

CBA  $\leftrightarrow$  BCA

$$NB = B - C$$

- Clear about purpose
- Alternatives?
- Who is impacted + how?
- Who matters? → STANDING

## Technical Steps

- Predict, quantify, monetize, + discount impacts
- Sensitivity analysis
- Analyst recommendation

Cost effectiveness Analysis

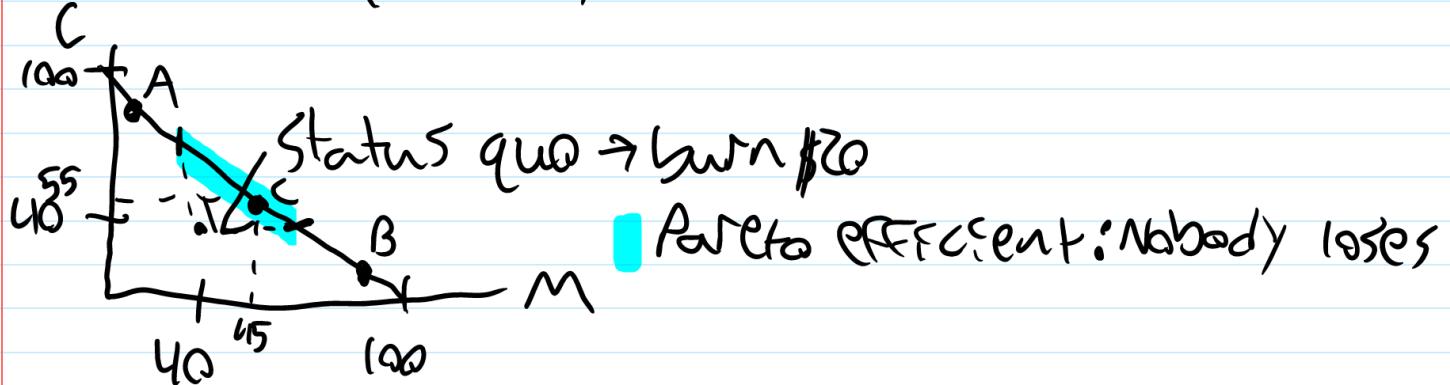
Economic Impact analysis

↳ NOT A CBA/BCA

# More Conceptual Foundations

How to measure efficiency?

Pareto efficiency



Kaldor-Hicks efficiency

If something is potentially Pareto, do it

$\beta + c?$

WTP  $\rightarrow$  willingness to pay

Opportunity Cost

$$\text{NB} = \beta - c$$
$$\beta/c = 5/3$$

New users +10

Old users -5

Const cost 3

$$\hookrightarrow \text{NB: } 10 - 5 + 3 = 8$$

$$\hookrightarrow \beta/c = \frac{10}{8} \text{ or } \frac{5}{3}$$

1.25 1.67

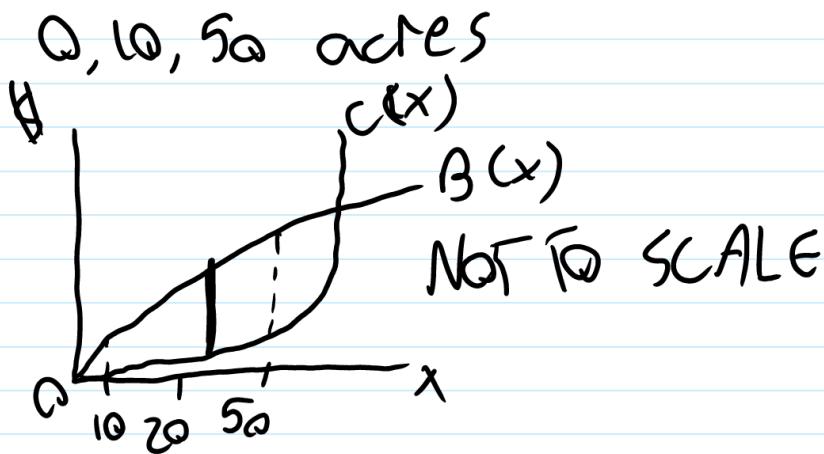
# Potential problems

Arrow's Impossibility theorem

- Depends on wealth distribution
- Standing

Optimum may not be under consideration

$$NB = B(x) - C(x)$$



# Passed Solution Review

City doesn't require helmets. I ride without a helmet

a. What are the benefits/costs of an ordinance to require helmets?

## Costs

Barrier to entry  
Enforcement  
Pushback  
decreased comforts

## Benefits

Increased Safety  
Stylishness

b. Societies costs/benefits?

## Costs

Enforcement  
Pushback

## Benefits

Less medical debt

a) Personal...

### Costs

- helmet cost
- reduced comfort
- helmet hair

### Benefits

- reduced risk of injury

b) Society...

### Costs

- enforcement
- increased pollution

### Benefits

- decreased healthcare costs

## Tariffs on Importers!

a. Growers are the focus! How is net benefit calculated as a spender?

$$\begin{array}{c} \text{Costs: tariff revenues } (\$m) \\ \text{Production } (6m) \\ \text{Reduced consumption } (13m) \\ \hline \end{array}$$

Benefits  
Profits ( $4m$ )

$$U - T - G - I = \boxed{-23m}$$

b. Treasury behaves as a guardian. How would net benefit be calculated if profit taxes are 20%.

Costs:  
Production ( $6m$ )  
Consumption ( $13m$ )

$$U + P - G - I = \boxed{-7m}$$

Benefits:  
Profits ( $4m$ )  
Revenue ( $8m$ )

# Passed Solution Review

TEMPLATE	PV (million dollars)		3.b Municipal standing	PV (million dollars)
National government grant	2.2		National government grant	2.2 B +
Construction and maintenance costs	12.5		Construction and maintenance costs	12.5 C -
Personnel costs	8.2		Personnel costs	8.2 C -
Revenue from municipal residents	8.6		Revenue from municipal residents	8.6 C O
Revenue from non-residents	2.2		Revenue from non-residents	2.2 B +
Use value benefit to municipal residents	16.6		Use value benefit to municipal residents	16.6 B +
Use value benefit to non-residents	3.1		Use value benefit to non-residents	3.1 - O
Scrap value	0.8		Scrap value	0.8 B +
NSB			NSB	-7.5 O
3.a National standing		PV (million dollars)	3.c Municipal guardian	PV (million dollars)
National government grant	2.2	-	National government grant	2.2 B +
Construction and maintenance costs	12.5	-	Construction and maintenance costs	12.5 C -
Personnel costs	8.2	B	Personnel costs	8.2 C -
Revenue from municipal residents	8.6	B	Revenue from municipal residents	8.6 B +
Revenue from non-residents	2.2	B	Revenue from non-residents	2.2 B +
Use value benefit to municipal residents	16.6	B	Use value benefit to municipal residents	16.6 - O
Use value benefit to non-residents	3.1	B	Use value benefit to non-residents	3.1 - O
Scrap value	0.8	B	Scrap value	0.8 - O
NSB		29.1	NSB	-7.7 O
3.d Municipal spender		PV (million dollars)		
National government grant	2.2	B +		
Construction and maintenance costs	12.5	C -		
Personnel costs	8.2	B +		
Revenue from municipal residents	8.6	B -		
Revenue from non-residents	2.2	B +		
Use value benefit to municipal residents	16.6	B +		
Use value benefit to non-residents	3.1	B O		
Scrap value	0.8	B +		
NSB		29.2		-6.9

Worked w/ Austin  
Passed Solution review

Project R has:  
20m Benefits  
16m Costs

F has:  
26m Benefits  
20m Costs

W has:  
10m Benefits  
2m Costs

Road to Improve Projects:  
16m Benefits to R  
10m Benefits to F  
-2m Benefits to W  
4m Benefits no Projects  
7m Costs

a) Project	Benefits	Costs	B/C	NB
R w/ Road	36	24	1.5	12
R no Road	20	16	1.25	4
F w/ Road	36	28	1.29	8
F no Road	26	20	1.3	6
W w/ Road	16	10	1.6	6
W no Road	10	7	5	-4
Road only	4			

b) Project R with a road should be selected according to the CBA decision rule

Worked w/ Austin  
Passed Solution Review

Costs: 500k  
600k

Benefits: 900k ← changed to 900k

$$900k - 500k - 600k = -200k$$

↑  
The book says 900,000 million. I'm going to use 900k

There is a net social loss of 200,000

Worked w/ Austin  
Passed Solution review

Costs: National or global?

40m	N
220m	N
180m	N

Benefits:

350m	N
70m	N
280m	G

$$NSB = -20m$$

$$\text{Required fraction} = 20/280 = 1/14$$

The program has a negative NSB of -20m  
The required fraction is 20/280

### 3.5 Incorporating the Social Cost of Raising Revenue through taxation

Excise tax on a good results in deadweight loss

SS is reduced w/ taxes

Impose or excess tax burden = proportion of tax or subsidy that results in deadweight loss

Increase in  $\eta_L$  from raising tax \$1 = METB

METB = marginal excess tax burden

$METB + 1 = MCPF$

↳ marginal cost of public funds

$$SS = CS + PS + (MCPF)GS$$

### 3.6 Measuring Changes in Welfare

#### 3.7 Conclusions

CBA aims to efficiently allocate resources

#### Appendix 3A CS and WTP

Compensating Variation

Indifference Curves

Income + Substitution Effects

Demand Curves

Marshallian Demand uses Income + Substitution Effects

Utility Compensated

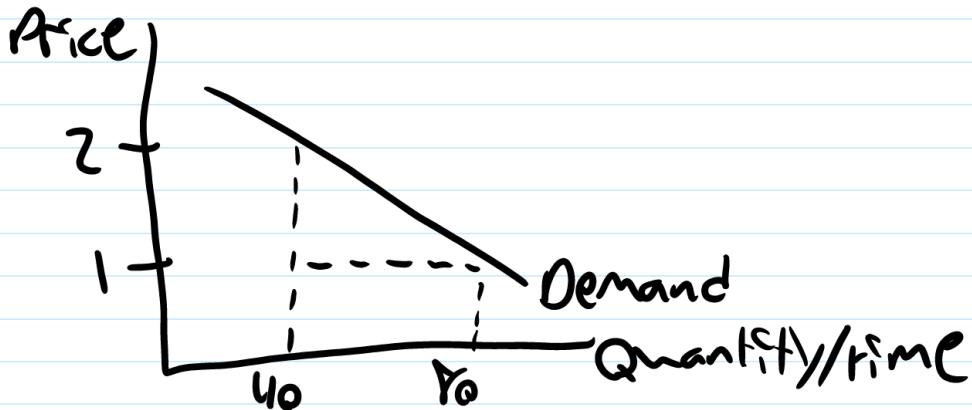
Hicksian Compensated Variation demand curve

Equivalence of CS + Compensating Variation

Equivalent Variation as an alternative to Compensating Variation

# Microeconomic foundations!

Demand closely related to willingness to pay (W+P)  
 "law of demand"



$$\text{Slope of demand is } \frac{\Delta Q}{\Delta P} = \frac{Q_2 - Q_1}{P_2 - P_1} = \frac{Q_2 - Q_1}{1 - 2} = -4Q$$

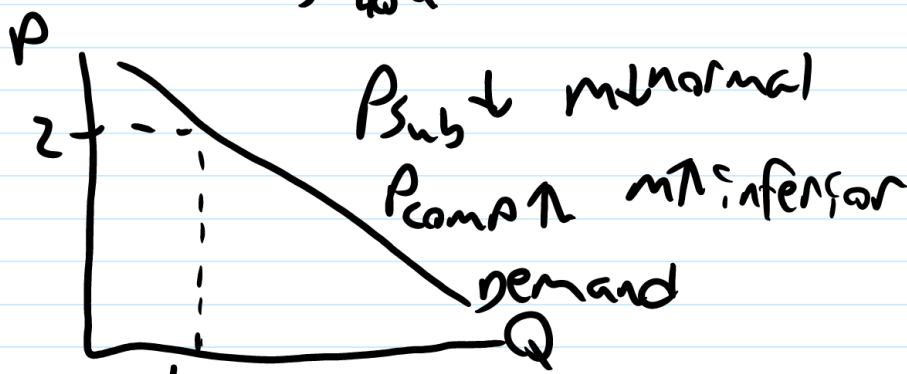
$Q = f(\text{Price}) \rightarrow \text{Demand Curve}$   
 $P = f(\text{Quantity}) \rightarrow \text{Inverse demand curve}$

$$\frac{\Delta Q}{\Delta P} = \frac{Q_2 - Q_1}{P_2 - P_1} = \frac{Q_2 - Q_1}{1 - 2} = -1$$

$$\frac{\Delta Q}{\Delta P} = -1 \rightarrow \Delta Q = -1 \Delta P$$

$$(Q - Q_1) = -1(Q(P - P_1))$$

$$Q = Q_1 + P_1 - P$$



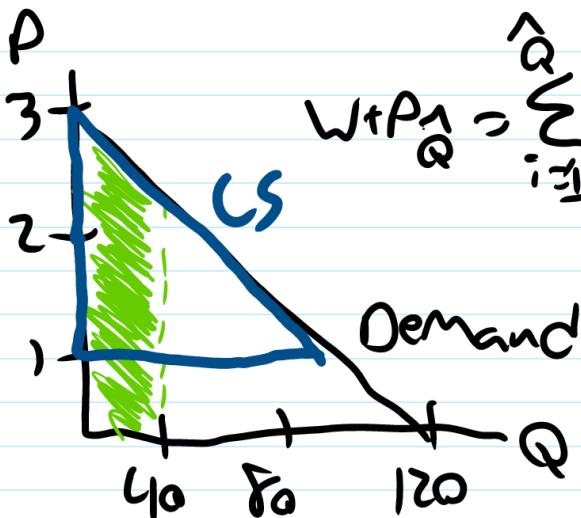
↳ Quantity Demanded

$$Q = f(P, P_{sub}, P_{comp}, M)$$

↳ normal, inferior

### 3.2 Demand, WtP, and Consumer Surplus

Tuesday, August 25, 2020 8:16 PM



$$WtP_Q = \sum_{i=1}^{\hat{Q}} P(1) + P(2) + \dots + P(\hat{Q})$$

$$\begin{aligned} WtP &= \int_0^Q P(x) dx = (2-1)(40-0) \\ &\quad + (3-2)\left(\frac{1}{2}(40-0)\right) \\ &= 80 + 20 = 100 \end{aligned}$$

$$CS = \frac{1}{2}(3-1)(f_0) = f_0$$

$$\Delta CS = WtP - Payments$$

$$\Delta CS = V(Q) - PQ$$

$\hookrightarrow$   $V$  is  $P$ ayment

$$\frac{dCS}{dQ} = \frac{dV}{dQ} - P = 0$$

$$P = \frac{dV}{dQ} = \text{inverse demand function}$$

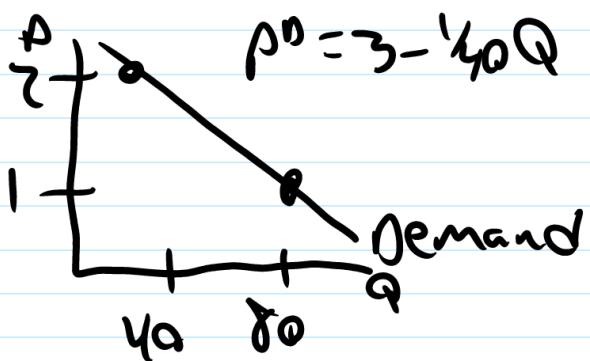


### 3.3 Elasticity

Tuesday, August 25, 2020 8:29 PM

$$\frac{\Delta Y}{\Delta X} \quad \frac{\Delta Q^D}{\Delta P}$$

$$\frac{\Delta Q^D}{\Delta P} \quad \frac{\% \Delta Q^D}{\% \Delta P} = \zeta_P^D$$



$$\begin{aligned}\zeta_P^D &= \frac{\% \Delta Q}{\% \Delta P} = \frac{\Delta Q / Q}{\Delta P / P} \\ &= \left( \frac{\Delta Q}{\Delta P} \right) \cdot \left( \frac{P}{Q} \right)\end{aligned}$$

"Point elasticity"

$$P^D = 3 - \frac{1}{4}Q$$

$$\% \Delta Q = \frac{40 - 80}{80} < \frac{40}{80} = 100\%$$

$$\% \Delta P = \frac{2 - 1}{1} = \frac{1}{1} = -100\%$$

$$\zeta^D = -1$$

$$\% \Delta Q = \frac{40 - 80}{80} = -1/2$$

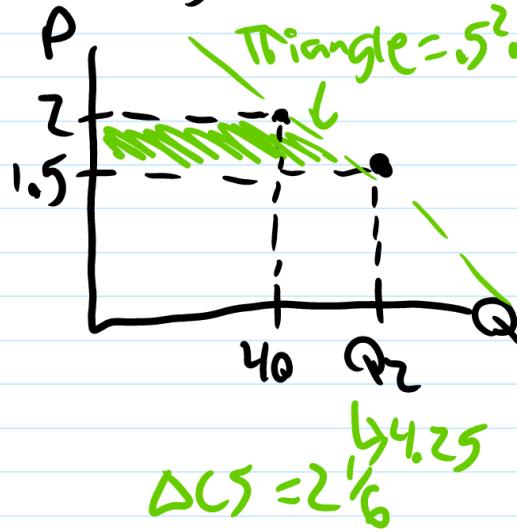
$$\% \Delta P = \frac{2 - 1}{1} = 1$$

$$\zeta^D = \frac{-1/2}{1} = -1/2$$

### 3.4 Elasticity to monetize an impact

Tuesday, August 25, 2020 8:41 PM

## Using Elasticity to Value Impacts on Consumers



$$(2 - 1.5) \cdot 4 = 2$$

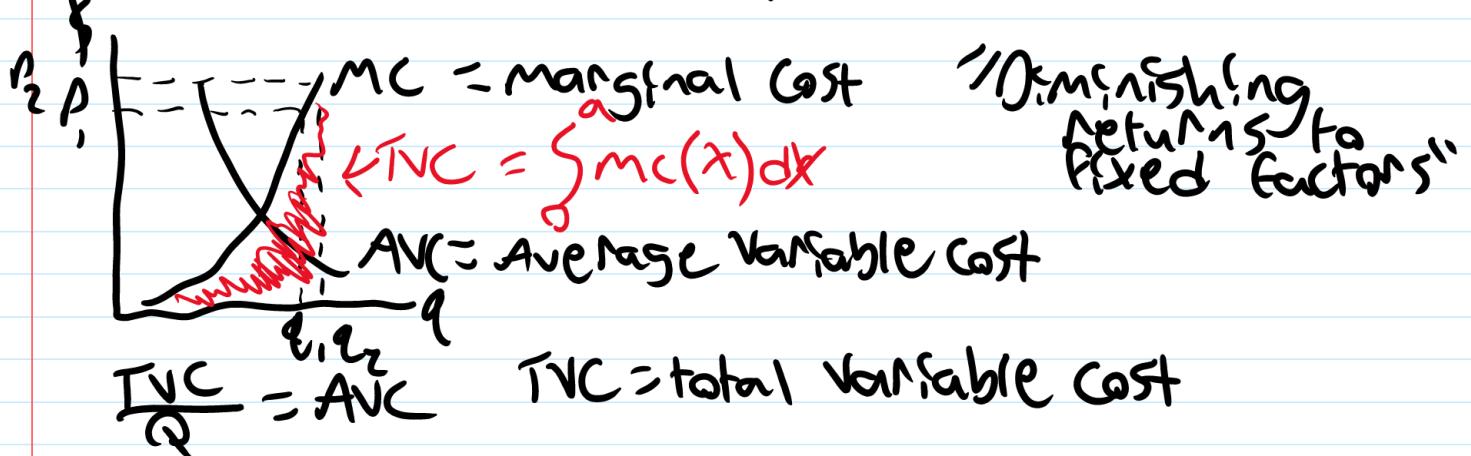
$$\frac{1}{2} (2 - 1.5)(Q_2 - 40)$$

$$30 = -\frac{1}{2}$$

$$\frac{\Delta Q}{\Delta P} = \frac{Q_2 - 40}{1.5 - 2} = -1/2$$

$$Q_2 - 40 =$$

## SUPPLY, Producer Surplus, Factor Surplus



$$\Pi = Pq - C(q) \rightarrow \frac{d\Pi}{dq} = P - \underbrace{\left[ \frac{dc}{dq} \right]}_{MC} = 0$$

