

# UNIVERSITY OF AMSTERDAM MASTER THESIS PROJECT

## Forgery: Synthesizing Database Transactions

Guy - Sean Rombaut

Supervised by: Dr. Tijs van der Storm Dr. Jouke Stoel

Organizations:

Internationale Nederlanden Groep (ING)

Centrum Wiskunde & Informatica (CWI)



## Contents

1	Abstract		
2	Preface	4	
3	3.1 Motivation	5 8 8 9	
4	4.1.1 Cardinalities       1         4.2 Data Operations       1         4.3 Data Invariants       1	0 0 2 3	
5	5.2       Architecture Overview       1         5.3       Alchemy Comparison       1         5.3.1       Forgery uses pure SQL       1         5.3.2       Alchemy has no evaluation and assertions are not supported       1         5.3.3       Forgery supports atoms control       1         5.4       Scheme Generation       2         5.4.1       Atoms Tables       2         5.4.2       Fields Relations       2         5.4.3       Cardinalities       2         5.4.3       Cardinalities       2         5.5.1       Using Stored Procedures       2         5.5.1       Using Stored Procedures       2         5.6.1       Scheme Generation       2         5.6.2       Procedures Generation for Predicates       2         5.6.3       Procedures Generation for Facts       3         5.7.1       Reverse Engineering       3	5 5 8 9 9 9 9 1 2 2 3 4 2 5 8 8 9 9 1 3 2 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	
6	6.2 Alchemy: Transmuting Base Alloy Specifications into Implementations	34 34 34	
7	Conclusions	ĸ	

CONTENTS 2

8	App	oendix		37
	8.1	Alloy	uick Reference	37
		8.1.1	Logic	37
		8.1.2	$\operatorname{Syntax}$	38
		8.1.3	Modelling	40
		8.1.4	${f Signatures}$	41
		8.1.5	Functions	42
		8.1.6	Predicates	42
		8.1.7	Facts	42
		8.1.8	$\Lambda_{ ext{ssertions}}$	42

### Abstract

The popularity of modeling languages is increasing. This is mostly due to the fact that using modeling languages is an efficient way to end up with a high quality system [5, p. 6]. By providing immediate feedback to users they allow early detection of design errors [7]. Nonetheless these models are far from being a real implemented product. Manual implementation is required which makes it more prone to mistakes. Our motivation for this research was to find a solution in this matter.

We decided to focus our research on the field of automatic database generation rather than whole programs as we found it very interesting. Considering the human factor, it is not possible to develop a fault-free software in practice [8]. When those issues occur the data itself may also be effected and this makes it more difficult to repair. Data errors can harm the reputation of an organization, diminish financial gains and create uncertainty in an organization.

Forgery is a tool for generating database schemes and synthesize transactions based on a predefined model. Forgery uses Alloy as a specification language for describing models and validating them. An Alloy model is a collection of constraints and relations that describes a set of structures. Using preand postconditions it defines the operations that are allowed in the system. Forgery converts them into database tables, procedures and structural constraints.

## Preface

This research was done for the Dutch bank ING. The original project aimed to find a solution regarding the communication issues between technical and non-technical teams inside the organization. For example, specifications ambiguity or misunderstandings between the teams.

The project was initially called *Fors* and later on was renamed to *Rebel*. *Rebel* is a domain specific language (DSL) that parses business software specifications into algebraic-based language which is called *Alloy*. With *Alloy* it is possible to validate models, and those can be implemented by the technical team.

Forgery aims to find a solution regarding faults in the process of the realization of a model. Forgery continues the process of Fors to support the realization. Together with Fors we may achieve two things: better specifications and better realization.

## Background

This chapter discusses the background of developing *Forgery*, the previous work that has been done and the motivation for it. It also contains the research question along with a description of the remaining chapters of this thesis.

#### 3.1 Motivation

The success of implementing software projects is directly affected by the quality of its specifications [1, p. 12]. The specifications are typically defined based on two conceptual views: business and technical and are usually defined by different teams or people with various backgrounds. The gap between those two different perspectives may lead to costly misunderstandings [3, p. 1]. Changing specifications after implementation of software often takes much more time and is also more expensive [10].

Today several tools exist for modeling and verifying software specifications. Examples are Alloy and Z-notation. These tools allow software engineers to create prototypes of their ideas and identify errors, before realization.

However, sometimes such modeling tools seems to be too complicated. Even though the mathematical notations of these tools are unambiguous, the use of set theories, logic and algebra requires special expertise [3, p. 10]. In addition, these tools are useful especially for prototyping general models and less effective when it comes to specific domains. We focus on such a specific domain (financial systems).

Because of the above-mentioned, we aimed at creating a new tool that would be better suited for prototyping financial systems and could be used by both the business and the development teams. We have developed our own Domain Specific Language (DSL) and called it *Fors* which derived from: Separating Configuration From Formal Specification [3]. The concept of a DSL is very simple: Instead of aiming to solve any kind of computing problem, DSLs aim to solve specific class of problems. [2]. In our case the DSL aims to solve problems of financial systems.

Fors expresses the operations of a system in a language whose vocabulary, syntax and semantics are formally defined in an easy and natural way. This way, Fors is comprehensible for both business and development teams. In addition, Fors is able to check the correctness of a software model. Fors parse formal specifications into Alloy syntax: algebraic logic formulas based on the notion of relations (We will elaborate on this more later in this thesis). Using an Alloy based engine we are able to solve such formulas and find ambiguities in a model.

Fors minimizes the gap between the business and the technical views by creating a common language and the ability to identify contradictions or faults in a specific model. However, there is still a main issue that remains: Programmers will have to implement the real product by hand (according to the specifications). Hence, it is not guaranteed that the final results would be exactly the same as defined in the specifications. When considering human factor also this system is prone to error.

Therefore, our motivation was to find out whether we would be able to create a tool for automatic system generation. We decided to scope our research on the data-side as we found it highly interesting.

As mentioned previously, data errors can harm the reputation of an organization, diminish financial gains and create uncertainty in an organization. Synthesizing the data may reduce or even avoid such events.

Data is usually stored in a record-keeping system called a database. A database therefore is a repository for a collection of data files on which users may perform a variety of operations (e.g. adding, modifying or reading files) [16, p. 11].

The scope of database is often described as having the following three aspects:

- Data Structure the structure is a representation of the arrangement, relationships, and contents of data [15]. The structure is described diagrammatically by the data schema.
- Data Manipulation the available operations that can be applied on the data. Mainly *CRUD* (Create, Read, Update and Delete) operations.
- Data Integrity refers to the accuracy and consistency (validity) of data over its lifecycle.

Using a database has numerous benefits that lay mostly in the fact that data control is centalized. First, redundancy can be reduced. In contrast to private files, by using a relational database it is possible to merge related or overlapping information. Second, by linking multiple rows and by use of transactions it is possible to avoid inconsistency of data (corollary of the previous point). Third, security (permissions) and standards (e.g. representation of the data) can be enforced. And last, using a database simplifies sharing data between multiple workstations [16, p. 16].

