print(space + '--> True:')
        self.print_tree(node[2], features,classes, space+ " ")
        print(space + '--> False:')
        self.print_tree(node[3], features,classes, space+ "
    def node_count(self, node):
        if isinstance(node, int) or isinstance(node, float):
            return 1 # Leaf node
        else:
            feature, _{-}, _{1}, _{r} = node
            left_count = self.node_count(1)
            right_count = self.node_count(r)
            return 1 + left_count + right_count
n_values = [32, 128, 512, 2048, 8192]
num_nodes = []
```

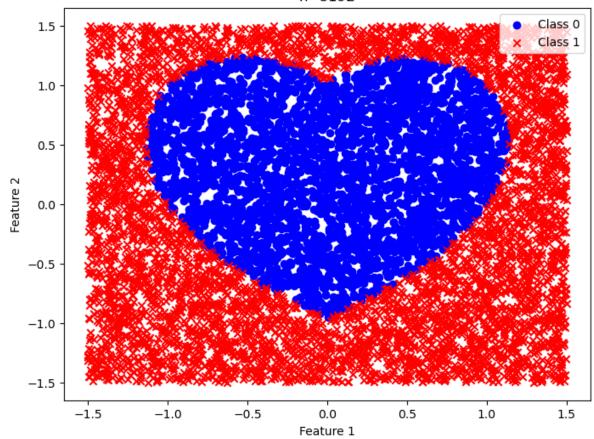
```
test_errors = []
def accuracy_score(y_true, y_pred):
    correct_predictions = 0
    total_samples = len(y_true)
    for true_label, predicted_label in zip(y_true, y_pred):
        if true_label == predicted_label:
            correct_predictions += 1
    accuracy = correct_predictions / total_samples
    return accuracy
for n in n_values:
    train_data = train_set[:n]
    X_train, y_train = train_data[:, :-1], train_data[:, -1]
    tree = DecisionTree()
    tree.fit(X_train, y_train)
    num nodes.append(tree.node count(tree.tree))
    y_pred = tree.predict(test_set[:, :-1])
    test error = 1 - accuracy score(test set[:, -1], y pred)
    test_errors.append(test_error)
    X_d1, y_d1 = train_data[:, :-1], train_data[:, -1]
    plt.figure(figsize=(8, 6))
    plt.scatter(X_d1[y_d1 == 0, 0], X_d1[y_d1 == 0, 1], label="Class 0", c="
    plt.scatter(X d1[y d1 == 1, 0], X d1[y d1 == 1, 1], label="Class 1", c="
    plt.title("n="+str(n))
    plt.xlabel("Feature 1")
    plt.ylabel("Feature 2")
    plt.legend()
    plt.show()
for i in range(len(n values)):
    print(f"n = {n values[i]}, Nodes = {num nodes[i]}, Test Error = {test er
plt.figure(figsize=(10, 5))
plt.plot(num_nodes, test_errors, marker='o')
plt.title("Learning Curve")
plt.xlabel("Nodes")
plt.ylabel("Test Error")
plt.show()
```



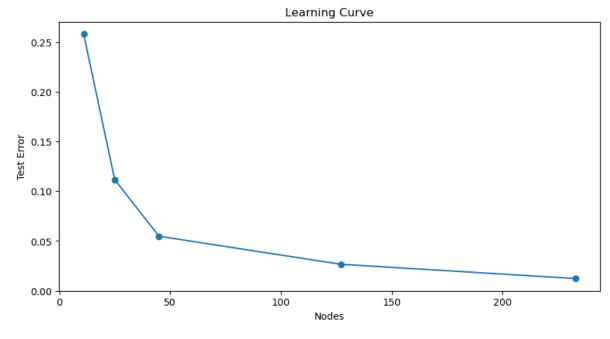








```
n = 32, Nodes = 11, Test Error = 0.2583
n = 128, Nodes = 25, Test Error = 0.1117
n = 512, Nodes = 45, Test Error = 0.0548
n = 2048, Nodes = 127, Test Error = 0.0265
n = 8192, Nodes = 233, Test Error = 0.0122
```



```
import numpy as np
import matplotlib.pyplot as plt
from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy_score

data = np.loadtxt("Dbig.txt")

np.random.seed(7)
```

```
np.random.shuffle(data)
n_nodes = []
t errors = []
n_values = [32, 128, 512, 2048, 8192]
for n in n_values:
    train_data = data[:n]
    X_train, y_train = train_data[:, :-1], train_data[:, -1]
    tree = DecisionTreeClassifier(random_state=7)
    tree.fit(X_train, y_train)
    n_nodes.append(tree.tree_.node_count)
    X_{\text{test}}, y_{\text{test}} = data[n:, :-1], data[n:, -1]
    y_pred = tree.predict(X_test)
    t_error = 1 - accuracy_score(y_test, y_pred)
    t_errors.append(t_error)
print("Results:")
for i in range(len(n values)):
    print(f"n = {n_values[i]}, Nodes = {n_nodes[i]}, Test Error = {t_errors[
plt.figure(figsize=(10, 5))
plt.plot(n_nodes, t_errors, marker='o')
plt.title("Learning Curve")
plt.xlabel("Nodes")
plt.ylabel("Test Error")
plt.show()
Results:
n = 32, Nodes = 11, Test Error = 0.2001
n = 128, Nodes = 25, Test Error = 0.1174
n = 512, Nodes = 53, Test Error = 0.0543
n = 2048, Nodes = 131, Test Error = 0.0218
n = 8192, Nodes = 241, Test Error = 0.0100
                                     Learning Curve
  0.200
  0.175
  0.150
  0.125
Test Error
  0.100
  0.075
  0.050
  0.025
```

