

past affects future so std error isn't right
 spurious correlations!

linear trends by regressing time and a variable

Time trends

$$Y_t = \alpha_0 + \alpha_1 t + \epsilon_t$$

$$X_t = \gamma_0 + \gamma_1 t + \epsilon_t$$

$$\hat{Y}_t = \hat{\alpha}_0 + \hat{\alpha}_1 t$$

$$\hat{\epsilon}_{it} = (Y_t - \hat{\alpha}_0 - \hat{\alpha}_1 t)$$

suppose $Y_t = \beta_0 + \beta_1 X_t + \delta t + \epsilon_t$

How is Y correlated with X ?

detrending = put in t trend take residuals afterwards

differencing =

Lags:

$$L_1 Y_t = Y_{t-1}$$

$$L_2 Y_t = Y_{t-2}$$

$$F_1 Y_t = Y_{t+1}$$

$$D_1 Y_t = Y_t - Y_{t-1}$$

\uparrow
 differencing

$$Y_t = \beta_0 + \beta_1 X_t + \delta t + \epsilon_t$$

$$Y_{t-1} = \beta_0 + \beta_1 X_{t-1} + \delta(t-1) + \epsilon_{t-1}$$

$$\hookrightarrow D_1 Y_t = Y_t - Y_{t-1} = \delta + \beta_1 (X_t - X_{t-1}) + (\epsilon_t - \epsilon_{t-1})$$