# Identification of cell signaling pathways based on biochemical reaction kinetics repositories

Student: Gustavo Estrela

Advisor: Marcelo da Silva Reis (Butantan Institute)

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Instituto de Matemática e Estatística Centro de Toxinas, Resposta-imune e Sinalização Celular (CeTICS) Laboratório Especial de Ciclo Celular, Instituto Butantan

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# Introduction

Cell signaling allows cells to respond to signals that come from its environment changing its behaviour accordingly.

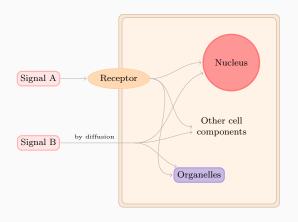
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Understanding the functioning of cell signaling is important in many biological areas.



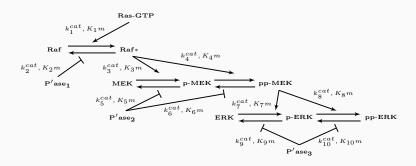
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We call the path of a signal a cell signaling pathway.

#### **Cell Signaling Pathways**

A cell signaling network can be characterized by a sequence of chemical reactions



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Using biochemical and enzymatic kinetics, we can model the concentration change of chemical species over time of a pathway.

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As the input, a description of a biological experiment and a set of experimental measurements are given. A possible output to the problem is composed by:

- a model composed by a set of chemical reactions that are relevant for the biological experiment;
- information about the reaction rate constants of the model.

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Hence, it is desirable to construct a method that can systematically modify these models and choose the one that better represents the experiment.

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On her work, the problem of identification of cell signaling pathways is treated as a feature selection problem.

# Feature Selection for Identification of Signaling Pathways

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The methodology proposed by Wu defines the set of features as a set of chemical reactions that can be added to a starting model. This set of chemical reactions is fetched from KEGG and stored in a database of interactions.

# Wu's Search Algorithm for Feature Selection

The search algorithm used by Wu is the Sequential Forward Selection (SFS).

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Wu defines the cost function as the minimum distance between experimental and simulated data.

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- the database of interactions used could be more nearly complete;
- the search algorithm could also consider removing interactions;
- the cost function could implement a proper penalization of models;

We propose to create a methodology that uses a feature selection approach for identification of signaling pathways, tackling the difficulties encountered by Wu.

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# What we Propose on this Project

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To define new cost functions, we intend to use Bayesian approaches of model selection that allow us to create estimates of probabilities such as p(M|D) or p(D|M).

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- Formulate systematic modifications to a model as the search space of a feature selection model.
- Test the methodology on known signaling pathways and also on pathways of interest in our lab.

# **Fundamental Concepts**

Kinetics Modeling of Chemical Reactions

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- Michaelis-Menten enzymatic kinetics.

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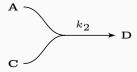
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has rate of:

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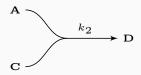
# **Kinetic Modeling of Second Order Iteration**

A second order reaction:



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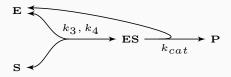


has rate of:

$$k_2[A][C]$$
.

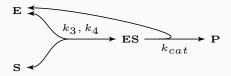
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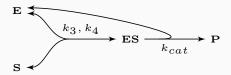
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# Kinetic Modeling of Enzymatic Reactions

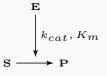
An enzymatic reaction:



Can be divided in two first order reactions plus a second order reaction. However, with the appropriate assumptions, it is possible to use a Michaelis-Menten simplification of this reaction.

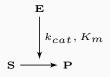
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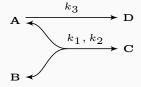
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and it has rate of:

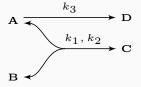
$$k_{cat} \frac{[E][S]}{K_M + [S]}.$$

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Then, the differential equation that models the concentration change of A is:

$$\frac{d[A]}{dt} = -k_1[A][B] + k_2[C] - k_3[D].$$

Bayesian Methods for Biochemical Model Selection

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- Approximate Bayesian Computation;
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For both methods, we resort to Metropolis-Hastings algorithm to generate samples of distributions.

With Metropolis-Hastings, we can generate a sample of a distribution  $p(\lambda)$  doing the following:

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- 5. Increase *t* by one and repeat from Step 2 if not reached iteration limit.

# Model Selection

Ranking with Marginal Likelihood Estimation

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$$p(D|M,\theta) = p_{\mathcal{N}_{(\vec{0},\Sigma)}}(\phi(M,\theta) - D).$$

Where  $\phi(M, \theta)$  is the simulated observation.

#### Marginal Likelihood of Data

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Calculating this integral is hard, therefore we resort to estimating another integral.