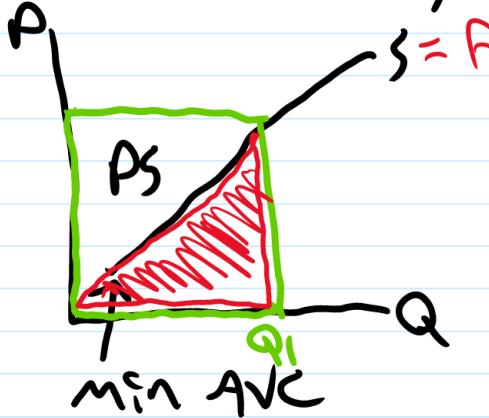
↳ PROFIT    ↳ COST

$$P - MC = 0$$

$P = MC \rightarrow \text{see graph}$

$$Q^S = \sum_{i=1}^n q_i(P)$$

↳ market supply



$$TVC \quad \Pi = Pq - TVC - TFC$$

↳ Firm MC

↳ Total Fixed Cost

$$PS = P_a - TVC$$

↳ Producer Surplus

$$SS = CS + PS$$

Social = Consumer + Producer

Long Run  $\leftrightarrow$  All inputs are variable

# Producer Surplus in the long run

$\Pi_{\text{Economic}} > 0 \rightarrow$  enter or expand

$P \downarrow \rightarrow \Pi^e \downarrow$

$\Pi^e < 0 \rightarrow$  exit or contract

$\hookrightarrow P \downarrow, \Pi^e \downarrow$

## Factor Surplus

$$PS = \Pi + FS$$

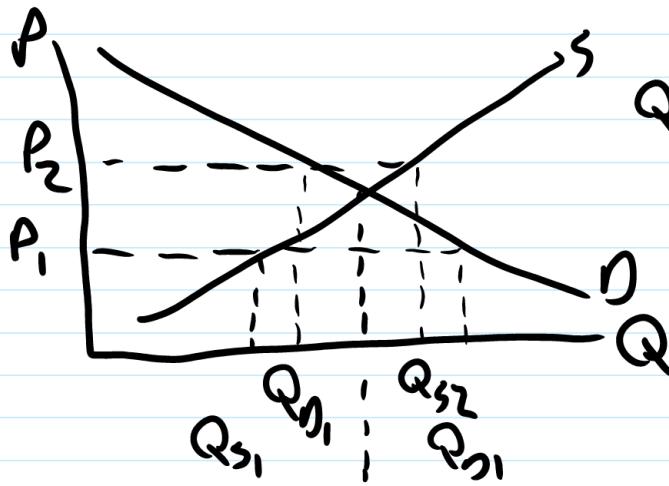
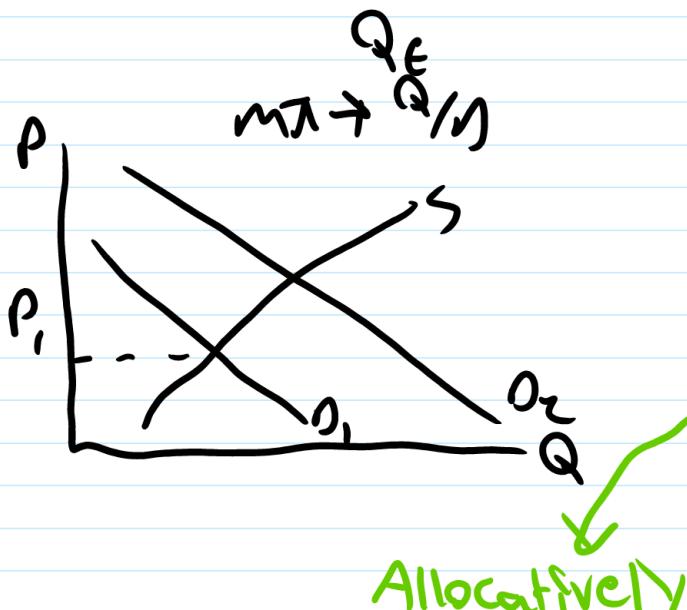
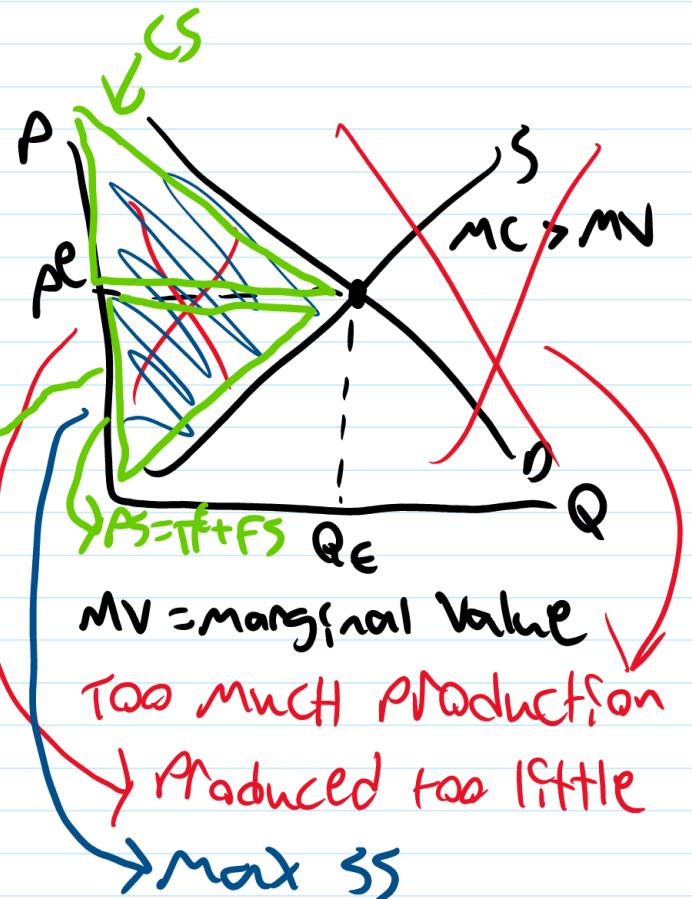
$$PS = \Pi^e + \text{Ricardian rents}$$

$\hookrightarrow FS$

$$SS = CS + PS$$
$$= CS + \Pi^e + FS$$

Social Surplus

Market equilibrium

 $Q_{S2} > Q_{D2}$   
↳ Surplus $Q_{D1} > Q_{S1}$   
↳ ShortageAllocatively  
Efficient  
Outcome

PS =  $F_S + F_D$   
 $MV = \text{marginal value}$   
 Too much production  
 Produced too little  
 Max SS

### 3.8 Factors of Production

Tuesday, September 1, 2020 6:10 PM

## FACTORS OF PRODUCTION:

- Labor
- Land (natural resources)
- Capital (roundaboutness of production)

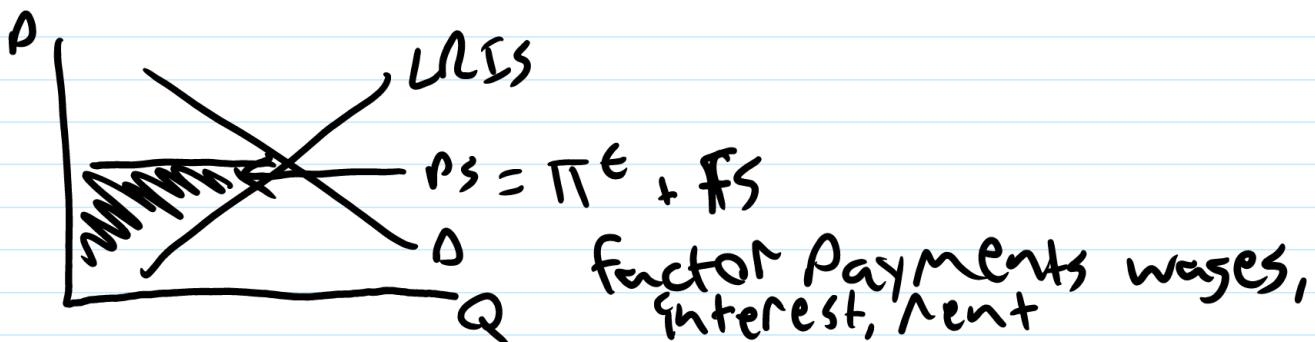
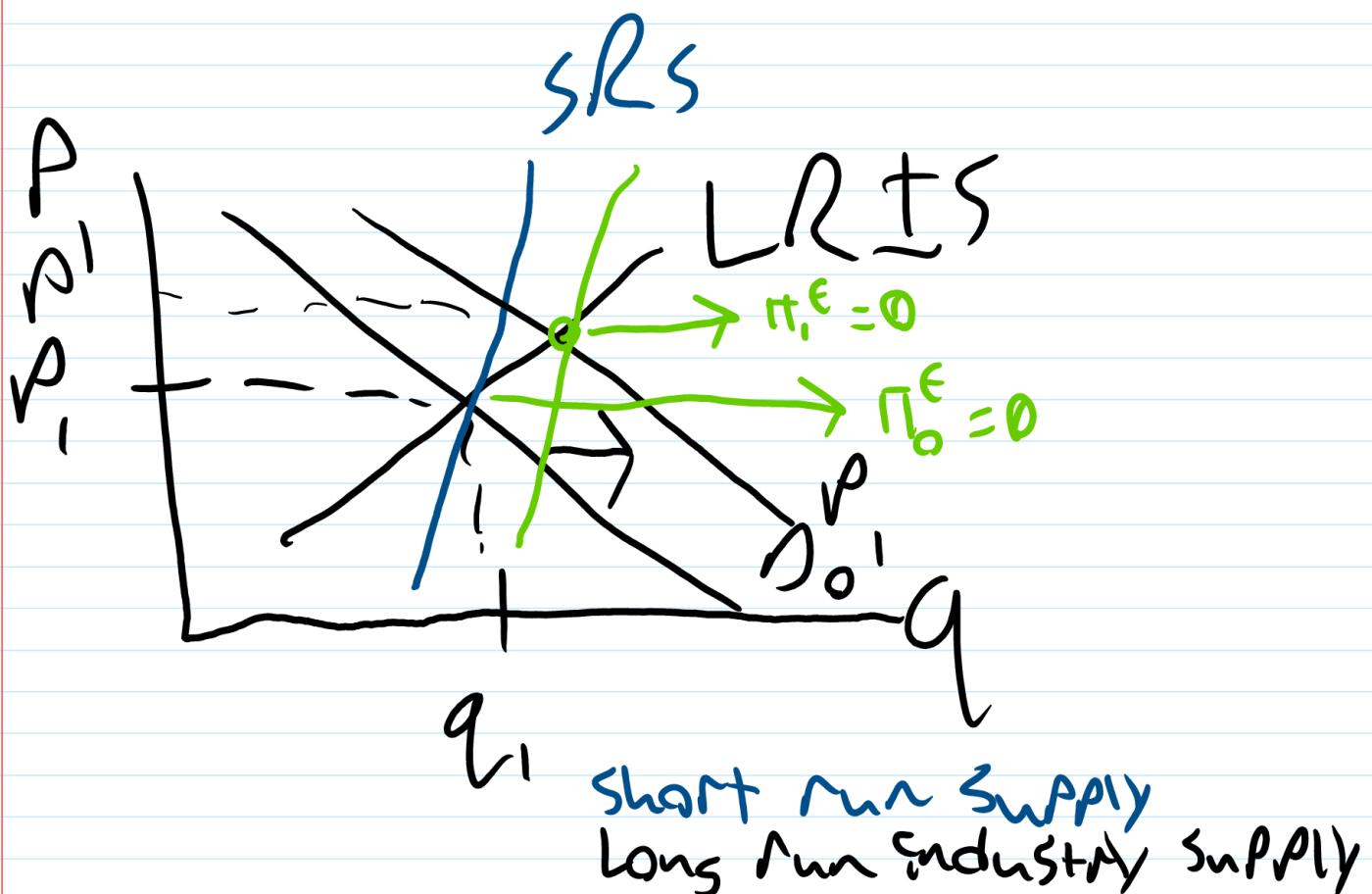
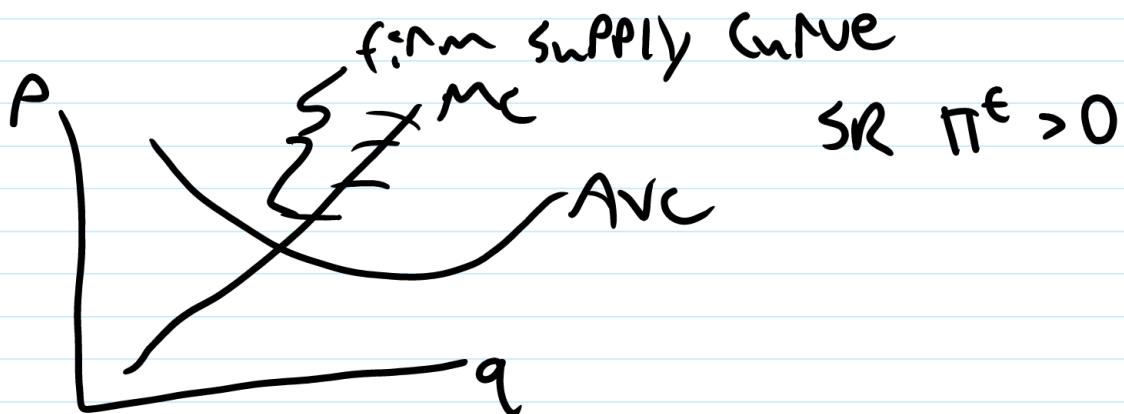
## Entrepreneurial Activity

↳ Paid w/ econ. profit

### 3.9 Long Run Equilibrium and Producer Surplus

Tuesday, September 1, 2020 6:20 PM

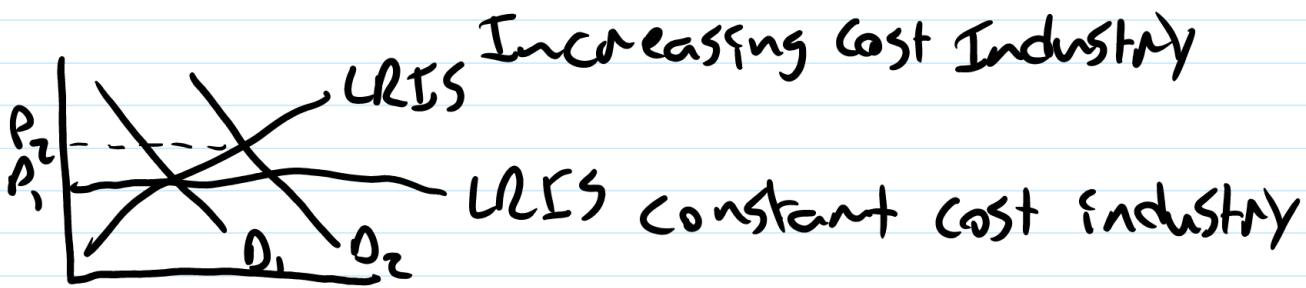
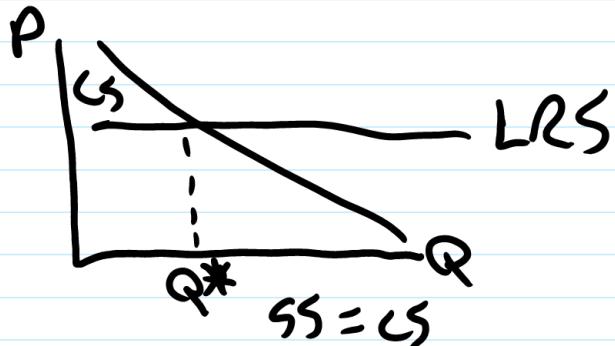
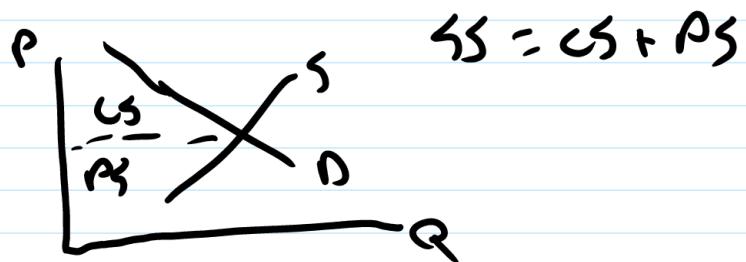
long run equilibrium  
PROFIT and factor SURPLUS