Fors uses Alloy; and Alloy is based on relations. We therefore investigated if it is possible to make a link between Alloy and relational databases. We consequently investigated the possibility to automatically generate a matching database.

A relational database consists of three main principles:

- Tables are the logical structure (although physically they can be stored in multiple ways like binary trees, hashing etc).
- The information principle the entire content of the database is represented in one specific way and only that way.
- The operators available to the user derive from an old state to a new one.

A relational database has the prefix *relational* not only because of entities and relationships but primarily because of the fact that relation is a mathematical term for a table [16, p. 26]. A relational system is based on the relational model of data.

**Example** - Simple student grades system:

Students Table	
	150

student_id (unique)	student_name
1	Guy
2	Vadim

grade_id (unique)	student_id	grade
1	1	9
2	1	7.5
3	2	8

Grades Table

In this example, we used the students table to store the names of the students. We used the grades table for storing the student's grades. In order to make a link between a student and a grade we used a unique numeric identifier.

The system user (e.g. a teacher) can now use multiple operations to manipulate the data. Each performed operation (e.g. deleting data) will generate a new table by changing the table from an "old" into a "new" state. For example, by deleting a grade row, this relation will be replaced by a new one (excluding the deleted row). In a similar fashion new tables will be generated when inserting or updating data.

We have already mentioned the term *relation* multiple times. Before we can fully define a relation we first have to introduce few more terms, which are crucial for understanding what a relation is.

Given a collection of data types (e.g. names, dates, addresses etc) Ti(i=1,2,3...), an attribute Ai is a pair of a data type Ti and a value of this type Vi (attribute value). So a tuple t, say - is a set of attributes.  $tn(n=1,2..) = \langle A1,V1 \rangle, \langle A2,V2 \rangle, ... \langle An,Vn \rangle$ 

Where n is the arity of t (unary, binary etc) [16, p. 142].

For example, a binary tuple of type contact, we have an attributes of name and address so t=<< Name, Guy>, < Address, Amsterdam>>

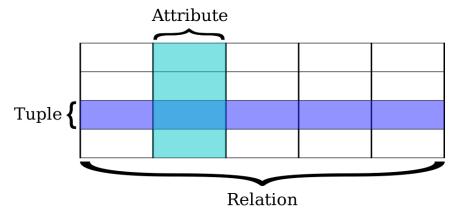
Few rules regarding tuples:

- Each tuple contains exactly one value for each of its attributes.
- Every subset of a tuple is a tuple.
- There are no duplicate tuples.

A relation r consists of heading and a body. The body of r is a set of tuples. And the heading of r is its tuples attribute types [16, p. 146].

```
 \begin{array}{l} \textbf{Example - Relation: } \textit{Grades} = \{<< Student, \textit{Guy}>, < \textit{Grade}, 9>>, \\ << Student, \textit{Guy}>, < \textit{Grade}, 7.5>>, \\ << Student, \textit{Vadim}>, < \textit{Grade}, 8>> \} \end{array}
```

In summary, if a relation is a table, the rows are the tuples, and the columns are the attributes. The heading of the table defines the data types.



The relations theory provides a set of operations which we can apply on relations - such operations allow us to add, delete or modify data. For example, subset of  $\subset$ , superset of  $\supset$ , equals = and others.

Practically, when it come to databases, many of them use SQL (Structured Query Language). SQL is a declarative language designed for constructing relational databases and managing the data that is held in it. For example, we can send a query to insert a new data.

In our thesis, we will try to convert Alloy syntax into SQL. Alloy is based on the notion of relations and it uses relations as its main structure. Therefore, the data model of Alloy can be translated directly into a relational database schema, using SQL. Obviously, Alloy is much more than a data structure. One of the other specifications of Alloy is that, it provides functions. We will discuss Alloy in depth in the next chapter.

#### 3.2 Problem Analysis

Using only Alloy specifications to automatically generate a database system has been challenging. In this section we will discuss the reasons.

#### 3.2.1 Data Structure

Although *Alloy* relations and database tables are both based on the theory of relations, their structural representation is different.

- Database tables are two-dimensional, while relations can have multiple dimensions.
- Database tables are ordered (top-bottom and left-right), while relations are not.
- Database tables can contain empty data (null) and duplicates, while relations/tuples can not.
- In database tables, type names are usually omitted, relations usually involve a type name.

Another difficulty is that, database systems make use of *keys* (primary, foreign and unique keys) that are a vital part of the table structure (e.g. avoiding duplicates and even improve performance). *Alloy* only partially deals with keys or not at all.

In order to generate tables that represent the corresponding Alloy relations, we need to agree on certain rules of interpreting these relations (e.g. row orderings are irrelevant) [16, p. 151].

#### 3.2.2 Data Operations

Alloy uses *predicates* as operations system. It allows users to create customized actions for modifying the data in the system using preconditions, postconditions and algebraic formulas (We will discuss about it in the next chapter). In database systems the core operations are insert, update or delete. We need to bridge between algebraic notation and a SQL query notation.

Furthermore, as mentioned before, in database systems the operators available to the user derive from old state to a new one. In *Alloy* this is not necessarily the case. We need to enforce the specifications to follow that way.

Lastly, we have to assure that the new state is valid (according to the specified conditions of the formula). For example, *Alloy* allows setting multiple operations inside single predicate. In database systems, each operation is discrete and it may occur that one operation succeeded and the following one didn't. In this case, the new state is invalid. To solve this for example, we can use transactions.

We will discuss about the solutions and the related work in the next chapters.

#### 3.3 Research Question

In this paper the following research question has been addressed:

#### How to bridge between Alloy-based specifications and realization?

To answer this question, the following sub-questions have been formulated:

- How can we meet Alloy specifications?
- What are the limitations of Alloy specifications?
- How to validate that Forgery works?

## Alloy

Alloy is a declarative specification language for describing models with structural constraints and behavior. Alloy used for modeling software systems. Alloy includes a tool called Alloy Analyzer for visualizing models, and for exploring and checking the properties of them.

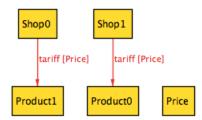
In this chapter we concentrate on the language part of Alloy, and we will present various examples as demonstration. We will not cover the whole language but focus on the essentials required to understand this work.

#### 4.1 Data Structure

Alloy data model is based on *atoms*, *signatures* and *fields*. Atom is the most basic specific element in Alloy. **signature** subsequently, is a set of atoms that also defines the data type. A field then describes the relation between different types of signatures. It is therefore a set of tuples that consists of different types of data. Finally, in Alloy these relations can be unary or binary (using  $\rightarrow$ ).

The following example describes a price list (tariff) of products in a shop.

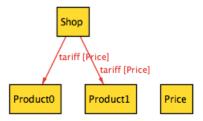
The signatures in this example are *price*, *product* and *shop*. The tariff describes the relation between each product and price within the shop. Simulating this model using Alloy Analyzer will generate all possible examples that follows the model. For example, we may have two shops that have two different products with the same price. In that case, we have two atoms of type shop, two atoms of type product, and single atom of type price.