#### Power-posterior distributions

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$$p_{\beta=1}(\theta) = \frac{p(D,\theta|M)}{\int_{\Theta} p(D,\theta|M)d\theta} = \frac{p(\theta|D,M)p(D|M)}{p(D|M)} = p(\theta|D,M).$$

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$$\ln p(D|M) = \int_0^1 \mathbb{E}_{p_{\beta}(\theta)}[\ln p(D|\theta, M)]d\beta.$$

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$$\sum_{t=0}^{T-1} (\beta_{t+1} - \beta_t) \frac{\mathbb{E}_{p_{\beta_{t+1}}(\theta)}[\log p(D|M, \theta)] + \mathbb{E}_{p_{\beta_t}(\theta)}[\log p(D|M, \theta)]}{2}$$

To produce the estimates of

$$\mathbb{E}_{p_{\beta_t}(\theta)}[\log p(D|M,\theta)]$$
 for  $t \in \{0,\ldots,T\}$ 

we need to produce samples of the power-posteriors  $p_{\beta_t}(\theta)$ .

The sampling of the power-posteriors are generated using Metropolis-Hastings algorithms in three steps.

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On the second and third step, the covariance matrix of the jump distribution is estimated with the current sample of the posterior.

On the third step a Populational Monte Carlo Markov Chain is performed. This algorithm allows us to mix samples from different temperatures.

Ranking with Approximate Bayesian Computation

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- 4. Repeat until some iteration limit.

The result of the algorithm is a sample of the distribution

$$p(\theta, M|d(\phi(M, \theta), D) < \epsilon).$$

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We can use the accepted parameters of tolerance  $\epsilon$  and model M to estimate

$$p(M|d(\phi(M,\theta))<\epsilon).$$

# Experiments on Model Selection

# Software used for Model Ranking Experiments

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We tested the two methods of model ranking using the software:

- SigNetMS: an implementation of the Marginal Likelihood method created in this project.
- ABC-SysBio: an implementation of ABC-SMC.

We ran two experiments based on the same procedure:

• Create 4 candidate models.

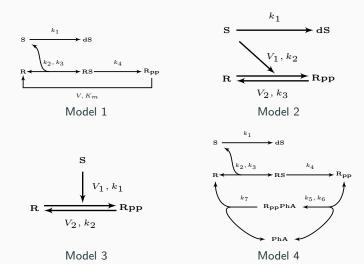
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- For one of the models, choose a set of parameter values and time steps and simulate data.
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- Neglect chosen parameter values and define prior distributions for every parameter.
- Rank the four models.

This experiment is originally from Vyshemirsky and Girolami (2007), in which they present results of Annealing Melting Integration.

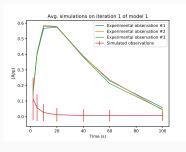


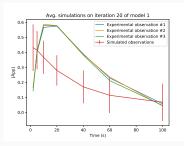
The model used to create the observations was Model 1.

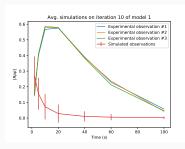
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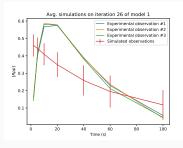
The priors distribution used for all parameters is Gamma(1,3).

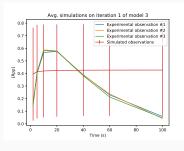
The ABC-SysBio software returned the following ranking of models:

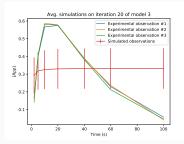


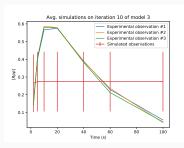


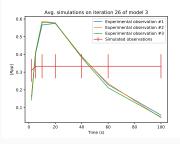












The ranking returned by SigNetMS on the first experiment is:

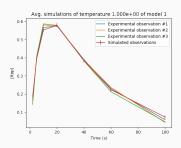
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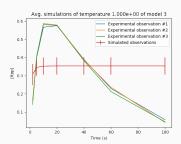
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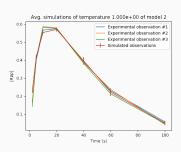
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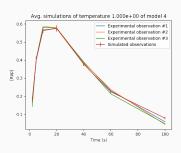
which is very similar to the ranking presented originally by Vyshemirsky and Girolami (2007):

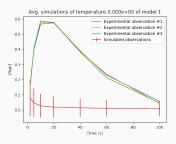
$$1 > 4 > 2 > 3$$
.