### 3.10 Social Surplus and Government Surplus

Tuesday, September 1, 2020 7:05 PM

## Social Surplus



## Government

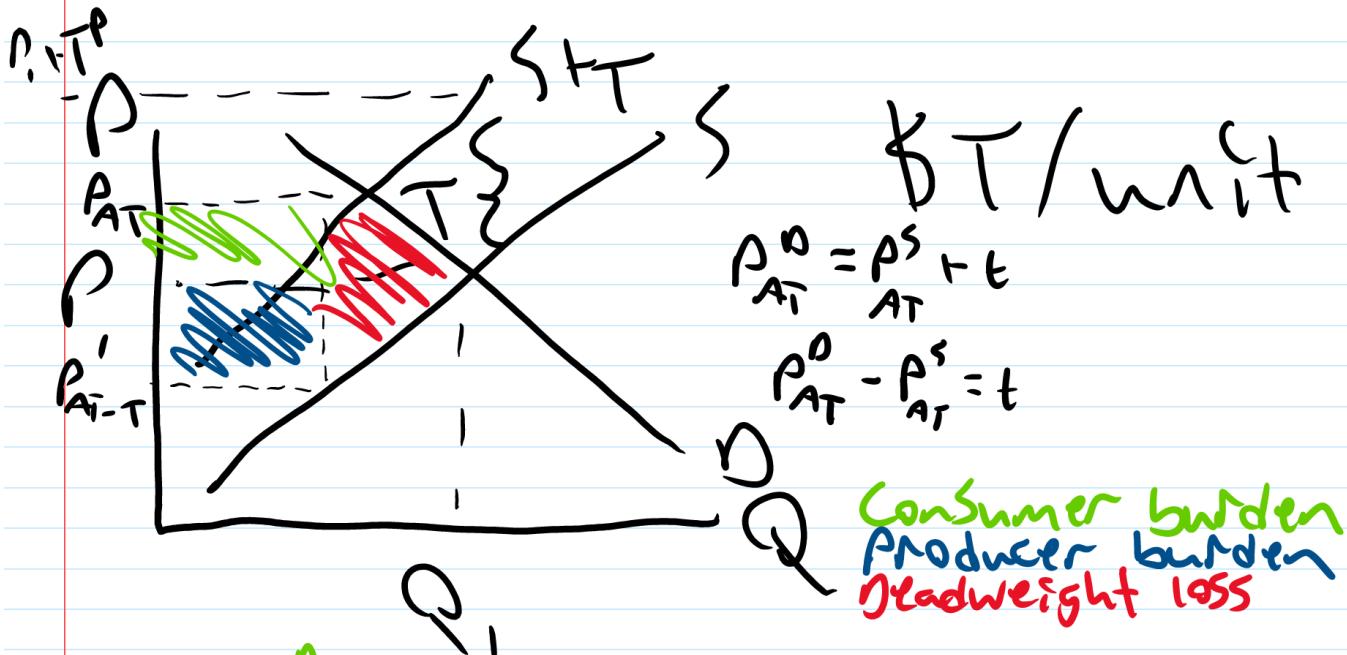
$$SS_1 = CS_1 + PS_1 \quad SS_2 = CS_2 + PS_2$$

$$\Delta SS = (CS_2 - CS_1) + (PS_2 - PS_1)$$

$$\Delta SS = \Delta CS + \Delta PS$$

$$\Delta SS = \Delta CS + \Delta PS + (1 + \lambda) \Delta GS \leftarrow \text{Budget Surplus}$$

$\downarrow$  marginal excess  
burden of taxation



$$CB = (P_{AT}^D - P_i) Q_{AT}$$

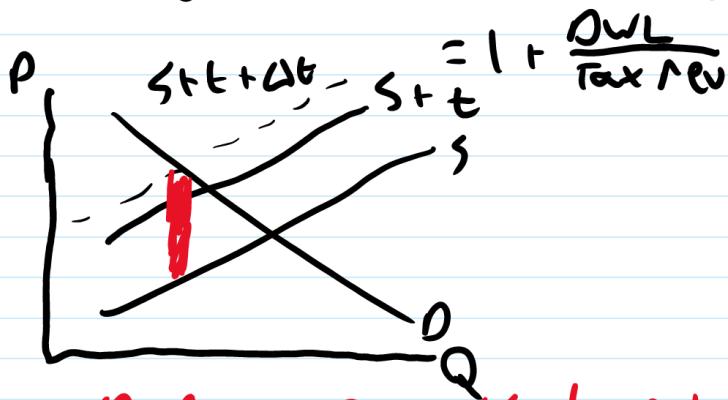
$$PB = (P_i - P_S^S) Q_{AT}$$

$$\text{Tax Rev} = (P_{AT}^D - P_S^S) Q_{AT}$$

$$= t \cdot Q_{AT}$$

Taxes distort outcomes

$$\frac{CB + PB + OWL}{CB + PB} = \frac{\text{Tax Revenue} + OWL}{\text{Tax Rev}}$$



$OWL = \text{excess burden}$

$MEBT =$

$MEBT > 0$

↳ Why have taxes?

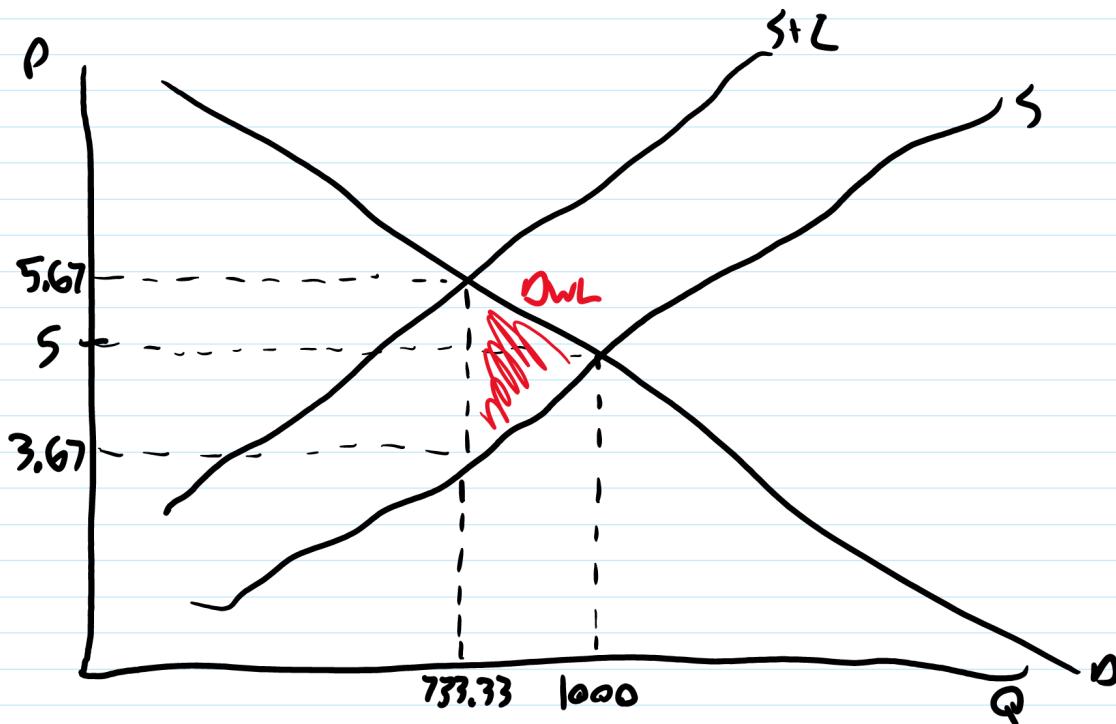
$$\Delta GS = \Delta CS + \Delta PS + (1 + \lambda) \Delta GS$$

Taxes destroy allocative efficiency

### 3.12 Tax Burden - Full Example

Saturday, September 5, 2020 5:51 PM

$$t = 2 \quad \bar{P}^d = -2 \quad \bar{P}^s = 1 \quad P_0 = 5 \quad Q_0 = 1000$$



$$-2 = \frac{Q - 1000}{P^0 - 5} \cdot \frac{5}{1000} \quad 1 = \frac{Q - 1000}{P^0 - 7}$$

$$P^0 = P^s + t$$

$$\frac{-2}{1} = \frac{1/P^0 - 5}{1/P^0 - 7} = \frac{P^0 - 7}{P^0 - 5} \rightarrow P^0 = 17/3 = 5.67$$

$$\frac{Q - 1000}{5.67 - 7} \cdot \frac{5}{1000} = 1 \rightarrow Q = 733.33$$

$$\Delta CS = -(5.67 - 5) \cdot 733.33 + \frac{1}{2}(733.33 - 1000) \cdot (5.67 - 5)$$

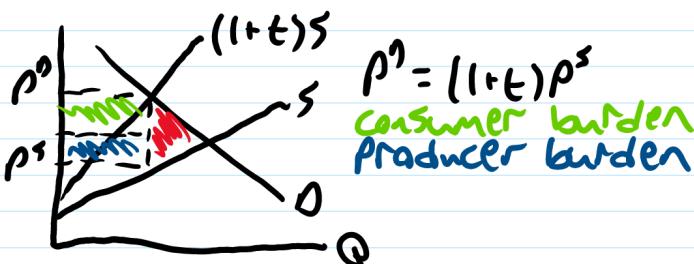
$$\Delta PS = (3.67 - 5) \cdot 733.33 + \frac{1}{2}(733.33 - 1000) \cdot (3.67 - 5)$$

$$\Delta GS = 2 \cdot 733.33 = 1466.67$$

$$\text{JWL} = \frac{1}{2}(1000 - 733.33) \cdot 2 = 266.67 \rightarrow 266.67 / 1466.67 = 0.18 \text{ Excess Burden}$$

Ad-valorem  
tax rate  
 $P^0 = (1+t) \cdot P^s$

constant tax  
 $P^0 = P^s + t$



### 3.13 Income and Substitution Effects and Willingness to Pay

Saturday, September 5, 2020 6:34 PM

Compensating Variation: Price goes up, Consumers hurt  
can supplement income to reduce impact

Equivalent Variation: Price goes up, what income loss is equivalent?

$$|CV| \approx |CS| \approx |EV|$$

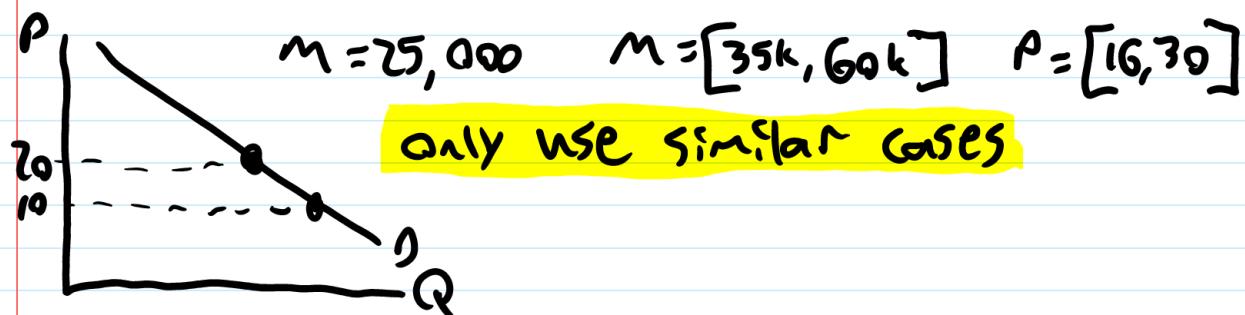
Giffen good has upward demand curve

↳ inferior good. Potatoes in famine. P ↑. Poorer, buy more potato.

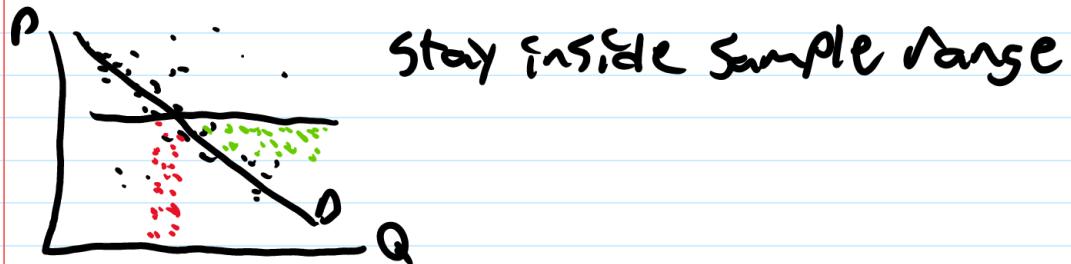
### 3.14 A Few Words on Empirical Approximations

Saturday, September 5, 2020 6:49 PM

## Extrapolation

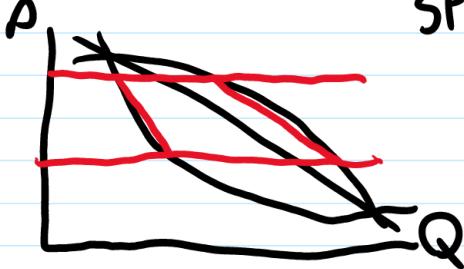


## Control Variables



## Linear Models

$$Q = P^{\beta_1} M^{\beta_2} e^{\beta_3}$$



Straight lines are good approximations



### 3.15 3.16 Gas Tax Full Example

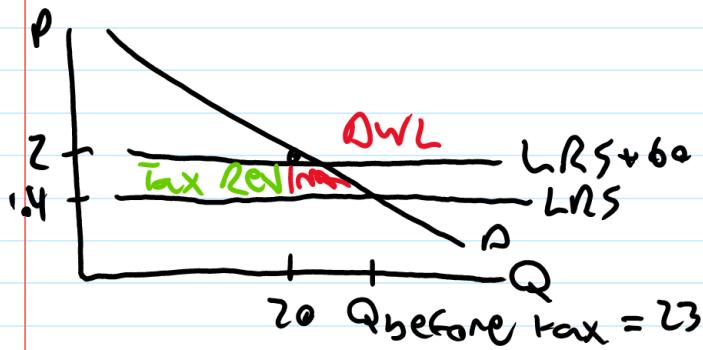
Thursday, September 10, 2020 8:20 PM

Floridians use about 20 million gallons of automotive gasoline per day. Including federal and state taxes, the tax rate is about \$0.60 per gallon. The elasticity of demand for gasoline is approximately -0.5.

- 1) Illustrate the current equilibrium.
- 2) Calculate the quantity consumed daily if the price was lower by the amount of the gas tax. Add it to your illustration.
- 3) How much tax revenue is raised? Label it in your illustration.
- 4) Calculate the loss of consumer surplus due to the gas tax. Label it in your illustration.
- 5) How much consumer surplus was lost per unit of revenue raised by the tax?

Assume that the current gas tax is \$0.50 per gallon too low to cover the cost of maintaining roadways in a safe condition for driving. If the tax were high enough to cover this cost...

- 6) What would consumption be? Add it to your illustration.
- 7) What would tax revenue be?
- 8) Calculate the loss of consumer surplus going from the original tax to the new tax. Show it in your illustration.
- 9) Going from the initial tax to the new tax, how much consumer surplus was lost per unit of additional tax revenue raised?
- 10) Compare your answer in (8) to your answer in (5). Can you explain the difference? What would happen to this ratio if the tax went from \$1.1 to \$1.15? Don't calculate anything. Just think it through and explain what would change and why.
- 11) Suppose elasticity of demand reasonably might be as high as 0.7 or as low as 0.3. How sensitive is your estimate of the consumer surplus loss from #4 to these possible differences?



$$\begin{aligned} \text{JWL} &= \frac{\Delta Q}{\Delta P} \\ &= \frac{\Delta Q}{0.60} = \frac{\Delta Q}{0.60} \cdot \frac{2}{20} = -0.5 \cdot \frac{\Delta Q}{6} \\ \Delta Q &= 3 \rightarrow Q_{WL} = 23 \end{aligned}$$

$$JWL = \frac{1}{2} \cdot 0.6 \cdot 3 = 0.9$$

$$\text{Tax Rev} = 12$$

$$6 \cdot \frac{\Delta Q}{25\%} = -12 \quad \frac{\Delta Q}{0.25} = -12 \cdot 5\%$$

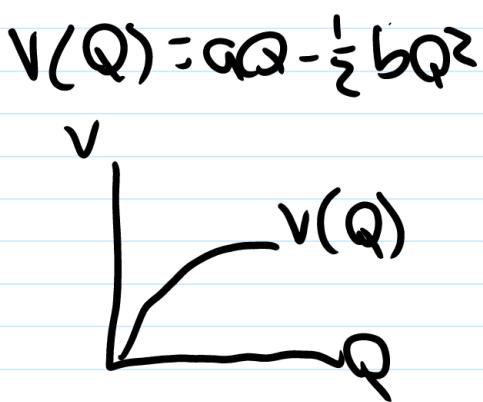
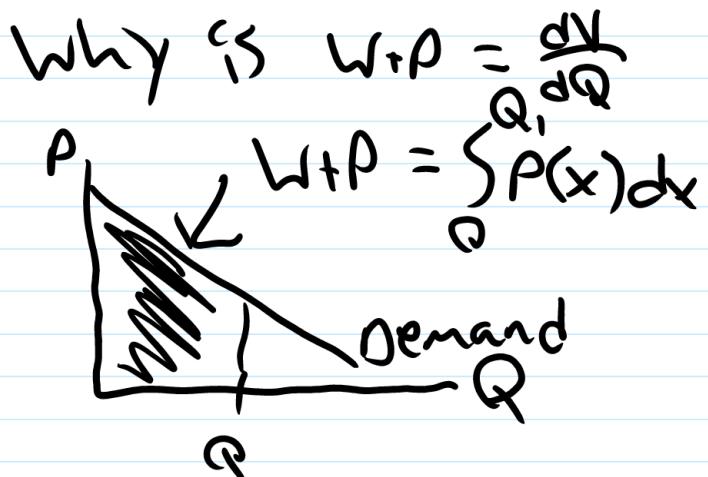
$$\text{I) } \Delta CS = -0.5 \cdot 17.5 - \frac{1}{2} \cdot 0.5 \cdot 2.5 = 9.375$$

$$\Delta CS / \Delta TR = -9.375 / 12.5 = -1.25$$

$$\text{II) } \left\{ \begin{array}{l} -0.7 \\ -0.3 \end{array} \right.$$

### 3 Extra Notes

Wednesday, August 26, 2020 2:20 PM



$$\text{maximize } v(Q) - P \cdot Q$$

optimal buy where derivative value = Price

Worked w/ Austin, River, + Alex  
Passed Solution Review

Suppose the elasticity of supply of cigarettes is 10.

- 1) Find estimates of the elasticity of demand for cigarettes, the current tax rate on cigarettes, average price, and annual quantity sold in Florida. Provide your sources.