#### 4.1.1 Cardinalities

Cardinality refers to the amount of elements in a set. Alloy allows us to define cardinality constraints on the data model. Alloy supports *lone* (size is at most 1), *one* (size is only 1), *some* (size is at least 1) and *no* (size is 0). For this example, we assume that we want only one shop in our model:

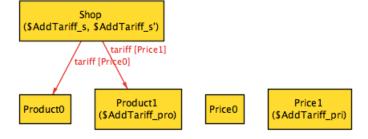
Alloy Analyzer will now only generate examples with exactly one shop.



#### 4.2 Data Operations

Alloy allows defining **pred**icates as operations that act on a specified model. A predicate may convert a certain state of the data system into a new one, based on the rules it defines. The predicates accept signatures as an input. The operations themselves are defined using algebraic formulas. We may use semantics such as + (union), & (intersection), in (subset),  $\rightarrow$  (tupling), and . (join).

The following example describes a predicate that allows adding a new tariff (of product pro with a price of pri to the shop). The shop s describes the old state while s' describes the new state of the system.



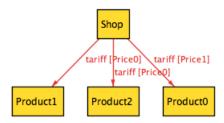
The shop had the product '0' with price '0' and after we added a product '1' with a price of '1'.

#### 4.3 Data Invariants

Alloy allows to create system invariants using **facts**. Those properties are meant to hold of all models constructed by Alloy. Any configuration that is an instance of the specification has to satisfy all the facts. In the previous example we could have products that doesn't belong to any shop (*Product*0).



Using facts, we can assure, for example, that each product must belong to a shop.



#### 4.4 Assertions

Assertions are constraints that were intended to follow from facts of the model. **Assertions** are used for checking that the desirable invariants exist using Alloy Analyzer. Alloy Analyzer tries to find counter examples that does not follow those constraints.

Our new requirement now is that we want that each shop will have maximum one tariff, but such invariant was not specified in our model yet.

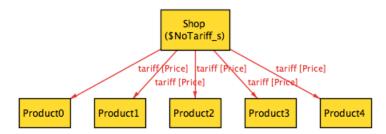
By simulating the model, all the assertions are checked *Lone Tariff*, Alloy Analyzer will alert that it found a counter example:

```
Executing "Check NoTariff for 5"

Solver=sat4j Bitwidth=0 MaxSeq=0 SkolemDepth=1 Symmetry=20
385 vars. 36 primary vars. 590 clauses. 13ms.

Counterexample found. Assertion is invalid. 8ms.
```

By clicking on the counterexample, Alloy Analyzer will present all found counter-models. The following counterexample shows that there are more than one tariff, which is in conflict with the mentioned constrained.



This way, we able to check our model, and make it is more robust minimizing mistakes. Assertions are similar to unit testing which are popular among programming languages.

## Forgery Solution

In this chapter we will discuss on the solution that we offer.

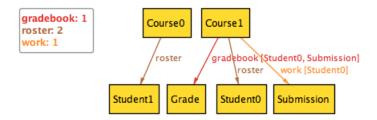
#### 5.1 Key Ingredients

As introduced in the background Alloy specification consists of four main parts: Signatures (and their Cardinalities), Predicates, Facts and Assertions. Together they hint about how the model should be implemented. Using few examples we will demonstrate the conversion from Alloy specifications to an implemented database.

The following example specifies a homework submission and grading system.

```
sig Submission { }
sig Grade { }
sig Student { }
sig Course {
         roster: Student,
         work: roster -> Submission,
         gradebook: work -> Grade
}
```

For those specifications Alloy will generate multiple models. Arbitrarily we chose the following one:



The system contains two courses and two student which are enrolled to each of those courses. Also, Student0 is enrolled to Course1, he submitted his work and got a grade for it.

First We need to generate a database schema for storing the data. As can be seen, Alloy Signatures can be translated directly into persistent database schemas. In Forgery, for each Signature we create a table, and for each field we create a junction table that points to the relevant signature tables. Each Signature table stores its atoms. The relations are linked by id's which are also the primary keys.

For example, the *student* table is created by the following SQL code:

The relation roster will result in a junction table that is created by the following SQL code:

We use foreign keys to enforce integrity. These constraints guarantee that, for example, a row in the table roster with a field student\_id referencing the student table will never have an student\_id value that does not exist in the students table. In addition, since Alloy refers to sets, according to the set theory, every element of a set must be unique; no two members may be identical. Hence, we create a a SQL unique index.

Now when we have a database which we can store data to, we need a way to insert, update or delete data. For example, creating Atoms and implementing Alloy's predicates. For that purpose we decided to use SQL stored procedures. Stored procedures are similar to procedures in other programming languages in that they can accept inputs, return output and support programming statements for performing operations on the database.

Alloy is based on the notation of algebraic mathematics. Operators over sets and relations have their usual semantics: + (union), & (intersection), in (subset),  $\rightarrow$  (tupling), and . (join). SQL supports simple operands such as +, - and set operations such as union, intersection, difference etc. That gives us enough flexibility to transform Alloy predicates into SQL procedures.[12]

We use the tag symbol (') for describing a state transition. For example, student s is the pre-condition, and s' is the post-condition. Also, we use the input underline prefix as an easy way to create new atoms. Each predicate converted to a SQL procedure, wrapped by transaction. In case of failure, a rollback will be applied.

The following predicate enrolls a new student to a course.

```
pred enroll(c, c': Course, _s: Student) {
        c'.roster = c.roster + s
}
   We generate a procedure that contains two Insert queries as the following:
DELIMITER //
CREATE PROCEDURE 'p enroll'(IN c INT(9), IN s VARCHAR(100))
DECLARE EXIT HANDLER FOR SQLEXCEPTION
BEGIN
        ROLLBACK;
END;
START TRANSACTION;
        INSERT INTO student ('value') VALUES (s);
        SET s = LAST INSERT ID();
        IF NOT EXISTS
                 (SELECT 'id' FROM 'roster' WHERE 'student id'= s AND 'course id'=c)
        THEN
                 INSERT INTO 'roster' ('student id', 'course id') VALUES (s, c);
COMMIT:
```

This procedure accepts two parameters: an existing course id (c), and a new student value (as mentioned - underline prefix refers to a new atom). The procedure is callable from running a normal query. For example:

```
p enroll(3, 'Jonathan');
```

END //

It will insert a new row with the value Jonathan to the student table, and another row to the roster table, with the new generated student id and the course id.

Similarly, *Facts* are also converted into procedures. *Facts* don't have inputs, however variables can be defined easily.

The following fact determine that all students must be enrolled to a course.

```
fact mustBeEnrolled {
         all c: Course, s: Student
        s in c.roster
}
  Also in this case we create a SQL procedure.
CREATE PROCEDURE 'f must been rolled '(OUT return value TINYINT UNSIGNED)
DECLARE EXIT HANDLER FOR SQLEXCEPTION
BEGIN
        SET return value=1;
END;
IF EXISTS
         (SELECT * FROM student WHERE id NOT IN (SELECT student_id FROM roster))
        THEN
                 SET return value=1
        ELSE
                 SET return value=0
END IF;
END //
```

Facts procedures modify the flag return\_value to 1 or 0 (logic True or False) which are equivalent to invariant failure or not accordingly. When the data was modified, the procedures are automatically called and in case of a invariant failure, the changes will be reverted to the previous valid state (using transactions).

