

Counterfactual Accuracies for Alternative Models

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Loan Approval



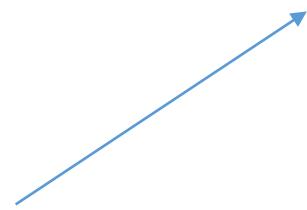
Loan Approval



Model A

Train Accuracy: 98%

Loan Approval

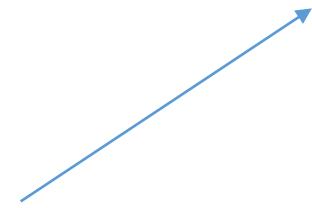


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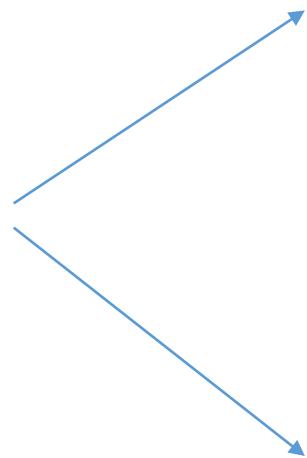
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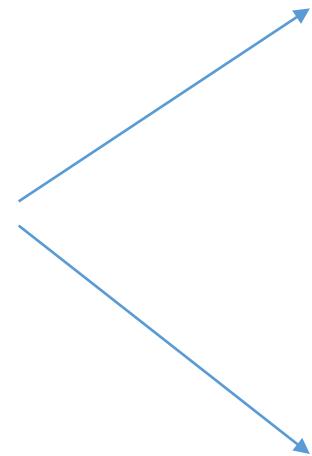


Model A
Train Accuracy: 98%

Model B
Train Accuracy: 96%



Loan Approval



Model A
Train Accuracy: 98%



Model B
Train Accuracy: 96%



Central Question

Given a particular test point z , if we were to find an alternative classifier in the same model class fitted to the same training data, how much training accuracy would we have to give up so that the prediction for the test point z would change?

Related Work

Rashomon Effect [Breiman 2001]: Multiple models may fit the training data well

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Predictive Multiplicity [Marx et al. 2019]: Analyzes the difference in predictions from models in a Rashomon set

Notation

$$\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$$

Training Dataset

$$\mathcal{F}$$

Family of Functions

$$\hat{R}(f) = \frac{1}{n} \sum_{i=1}^n \ell(f(x_i), y_i)$$

**Average Loss
(Empirical Risk)**

Our Approach

Empirical Risk Minimization

$$f_o = \arg \min_{f \in \mathcal{F}} \sum_{i=1}^N \ell(f(\mathbf{x}_i), y_i)$$

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This Work

$$\begin{aligned} f_{\mathbf{z}} &= \arg \min_{f \in \mathcal{F}} \sum_{i=1}^N \ell(f(\mathbf{x}_i), y_i) \\ \text{s.t. } f_o(\textcolor{brown}{z}) &\neq f_{\mathbf{z}}(\textcolor{brown}{z}) \end{aligned}$$