Average price per pack: \$5.50

<https://www.salestaxhandbook.com/florida/tobacco>

Current tax rate: \$1.34/pack = 24.36%

<https://www.salestaxhandbook.com/florida/tobacco>

Elasticity of Demand: -3

<https://opentextbc.ca/principlesofeconomics/chapter/5-3-elasticity-and-pricing/>

Quantity smoked: 14.6 cigarettes \* .167 smokers/population \* 21477737

population = 52,367,018.3534/year

<https://www.sun-sentinel.com/health/fl-reg-florida-smokers-20180822-story.html>

<https://truthinitiative.org/research-resources/smoking-region/tobacco-use-florida-2019>

<https://www.census.gov/quickfacts/FL>

- 2) How high would the price, including the tax, need to be to cut consumption by half?

$$\frac{\% \Delta Q}{\% \Delta P} = -3 \rightarrow \frac{-0.5}{\% \Delta P} = -3 \rightarrow \frac{0.5}{3} = \frac{1}{6} \Delta P \rightarrow \% \Delta P = 1.667$$

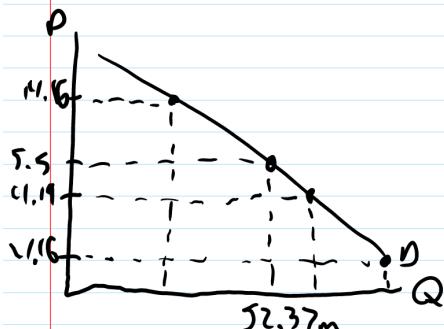
The new price would be  $(1.667 \cdot 5.5) + 5.5 = 14.6675$

- 3) How high would the tax have to be to push the after tax price that high?

$$\begin{aligned} 14.6675 - 5.5 &= 9.1675 \\ 9.1675 &= (5.5 - 1.34) \cdot X \\ X &= 9.1675 / (5.5 - 1.34) \\ X &= 9.1675 / 4.16 \\ X &= 2.2039 \end{aligned}$$

New tax is 220.39% = \$9.1675

- 4) Estimate the consumer and producer burden of the current cigarette tax.



$$\begin{aligned} -3 &= \frac{\Delta Q}{\Delta P} \left( \frac{P}{5.5 - P} \right) & 10 &= \frac{\Delta Q}{\Delta P} \left( \frac{P}{4.16 - P} \right) \\ -0.3 &= \frac{4.16 - P}{5.5 - P} \rightarrow -0.165 + 0.03P = 4.16 - P & 1.03P &= 4.325 \\ P &= 4.199 \end{aligned}$$

$$\begin{aligned} \text{Tax} &= 1.34 \\ CB &= (5.5 - 4.199)(52,367) \approx 67.12m \\ PB &= (4.199 - 4.16)(52,367) \approx 2.04m \end{aligned}$$

- 5) How sensitive are your answers to modest errors in estimates of the elasticities of demand and supply?

The elasticity of demand is relatively small, so it is less sensitive to small changes while the elasticity of supply is a larger number and therefore more sensitive to small changes.

- 6) Do you think the tax creates a DWL or improves efficiency? Why?

I'm not really sure if it creates a DWL or improves efficiency. I can't imagine that raising the tax is very efficient. Most people who smoke are addicted and will continue to purchase cigarettes no matter the cost.

Worked w/ Austin  
Passed Solution Review

Demand for Gizmos:  $q = 6 - .5p + .0002I$

$$I = \text{Income} = 60k$$

$$\begin{aligned} \text{a)} Q &= 6 - .5P + .0002(60k) \\ Q &= 6 - .5P + 12 \\ Q &= 18 - .5P \\ .5P &= 18 \\ P &= 36 \end{aligned}$$

$$\begin{aligned} \text{b)} q &= 6 - .5(10) + .0002(60k) \\ q &= 6 - 5 + 12 \\ q &= 18 - 5 \\ q &= 13 \end{aligned}$$

$$\text{c)} \frac{\Delta Q}{\Delta P} = \frac{6 - 13}{10 - 12} = \frac{-7}{2} = -3.5$$

$$\begin{aligned} \text{d)} \frac{1}{2} \cdot 13 \cdot (36 - 10) &= \\ \frac{1}{2} \cdot 13 \cdot 26 &= \\ 169 &= \end{aligned}$$

$$\begin{aligned} \text{e)} q &= 6 - .5(12) + .0002(60k) \\ q &= 6 - 6 + 12 \\ q &= 12 \end{aligned}$$

$$\begin{aligned} \frac{1}{2} \cdot 12 \cdot (36 - 12) &= 6 \cdot 24 = 144 \\ 169 - 144 &= 25 \\ \text{The loss in CS is } 25 & \end{aligned}$$

$$\begin{aligned} \text{f)} Q &= 6 - .5P + .0002(80k) \\ Q &= 6 - .5P + 16 \\ Q &= 22 - .5P \\ .5P &= 22 \\ P &= 44 \end{aligned}$$

$$\begin{aligned} q &= 6 - .5(10) + .0002(80k) \\ q &= 6 - 5 + 16 \\ q &= 17 \end{aligned}$$

$$\begin{aligned} q &= 6 - .5(12) + 16 \\ q &= 6 - 6 + 16 \\ q &= 16 \end{aligned}$$

$$\frac{1}{2} \cdot 17 \cdot (44 - 10) = 8.5(34) = 289$$

$$\frac{1}{2} \cdot 16 \cdot (44 - 12) = 8 \cdot 32 = 256$$

$$289 - 256 = 33$$

The loss in CS is 33

# Worked w/ River Passed Solution review

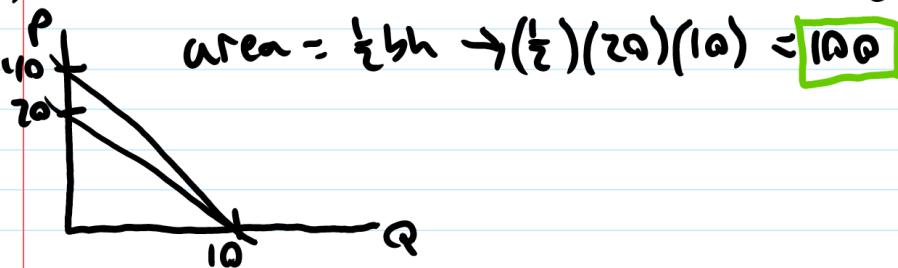
2. At the current market equilibrium, the price of a good equals \$40 and the quantity equals 10 units. At this equilibrium, the price elasticity of supply is 2.0. Assume that the supply curve is linear.
- Use the price elasticity and market equilibrium to find the supply curve.  
(Hint: the supply curve has the following form:  $q = a + (\Delta q/\Delta p)p$ . First, find the value of  $\Delta q/\Delta p$ ; then, find the value of  $a$ .)
  - Calculate the producer surplus in the market.
  - Imagine that a policy results in the price falling from \$40 to \$34. By how much does producer surplus fall?
  - What fraction of the lost producer surplus is due to the reduction in the quantity supplied and what fraction is due to the fall in price received per unit sold?

$$a) \frac{\epsilon}{\epsilon} = \frac{\Delta q}{\Delta p} \cdot \frac{P}{q} \rightarrow 2 = \frac{\Delta q}{\Delta p} \cdot \frac{40}{10} \rightarrow 2 = \frac{\Delta q}{\Delta p} \cdot 4 \rightarrow \frac{\Delta q}{\Delta p} = .5$$

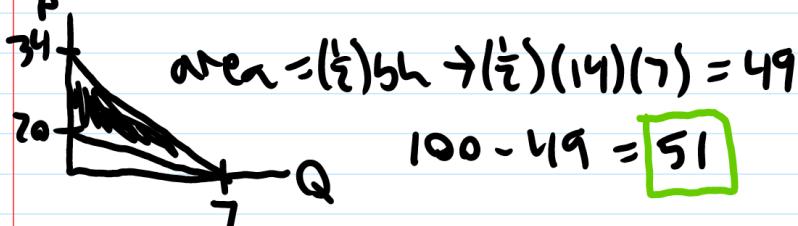
$$q = a + .5p \rightarrow 10 = a + .5(40) \rightarrow 10 = a + 20 \rightarrow a = -10$$

Supply Schedule:  $q = -10 + .5p$

$$b) q = -10 + .5p \rightarrow .5p = 10 + q \rightarrow p = 20 + 2q$$



$$c) q = -10 + .5(34) \rightarrow q = -10 + 17 \rightarrow q = 7$$



$$d) PS = (6 \cdot 7) + (\frac{1}{2} \times 6) / 7 \\ PS = 42 + 21 \\ PS = 63$$



Price loss due to  $q: \frac{21}{63} = 1/3$   
Price loss due to  $p: \frac{16}{63} = 2/3$

Changes in SS are areas, usually triangles or trapezoids

### 4.1 Knowing the slope or Price elasticity of demand

MPC - Marginal Private Cost  
MSC - Marginal Social Cost

#### 4.1.1 Linear demand curve

$$q = \alpha_0 + \alpha_1 p \text{ where: } q = \text{quantity at Price } P$$

Quantity if  $P=0$   
 $\alpha_1$ , change in  $q$ , if price increases by 1

$$\epsilon_d = \alpha_1 \frac{P}{q} \rightarrow \alpha_1 = \epsilon_d \frac{P}{q}$$

Construction of a linear demand curve to measure changes in SS requires an estimate of slope or  $\epsilon_d$  and  $P$  and  $q$  of  $\epsilon_d$

#### 4.1.2 Constant elasticity demand curve

$$q = \beta_0 p^{\beta_1} \rightarrow \ln(q) = \ln(\beta_0) + \beta_1 \ln(p)$$

$$\text{Area} = \left( \frac{1}{\beta_0} \right)^{1/\beta_1} \left( \frac{q_i^P - q_0^P}{P} \right) \text{ where } P = 1 + (\beta_1)$$

### 4.2 Extrapolating from a few observations

#### 4.3 Econometric Estimation w/ many observations

Linear regression is a good starting point

##### 4.3.1 Model specification

$$q = f(p, I, T)$$

↓  
Temperature  
↓ Income  
↓ Price

OLS = ordinary least squares

##### 4.3.2 Types of Data

Cross-Sectional vs Time Series

↳ Single or multiple units      ↳ repeated on same unit

GLS = generalized least squares

Can mix cross-sectional + time series

##### 4.3.3 Identification

Endogenous Variables: Variables determined simultaneously  
Exogenous Variables: Variables that are fixed or determined outside the model

##### 4.3.4 Confidence Intervals

##### 4.3.5 Prediction vs Hypothesis testing

### Appendix 4A Multiple Regression

Independent = explanatory

$\beta_0$  = intercept parameter or constant

$R^2$  = square of correlation between actual + predicted value of dependent variable

Multicollinearity = explanatory var can be written as linear combo of others

## Intro

Change in allocative efficiency:

$$\Delta SS = \Delta SS_{\text{I}} + \Delta SS_{\text{S}}$$

↓      ↓      ↓  
output input secondary markets

### 5.1 Shadow Pricing

When no market price exists or it is distorted,  
shadow pricing exists

### 5.2 Valuing impacts in efficient markets

#### 5.2.1 Direct increase in supply available to consumers

#### 5.2.2 Direct reduction in costs to producers

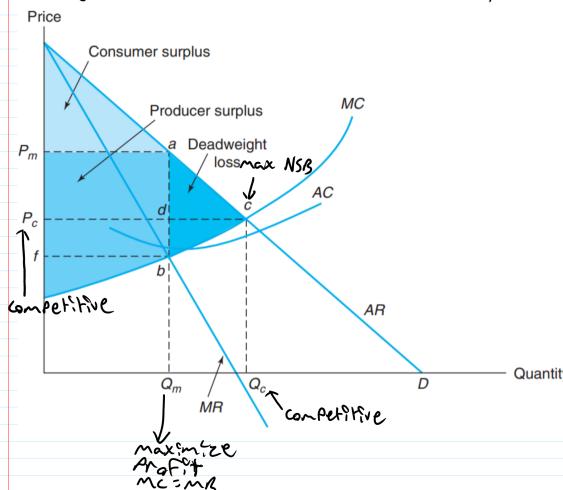
### 5.3 Valuing impacts in distorted markets

If output market becomes distorted, hard to determine  
correct surplus changes

- five types of failures:
- monopoly
- information asymmetry
- externalities
- public goods
- addictive goods

#### 5.3.1 Monopoly

results in OOL and reduces SS  
Marginal Revenue (MR) is below demand (AR)



$$SS = CS + PS$$

Monopolist maximizes profits

#### 5.3.2 Natural monopoly

Natural monopoly enjoys economies of scale over a wide range of outputs

Large fixed costs relative to variable costs

$MC < AC$  over range

#### 5.3.3 Information asymmetry

Government can intervene + provide missing info

- 1) Search goods: products with researchable characteristics
- 2) Experience goods: consumers can only gain full knowledge after purchasing
- 3) Post-experience goods: consumption does not necessarily reveal information

#### 5.3.4 Externalities

- an effect that production or consumption has on third parties
- by product for which there is no market
- problem of "missing markets"
- negative imposes social costs
- positive produces benefits
- to reduce OOL from negative externalities, increase taxes

#### 5.3.5 Public goods

- non-excludable goods → everyone has access
- pure public goods are non-excludable + non-rivalrous
- non-excludable = jointness in supply
- can cause free-rider problem
- non-rivalry → one's use does not exclude another's
- non-rivalry causes market failure
- toll goods are non-rivalrous + excludable
- open-access resources are non-excludable + non-rivalrous

#### 5.3.6 Addictive goods

- rational addiction When consumers take consequences into account
- negative interpersonal externalities - harm imposed on future self b/c current self

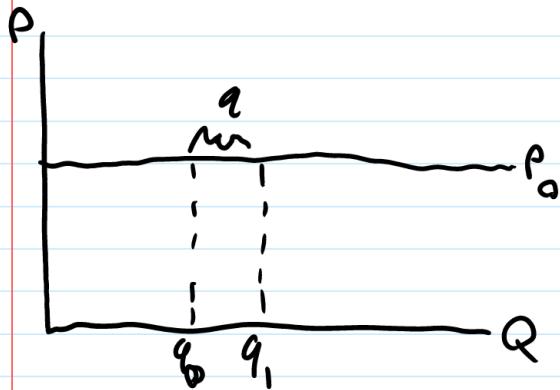
Output + Input markets

Efficient or distorted markets

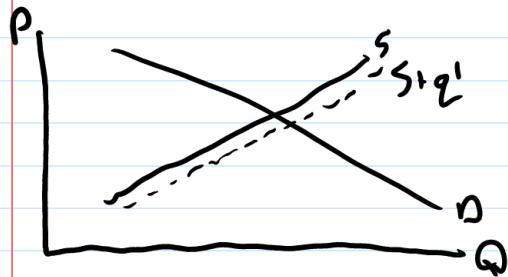
Primary or Secondary markets

## 5.2 Efficient Output Markets - Introduction

Friday, September 11, 2020 11:57 AM



a)  $q'$  sold @ mkt prfce  
 $\Delta GS = P \cdot q'$

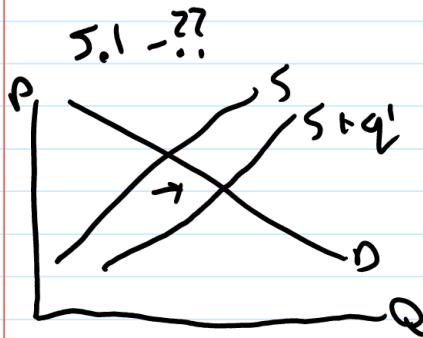


$q/q'$  is tiny

b) govt gives it away

- best case  $\Delta GS = P \cdot q'$
- resale possible
- worst case  $\Delta GS \leq P \cdot q'$
- resale not possible

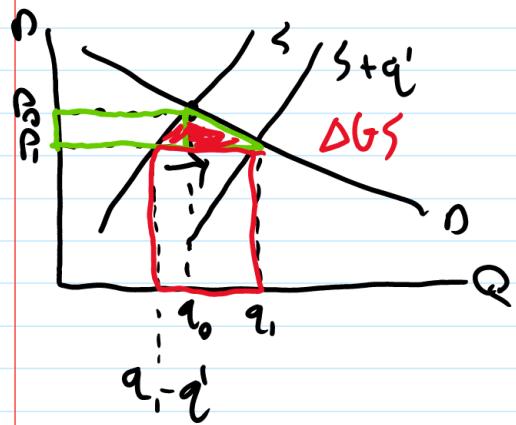
When things are free, they're hard to value



5.1 - ??

