JSON Representation for Graphs

Introduction

This is a brief report on the considerations related to and explorations of various JSON representations for general graphs. Our considerations and requirements are listed below and we hope to find ready-made solutions in the form of accepted and popular formats on the internet or decide to adopt the best practices and modify them to our own needs.

Goal

Our primary goal is to find a good JSON representation for graphs that are of interest in the area of source code analysis and compilation. Of particular interest are: control flow graph, data flow graph, call graph, AST, and other structured data that has an underlying graph or tree model. We hope that one format will fit them all.

Requirements/concerns:

First and foremost we like to keep everything simple. The format should be easy to understand by humans and computers, and easy to produce. It should use a small set of explicit "key"-words, like "nodes", "edges", etc. Especially for graphs, it is important to represent edges explicitly. They typically have a type and other attributes that are of importance. We are fine with having either all edges being directed or all undirected, so that should be an attribute of the graph and not per edge. On the other hand, we do foresee multiple distinct edges between the same pair of nodes; so that feature must be representable. Another trade-mark of simplicity is that there is no redundant information and a particular fact is expressed in one way only.

For certain applications it is important that the order of some objects can be relied upon. In JSON that means using arrays instead of objects. It is nice to output tree nodes in e.g. a depth-first order (and indicate so with an attribute like "order": "dfs"), or specify that graph nodes are in topological order. No matter, the representation must then be able to preserve that order.

We also want a format that is easily manipulated to enable conversions to and from other formats (XML, GraphViz Dot).

Note that using JSON we will always need to use references: JSON cannot natively express a graph (at most a tree) structure. In an undirected graph we should allow for direction-agnostic references to nodes, like "between": ["node1", "node2"] (still ordered, if wanted); in a directed graph we often see:

"source" and "target" (or from/to or tail/head). Let's use the neutral term "between" for both.

Should a node be merely a key and its value or an object by itself? Or, should a list of nodes be an array of objects? Nodes and edges being JSON arrays gives a means for ordering them. It will also be easier to select them as a group and iterate over the elements.

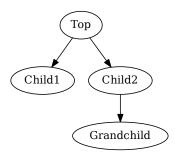
We should make a distinction between a node id (an identification used for reference) and a node label. The latter is human oriented; the id has only meaning within the representation and could be a generated UUID.

Do edges need an id? For sure multi-edges do, to distinguish them somehow, but that's application dependent. But in JSON it is allowed to have array elements being identical, so even without identification it is possible to represent multiple edges between the same two nodes (they will then be indistinguishable except when they have different attributes for instance). So let's leave edge ids optional.

A good way to steer the decision making process is to attempt to capture some examples in the proposed format.

Simple example of a tree in proposed format

This figure is represented by the JSON object below.



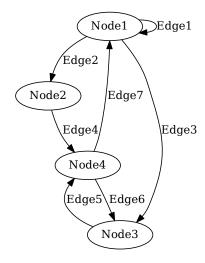
```
"graph": {
    "version": "1.0",
    "type": "tree",
    "directed": true,
    "root": 0,
    "nodes": [
        { "id": 0, "label": "Top" },
        { "id": 1, "label": "Child1" },
```

```
{ "id": 2, "label": "Child2" },
    { "id": 3, "label": "Grandchild" }
],
    "edges": [
    { "between": [ 0, 1 ] },
    { "between": [ 0, 2 ] },
    { "between": [ 2, 3 ] }
]
}
```

Note that the ids are chosen to be integers and that they could be consistently renamed without affecting the tree structure. The root property indicates the root node of the tree whose id value equals its value, 0 in this case. The idea is also that both node and edge objects can have many more attributes of any JSON type. Only a few keys and their types are prescribed. All this will be formally specified in a schema.

Simple example of a directed graph in proposed format

This directed graph is represented by the JSON as follows.



```
"graph": {
    "version": "1.0",
    "directed": true,
```

```
"nodes": [
      { "id": "Node1" },
      { "id": "Node2" },
      { "id": "Node3" },
      { "id": "Node4" }
    ],
    "edges": [
      { "between": [ "Node1", "Node1" ], "label": "Edge1" },
      { "between": [ "Node1", "Node2" ], "label": "Edge2" },
      { "between": [ "Node1", "Node3" ], "label": "Edge3" },
      { "between": [ "Node2", "Node4" ], "label": "Edge4" },
      { "between": [ "Node3", "Node4" ], "label": "Edge5" },
      { "between": [ "Node4", "Node3" ], "label": "Edge6" },
      { "between": [ "Node4", "Node1" ], "label": "Edge7" }
    ٦
}
```

Here we see that the original node names are used as ids and that edge names are explicitly listed by the label attribute. Since the graph is directed we know that the between array has to be considered ordered: the first element is the node where the edge originates from and the second element is the node where the edge ends up. It is tempting to completely remove the nodes key and its value, since all nodes are known via the edges. However, in most cases nodes will have more data associated and hence need to be listed anyway. Therefore the nodes and edges keys will be deemed mandatory and all references to nodes in the edges list must be mentioned also in the nodes list. Not necessary the other way around since we allow for isolated nodes in a graph.