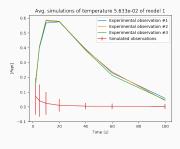


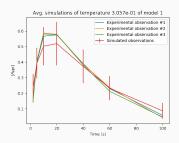


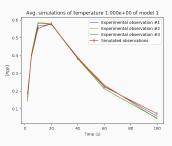


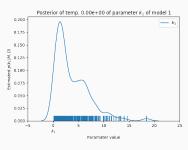


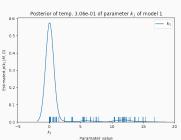


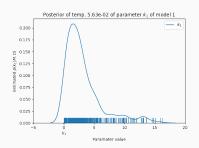


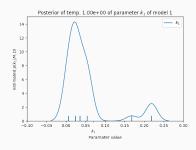




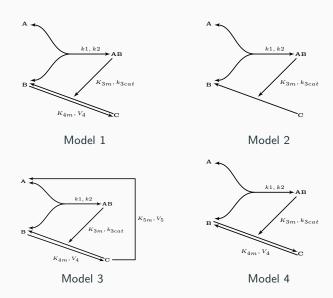








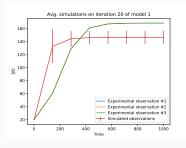
This experiment is very similar to the later and it was designed by us.

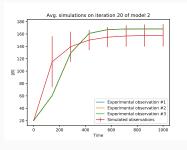


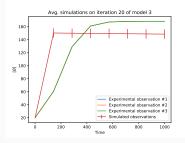
We used the following prior distributions for model parameters:

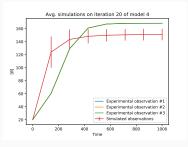
Parameter	Models	Prior
k1	1, 2, 3, 4	Gamma(1, 0.01)
k2	1, 2, 3, 4	Gamma(2, 0.5)
k <sub>3cat</sub>	1, 2, 3, 4	Gamma(4,1)
$K_{3m}$	1, 2, 3, 4	Gamma(2, 1500)
$V_4$	1, 3, 4	Gamma(2,1)
$K_{4m}$	1, 3, 4	Gamma(2, 100)
$V_5$	3	Gamma(2, 0.4)
K <sub>5m</sub>	3	Gamma(2, 100)

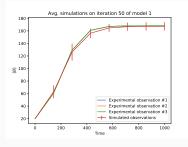
The ABC-SysBio software returned the following ranking of models:

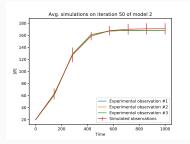


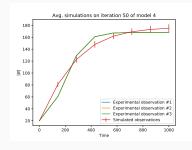


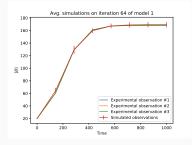


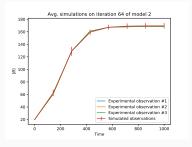


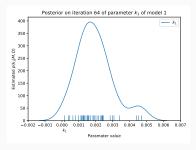


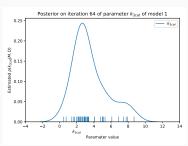


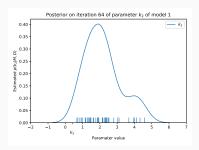


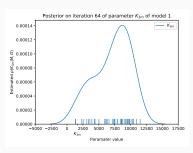




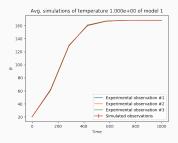


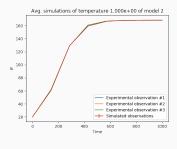


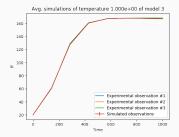


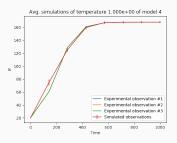


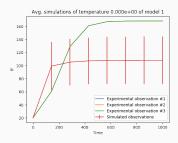
 $SigNetMS\ returned\ the\ following\ ranking\ of\ models:$ 

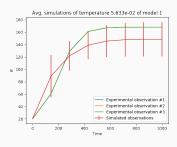


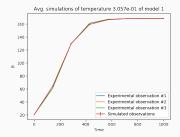


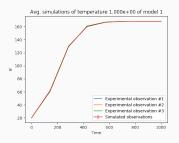


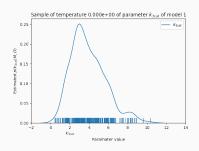


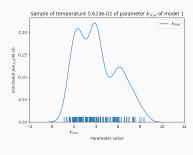


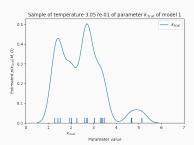


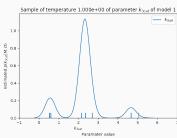












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- Complete program credits requirement.
- Improve computationally SigNetMS, since we chose it as our cost function for models.
- Studies of databases of chemical kinetics such as SABIO-RK and BRENDA.
- Creation of a relational database of chemical interactions focused on our further applications.

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- Apply the method in ERK signaling pathways of tumor cell lines Y1 and HEK293.

Thank you!