### 5.3 Efficient Output Markets - Direct Supply

Friday, September 11, 2020 12:05 PM



$$\Delta PS = -(P_0 - P_1) \cdot (q_1 - q_0) = -\frac{1}{2}(P_0 - P_1)(q_0 - q_1 + q_1)$$

$$\Delta CS = (P_0 - P_1)q_0 + \frac{1}{2}(P_0 - P_1)(q_1 - q_0)$$

$$\Delta PS + \Delta CS = q_1 \cdot (P_0 - P_1) \cdot \frac{1}{2}$$

$$\Delta GS = P_1 \cdot q_1$$

- assuming Gov't sells at market price  
↳  $P_1$

$$\Delta SS = \alpha_c \Delta CS + \alpha_p \Delta PS + (1 + MEBT) \cdot \Delta GS$$

$$\alpha_c = \alpha_p = 1$$

$$= q_1 \cdot (P_0 - P_1) \cdot \frac{1}{2} + (1 + MEBT) \cdot P_1 \cdot q_1$$

assume given away, no sale possible

$$\Delta GS = 0$$

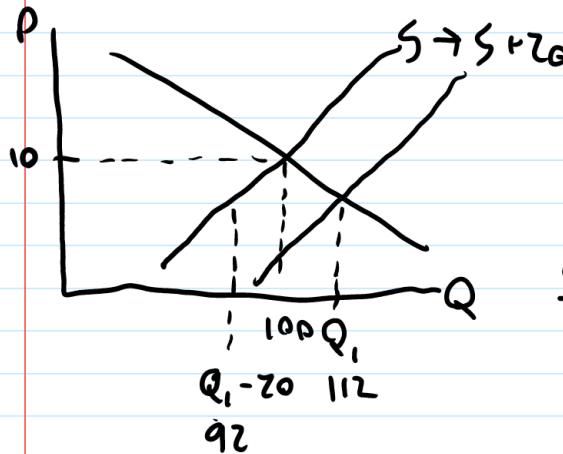
$\Delta CS$  is higher by  $P_1 \cdot q_1$

- given away, no result

## 5.4 Efficient Output Markets - Direct Supply - Example

Friday, September 11, 2020 12:35 PM

$$\left. \begin{array}{l} \frac{\partial Q_1}{\partial P_1} = -3 \\ \frac{\partial Q_2}{\partial P_1} = 2 \end{array} \right\} \Rightarrow \frac{\partial Q_1}{\partial P_1} + \frac{\partial Q_2}{\partial P_1} = -3 + 2 = -1 \quad P_1 = 10, Q_1 = 100, Q_2 = 20$$



$$\frac{Q_1 - 100}{P_1 - 10} \cdot \frac{10}{100} = -3 = \frac{\Delta Q_1}{\Delta P_1}$$

$$\frac{Q_2 - 20 - 100}{P_1 - 10} \cdot \frac{10}{100} = 2 = \frac{\Delta Q_2}{\Delta P_1}$$

$$\frac{Q_1 - 100}{Q_2 - 112} = -1.5$$

$$Q_1 = 280/2.5 = 112$$

$$\frac{12}{P_1 - 10} \cdot \frac{10}{100} = -3 = \frac{\Delta P_1}{\Delta Q_1}$$

$$(100 \cdot 3.6) + \frac{1}{2} \cdot 12(10 - 6.4)$$

$$360 + 6 \cdot 3.6$$

$$381.6 = \Delta CS$$

$$\Delta PS = -3 \cdot 6 \cdot 92 =$$

$$\Delta GS = 6.4 \cdot 12 =$$

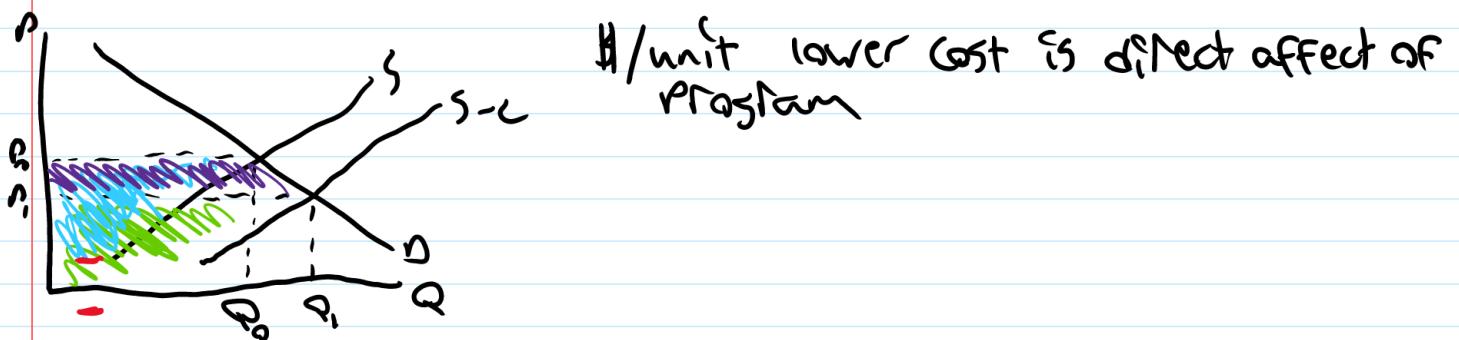
$$\Delta SS = 381.6 - 345.6 + (1 - MGRB) \cdot 76.8 = 132$$

$\downarrow$   
25

$$\Delta SS = \Delta CS - \Delta PS + (1 - MGRB) \cdot \Delta GS$$

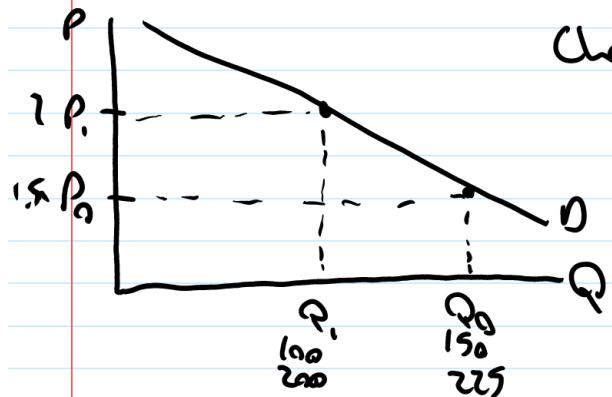
## 5.5 Efficient Output Markets - Producer Cost Reductions

Friday, September 11, 2020 12:58 PM



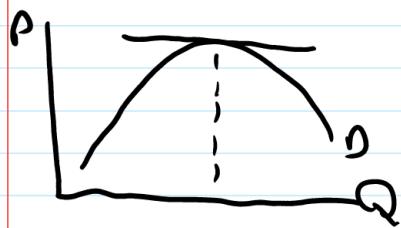
## 5.6 Monopoly Review - Demand and Revenue

Saturday, September 12, 2020 6:26 PM



choose to sell at price or by quantity  
but not both

$$\Pi = P(Q) \cdot Q - C(Q)$$



$$R = P(Q) \cdot Q \rightarrow \frac{dR}{dQ} = \frac{dP}{dQ} \cdot Q + P(Q) \cdot 1$$

$$MR = P + \frac{dP}{dQ} \cdot Q = P(1 + \frac{dP}{dQ} \cdot \frac{Q}{P})$$

↓  
Inverse of  $\frac{dP}{dQ}$

$$MR = P(1 + 1/3)^Q$$

## 5.7 Monopoly Review - Profit Maximization

Saturday, September 12, 2020 7:12 PM

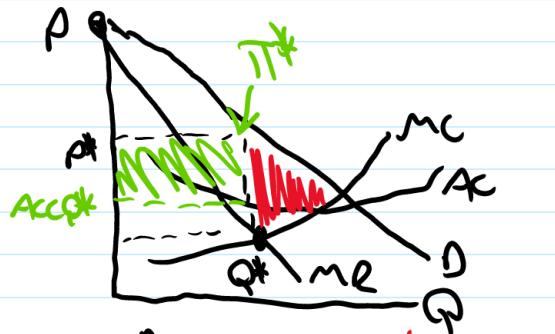
$$\Pi = P(Q) \cdot Q - C(Q)$$

$$\frac{d\Pi}{dQ} = \frac{dP}{dQ} \cdot Q + P - \frac{dC}{dQ} = 0$$

$$MR = MC$$

10  
7      5      Yes?  
Sell?  
12      NO

MR  $\neq$  MC? Sell!



$$P^* = a - bQ$$

$$MR = a - 2bQ$$

$Q^* \rightarrow \text{Loss}$

$$P^* = a - bQ$$

$$L = P \cdot Q = (a - bQ)Q$$

$$\frac{dL}{dQ} = -b \cdot Q + a - bQ = a - 2bQ$$

MR is twice as steep as D

$$MR = a - 2bQ = P[1 + \frac{1}{3}Q]$$

Acc\*Q\* = Average cost of Q\*

$$\text{Profit/unit} = P^* - Acc*Q^*$$

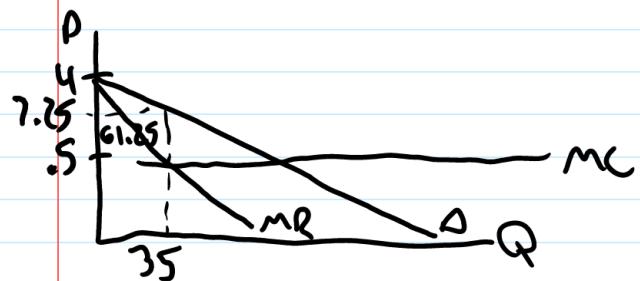
## 5.8 Monopoly Review - Numeric Example

Saturday, September 12, 2020 7:29 PM

$$P = 4 - .05Q$$

$$C(Q) = F + CQ$$

$$\begin{aligned}MR &= 4 - .1Q \\.5 &= 4 - .1Q \\3.5 &= .1Q \\Q &= 35\end{aligned}$$



$$\begin{aligned}P &= 4 - .05 \cdot 35 \\P &= 2.25\end{aligned}$$

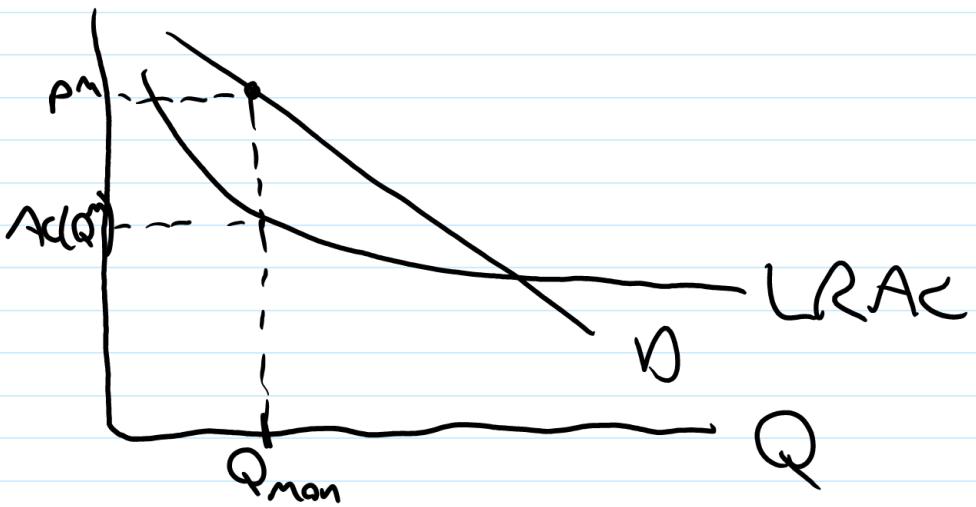
$$\Pi = 1.75 \cdot 35 = \$1.25$$

## 5.9 Monopoly Review - Why do they persist

Saturday, September 12, 2020 7:35 PM

- 1)  $\pi^e > 0 \rightarrow$  Should attract entry  $\rightarrow$  Barrier to entry
- 2)  $\text{OVL} > 0 \rightarrow$  Society wants to get rid of monopoly

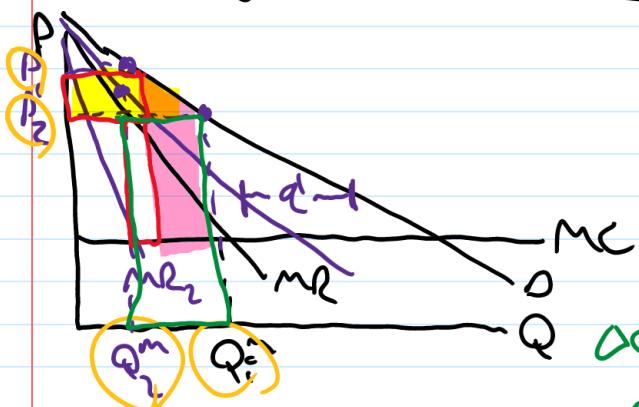
Natural Monopoly Utilities



## 5.10 Valuing Direct Supply in Monopoly Markets

Thursday, September 17, 2020 4:08 PM

### Valuing Impacts in Monopolized Markets



Program provides  $q'$ , sold at market price

$D - q' = \text{Residual demand}$

$$\Delta GS = P_2^m \cdot q'$$

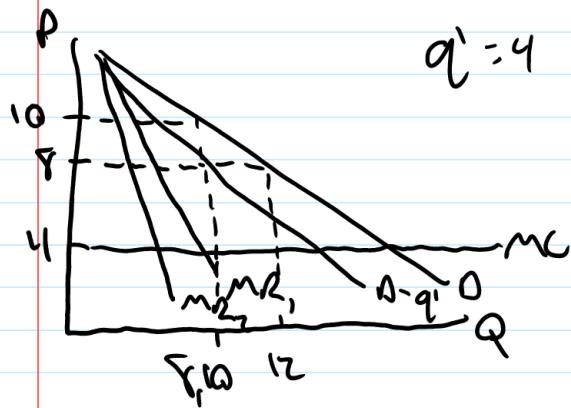
$$\Delta CS = (P_1^m - P_2^m) \cdot Q_1^m + \frac{1}{2} (P_1^m - P_2^m) (Q_2^m + q' - Q_1^m)$$

$$\Delta PS = (P_1^m - MC) \cdot Q_1^m - (P_2^m - MC) Q_2^m$$

= DWL

## 5.11 5.12 Valuing Direct Supply in Monopoly Markets - Examples

Thursday, September 17, 2020 4:28 PM



$$q^* = 4$$

$$\Delta CS = (10 - 8) \cdot 10 + \frac{1}{2} (10 - 8)(12 - 10) = 22$$

$$M\Gamma\beta = .2$$

$$\Delta PS = (10 - 4)(10) - (8 - 4)(8) = -28$$

$$\Delta GS = 22 - 28 + 1.2 \cdot 32$$

$$\Delta GS = (8)(4) = 32$$

$$P_0 = 10, Q_0 = 10, q^* = 4, \gamma^* = -2$$

$$-2 = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q} \Rightarrow -2 = \frac{Q - 10}{P - 10} \cdot \frac{10}{10} \Rightarrow -2(P - 10) = Q - 10 \Rightarrow 3Q = Q - 2P \\ Q = 3Q - 2P \\ P = 15 - .5Q$$

$$\text{Individual demand} \Rightarrow Q - q^* \Rightarrow Q^{\text{res}} = 3Q - 2P - 4 = 26 - 2P$$

$$MR = 2P = 26 - Q \Rightarrow P = 13 - .5Q$$

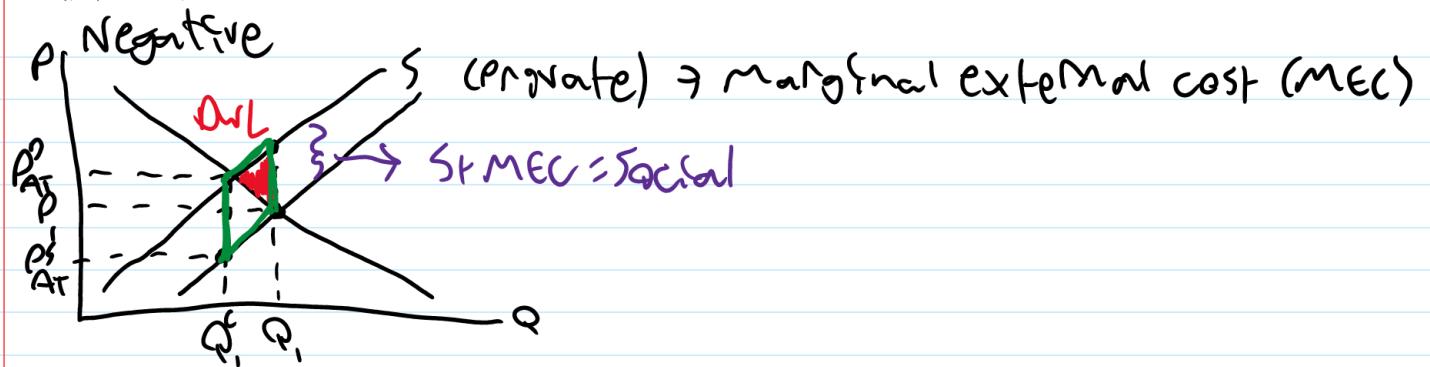
$$MR = MC \Rightarrow MR = P(1 + \frac{1}{\gamma}) = MC \\ 10(1 + \frac{1}{-2}) = MC \\ 10(\frac{1}{2}) = MC \\ MC = 5$$

$$13 - Q = 5 \\ Q = 8$$

$$P = 13 - \frac{1}{2} \cdot 8 = 9$$



Embodies Pareto Efficiency



tax = MEC  $\rightarrow$   $Q_{\text{eff}}$   $\rightarrow$  eliminate DWL

$$P_{AT}^0 - P_{AT}^S = t = MEC$$

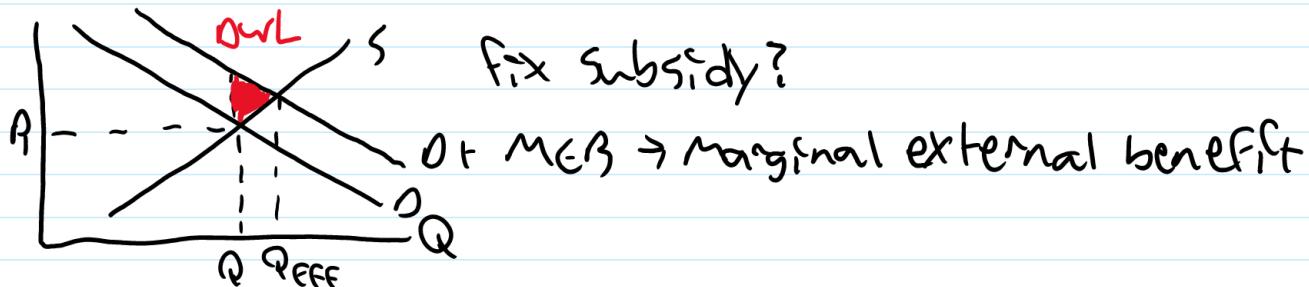
$$\Delta CS = -(P_{AT}^0 - P_i) \cdot Q_{\text{eff}} - \frac{1}{2}(P_{AT}^0 - P_i)(Q_i - Q_{\text{eff}})$$

$$\Delta PS = (P_i - P_{AT}^S) \cdot Q_{\text{eff}} - \frac{1}{2}(P_i - P_{AT}^S)(Q - Q_{\text{eff}})$$

$$\Delta GS = t \cdot Q_{\text{eff}} = MEC \cdot Q_{\text{eff}}$$

$$\Delta \text{External Value} = MEC \cdot (Q_i - Q_{\text{eff}}) \quad \text{External Gain}$$

## Positive Externalities



## 5.14 Distorted Output Markets - Addiction

Saturday, September 19, 2020 2:16 PM

Person is resistant to treatment and adds value to drugs

Addicts are 2 people and play against themselves

Who was standing?