#### 5.2 Architecture Overview

Forgery consists of 7 main modules:

- 1. Syntax Validator: Forgery checks the input using Alloy API. A failure throws an exception, and stops the execution.
- 2. Parser and Mappers: Forgery parses the Alloy syntax and generates ASTs (Abstract Syntax Trees). Those ASTs are flattened to a simpler map structures for later processing.
- 3. Tables Generator: Creating SQL tables including keys, relations and uniqueness constraints.
- 4. Procedures Generator for Facts and Cardinalities: Creating SQL procedures for verifying the specified invariants and cardinalities.
- 5. Procedures Generator for Predicates: Creating SQL procedures for systemic operations according to the specifications.
- 6. Traces Generator: Reverse engineering for Alloy traces, used for the Validator.
- 7. Validator: replicating the operations that made in Alloy for finding models and comparing data to validate behavioural similarities.

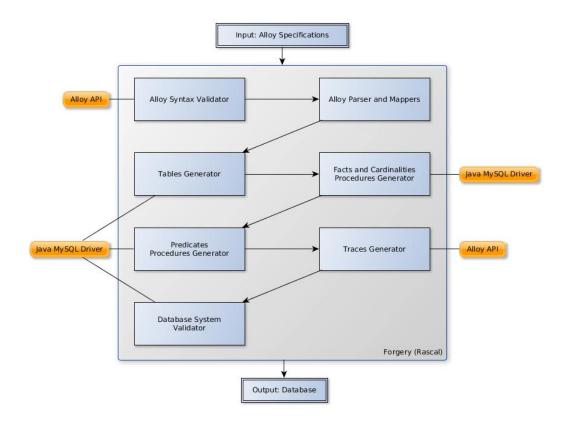


Figure 5.1: Forgery architecture

We implemented Forgery using Rascal. We chose Rascal due to its powerful DSL and AST (Abstract Syntax Trees) tools. Since we used a standard SQL language, any arbitrary database system can be used. We used MySQL due to his popularity.

#### 5.3 Alchemy Comparison

Although related papers will be presented in a different chapter, there is a unique paper called Alchemy [4] that we have studied. Due to overlapping research we will present it here. Similarly to Forgery, Alchemy compiles Alloy specifications into database implementation. We will discuss about the main differences here.

#### 5.3.1 Forgery uses pure SQL

Alchemy generates a synthesizing API as a layer that communicates with the database. In other words, the data validity can be guaranteed only when this API is used. In contrast, Forgery generates a SQL system with constraints that are implemented in the tables and the database level itself. Hence, it is more robust - the validation occurs in the data storing level. Also, SQL language is usually more familiar for technical people. And therefore, it may give a communication advantage.

#### 5.3.2 Alchemy has no evaluation and assertions are not supported

As introduced before, Alloy supports assertions for checking the model. Using the powerful Analyzer we able to detect mistakes in our specifications. Forgery supports assertions and even use their traces for evaluation. Alchemy introduced a shortcut to write predicates. However, those predicate specifications might be in contradiction to invariants. They added an auto-repair functionality that fix the data in case it has a conflict. However, since the specifications are invalid by the nature of Alloy. The assertions and the analyzer cannot be used. Alchemy does not have evaluation method.

#### 5.3.3 Forgery supports atoms control

Alchemy does not generate command options to insert or delete atoms. By default, Forgery creates such procedures (With an option to create them manually) so atoms can be created.

#### 5.4 Scheme Generation

In this section we will discuss about how forgery generates the database scheme; including tables, fields etc. We will use the similar example as described in the overview with additional functionality and we will dive deeper into details. We will also remind some definitions in regarding Alloy.

The example describes a homework submission and grading system. Student's work may be submitted in pairs or individually. The gradebook stores the grade for each student on each submission. The system has some constraints and actions like enrolling students but they will be discussed later on.

```
sig Submission {}
sig Grade {}
sig Student {}
sig Course {
         roster: set Student,
         work: roster -> lone Submission,
         gradebook: work -> lone Grade
}
```

Alloy uses **signatures** (e.g. Submission) to describe a data model [14, p. 30]. Every signature defines a data type, and consists set of atoms drawn from that type. Atoms are elements that are created based on the system user's inputs. Forgery allows atoms to be created only within those signatures.

In addition, a signature can define fields (e.g. in Course). A field describes a relation between different types of Signatures. Basically, it is a set of tuples which consists different types of data. Such a relation can be unary or binary. E.g. roster and work respectively.

#### 5.4.1 Atoms Tables

The signatures Student, Submission, Grade and Course are sets of atoms:

 $Student = \{Guy, Tijs, Jouke..\}$   $Submission = \{homework, project..\}$   $Grade = \{5.5, 8..\}$   $Course = \{Construction..\}$ 

For each signature, atoms table is created. Every table has two fields: id and value. The id field is a primary key for identifying the atom, and value is the input data. Chosen types: Int for id as it is always an integer, and Varchar for value so it can contain any type of input (strings, numbers etc).

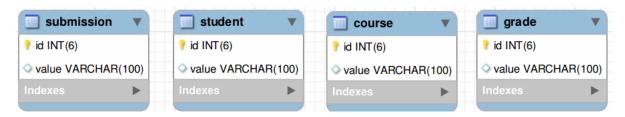


Figure 5.2: Generated tables for Signatures

#### 5.4.2 Fields Relations

The signature Course defines the following relations: roster (enrolled students), work and gradebook.

```
roster = \{ < Construction, Guy >, < Construction, Tijs > .. \} work = \{ < Construction, Guy, hwk1 > .. \} gradebook = \{ < Construction, Guy, homework, 8 > .. \}
```

For every relation, a junction table is created. It describes the relationship between the different multiple relations and the atoms. Every table contains the ids of the atoms that the relation describes. The table name is based on the relation name (right side before the colon sign :). Relation can be unary or binary. Binary relation is expressed by the tuple sign  $\rightarrow$ .

Moreover, Forgery adds SQL Foreign Keys that links between the tables. They are naturally extracted from the Alloy semantics. It guarantee that every junction table will contain valid data that points to existing atoms.

When a relation points to a another relation, Forgery extracts the atomic type. Which means, in other words, Forgery flattens all the relations so the tables will contain pointers to atomic tables only, and this way, the relationships between the tables would be simpler. It adds data redundancy but it makes the algorithm much more simpler.

