

Lagrangian

$$L = U(x, y) + \lambda(m - p_x x - p_y y)$$

$$\frac{dL}{dx} = \frac{dU}{dx} - \lambda p_x = 0$$

$$\frac{dL}{d\lambda} = m - p_x x - p_y y = 0 \rightarrow m = p_x x + p_y y$$

$$\frac{MU_x}{p_x} = \frac{MU_y}{p_y} \quad \text{and} \quad \frac{MU_x}{MU_y} = \frac{p_x}{p_y}$$

$$MRS_{xy} = \frac{MU_x}{MU_y} = \frac{p_x}{p_y}$$

$$MU_x = 2 \quad \text{and} \quad MU_y = 1 \rightarrow 2y = 1x$$