## 5.15 Distorted Output Markets - Asymmetric Information

Saturday, September 19, 2020 2:20 PM

All markets are uniquely distorted

- moral hazard  
"Peltzman Effect" → People Push limits
- adverse selection  
"market for lemons" → (used cars)
- Insider information

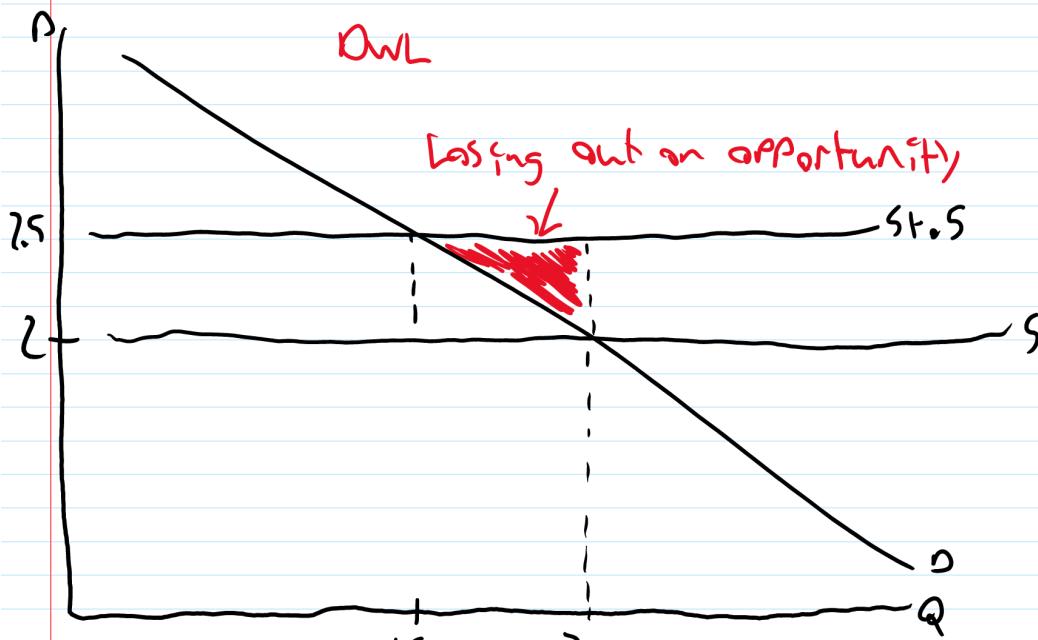
## 5 Extra Problems

Friday, September 11, 2020 2:02 PM

Suppose the current price of gasoline is \$2 per gallon, at which price 20 million gallons are consumed daily. The elasticity of demand is -0.8. Suppose that in addition to the private costs of production and sales born by sellers, each gallon of gasoline consumed releases carbon and pollutants into the air imposing a burden on the rest of society equivalent to \$0.50 per gallon. Assume this is a constant cost industry and that the METB is 0.2.

- 1) Over consumption of gasoline will lead to a DWL. How much overconsumption is there?  
Hint: You must first calculate the allocatively efficient quantity, which would balance the full costs against the benefits of consumption.
- 2) Illustrate.
- 3) How big is the DWL? Include it in the illustration.
- 4) How might the DWL be corrected?
- 5) All things considered, what would be the net benefit of that correction?

$$\left. \begin{array}{l} \frac{\partial^d}{\partial P} = -0.8 \\ Q = 20m \\ P = 2 \\ METB = 0.2 \end{array} \right\} =$$



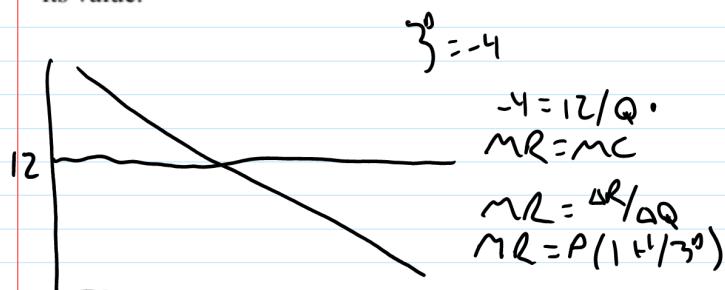
$$-0.8 = \frac{\partial Q}{\partial P} \cdot \frac{2}{20m} \Rightarrow 16m$$

$$-0.8 = \frac{\Delta Q}{\Delta P} \cdot \frac{2}{20m} \Rightarrow -0.8 = \Delta Q = -4m$$

$$\frac{1}{2}(0.5)(-1) = -0.25 = \text{DWL}$$

IF DWL is negative, flip triangle to above demand  
NSB of 50¢ tax

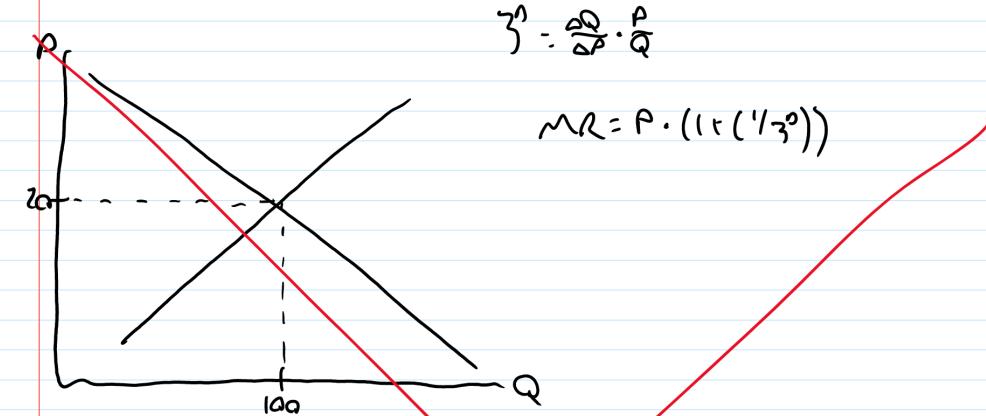
1. Suppose a profit maximizing monopolist is charging a price of \$12, and the best available estimate of the elasticity of demand is -4. If the monopolist's marginal cost is constant, estimate its value.



# Passed Solution Review

A profit maximizing monopolist charges \$20 and sells 100 units. Elasticity of demand is -2.5. The monopolist's cost function is  $C(Q) = F + cQ$  where  $F$  is a fixed cost and  $c$  is the constant per unit variable cost.

- What is the per unit variable cost?
  - What is the highest fixed cost could be if the monopolist has not chosen to exit the industry?
  - Write a linear approximation of both demand and inverse demand around the current price.
- Hint, use the formula for point elasticity and the current price and quantity, then rearrange for  $Q$  to get demand and  $P$  to get inverse demand.



a)  $\omega_{100} = .2$  dollars per unit

$$\gamma^0 = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q} \rightarrow -2.5 = \frac{Q_1 - Q_0}{P_1 - P_0} \cdot \frac{20}{100} = \frac{Q_1 - 100}{P_1 - 20} \cdot \frac{20}{100}$$

If  $F = 20$ , then no profit can be made. But so long as  $F < 20$ , then at least some profit can be made

$$\gamma^0 = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

$$-2.5 = \frac{Q_1 - Q_0}{P_1 - P_0} \cdot \frac{P}{Q_0} \rightarrow -2.5 = \frac{Q_1 - 100}{P_1 - 20} \cdot \frac{20}{100} \rightarrow -2.5 = \frac{Q - 100}{P - 20} \cdot .2$$

$$-12.5 = \frac{Q - 100}{P - 20} \rightarrow -12.5(P - 20) = Q - 100 \rightarrow -12.5P + 250 + 100 = Q$$

$$Q = -12.5P + 350$$

$$Q - 350 = -12.5P \rightarrow P = \frac{Q - 350}{-12.5} \rightarrow P = 28 - .08Q$$

## Restarted vs Austin + River

a)  $y = mx + b$   
 ~~$P = \gamma^0 Q + b$~~   
 ~~$20P = -2.5Q + 100$~~   
 ~~$P = -12.5Q + 5$~~

$$MR = P(1 + 1/\gamma^0) = MC$$

$$MR = 20(1 + 1/-2.5) = MC$$

$$MR = 20 + 20/-2.5 = MC$$

$$MR = 12 = MC$$

**Variable cost = 12**

b)  $\Pi = \text{Revenue} - \text{Cost}$   
 $\Pi = (20 \cdot 100) - (F + cQ)$   
 $\Pi = 2000 - F + (12 \cdot 100)$   
 $\Pi = 2000 - F + 1200$   
 $F = 800$

c) It turns out I got this right by myself!

$$\gamma^0 = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

$$-2.5 = \frac{Q_1 - Q_0}{P_1 - P_0} \cdot \frac{P}{Q_0} \rightarrow -2.5 = \frac{Q_1 - 100}{P_1 - 20} \cdot \frac{20}{100} \rightarrow -2.5 = \frac{Q - 100}{P - 20} \cdot .2$$

$$-12.5 = \frac{Q - 100}{P - 20} \rightarrow -12.5(P - 20) = Q - 100 \rightarrow -12.5P + 250 + 100 = Q$$

$$Q = -12.5P + 350$$

$$Q - 350 = -12.5P \rightarrow P = \frac{Q - 350}{-12.5} \rightarrow P = 28 - .08Q$$

Worked w/ Alex, Austin, + River

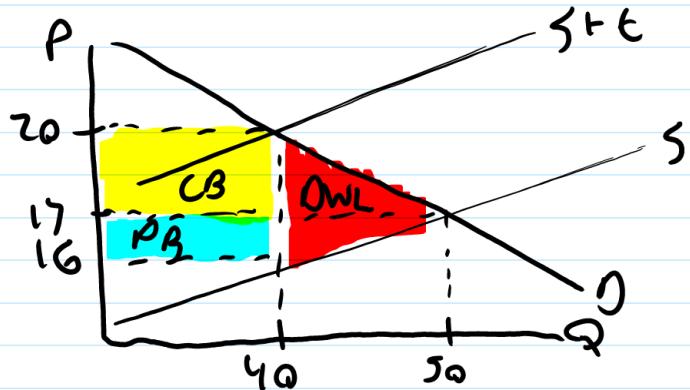
At the current market equilibrium, price is \$17 and quantity is 50. A tax of 25% is imposed, after which the price paid by consumers including the tax is \$20 and the new equilibrium quantity is 40. Sketch a figure illustrating the equilibrium before and after the tax. Calculate tax revenue, the producer burden, the consumer burden, and the excess burden. Label each.

Hint: If  $\tau$  is the tax rate, the price paid by consumers is  $(1+\tau)$  times the price received by suppliers once the tax is remitted to the government.

$$P = 17 \quad Q = 50 \quad t = 25\%$$

$$P+t = 20 \quad Q-t = 40$$

Pasted Solution Review



$$\text{Tax Revenue: } (20 - 17) \cdot 40 = 4 \cdot 40 = \$160$$

$$\text{Producer burden: } (40 - 0) \cdot (17 - 16) = 40 \cdot 1 = \$40$$

$$\begin{aligned} P_p &= 15.75 \\ P &= 17 \\ P_c &= 20 \end{aligned}$$

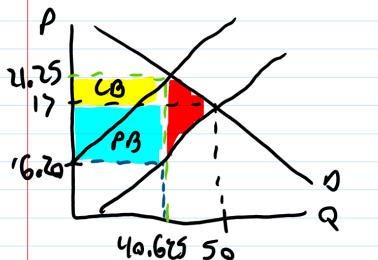
$$\begin{aligned} Q_p &= 40 \\ Q_e &= 50 \\ Q_c &= 40 \end{aligned}$$

$$\text{Consumer burden: } (20 - 17) \cdot (40 - 0) = 3 \cdot 40 = \$120$$

$$\begin{aligned} \text{OWL: } &\frac{1}{2}(50-40)(17-16) + \frac{1}{2}(50-40)(20-17) = \frac{1}{2}(10)(1) + \frac{1}{2}(10)(3) \\ &= 5 + 15 = 20 \end{aligned}$$

Worked w/ Alex, Austin, &amp; River

At the current market equilibrium, price is \$17 and quantity is 50. A tax of 25% is imposed. The elasticity of demand is -0.75 and the elasticity of supply is 4. Find the new equilibrium quantity, the after tax price paid by consumers, the after tax price received by suppliers, tax revenue, the producer burden, the consumer burden, and the excess burden. Draw a figure to illustrate. Hint: It will help to sketch the figure noting what you know and what you need to figure out before starting the algebra!



$\eta^d = -0.75$  Passed Solution Review  
Big Yices

$$\text{Equilibrium Quantity: } \Delta P = 17 + .25 = 4.25 \quad \left\{ \begin{array}{l} \eta^d = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q} \\ (\eta^d \cdot Q_1) / (P_1 \cdot \eta^d) = \eta^d \end{array} \right. \quad \text{Should've done } (\eta^d \cdot Q_1) / (P_1 \cdot \eta^d) = \eta^d$$

$$-0.75 = \frac{\Delta Q}{4.25} \cdot \frac{17}{50} \rightarrow -\frac{2}{4} \cdot \frac{50}{17} = \frac{\Delta Q}{4.25} \rightarrow -\frac{150}{68} = \frac{\Delta Q}{4.25} \rightarrow \Delta Q = -9.375$$

$Q_2 = 40.625$

That mistake comes

$$\text{After tax Prod: } P_2 = \frac{1.25Q}{1.25P} \rightarrow \% \Delta P = \frac{(-9.375/50)}{4} \rightarrow \% \Delta P = -0.7969$$

$P_2 = 16.203$

$$\text{After tax consumer: } 17 + 1.25 = 21.25$$

$$CB: (40.625)(21.25 - 17) = 40.625 \cdot 4.25 = 172.65625$$

$$PB: (40.625)(17 - 16.203) = 40.625 \cdot 0.797 = 32.378125$$

$$\text{Tax Revenue: } 172.65625 + 32.378125 = 205.03$$

$$OVL: \frac{1}{2}(50 - 40.625)(17 - 16.2) + \frac{1}{2}(50 - 40.625)(21.25 - 17)$$

$$= \frac{1}{2}(9.375)(.8) + \frac{1}{2}(9.375)(4.25) = 3.75 + 19.92 = 23.67$$

Using  $\eta^d$ :

$$\frac{Q-SQ}{SQ} / \frac{P_d - 17}{17} = -0.75 \rightarrow Q = 17.5 - 2.125P_d$$

Using  $\eta^s$

$$\frac{Q-SQ}{SQ} / \frac{P_s - 17}{17} = 4 \rightarrow Q = 150 + 11.76P_s$$

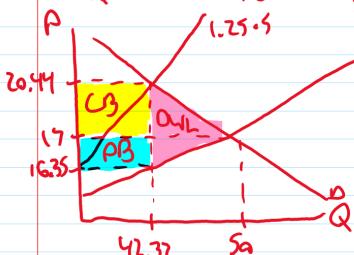
Therefore...  $1.75P_s = P_d$

Solving w/ substitution

$$-150 + 11.76P_s = 17.5 - 2.125P_s \rightarrow P_s = 16.35$$

$$P_d = 1.75P_s \rightarrow P_d = 1.75 \cdot 16.35 \rightarrow P_d = 20.44$$

$$Q = -150 + 11.76 \cdot 20.44 \rightarrow Q = 42.32$$



$$\text{Revenue} = .25 \cdot 16.35 \cdot 42.32 = 173.03$$

$$CB = (20.44 - 17) \cdot 42.32 = 145.69$$

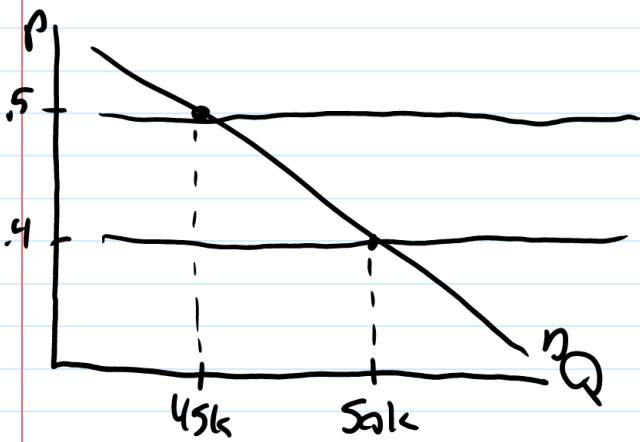
$$PB = (17 - 16.35) \cdot 42.32 = 27.34$$

$$OVL = CB = (20.44 - 16.35)(50 - 42.32)/2 = 15.69$$

# Passed Solution Review

Suppose the government is considering an increase in the toll on a certain stretch of highway from \$.40 to \$.50. At present, 50,000 cars per week use that highway stretch; after the toll is imposed, it is projected that only 45,000 cars per week will use the highway stretch.

Assuming that the marginal cost of highway use is constant (i.e., the supply curve is horizontal) and equal to \$.40 per car, what is the social change in surplus attributable to the increase in the toll? (Hint: the toll increase will cause the supply curve, not the demand curve, to shift.)



$$\Delta SS = \frac{1}{2}(.5 - .4)(50 - 45)$$

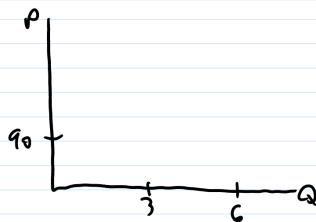
$$= \frac{1}{2}(.1)(5)$$

$$=.05 \cdot 5$$

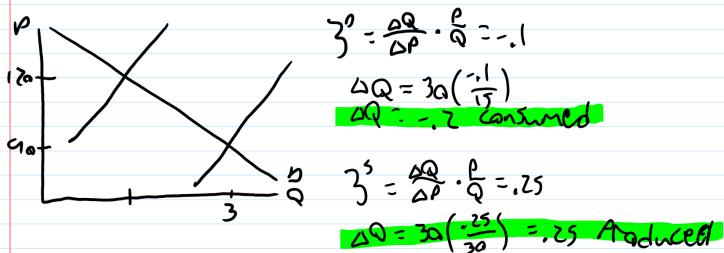
$$=.25k = \boxed{25k = \Delta SS}$$

## Passed Solution review

A country imports 3 billion barrels of crude oil per year and domestically produces another 3 billion barrels of crude oil per year. The world price of crude oil is \$90 per barrel. Assuming linear curves, economists estimate the price elasticity of domestic supply to be 0.25 and the price elasticity of domestic demand to be 0.1 at the current equilibrium.



