

10-1 The Nature of Time Series Data

Data must go in order

A series of random variables indexed by time is a **stochastic process** or **time series process**

↑
random

10-2 Examples of Time Series Regression models

10-2a Static models

a static model time has an immediate effect
good for judging tradeoffs between y and z

10-2b Finite Distributed Lag models

FOL model

one or more variables can affect y w/ a lag

δ_0 is the **impact propensity** or **impact multiplier**

Lag distribution summarizes dynamic effect that a temporary increase in z has on y

Long-run Propensity/multiplier (LRP)

for any horizon h , we can define the **Cumulative effect**

10-2c A convention about the time index

Time starts at $t=1$

10-3 Finite Sample Properties of OLS under classical assumptions

10-3a Unbiasedness of OLS

Assumptions:

- 1) Linear in Parameters
- 2) No Perfect collinearity
- 3) Zero conditional mean
- 4) Homoskedasticity
- 5) No serial correlation
- 6) Normality

10-3b The Variance of the OLS estimators and the Gauss-Markov Theorem

Homoskedasticity:

Conditional on x , variance of v_t is same for all t

$$\hookrightarrow \text{Var}(v_t) = \sigma^2, t=1, 2, \dots, n$$

No serial correlation:

Conditional on x , errors in two times are uncorrelated

$$\hookrightarrow \text{Corr}(v_t, v_s | x) = 0, \text{ for all } t \neq s$$

↳ suffer from serial/autocorrelation when false

10-3c Inference under the classical linear model Assumptions

Normality:

errors v_t are independent of x and are independently and identically distributed as $\text{Normal}(0, \sigma^2)$