The minimum graph in proposed format

The example shows the minimum required keys and their values. It happens to represent an empty (undirected) graph.

```
{
   "graph": {
      "version": "1.0",
      "directed": false,
      "nodes": [],
      "edges": []
   }
}
```

Alternative notation using a node adjacency list

{

"graph": {

"version": "1.0",

Here is the same tree again but this time formulated using an adjacency style notation where each node directly list its own edges. Since we have no additional edge information, we allow the edges to merely consist of a list of node ids. It is also assumed that absence of the edges means the same as an empty list ("edges": []).

```
"type": "tree",
    "directed": true,
    "root": 0,
    "nodes": [
      { "id": 0, "label": "Top",
                                   "edges": [ 1, 2 ] },
      { "id": 1, "label": "Child1" },
      { "id": 2, "label": "Child2", "edges": [ 3 ] },
      { "id": 3, "label": "Grandchild" }
    ]
 }
}
The alternative notation for the graph example is as follows:
  "graph": {
    "version": "1.0",
    "directed": true,
    "nodes": [
      { "id": "Node1",
        "edges": [ { "on": "Node1", "label": "Edge1" },
                   { "on": "Node2", "label": "Edge2" },
                   { "on": "Node3", "label": "Edge3" } ]
      { "id": "Node2",
        "edges": [ { "on": "Node4", "label": "Edge4" } ]
      { "id": "Node3",
        "edges": [ { "on": "Node4", "label": "Edge5" } ]
      },
      { "id": "Node4",
        "edges": [ { "on": "Node3", "label": "Edge6" },
                   { "on": "Node1", "label": "Edge7" } ]
      }
   ]
 }
```

}

Observations

From scanning available JSON graph formats on the web, we learn that many follow similar ideas as what the overall structure is concerned but deviate in the details. The node and edge list approach is prevalent. There are a few serious graph JSON formats that strive to become a standard and that are backed by several organizations. In principle it should be easy to convert between the formats, so choosing the "wrong" one is not that bad. Especially if we allow for additional properties in objects, any schema can always be extended to allow insertion of missing or additional information. Of course our basic requirements still stand and must be expressible in the format of choice.

References consulted

- [1] jsongraphformat
- [2] jsongraph
- [3] jsongraphformat
- [4] graphalchemist
- [5] graph-json

Appendix: IBM Graph JSON Schema

The JSON schema below defines the IBM AI4Code JSON Graph Format. At the top-level there should be a JSON object with a graph property, which itself must be an object. That object has several required properties, the most important being the nodes and edges properties, both of which must be arrays, thus guaranteeing an ordered list of items. The array elements are to be objects. It is to be understood that applications that rely on for instance the order of children nodes of a parent node, may assume that the (outgoing) edges will occur in that order in the edges array. Node order may have a significance too. For instance the nodes array might list the nodes in a topological order. This can be specified using the order property.

All nodes and edges may have other properties beyond the required ones as specified by the schema. If in the future these tend to be of general use, the schema might be extended to include those and thereby formalize their definition.

The alternative adjacency style can co-exist with the proposed node and edge list schema. This has been captured in the following schema that is able to validate both styles and even combinations of them in a single graph description.

The key on is used as a neutral term to avoid to which suggests direction but would not make much sense in an undirected graph.

```
"$schema": "http://json-schema.org/draft-04/schema#",
"title": "Alternate JSON Schema for IBM AI4Code GraphJSON Format",
"description": "Prepared by Geert Janssen <geert@us.ibm.com>\nCopyright IBM Corporation 20
"type": "object",
"properties": {
  "graph": { "$ref": "#/definitions/graph" }
},
"required": [ "graph" ],
"additionProperties": true,
"definitions": {
  "graph": {
    "type": "object",
    "properties": {
      "version" : { "enum": [ "1.0" ] },
      "type":
                 {
        "description": "Indication of type, e.g. tree or dag.",
        "type": "string"
      },
      "directed": { "type": "boolean" },
                  { "type": "string" },
      "label":
      "root": {
        "description": "Indication of the root node for a tree.",
        "$ref": "#/definitions/unsigned_or_string"
      },
      "order": { "enum": [ "none", "topological", "reverse-topological",
                           "dfs", "bfs" ] },
      "metadata": { "type": "object" },
      "nodes": {
        "description": "Mandatory node list.",
        "type": "array",
        "items": { "$ref": "#/definitions/node" }
      },
      "edges": {
        "description": "Optional edge list.",
        "type": "array",
        "items": { "$ref": "#/definitions/edge" }
      }
    },
    "required": [ "version", "directed", "nodes" ],
```

```
"additionProperties": true
},
"node": {
  "type": "object",
  "properties": {
             { "$ref": "#/definitions/unsigned_or_string" },
    "label": { "type": "string" },
    "edges": {
      "description": "Optional adjacency-style notation.",
      "type": "array",
      "items": { "$ref": "#/definitions/adjacency_edge" }
    },
    "metadata": { "type": "object" }
  },
  "required": [ "id" ],
  "additionProperties": true
},
  "description": "Edge object in an edge list.",
  "type": "object",
  "properties": {
            { "$ref": "#/definitions/unsigned_or_string" },
    "label": { "type": "string" },
    "between": {
      "description": "An ordered pair of 2 nodes.",
      "type": "array",
      "items": { "$ref": "#/definitions/unsigned_or_string" },
      "minItems": 2,
      "maxItems": 2
    },
    "metadata": { "type": "object" }
  },
  "required": [ "between" ],
  "additionProperties": true
},
"adjacency_edge": {
  "description": "Edge in a node adjacency list.",
  "oneof": [
    { "description": "An array of node ids.",
      "$ref": "#/definitions/unsigned_or_string"
    },
    {
      "description": "An array of edge objects.",
```

```
"type": "object",
          "properties": {
            "id":
                    { "$ref": "#/definitions/unsigned_or_string" },
            "label": { "type": "string" },
                    { "$ref": "#/definitions/unsigned_or_string" }
          },
          "required": [ "on" ],
          "additionProperties": true
     ]
    },
    "unsigned_or_string": {
      "description" : "A non-negative integer or a string.",
      "oneof": [
        { "type": "integer", "minimum": 0 },
        { "type": "string" }
   }
 }
}
```