

Cost, Demand, and Profit MaximizationCost, Its Determinants, and Marginal Cost $C(q)$  = Firm Cost $C = C(q; w, r, z) \rightarrow$  cost of  $q$  units depends on  $q$ , Wage rate ( $w$ ), Capital costs ( $r$ ), and other factors ( $z$ )**Marginal cost** = cost of making one more unit

$$MC = \frac{dC}{dq} \quad d = \text{change (derivative)}$$

4 ways to approximate cost:

$$C(q) = f + cq \rightarrow C > 0, f \geq 0, MC = C$$

$$C(q) = f + cq^d \rightarrow C > 0, d > 0, f \geq 0, MC = cdq^{d-1}$$

$$C(q) = f + aq + bq^2 \rightarrow a' > 0, b' > 0, f \geq 0, MC = a + 2bq$$

$$C(q) = f + aq + bq^2 + cq^3 \rightarrow a' > 0, b' < 0, c' > 0, f \geq 0, MC = a + 2bq + 3cq^2$$

Demand and its Determinants, Inverse Demand

$$q = q(p)$$

 $m$  = incomePrice of substitutes ( $p_s$ ) and complements ( $p_c$ ) $n$  = market size $z$  = other variables

$$q = q(p, m, p_s, p_c, n, z)$$

 $\hookrightarrow$  implies that  $q$  depends on  $p$ 

$$p = p(q, m, p_s, p_c, n, z)$$

$$p = p(q)$$

Measuring the sensitivity of Quantity Demanded to Price

Elasticity is a percentage

$$\text{elasticity of demand} = \eta \text{ (eta)} = \% \Delta q / \% \Delta p = \Delta q / q / \Delta p / p$$

 $\uparrow$  not constant over demandDemand ApproximationsLinear Demand Approximations $\varepsilon$  = random error

$$q_0 = A - \beta p$$

$$p = \frac{A}{\beta} - \frac{1}{\beta} q$$

Log Linear (constant elasticity) Demand Approximations

$$q = Ap^{-\beta}$$

$$\ln(q) = \ln(A) - \beta \ln(p)$$

$$dq/dp = -\beta Ap^{-\beta-1}$$

 $\uparrow$  w/ respect to independent, are constant and equal to that variable's coefficientRevenue and Marginal Revenue

$$\text{Revenue} = \text{Price} \cdot \text{quantity}$$

Firms have **Market Power** if they have a non-negligible effect on market price**Marginal revenue** = gain in revenue from one unit sold

$$MR = p + \frac{dp}{dq} q$$

Marginal Revenue and Elasticity

$$dR/dq = p \left( 1 + \frac{1}{\eta} \right)$$

Profit Maximization

$$q^* = \text{profit maximizing } q$$

$$\hookrightarrow p^*$$

$$p = \left( \frac{n}{1+n} \right) MC$$