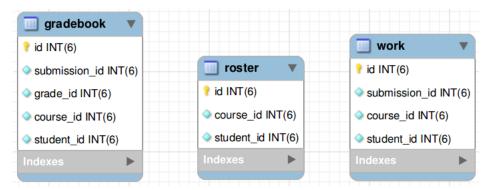


Figure 5.3: Generated tables for Relations

#### 5.4.3 Cardinalities

Alloy syntax supports multiple quantifiers to describe constraints on the data model: *lone* (at most one atom), *some* (at least one atom) and *one* (single atom). Forgery uses two techniques to implement those constraints:

- 1. Adding Unique Indexes for tables: the shared condition of *lone*, *one* and *set* is that the table must not contain more than one similar element. Adding Unique Index guarantee this condition (although only partially/weaker condition for *one*).
- 2. Creating Stored Procedures: one and some cardinalities cannot be fully implemented by applying structural constraints into the SQL table itself. Therefore, we create a SQL procedure instead for each cardinality. The procedure contains a query that counts the rows and group it based on the cardinality criteria and then compare it to the specified cardinality. Those procedures are automatically called when the data is changed. If any violation occurs, the data will be reverted and error will be shown (transactional action). The cardinality procedures are stored in the database and can be identified with the prefix  $c_{-}$ . More about procedures will be explained in the next chapter.

#### 5.5 Predicates Generation

This overview will discuss about the logic behind interpretation of Alloy predicates and creation of atoms. The same example from the previous chapter will be used with few additional statements.

The new statements introduces new features such as adding or deleting students, as they enroll in or drop the course, and assigning grades for each of their submitted work in pairs.

```
sig Submission {}
sig Grade {}
sig Student {}
sig Course {
        roster: set Student,
        work: roster -> lone Submission,
        gradebook: work -> lone Grade
pred Enroll (c, c' : Course, _sNew : Student) {
        c'.roster = c.roster + sNew and no c'.work [sNew]
pred Drop (c, c': Course, s: Student) {
        s not in c'.roster
pred SubmitForPair (c, c': Course, s1: Student, s2: Student,
_bNew : Submission) {
        // pre-condition
        s1 in c.roster and
        s2 in c.roster and
        // update
        c, work = c. work + (s1 \rightarrow bNew) + (s2 \rightarrow bNew)
pred AssignGrade (c, c': Course, s: Student, b: Submission,
g : Grade) {
        c'. gradebook = c. gradebook + (s -> b -> g)
}
```

#### 5.5.1 Using Stored Procedures

Stored Procedure is a SQL feature that encapsulates a query for re-usability purposes. It is used as a layer that communicates with the database internally. Stored Procedures allow faster execution time and they may be useful as a safer synthesizing mechanism (E.g. privileges) [11].

Basically, Stored Procedures are similar to other programming languages in that they can accept input parameters and return multiple values. Also, they may contain programming statements for performing operations in the database and indicate status of failure or success.

Forgery uses stored procedures for multiple purposes. One of them was already introduced previously in reference to cardinalities. Some others will be covered as well in this chapter.

#### Alloy Predicates

Alloy uses **pred**icates (e.g. Enroll) to capture the actions that are supported in the system. Each predicate describes the required state that the system should be in when applying it. Predicates has a header and a body.

#### Predicates Header:

Predicates accept inputs from the user that are used for the states transformation. Each input contains a variable and a mapping to his belonged table. Similarly to Alchemy [4], Forgery uses the prime symbol ' as a variable suffix to distinguish between pre- and post-states of the operation (e.g. c and c').

The inputs may be one of the two different types: an integer or a string. Inputs accept integers as default and each of them represents an Atom id. However, when it comes to a new Atom the id does not exist yet. Therefore, Forgery uses the underline symbol \_ in the variable prefix to refer to a new atom. In this case, the input type is a string, which is the data that the Atom carries. It may be a name of a course or a student and it may be just empty, depends on our model.

For each request for new atom, an Insert query will be added to the procedure, and the created id will be placed in the variable value. E.g. in our example sNew:Student the generated query will be:

```
INSERT INTO student('value') VALUES (_sNew);
SET _sNew = LAST_INSERT_ID();
Predicates Body:
```

The predicates body may contain a formula in which the defined variables in the header are used. The formula semantics of Alloy is based on the class of relational algebras. A predicate may define multiple formulas. Formulas are joined together using the *and* word (or using a new line separator). Forgery handles them as a list of operations which performed serially one after one (transactionally - all of them must succeed before the commit). Forgery assumes that the formulas are correct because they are first tested using Alloy Syntax Checker. For example, two operands of an operation must be of the same relation type. Also, each formula refers to a pre- or a post-condition.

#### Supported operators:

1. (not)in operator - Used as precondition to check if the element exists or not. [Output: True or False]. Example: s1 in c.roster

```
IF NOT EXISTS
  (SELECT 'id' FROM 'roster' WHERE 'student_id'=s1 AND 'course_id'=c)
THEN
  SELECT 'An error has occurred, operation rollbacked
  & the stored procedure was terminated';
  ROLLBACK;
END IF;
```

```
    Union - the operator '+' is used to compute union of sets. [Output: A set]. Example: c'.roster = c.roster + s1
        INSERT INTO 'roster' ('student_id', 'course_id') VALUES(s1, c);
    Difference - the operator '-' works similarly to union, but with delete statement instead. [Output: A set]. Example: c'.roster = c.roster - s1
        DELETE FROM 'roster' WHERE 'student_id'=s1 AND 'course_id'=c;
    Join - the operator is represented by square braces [] or using the dot (.) sign (although in other languages it usually means object access). Note: r1.r2 <=> r2[r1].
        In Delete operations join is performed using the "WHERE" selector.
        In Insert operations join is performed like a tuple (see tupling example). In other cases, it is used as an independent pre-condition. Example: no c'.work[_sNew]
```

```
IF EXISTS
(SELECT id FROM 'work' WHERE 'student_id'=_sNew AND 'course_id'=c)
THEN

SELECT 'An error has occurred, operation rollbacked
    and the stored procedure was terminated';
    ROLLBACK;
```

**END** IF;

5. Tupling - represented by  $\rightarrow$  symbol. As mentioned before, a tuple is equivalent to a table row (containing attributes / columns). We use it for operations such as insert or delete. Example:  $c'.work = c.work + (s1 \rightarrow b) + (s2 \rightarrow b)$ 

#### **Atoms Creation:**

Forgery supports two ways for creating new Atoms. The first way, which was introduced already is by using underline \_ variable prefix. The other way is by using the Forgery "create" procedures. Forgery automatically generates atom creation procedure for each signature. For example:

```
DELIMITER //
CREATE PROCEDURE 'create_submission' (IN atomVal VARCHAR(100))
BEGIN
DECLARE EXIT HANDLER FOR SQLEXCEPTION
BEGIN
ROLLBACK;
END;

START TRANSACTION;
INSERT INTO 'submission' ('value') VALUES (atomVal);
— facts and cardinalities are included here.

COMMIT;
END //
```

As mentioned before, *Forgery* verifies all the invariants (cardinalities and facts) in each procedure. This rule applies here. This means that if there is any violation, the data will be reverted.