```
In [112... #q4
    #for 15 points in lagrange
    import numpy as np
    from scipy.interpolate import lagrange
```

100

150

Nodes

200

250

```
from sklearn.metrics import mean_squared_error
          from numpy.polynomial.polynomial import Polynomial
         a, b, n = 0, 2*np.pi, 16
         x_train = np.random.uniform(a, b, n)
         y_train = np.sin(x_train)
         model = lagrange(x_train, y_train)
         x_test = np.random.uniform(a, b, 12)
         y_{test} = np.sin(x_{test})
         y_train_pred = model(x_train)
         y test pred = model(x test)
         train_error = mean_squared_error(y_train, y_train_pred)
         test_error = mean_squared_error(y_test, y_test_pred)
         print(f'Training error: {train error}')
         print(f'Testing error: {test_error}')
         for std_dev in [0.1,0.3, 0.5,0.6, 1.0]:
             xn_train = x_train + np.random.normal(0, std_dev, n)
             yn train = np.sin(xn train)
             nlagrange = lagrange(xn_train, yn_train)
             yn train pred = nlagrange(xn train)
             yn_test_pred = nlagrange(x_test)
             ntrain error = mean squared_error(yn_train, yn_train_pred)
             ntest_error = mean_squared_error(y_test, yn_test_pred)
             print(f"\nTrain Error (Std Dev {std dev}): {ntrain error:.4f}")
             print(f"Test Error (Std Dev {std_dev}): {ntest_error:.4f}")
         Training error: 1.2389859720873664e-09
         Testing error: 5.650500910294485e-09
         Train Error (Std Dev 0.1): 0.0000
         Test Error (Std Dev 0.1): 0.0000
         Train Error (Std Dev 0.3): 0.0000
         Test Error (Std Dev 0.3): 0.0000
         Train Error (Std Dev 0.5): 0.0195
         Test Error (Std Dev 0.5): 0.0214
         Train Error (Std Dev 0.6): 0.0000
         Test Error (Std Dev 0.6): 0.0000
         Train Error (Std Dev 1.0): 0.0000
         Test Error (Std Dev 1.0): 0.0000
In [103... #q4
         #for 100 points in lagrange
         import numpy as np
         from scipy.interpolate import lagrange
         from sklearn.metrics import mean_squared_error
         from numpy.polynomial.polynomial import Polynomial
         a, b, n = 0, 2*np.pi, 100
```

```
x_train = np.random.uniform(a, b, n)
       y_train = np.sin(x_train)
       model = lagrange(x_train, y_train)
       x test = np.random.uniform(a, b, 12)
       y_test = np.sin(x_test)
       y train pred = model(x train)
       y_test_pred = model(x_test)
       train_error = mean_squared_error(y_train, y_train_pred)
       test_error = mean_squared_error(y_test, y_test_pred)
       print(f'Training error: {train error}')
       print(f'Testing error: {test_error}')
       for std_dev in [0.1, 0.5, 1.0]:
          xn_train = x_train + np.random.normal(0, std_dev, n)
          yn train = np.sin(xn train)
          nlagrange = lagrange(xn train, yn train)
          yn_train_pred = nlagrange(xn_train)
          yn test pred = nlagrange(x test)
          ntrain_error = mean_squared_error(yn_train, yn_train_pred)
          ntest_error = mean_squared_error(y_test, yn_test_pred)
          print(f"\nTrain Error (Std Dev {std dev}): {ntrain error:.4f}")
          print(f"Test Error (Std Dev {std dev}): {ntest error:.4f}")
       Training error: 4.7308517241752454e+145
       Testing error: 2.558239489468512e+143
       Train Error (Std Dev 0.1): 804769116641478203675236899333503430705539977386
       83901313232621535232.0000
       Test Error (Std Dev 0.1): 1417556612495417974539935803963236622522960561144
       528781599125308951478932953422307136453491044706743505308114008555849564258
       0310803028639744.0000
       Train Error (Std Dev 0.5): 166701366862061847190678583873893790736465671187
       51865685020770280042135552.0000
       Test Error (Std Dev 0.5): 1810045157110036254649026029081493367888596433036
       393878884096147456.0000
       Train Error (Std Dev 1.0): 269458193076389965809838506495671396618891956633
       206685476417352254100309278720.0000
       Test Error (Std Dev 1.0): 3316693991057072864623418241046942748443046023105
       935722435084965446414858699272620162364429710851853082027810445441365095395
       270171033600.0000
In [ ]:
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In []:
```