- a. Consider the changes in social surplus that would result from imposition of a \$30 per barrel import fee on crude oil that would involve annual administrative costs of \$250 million. Assume that the world price will not change as a result of the country imposing the import fee, but that the domestic price will increase by \$30 per barrel. Also assume that only producers, consumers, and taxpayers within the country have standing. Determine the quantity consumed, the quantity produced domestically, and the quantity imported after the imposition of the import fee. Then estimate the annual social benefits of the import fee.



$$Q_d = 6 - 0.2 \cdot 75 = 5.5$$

$$Q_s = 3 + 0.25 \cdot 75 = 3.25$$

$$Q_d - Q_s = Q_T$$

$$5.5 - 3.25 = 2.25$$

*Forgot to do Parts B+C*

- b. Economists have estimated that the marginal excess burden of taxation in the country is 0.25 (see Chapter 3). Reestimate the net social benefits assuming that 20 percent of the increase in producer surplus is realized as tax revenue under the existing tax system. In answering this question, assume that increases in tax revenues less the cost of administering the import fee are used to reduce domestic taxes.

$$CS = -17.5 \text{ b}$$

After tax  $P_s = 75 \text{ b}$   
 Net tax gain = 9.5 b  
 Net tax gain \* MEB = 2.375 b

$$\text{Net benefits} = 16.75 \text{ b}$$

- c. The reduction in the country's demand for imports may affect the world price of crude oil. Assuming that the import fee reduces the world price from \$90 to \$80 per barrel, and thus, the after-tax domestic price is \$80 + \$30 = \$110 per barrel, a net increase in domestic price of \$20 per barrel, repeat the analysis done in parts a and b.

$$-0.1 = (\Delta Q / \Delta P)(P/Q) \leftarrow \text{quantity consumed}$$

$$\Delta Q = (-0.1)(\Delta P)(Q/P)$$

$$\Delta Q = (-0.1)(20)(60)/(90)$$

$$\Delta Q = -0.133 \text{ b}$$

Change in domestic supply

$$\Delta Q = (0.25) \Delta P (Q/P)$$

$$\Delta Q = (0.25)(20)(60)/(90)$$

$$\Delta Q = 0.167 \text{ b}$$

$$CS = 17.67 \text{ b}$$

$$P_s \text{ gain} = 61.67 \text{ b}$$

$$\text{Net tax gain} = 10.75 \text{ b}$$

$$\text{Net social benefits} = 47.016$$

## Valuing Impacts in Input Markets

opportunity cost of resources used = cost input markets

### 6.1 Valuing costs in efficient markets

#### 6.1.1 Perfectly elastic supply curves

Small purchases see horizontal supply curves

Reasonable to assume that expenditures for project inputs equal their social costs

#### 6.1.2 Perfectly inelastic Supply Curves

#### 6.1.3 Efficient Markets w/ Noticeable Price Effects

big projects have upward sloping supply curves

### 6.2 Valuing costs in distorted markets

when efficient,  $P = MC$

#### 6.2.1 Purchases at below opportunity costs

Jury stipends per diem

#### 6.2.2 Purchases when inputs are in fixed supply

#### 6.2.3 Hiring unemployed labor

unemployed workers are "in surplus"

Five measures of social cost of hiring  $L$  unemployed workers

$$E < actual < B$$

#### 6.2.4 Hiring labor when Rural $\rightarrow$ urban migration within a developing country is important

Rural  $\rightarrow$  urban for higher wages

$$\begin{aligned} L &= \text{city workforce size} & E &= \text{employed } (L - v) \\ U &= \text{tot unemployed} \end{aligned}$$

$$\text{migrate if } RW < VW(E/L)$$

Urban projects draw urban workers

#### 6.2.5 Purchases from a monopoly

monopoly rents

budgetary expenditures  $>$  social costs

#### 6.2.6 The general rule

opportunity cost = expenditures on inputs - gains in PS or CS

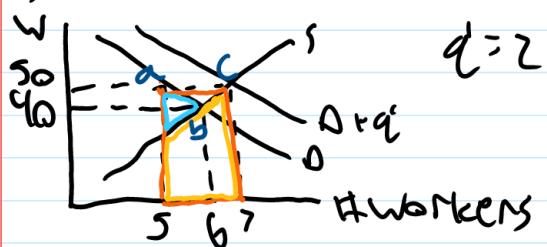
## 6.1 6.2 Opportunity Cost of Inputs in Efficient Markets

Saturday, September 26, 2020 3:59 PM

### Impacts in efficient Input Markets

Land, labor, Capital, materials  $\rightarrow$  opportunity cost?

- 1) No impact on price  $\rightarrow$  budgetary expenditure (I + METB)
- 2) Drive up price



$$\Delta PS = 5Q \cdot (7-5) = 5Q \cdot 2 = 100$$

How much is lost or something else?

Part of social cost

Net value in private market

$$\begin{aligned} \text{Social cost} &= (7-5)(50) - abc + (METB)(7-5)(50) \\ &= (1+METB)(7-5)(50) - abc \end{aligned}$$

$$\Delta CS = (50-40)(5) - \frac{1}{2}(50-40)(6-5) = -55$$

$$\Delta PS = (50-40)(6) + \frac{1}{2}(50-40)(7-6) = 65$$

$$\Delta EXP = (7-5)(50) = 100$$

$$METB = .25$$

$$\Delta SS = 65 - 55 - (1+.25)(100)$$

$$abc = \frac{1}{2}(50-40)(7-5) = 10 = \Delta PS - \Delta CS \rightarrow abc = \Delta PS - \Delta CS$$

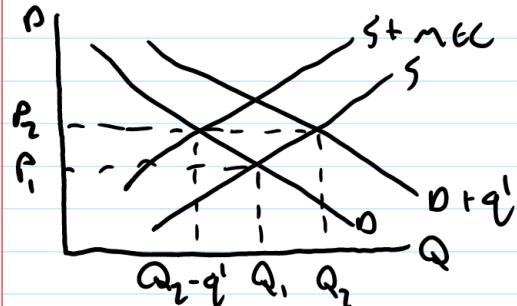
## 6.3 Opportunity Cost of Inputs Purchased in Distorted Markets

Saturday, September 26, 2020 4:27 PM

- Externalities

- Price unchanged  $\rightarrow Q_2 - Q_1 = q'$   
 $\hookrightarrow \text{Cost} = (1 + MEC\beta)(ExP) + (MEC)(q')$   
 $= (1 + MEC\beta)(PS)(q') + (MEC)(q')$

- Price changed



$$\Delta \text{External Cost} = (Q_2 - Q_1)(MEC)$$

$$Q_p^o = Q_2 - q'$$

- Tax to another jurisdiction?

MECB • Revenue Paid

- Legal restrictions on price?

Jury Compensation

\$15/hr but wage = \$50/hr  $\rightarrow$  not compensated  
 $\text{Cost} = 50q' + (MEC\beta)(15)(q')$

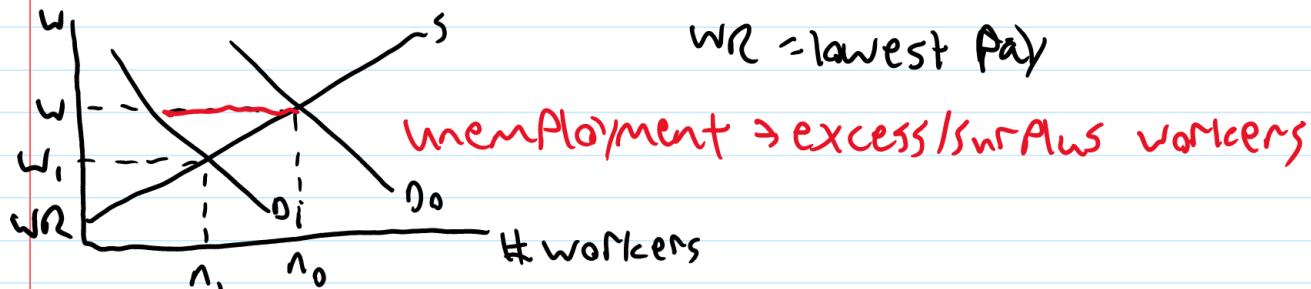
## 6.4 Opportunity Cost of Labor in Markets with High Unemployment

Saturday, September 26, 2020 4:40 PM

Natural rate of unemployment = 2.5-4 %

↳ Lowest unemployment before inflation

Wages are sticky on the way down



SWAG

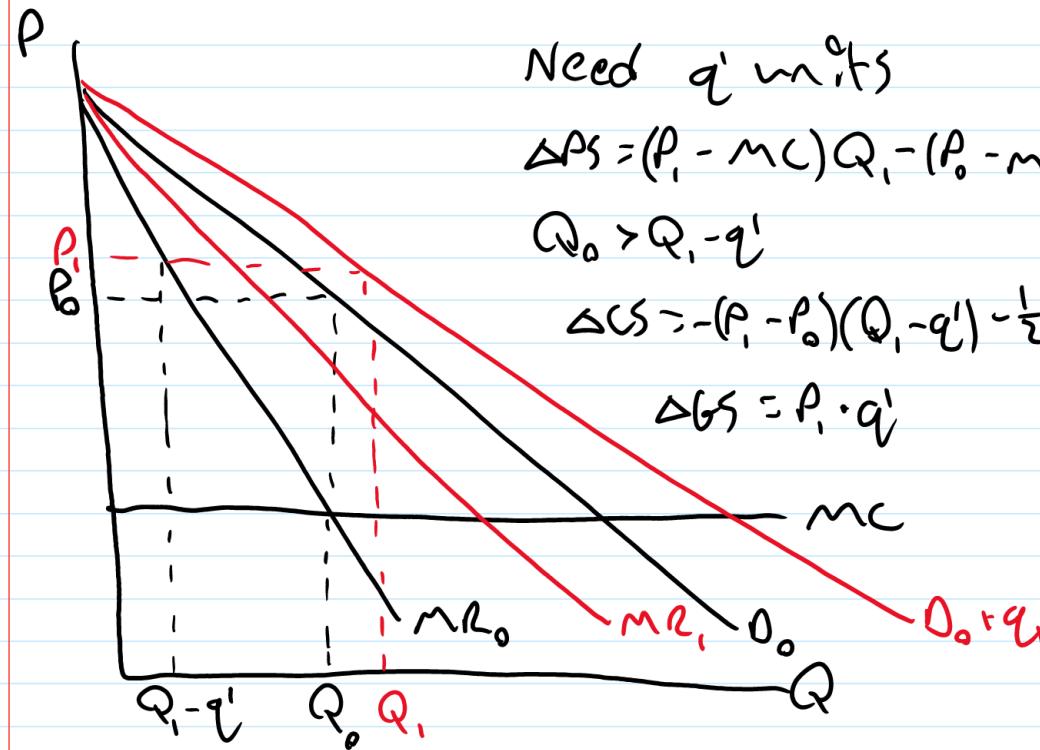
$$\text{OC per worker} \approx (W_1 + W_2)/2 = (50 + 20)/2 = 35$$

$$\text{Social cost} = 35q' + S(q)mer\beta(q')$$

$$WR = ? \quad WR = 0 \quad W/2 = \text{OC/worker}$$

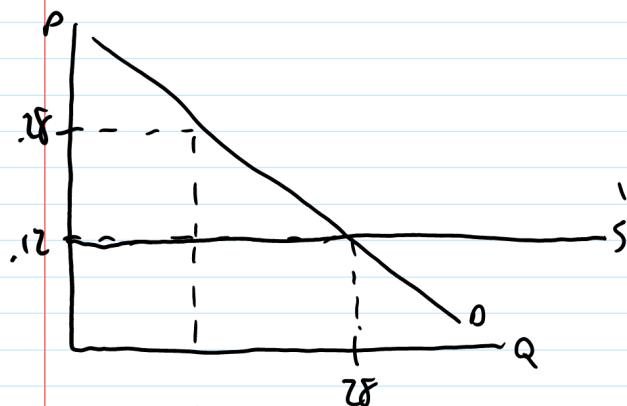
## 6.5 Opportunity Cost of Inputs Purchased from a Monopolist

Wednesday, September 30, 2020 5:12 PM



worked w/ Nick Lane  
Passed Solution Review

$$\bar{P} = -.75 \quad P_s = .12 \quad MC = .12 \quad Q_0 = 28 \quad MEC = .05/1 \quad METB = .25$$



Flat because electricity  
utility is a monopoly

$$-.75 = \frac{Q - 28}{P - .12} \cdot \frac{.12}{28}$$

$$Q = \frac{Q - 28}{P - .12} \cdot \frac{.12}{28}$$

$$\begin{aligned} \bar{P} &= (-175P + 49) / (P - .17) \cdot \frac{.12}{28} \\ \text{Numerator has to be } 0 \\ Q &= -175P + 49 \\ 175P &= 49 \\ P &= .28 \end{aligned}$$

$$\begin{aligned} \bar{P} &= (Q - 28) / (P - .12) \cdot \frac{.12}{28} \\ -.75 &= Q - 28 / P - .12 \\ -175P + 21 &= Q - 28 \\ Q &= -175P + 49 \end{aligned}$$

→

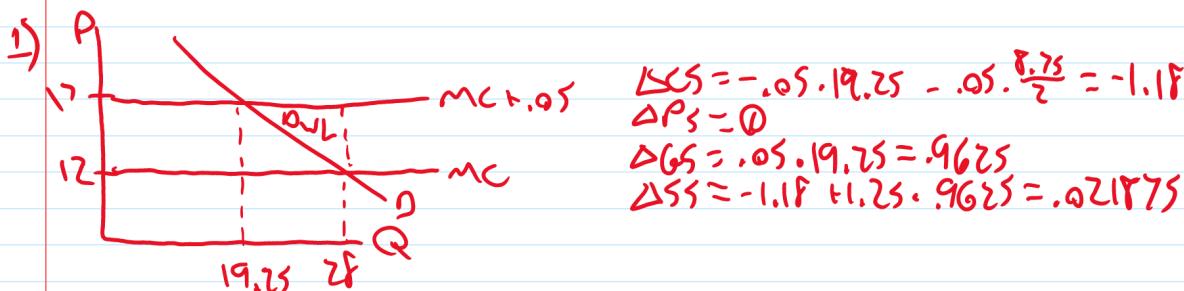
$$\begin{aligned} \bar{P} &= -(175P + 49 - 28) / (P - .17) \cdot \frac{.12}{28} \\ Q &= -175P + 21 \\ 175P &= 21 \\ P &= .12 \end{aligned}$$

Sorry! We got stuck here ::  
We're going to use  $P$  and  $Q$  instead of real numbers

$$\begin{aligned} 1) \text{Cost} &= 21,500,000P \\ \text{benefit to tax payers} &= .05Q \\ \text{decreased emissions} &= (Q - Q_0) \cdot 21,500,000 \end{aligned}$$

$$3) \frac{(Q - Q_0) \cdot 21500000}{7600000000} = 43(Q - Q_0) / 15200$$

1) Emissions could be effectively regulated in cities and other areas with high smog such as LA or cities in India and China. This is because smog is usually very local to the city and has a large negative impact.



$$2) \frac{1.18 \text{ Person}}{\text{day}} \cdot \frac{365 \text{ day}}{\text{year}} \cdot 21.5 \text{m People} = 9.44 \text{B/year gain}$$

$$\frac{.9625 \text{ Person}}{\text{day}} \cdot \frac{365 \text{ day}}{\text{year}} \cdot 21.5 \text{m People} \cdot 1.25 = 9.27 \text{B/year cost}$$

$$\frac{1.75 \text{ kWh}}{\text{Person day}} \cdot \frac{365 \text{ day}}{\text{Year}} \cdot \frac{.05}{\text{kWh}} = 3.43 \text{B/year benefit}$$

$$\text{Florida Benefit} = 21.5 \text{m} / 7.6 \text{B} = .283\% \text{ or } 9.7 \text{m/year}$$

# Worked w/Austin Assigned Solution Review

Initially, a profit maximizing local monopolist charges \$15 and sells 500 units per week. Elasticity of demand is -3. The monopolist's cost function is  $C(Q) = F + cQ$  where  $F$  is a fixed cost and  $c$  is the constant per unit variable cost.

a) What is the per unit cost of the product?

b) What are the demand and inverse demand functions?

Now assume the local government begins to provide 100 units per week at the market price.

c) What is the residual demand left for the monopolist?

d) Find the new price and the monopolist's quantity and the total market quantity.

e) Assume the METB is 0.25. Find the changes in CS, PS, GS, and SS.

f) Depict all of this in a diagram. You probably want to sketch the diagram right at the start of the problem for reference as you work, and then to redraw a neat version to submit.

$$g) \text{per unit} = 15/500 = .03/\text{unit}$$

$$h) \frac{d}{P} = \frac{\Delta Q}{\Delta P} \cdot \frac{P}{Q}$$

$$-3 = (Q - 500)/(P - 15) \cdot 15/500$$

$$-100 = (Q - 500)/(P - 15)$$

$$-100P + 1500 = Q - 500$$

$$Q = 2000 - 100P$$

$$Q - 2000 = -100P$$

$$P = 20 - Q/100$$

$$i) \text{res} = Q - q'$$

$$\text{res} = (2000 - 100P) - 100$$

$$\text{res} = 1900 - 100P$$

$$P = 19 - .01Q^2$$

$$j) P = 19 - .01Q^2$$

$$P = 19 - (.01 \cdot 1450)$$

$$P = 14.5$$

$$Q = 1900 - ((100 - 14.5))$$

$$Q = 450$$

$$k) \Delta CS = (.5 \cdot 500) + (\frac{1}{2} \cdot 50 \cdot .5)$$

$$\Delta CS = 262.5$$

$$\Delta PS = (-1 \cdot .5 \cdot 500) - (50 \cdot 4.5)$$

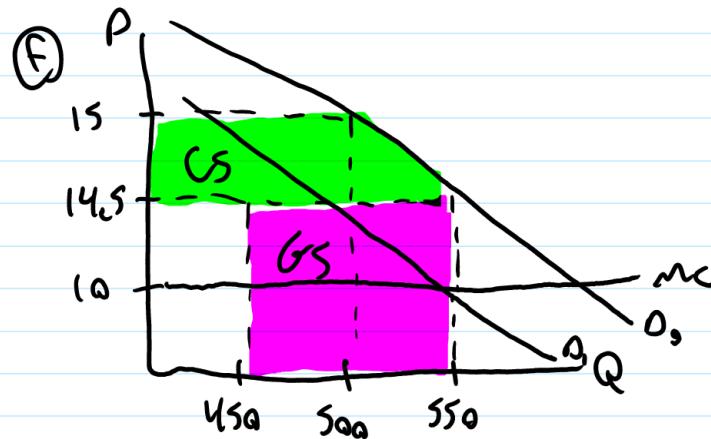
$$\Delta PS = -475$$

$$\Delta GS = (100 \cdot 4.5)$$

$$\Delta GS = 1450$$

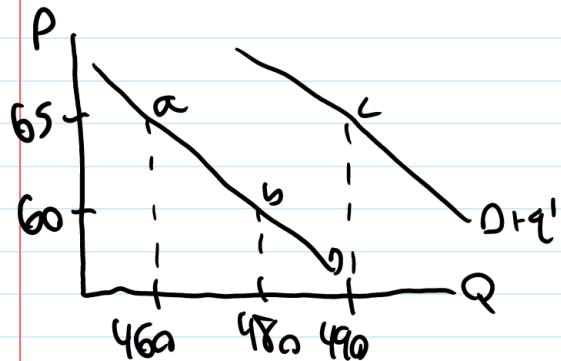
$$\Delta SS = 262.5 - 475 + (1.25 \cdot 1450)$$

$$\Delta SS = 1000$$



Passed Solution Review

Suppose a project needs to hire 10 electricians. At the initial wage of 60K/year (including benefits) 480 are currently employed in the local area and 20 are estimated to be unemployed. The MEBT is 0.2. Estimate the opportunity cost of hiring the workers. Explain, and defend any assumptions you make.