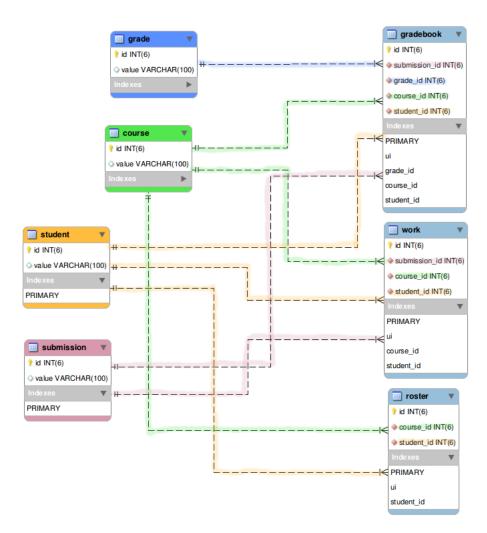


Figure 5.4: Generated Relational Database

#### 5.6 Forgery Algorithms

#### 5.6.1 Scheme Generation

The scheme is generated based on the signatures, fields and cardinalities.

Let S be a list of signatures, s is a single signature, R is its contained relations, r is a single relation.

#### Algorithm 1 Database scheme mapper

```
1: function Create Scheme(S)
       tables = ()
                                                                          ⊳ map (table name: list of fields)
2:
       for each signature s in S do
3:
          add (s.name: id, value) to tables
4:
          for each relation r in s.R do
5:
              fields = \{\}
                                                                      > set of table fields with cardinalities
6:
              add s.name. 'id' to fields
7:
              add Atomic fields (r.op1, tables, S) to fields
8:
              if r.type is Binary then
9:
                 add Atomic fields (r.op2, tables, S) to fields
10:
11:
              add (r.name: fields) to tables
12:
          end for
13:
       end for
14:
15:
       return \ tables
16: end function
```

#### Algorithm 2 Returns the signature atoms tables

```
1: function Atomic Fields (r, tables, S)
2: if r.name in S.names then
3: return r.name.'_id'
4: end if
5: return tables [r.name]
6: end function
```

#### Algorithm 3 Returns the query

```
1: function GENERATE QUERY(tables)
      query = ""
2:
      for table in tables do
3:
          add SQL Statement ("Create Table", table.name) to query
4:
          {\bf for}\ field\ {\rm in}\ tables[table]\ {\bf do}
5:
             add SQL Statement ("Create Column", field.name) to query
6:
             add SQL Statement ("Foreign Key", field.name) to query
7:
             if field.cardinality is lone or one or set then
8:
                 add SQL Statement ("Create Unique Index", fields) to query
9:
             end if
10:
             if field.cardinality is some or one then
11:
                 // Cardinality will be created using procedures
12:
             end if
13:
14:
          end for
          add SQL Statement ("Create Column", 'id') to query
15:
          add SQL Statement ("Create Primary Key", 'id') to query
16:
      end for
17:
18:
      return query
19: end function
```

#### 5.6.2 Procedures Generation for Predicates

Let p be a predicate, containing its name, its inputs and its body. The body contains the pre- and the post-conditions (operations). l is a line of operation. i is an input. It contains its type, its name and its value.

## Algorithm 4 Returns the predicates query function GENERATE PROCEDURES(predicates)

```
query = ""
2:
      for p in predicates do
         add SQL Statement ("CREATE PROCEDURE p.name (list of p.inputs)") to query
4:
         add SQL Statement ("DECLARE EXIT HANDLER FOR SQLEXCEPTION; BEGIN; ROLL-
   BACK; END; START TRANSACTION;") to query
         for i in p.inputs do \triangleright if it is a new atom, we need to insert it, and get its new generated id.
6:
            if i.name[0,1] is " " then
               add SQL Statement ("INSERT INTO i.type SET value='i.value'; SET var i.name =
8:
   LAST INSERT ID();") to query
            end if
10:
         end for
         for l in p.body do
                                                                         ▶ Operations over tables
            if \ l.algebraic Operation \ is + then
12:
               add SQL Statement
                                         ("IF
                                                NOT
                                                       EXISTS
                                                                  INSERT
                                                                            INTO l.op1
                                                                                           SET
   value='p.varInputs[l.op2]''') to query
            else if l.algebraicOperation is - then
14:
               add
                      SQL
                             Statement
                                         ("IF
                                                EXISTS
                                                           DELETE
                                                                       FROM
                                                                                l.op1
                                                                                        WHERE
   value='p.varInputs[l.op2]'") to query
            else if l.algebraicOperation is in then
16:
               add SQL Statement ("IF NOT EXISTS (SELECT * FROM l.op2 WHERE
   value='p.varInputs[l.op1]') THEN (SELECT 'precondition violated'; ROLLBACK);") to query
            else if l.algebraicOperation is notin then
18:
               add SQL Statement ("IF EXISTS (SELECT * FROM l.op2 WHERE
   value='p.varInputs[l.op1]') THEN (SELECT 'precondition violated'; ROLLBACK);") to query
            else if l.algebraicOperation is = then
20:
               add SQL Statement ("IF EXISTS (CHECKSUM TABLE l.op1, l.op2) THEN (SELECT
   'precondition violated'; ROLLBACK);") to query
            end if
22:
         end for
         add SQL Statement ("COMMIT;") to query
24:
         add SQL Statement ("Create Table", table.name) to query
26:
         for field in tables[table] do
            add SQL Statement ("Create Column", field.name) to query
            \mathbf{add} SQL Statement ("Foreign Key", field.name) to query
28:
            if field.cardinality is lone or one or set then
               add SQL Statement ("Create Unique Index", fields) to query
30:
            end if
            if field.cardinality is some or one then
32:
               add SQL Statement ("Create Cardinality Procedure", fields) to query
            end if
34:
         add SQL Statement ("Create Column", 'id') to query
36:
         add SQL Statement ("Create Primary Key", 'id') to query
      end for
      return query
40: end function
```

#### 5.6.3 Procedures Generation for Facts

#### 5.7 Evaluation

#### 5.7.1 Reverse Engineering

When *Alloy* simulates a model, it generates traces and saves them as a temporary XML file. Those traces describe the data history of the system and the transition between them.

The idea was to use those traces to imitate the same behavior in our generated database system. In other words, use the same initial data, and follow the same operations that Alloy did. Then, we are able to compare the results of Forgery to those in *Alloy*.

We use this reverse engineering technique to make sure our solution is consistent to Alloy behavior and evaluates our system that way.

However, we found that the traces miss some important information.

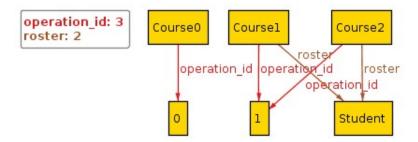
By default, the traces are not ordered and this has to be configured manually. Otherwise, the traces are useless because we cannot identify the order of the operations and imitate them. To enable ordering in Alloy, the ordering library has to be included and initialized using a predicate named *init*. Moreover, the logic behind the transition from one step to another has to be defined. It can be done using a fact named *traces*.

Besides, although we can now have an ordered list of the data history, we unable to identify which predicates were used. It means that we cannot sure which operation to use to imitate the transition between the different steps. In order to deal with it we used a small trick. We added an arbitrary atom called  $operation_id$  so Alloy will create traces for it. This atom identifies each operation. On each step we use the traces of this identifier to know what operation was used.