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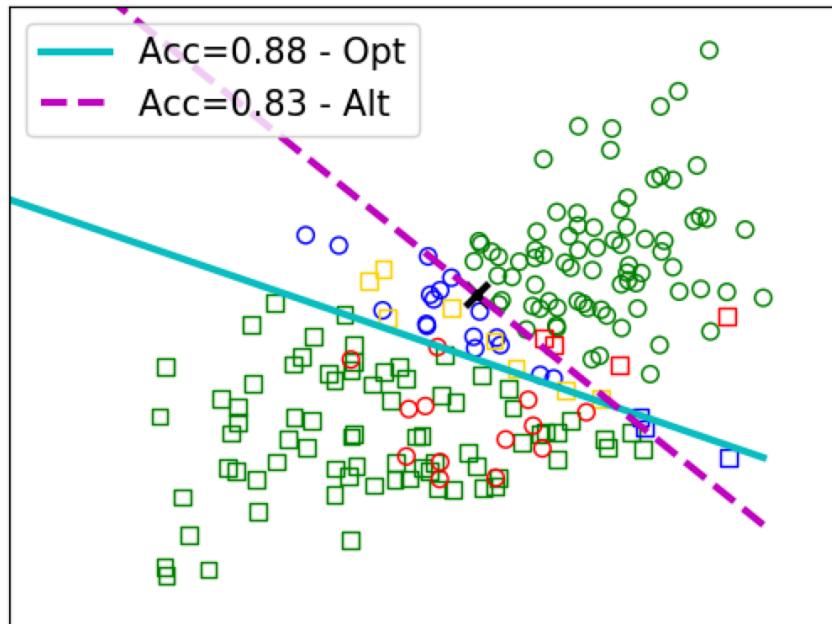
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Counterfactual Accuracy: $\tilde{C}_z = \widehat{R}(f_z) - \widehat{R}(f_o) = \left(1 - \widehat{R}(f_o)\right) - \left(1 - \widehat{R}(f_z)\right)$

Some Results

Two Overlapping Gaussians



Green: Correct in both

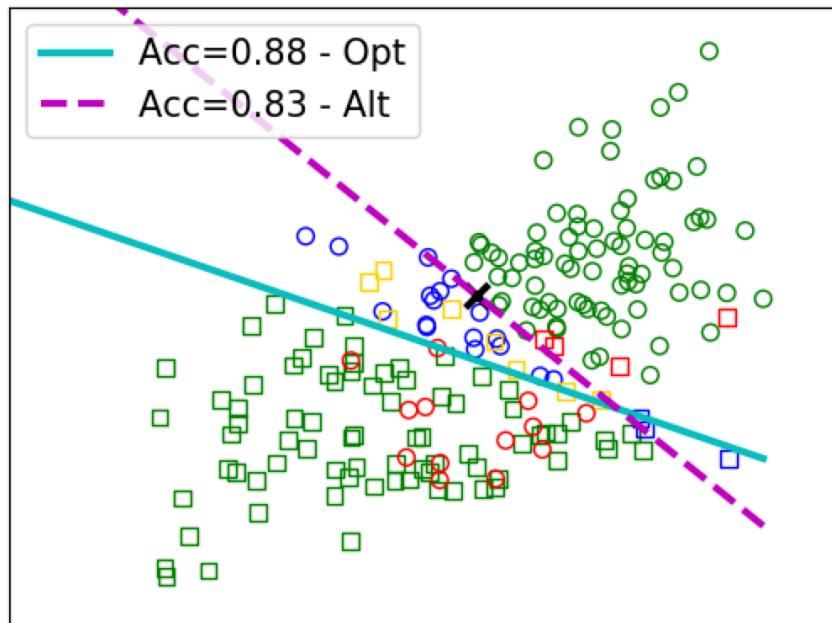
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Blue: Originally right, now wrong

Yellow: Originally wrong, now right

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Two Overlapping Gaussians



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Dataset	Average Counterfactual Accuracy	Average number of predicted label flips
Adult	0.667%	~225
COMPAS	1.437%	~260

Future Work

- **Faster computation:** Moving beyond a warm start from the parameters of the old model, how can avoid recomputing the entire objective from scratch?

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- **Faster computation:** Moving beyond a warm start from the parameters of the old model, how can avoid recomputing the entire objective from scratch?
- **Experimentation:** What do ML practitioners learn about their datasets from knowing this quantity for their training data?

References

Breiman, Leo. "Statistical modeling: The two cultures (with comments and a rejoinder by the author)." *Statistical science* 16.3 (2001): 199-231.

Fisher, Aaron, Cynthia Rudin, and Francesca Dominici. "All models are wrong but many are useful: Variable importance for black-box, proprietary, or misspecified prediction models, using model class reliance." arXiv preprint arXiv:1801.01489 (2018).

Marx, Charles T., Flavio du Pin Calmon, and Berk Ustun. "Predictive Multiplicity in Classification." arXiv preprint arXiv:1909.06677 (2019).