Assuming new wage is 65k as it does in problem 2

$$q' = 10$$

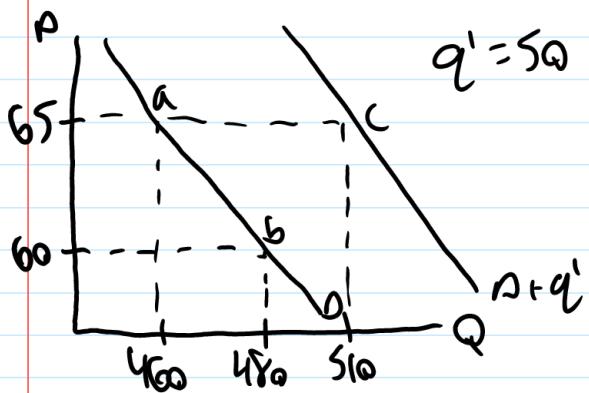
$$abc = \frac{1}{2}(65-60)(.49-.46) = 75,000$$

$$\begin{aligned} SC &= (490 - 460) \cdot 65000 - abc + MEBT(490 - 460)(65000) \\ SC &= 30 \cdot 65000 - 75000 + (.2 \cdot 30 \cdot 65000) \\ SC &= 2,265,000 \end{aligned}$$

Since there is low unemployment, worker time is valued at market rate. Since the number hired is a small amount compared to total workforce, hiring does not affect the wage. Thus,  $SC = 1.02 \cdot 60 \cdot 10 = 720$

Passed Solution Review

Suppose a project needs to hire 50 electricians. At the initial wage of 60K/year (including benefits) 480 are currently employed in the local area and 20 are estimated to be unemployed. The MEBT is 0.2. After electricians are hired for the project, the local wage increases to 65K/year and the number employed locally increases to 510. Estimate the opportunity cost of hiring the workers. Draw a diagram to illustrate. Explain, and defend any assumptions you make.



$$\text{abc} = \frac{1}{2}(65 - 60)(.51 - .46) = 125k$$

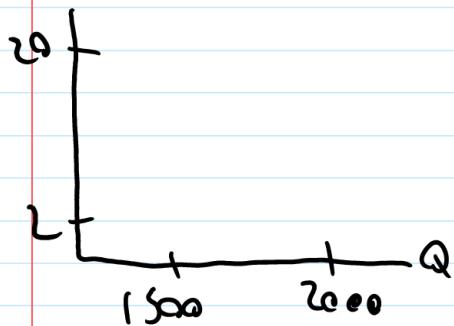
$$\begin{aligned} \text{sc} &= (510 - 460) \cdot 65k - \text{abc} + (\text{MEBT})(510 - 460)(65000) \\ \text{sc} &= (50) \cdot 65k - 125k + (.2 \cdot 50 \cdot 65000) \\ \text{sc} &= 3,775,000 \end{aligned}$$

We're assuming opportunity cost = social cost

Worked w/ Nick L + Austin

Imagine a rural area with a current wage rate of \$20 at which 1500 workers are employed and 500 are unemployed. A government project will hire 50 workers at the going wage rate. Assume reservation wages for those hired are more or less uniformly distributed between \$2 and \$20. The METB is 0.2. Estimate the expected opportunity cost of project labor.

$$\text{OC/worker } (20+2)/2 = 11 \rightarrow \text{reservation wage}$$

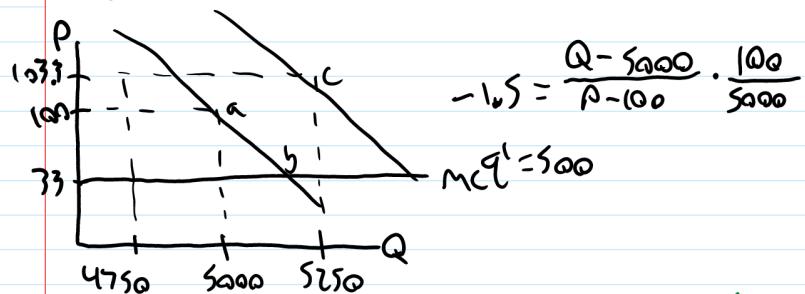


$$\text{worker OC} = 11 \cdot \$10 = \$550$$

$$\text{overall OC} = (11 \cdot 50) + (20 \cdot 2 \cdot 50) = 750$$

# Passed Solution Review

A project requires signing buying 500 cubic yards of concrete per week for the next year from the only local provider. The currently price is \$100 per yard and the provider sells 5,000 yards per week. Assuming marginal cost is constant, elasticity of demand at the current price is -1.5, and using a linear demand approximation, estimate the opportunity cost of the weekly government purchase. The METB is 0.2. Note you will need to find the original demand, the new demand, the new price, and the new quantity purchased by those other than the government in the process.



$$-1.5 = \frac{Q - 5000}{P - 100} \cdot \frac{100}{5000}$$

$$MC = 50$$

$$MC = P(1 + 1/\eta) = 100(1 + 1/-1.5) = 33\frac{1}{3} \quad P = MC(n/(1+n))$$

$$(-1.5)(50)(P-100) + 5000 = Q \Rightarrow 12500 - 75P$$

$$Q^m = Q + q^* - 75P = 13000 - 75P$$

$$75P = 13000 - Q^m$$

$$P = \frac{13000 - Q^m}{75}$$

~~$$MR = 173.\overline{3} - .75 = 33.\overline{3} \quad MR \Rightarrow P = 166.67 - 1/75q \Rightarrow MR = 166.67 - 2/75q$$~~

$$-0.26Q^2 = -140$$

$$Q^2 = 525Q = Q^2$$

$$525Q = 13000 - 75P \quad Q = 13000 - 75P$$

$$75P = 775Q$$

$$P = 103.\overline{3}$$

$$\downarrow \\ 825$$

~~$$SC = (525Q - 4750) \cdot 103.\overline{3} - (\frac{1}{2} \cdot (103.\overline{3} - 100)(525Q - 4750)) + (0.2(525Q - 4750)(103.\overline{3}))$$~~

~~$$SC = 500 \cdot 103.\overline{3} - 825 + 10333.\overline{3}$$~~

~~$$SC = 51666.\overline{66} - 825 + 10333.\overline{3}$$~~

~~$$SC = 61,175$$~~

New MR:

$$Q = 13000 - 75A \Rightarrow A = 173.33 \Rightarrow MR = 173.33 - 2/75q$$

$$\text{New } q: MR = MC \Rightarrow 173.33 - 2/75q = 33.33 \Rightarrow q = 5250$$

$$\text{Private } q = 5250 - 500 = 4750$$

$$\text{New } P: 5250 = 13000 - 75P \Rightarrow P = 103.33$$

New Surplus:

$$\Delta CS = -3.33 \cdot 4750 - 3.33 \cdot 250/2 = -1633.75$$

$$\Delta P_3 = 70 \cdot 5250 - 66.67 \cdot 5000 = 34150$$

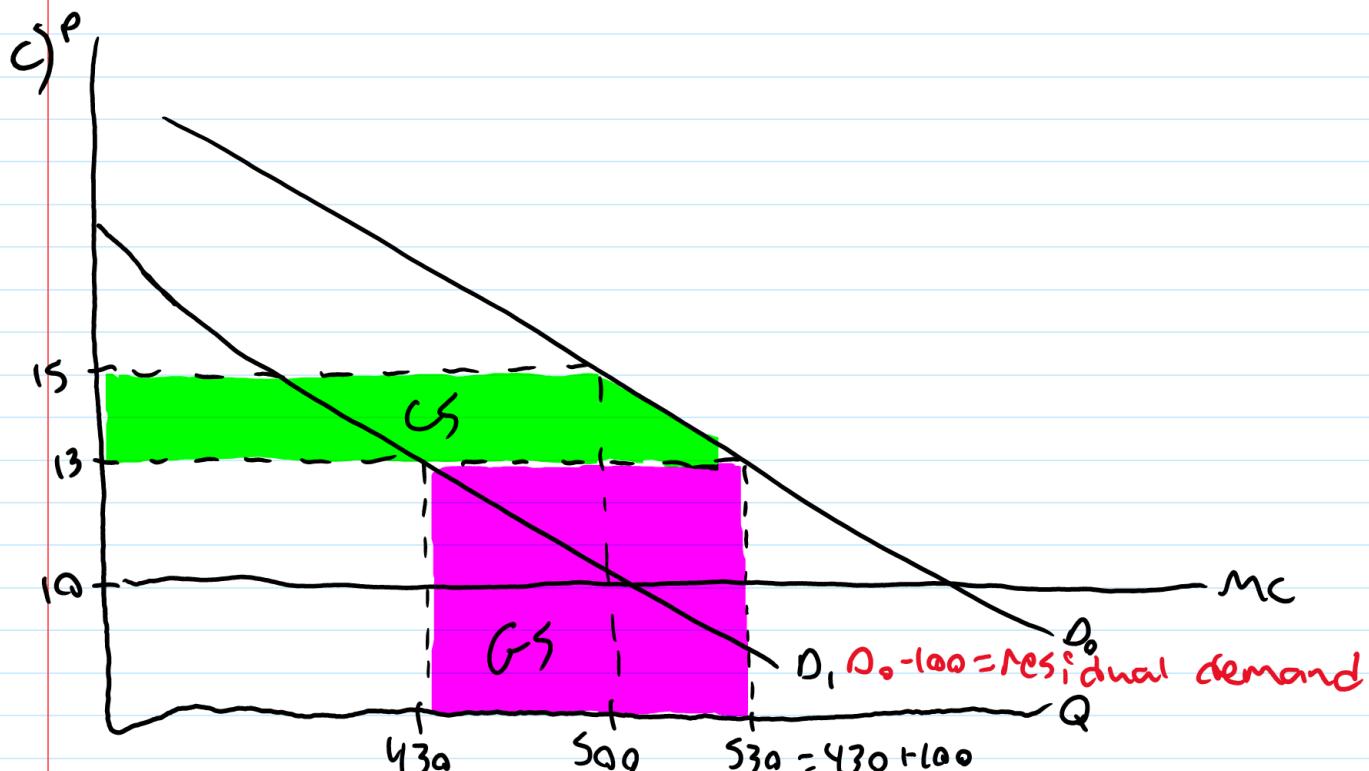
$$\Delta G = -103.33 \cdot 500 = -51665$$

$$\Delta S = 4700 + 4950 - (1.2 \cdot 51665) = -61748$$

Worked w/ Austin  
Passed Salton for review

Initially, a profit maximizing local monopolist charges \$15 and sells 500 units per week. Per unit variable cost is \$10. Now assume the local government begins to provide 100 units per week at the market price. As a result, the market price falls to \$13 and the quantity sold by the monopolist falls to 430.

- Find the changes in CS, PS, and GS created by the monopoly.
- Assume the METB is 0.25. Find the changes in SS.
- Depict all of this in a diagram. You probably want to sketch the diagram right at the start of the problem for reference as you work, and then to redraw a neat version to submit.



$$\text{a)} \Delta CS = (2 \cdot 500) + \left( \frac{1}{2} \cdot 2 \cdot 30 \right) \\ = 1000 + 30$$

$$\Delta CS = \$1030$$

$$\Delta PS = (-1)(15-13)(500) - (500-430)(13-10) \\ = (-1 \cdot 2 \cdot 500) - (70 \cdot 3) \\ = -1000 - 210$$

$$\Delta PS = -1210$$

$$\Delta GS = (530 - 430)(13)$$

$$\Delta GS = 1300$$

$$\text{b)} \Delta SS = \Delta CS + \Delta PS + (1 + \text{METB}) (\Delta GS) \\ = 1030 - 1210 + (1.25 \cdot 1300) \\ = -180 + 1625$$

$$\Delta SS = 1445$$

# 5 & 6 are Switched Passed Solution Review

- 1) What is the difference between Pareto efficiency and Hicks-Kaldor efficiency, and why is it relevant to benefit cost analysis? It helps some hurts none. Hicks-Kaldor if total benefits exceed total costs, BCA's use Hicks-Kaldor or nothing. In Pareto efficiency, so long as one person is better and no one is worse off, it is Pareto efficient. In Hicks-Kaldor efficiency, it is efficient so long as people benefit more than those who are worse off so long as the people worse off could be compensated by the benefits. It is relevant because when doing a BCA of a project, especially a public project, it is important to consider how the community will be affected and to consider how a project can be made Pareto efficient so that no one is worse off after the project is finished.

- 2) Why are benefit cost ratios inappropriate for evaluating alternative projects?  
 Benefit-cost ratios are inappropriate for evaluating alternative projects because the ratio is not indicative of total value added. It would be better to gauge projects by the net benefits. A project that has a benefit value of 15 and a cost value of 14 will have a much lower ratio than a project with 5 benefits and 1 cost.

*1) Can be manipulated by counting effects as benefits or costs*

*2) a project w/ a low ratio may have large net benefits*

- 3) Suppose your company is preparing a benefit-cost analysis to use to lobby the local government for a policy you want passed. Why would you want to know if the relevant decision makers are guardians or spenders? Spenders would focus on benefits while guardians would focus on revenues to the local government. The distinction between guardians and spenders is important because that largely controls their decisions on how to spend money. Guardians will be less likely to pass a new policy if it involves spending money while a spender will be more likely to pass a policy if the money spent benefits the greater good.

- 4) A government project directly purchases 20 units in a local market. The METB is 0.2. The elasticity of demand is  $-2/3$ . Other pertinent information is summarized in the figure provided. Calculate the changes in PS, CS, GS, and SS associated with the purchase.

$$MC = 133.\bar{3}(1 - \frac{1}{-2/3}) = 200/3$$

Calculate new price

$$\% \Delta Q = \frac{15/90 - 100}{100} = -6.7\%, -\frac{1}{3} = 6.67\% \cdot (-2/3) = 25\%$$

$$P = \frac{\partial Q}{\partial P} \cdot \frac{P}{Q} \rightarrow -\frac{2}{3} = \frac{95-75}{P-100} \cdot \frac{100}{90} \rightarrow -\frac{2}{3} = \frac{20}{P-100} \rightarrow P-100 = -\frac{100}{3} \rightarrow P = 200/3$$

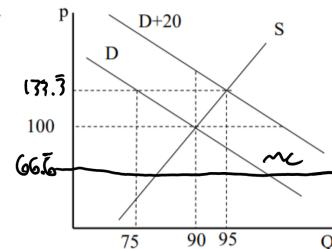
$$-\frac{2}{3} = \frac{0.1}{200/3 - P} \cdot 100/3 \rightarrow 100 - P = -100/3 \rightarrow P = 100 + 100/3 = 400/3$$

$$\Delta CS = (\frac{100}{3} \cdot 90) + (\frac{100}{3} \cdot 5 \cdot \frac{1}{3}) = 3083.\bar{3} - (25 \cdot 75) - (\frac{1}{2} \cdot 25 \cdot 15) = -2462.5$$

$$\Delta PS = (\frac{100}{3} \cdot 75) - (\frac{100}{3} \cdot 90) = -3500 \quad (25 \cdot 90) + (\frac{1}{2} \cdot 25 \cdot 15) = 2312.5$$

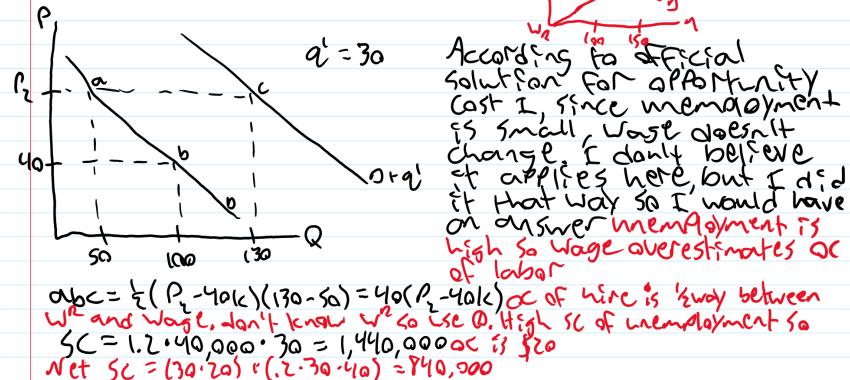
$$\Delta GS = (100 \cdot 20) - 2000 \quad (-125 \cdot 20) = -2500$$

$$\Delta SS = 3083.\bar{3} - 3500 + (1.2 \cdot 2500) = 1983.\bar{3} \quad (-2462.5) + 2312.5 - (-2500) = -2750$$



- 6) A local government project requires 30 workers for a year from a market in which currently 100 workers are employed, 50 are unemployed, and the annual wage is \$40K. The MEBT is 0.2.

- a) Draw a figure illustrating the state of the market.  
 b) Calculate the opportunity cost of hiring the workers.



$$\Delta BC = \frac{1}{2} (P_2 - 40)(130 - 50) = 40(P_2 - 40) \quad \text{OC of hire is halfway between } W \text{ and } W+100, \text{ don't know } W^2 \text{ so use } 0. \text{ High sc of unemployment so}$$

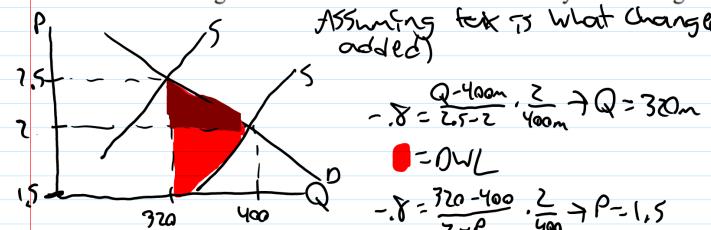
$$SC = 1.2 \cdot 40,000 \cdot 30 = 1,440,000 \quad \text{OC is } \$20$$

$$\text{Net } SC = (30 \cdot 20) + (1.2 \cdot 30 \cdot 40) = 740,000$$

- 5) Suppose:

- i) the price of gasoline is \$2 per gallon  
 ii) current consumption is 400 (million) gallons per day  
 iii) the elasticity of demand is  $-0.8$   
 iv) retail provision of gasoline may be approximated as a constant cost industry  
 v) there is an external cost of \$0.5 per gallon of gas  $\leftarrow$  tax!

Calculate deadweight loss associated with the externality. Draw a figure to illustrate.



$$\Delta WL = (2.5 - 1.5) \cdot \frac{1}{2} \cdot 80 = 40,000,000$$

$$\Delta NL = \frac{1}{2} \cdot (2.5 - 2) \cdot (80) = 20,000,000$$