Forgery ignores the predicate init, the fact traces and the field  $operation_id$  as they are not relevant for generating the database system.

In the following example we added the mentioned tweaks, so we able to generate the correct traces. The code is included, and later the data flow is explained briefly.

```
open util/ordering[Course] as CourseOrder
sig Student {}
sig Course {
        roster : set Student,
        operation id: Int
}
pred Enroll (c, c': Course, st: Student) {
        c '.roster = c.roster + \_st
        and c'. operation id = 1
pred init(c: Course) {
        no c.roster
        and c. operation id = 0
}
fact traces {
    init [first]
    all c: Course - last | let c' = next[c] |
        some st: Student
        Enroll [c,c',st]
}
  Alloy's output:
```



The data flow:

- 1. Initializing (0): The precondition for the initializing state is that there are no students enrolled and therefore no students enrolled to Course0.
- 2. Enrolling (1): The student is enrolled to Course1.
- 3. Enrolling (1): The student is enrolled to Course 2.

#### 5.7.2 Validation Scenarios

In order to validate Forgery's output we have to consider the following scenarios:

True Positive	True Negative
False Positive	False Negative

#### True Positive - False Negative

- True Positive: Correct models in *Alloy* and in *Forgery*.
- False Negative: Correct models in Alloy but incorrect in Forgery.

For those two cases, we iterate over all the correct *Alloy* models. And then, we imitate each step using the traces in Forgery as described before.

#### True Negative - False Positive

- True Negative: Incorrect models in Alloy and in Forgery.
- False Positive: Incorrect models in Alloy but correct in Forgery.

For those two cases, we use the assertions results (counter-example traces) and imitate each step in Forgery as described before.

Simulating those four scenarios in Forgery for different inputs will support us finding bugs in Forgery, and fix them so it will better matched to Alloy's behavior.

### Related Work

Alloy is increasingly becoming a popular declarative modeling language. It is powerful by providing early error detection, supported by analysis tools for simulating and debugging models [7]. There were few related papers that were written about Alloy.

#### 6.1 From UML to Alloy and Back Again

This paper presents a study involving UML2Alloy, a tool for transforming UML models in form of UML class diagrams which are augmented with OCL constraints, to Alloy. The conversion allows analysis of UML models via Alloy, to identify consistencies in those UML models.

# 6.2 Alchemy: Transmuting Base Alloy Specifications into Implementations

We present Alchemy, which compiles Alloy specifications into implementations that execute against persistent databases. Alchemy translates a subset of Alloy predicates into imperative update operations, and it converts facts into database integrity constraints that it maintains automatically in the face of these imperative actions.

# 6.3 Mapping between Alloy specifications and database implementations

An abstract Alloy specification is far from an actual implementation, and manually refining the former into the latter is unfortunately a non-trivial task. This paper identifies a subset of the Alloy language that is equivalent to a relational database schema with the most conventional integrity constraints, namely functional and inclusion dependencies.

### 6.4 Towards an Operational Semantics for Alloy

In this paper we demonstrate the subtlety of representing state in Alloy speci- fications. We formalize a natural notion of transition semantics for state-based specifications and show examples of specifications in this class for which analy- sis based on relational algebra can induce false confidence in designs.

## Conclusions

In this work we presented *Forgery* as a tool that supports the realization of *Alloy* based specifications. We able to generate a full-scale database including structural tables, constraints and functions for data updating operations. The output is a pure SQL that doesn't require any external API or additional dependencies. In addition, it is easily expandable by using different SQL features. For example it is possible to manage privileges of users and that way increasing security.

As mentioned before, it is not possible to develop fault-free software in practical scenario considering human nature [8]. That also applies for *Forgery*. Hence, we developed a validation mechanism with reverse engineering that allows to compare the results to those in *Alloy*. Moreover, enabling Assertions helps to find issues in the model; A feature that was not possible in Alchemy.

Together with *Fors* we created a toolchain that supports the main software development processes: modelling and implementation. Those two important processes have direct affect on the software quality. By improving them organizations might save lot of money and other resources.

There are still challenges to be solved in *Forgery*, for instance, expanding the set of supported *Alloy* syntax and resolving potential exceptions. However, to the best of our knowledge, considering multiple scenarios, *Forgery* has achieved his goals.

## Bibliography

- [1] Pete Sawyer and Gerald Kotonya, Software Requirements (IEEE, 2001).
- [2] Walid Taha, Domain-Specific Languages (Rice University, 2008).
- [3] Chiel Peters, Fors: Separating Configuration From Formal Specification (University of Amsterdam, 2014).
- [4] Daniel J. Dougherty et al, Alchemy: Transmuting Base Alloy Specifications into Implementations (Worcester, 2008).
- [5] Daniel Jackson, Software Abstractions: Logic, Language and Analysis (MIT, 2012).
- [6] Sabrina De Capitani et al, Database Security (Wiley, 2002).
- [7] Loic Gammaitoni et al, Verifying Modelling Languages using Lightning (University of Luxembourg, 2014).
- [8] Ajeet Kumar et al, Early Software Reliability Prediction: A Fuzzy Logic Approach (Springer, 2013).
- [9] Rob Seater and Greg Dennis, Tutorial for Alloy Analyzer 4.0 (MIT, 2014).
- [10] Barry Boehm and Victor R. Basili, Software Defect Reduction Top 10 List (IEEE, 2001).
- [11] Tony Patton, Determine when to use stored procedures vs. SQL in the code (TechRepublic, 2005).
- [12] T. M. Murali, SQL and Relational Algebra (VirginiaTech Engineering College, 2010).
- [13] Khaleel Ahmad and Nitasha Varshney, On Minimizing Software Defects during New Product Development Using Enhanced Preventive Approach (IJSCE, 2012).
- [14] Daniel Jackson, Micromodels of software: lightweight modelling and analysis with Alloy (MIT, 2002).
- [15] Michael Brackett, Data Architecture and Data Structures (DATAVERSITY, 2013).
- [16] Christopher J. Date, An Introduction to Database Systems (Pearson, 2003).

## Appendix

#### 8.1 Alloy Quick Reference

Full Reference: http://www.ics.uci.edu/alspaugh/cls/shr/alloy.html

#### 8.1.1 Logic

The Alloy logic is a first-order logic in which the domain is the set of all relations, and terms include relational expressions such as joins.

Everything in Alloy is a relation!

- A relation is a set of tuples of the same (positive) arity. Each tuple lists entities that are related to each other. The size of the relation is the number of tuples; the arity of the relation is the arity of the tuples.
- Sets are represented by unary relations. Each 1-tuple in the unary relation contains an element of the set.
- Scalars are represented by singleton sets. Since a set is a unary relation, an scalar is thus represented as a singleton (size 1) unary relation.

As a result, the operators apply to relations, sets, and scalars, and there are very few cases that produce no result.

Page numbers refer to Daniel Jackson, Software Abstractions, MIT Press 2006.

