

## ANEXO-I. DERIVADAS PARCIAIS DE FUNÇÕES ELEMENTARES.

As igualdades estão enunciadas apenas para  $\frac{\partial}{\partial x}$  e  $\frac{\partial u}{\partial x}$ , mas obviamente são as mesmas para:  $\frac{\partial}{\partial y}$  e  $\frac{\partial u}{\partial y}$  e  $\frac{\partial}{\partial z}$  e  $\frac{\partial u}{\partial z}$ ;

$$\textcircled{01} \frac{\partial [u^n]}{\partial x} = n \cdot u^{n-1} \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{02} \frac{\partial (\sin u)}{\partial x} = \cos u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{03} \frac{\partial (\cos u)}{\partial x} = -\sin u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{04} \frac{\partial (\operatorname{tg} u)}{\partial x} = \sec^2 u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{05} \frac{\partial (\operatorname{cotg} u)}{\partial x} = -\operatorname{cosec}^2 u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{06} \frac{\partial (\sec u)}{\partial x} = \sec u \cdot \operatorname{tg} u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{07} \frac{\partial (\operatorname{cosec} u)}{\partial x} = -\operatorname{cosec} u \cdot \operatorname{cotg} u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{08} \frac{\partial (\operatorname{arcsen} u)}{\partial x} = \frac{1}{\sqrt{1-u^2}} \cdot \frac{\partial u}{\partial x}; |u| < 1; \quad \textcircled{09} \frac{\partial (\operatorname{arccos} u)}{\partial x} = \frac{-1}{\sqrt{1-u^2}} \cdot \frac{\partial u}{\partial x}; |u| < 1;$$

$$\textcircled{10} \frac{\partial (\operatorname{arctg} u)}{\partial x} = \frac{1}{1+u^2} \cdot \frac{\partial u}{\partial x}; \quad \textcircled{11} \frac{\partial (\operatorname{arccotg} u)}{\partial x} = \frac{-1}{1+u^2} \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{12} \frac{\partial (\operatorname{arcsec} u)}{\partial x} = \frac{1}{u\sqrt{u^2-1}} \cdot \frac{\partial u}{\partial x}; |u| > 1; \quad \textcircled{13} \frac{\partial (\operatorname{arccosec} u)}{\partial x} = \frac{-1}{u\sqrt{u^2-1}} \cdot \frac{\partial u}{\partial x}; |u| > 1;$$

$$\textcircled{14} \frac{\partial (\ln u)}{\partial x} = \frac{1}{u} \cdot \frac{\partial u}{\partial x}; u > 0;$$

$$\textcircled{15} \frac{\partial (e^u)}{\partial x} = e^u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{16} \frac{\partial (\log_a u)}{\partial x} = \frac{1}{u \cdot \ln a} \cdot \frac{\partial u}{\partial x}; u > 0, a > 0, a \neq 1; \quad \textcircled{17} \frac{\partial (a^u)}{\partial x} = a^u \cdot \ln a \cdot \frac{\partial u}{\partial x}; a > 0;$$

$$\textcircled{18} \frac{\partial (\operatorname{senh} u)}{\partial x} = \operatorname{cosh} u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{19} \frac{\partial (\operatorname{cosh} u)}{\partial x} = \operatorname{senh} u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{20} \frac{\partial (\operatorname{tgh} u)}{\partial x} = \operatorname{sech}^2 u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{21} \frac{\partial (\operatorname{cotgh} u)}{\partial x} = -\operatorname{cosech}^2 u \cdot \frac{\partial u}{\partial x}; \quad \textcircled{22} \frac{\partial (\operatorname{sech} u)}{\partial x} = -\operatorname{sech} u \cdot \operatorname{tgh} u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{23} \frac{\partial (\operatorname{cosech} u)}{\partial x} = -\operatorname{cosech} u \cdot \operatorname{cotgh} u \cdot \frac{\partial u}{\partial x};$$

$$\textcircled{24} \frac{\partial (\operatorname{arcsech} u)}{\partial x} = \frac{1}{\sqrt{u^2+1}} \cdot \frac{\partial u}{\partial x}; \quad \textcircled{25} \frac{\partial (\operatorname{arcosh} u)}{\partial x} = \frac{1}{\sqrt{u^2-1}} \cdot \frac{\partial u}{\partial x}; u > 1;$$

$$\textcircled{26} \frac{\partial (\operatorname{arctgh} u)}{\partial x} = \frac{1}{1-u^2} \cdot \frac{\partial u}{\partial x}; |u| < 1; \quad \textcircled{27} \frac{\partial (\operatorname{arccotgh} u)}{\partial x} = \frac{1}{1-u^2} \cdot \frac{\partial u}{\partial x}; |u| > 1;$$

$$\textcircled{28} \frac{\partial (\operatorname{arcsech} u)}{\partial x} = \frac{-1}{u\sqrt{1-u^2}} \cdot \frac{\partial u}{\partial x}; 0 < u < 1;$$

$$\textcircled{29} \frac{\partial (\operatorname{arccosech} u)}{\partial x} = \frac{-1}{|u|\sqrt{u^2+1}} \cdot \frac{\partial u}{\partial x}; u \neq 0;$$