### 8.1.2 Syntax

Set constants 50		
univ	The universal set	
none	The empty set	

Relation constants 50			
iden	The identity relation		

Set operators 52		
Symbol	Name	Result
+	Union	A set
&	Intersection	
-	Difference	
in	Subset	T or F
=	Equality	

Relation operators 55			
Symbol	Symbol Name		
->	(Arrow) product	R1 -> R2	
	Join	R1 . R2	
	Join (a second notation for it)	R2 [R1]	
~	Transpose	~ R	
^	Transitive closure	^ R	
*	Reflexive transitive closure	* R	
<:	Domain restriction	Set <: R	
:>	Range restriction	R :> Set	
++	Override	R1 ++ R2	

Logical operators 69			
Symbol	Keyword	Name or result	
!	not	negation	
&&	and	conjunction	
	or	disjunction	
=>	implies	implication	
<=>	iff	logical equivalence	
	else	$A=>B$ else $C \equiv (A\&\&B)  (!A\&\&C)$	

${\bf Quantifiers/predicates} \ 70$			
Quantification		Predicate on relations	
	$oxed{Q}$ var:set $overline{ }$ formula	Q e	
all	universal	_	
some	existential	size is 1 or greater	
no	¬∃	size is 0	
lone	zero or one exists	size is 0 or 1	
one	exactly one exists	singleton	

let 73	
$let x = e \mid A$	A with every occurrence of x replaced by expression e

#### Signatures and relations

(Parts of this subsection describe the Alloy language.)

Each set of atoms is defined by a signature, with keyword sig.

A signature can contain zero or more relation declarations, separated by commas. Each declaration names a (binary) relation between the set defined by the signature and a set or relation.

Relationships among signatures			
S in T U in T	subset	Every S is a T, and every U is a T	An S can also be a U
S extends T U extends T	extension		An S cannot also be a U

The extended signature must be either a top-level signature or a subsignature.

#### Constraining a declaration

There are two ways:

- 1. with set or relation multiplicity constraints in the signature. These are a quick shorthand. The example above has several of these (all are lone).
- 2. with a fact 117 that states a constraint on the set or relation. The constraint is expressed in the Alloy logic.

(The fact keyword may be omitted if the fact is only about the relations of a single signature, and it immediately follows that signature — then it is a signature fact, and is implicitly universally quantified over the signature's set, and may use this as if it were the variable of this implied quantification.)

#### Multiplicity constraints in declarations

Set declarations with multiplicities 76			
e is a e	e is a expression producing a set (arity 1)		
x: set e	x a subset of e		
x: lone e	x empty or a singleton subset of e		
x: some e	x a nonempty subset of e		
x: one e	x a singleton subset of e (i.e. a scalar)		

x: e	x a singleton subset of e
7. 0	(equivalent to one)

Relation declarations with -> multiplicities 77			
A and	A and B are expressions producing a relation		
m and n are some, lone, one, or not present (which is equivalent to set)			
r: A m -> n B	m elements of A map to each element of B		
each element of A maps to n elements of B			

#### **Facts**

117 A fact contains a formula in the Alloy logic that is assumed to always be true. See the Alloy language for more details.

#### Disjointness

71 disj before a list of variables restricts their bindings to be disjoint.

#### Cardinality constraints

80 The prefix operator # (cardinality) on a relation produces the relation's size. The result can be operated on with + - = <> = <> =. Positive integer literals can appear in cardinality expressions. sum x: e | ie sums the value of ie for each x in set e.

#### 8.1.3 Modelling

The Alloy language uses the Alloy logic plus some other constructs to make models. In Alloy, a model is "a description of a software abstraction" 4.

(Recall that in FOL a model means something different.)

#### Language constructs

The Alloy language adds these constructs to the Alloy logic:

- 1. A module line gives the relative pathname of the model's file (minus the ".als" suffix). The pathname is relative to the directory that imported module pathnames are going to be relative to. (Obviously, the module line is mostly redundant with the file's full pathname.)
- 2. A sig (signature) declares one or more sets of atoms, and their relations to other sets.
- 3. A fun (function) defines a way of getting a relation (or set, or atom). It can take parameters that are used in getting its result. It can define a relation (usually using ->) and make use of it to produce its result. It is a FOL function for the Alloy logic, in which expressions are relations.
- 4. A pred (predicate) defines a formula (true or false). It can take parameters that are used in getting its result. It is a FOL predicate for the Alloy logic.
- 5. A fact defines a formula that you assume is valid (always true, for any world). The Alloy analyzer uses facts as axioms in constructing its examples and counterexamples.
- 6. You run a predicate in order to see the examples (if any) the Alloy analyzer finds for which the predicate is true.

You define the scope that the analyzer checks by saying things like "run for 3" or "run for 3 but 4 Dog". The analyzer will then check only possible examples that contain no more than that many of atoms from each set.

If it finds an example, then the predicate is satisfiable.

If it finds no examples, the predicate may be either invalid (false for all possible examples); or it may be satisfiable but not within the scope you used.

- 7. An assert (assertion) defines a formula that you claim will always be true. An assertion differs from a fact in that the Alloy analyzer will check an assertion to see if it is true for all the examples in a scope, whereas the analyzer assumes each fact is true and uses them to constrain which examples it looks at.
- 8. You check an assertion in order to see whether the Alloy analyzer finds any counterexamples.

You define the scope as for a run command.

If it finds a counterexample, then the predicate is unsatisfiable.

If it finds no counterexamples, the predicate may be either valid (true for all possible examples); or it may be unsatisfiable but not within the scope you used.

#### Which construct to use where?

- 1. Writing a model (Alloy file) that might need to import other models? Use module.
- 2. Need a set of atoms? Use a sig.
- 3. Need an expression, whose value is a function (or set, or scalar)? Use a fun (function).
- 4. Need a formula, whose value is true or false? Use a pred (predicate).
- 5. Need to state an axiom that you want to be true always? Use a fact (function).
- 6. Need an example for which a pred is true? run the predicate to see if one exists. It's like using an existential quantifier over all the predicate's parameters.
- 7. Want to claim something is always true? Use an assert (assertion).
- 8. Want to see if an assert is unsatisfiable? check the assertion to see if any counterexample can be found.

#### 8.1.4 Signatures

Signatures 91		
sig A {fields}	Declares a set A of atoms	
sig A extends B {fields}	Declares a subset A of set B, disjoint from all other extends subsets of B	
sig A in B {fields}	Declares a subset A of B	
$sig A in B + C \{fields\}$	Declares a subset A of the union (+) of sets B and C	
abstract sig A {fields}	Declares a set A that contains no atoms other than the ones in its subsets (if any)	
one sig A {fields}	Declares a singleton set A	
lone sig A {fields}	Declares a set A of 0 or 1 atom	
some sig A {fields}	Declares a nonempty set A	
sig A, B {fields}	Declares two sets A and B of atoms Wherever A appeared above, a list of names can appear	

Fields (in a signature for set A) 95		
f: e	Declares a relation f that's a subset of A->e. e can be any expression that produces a set — union, intersection,, any combination.	
f: lone e	Each A is related to no e or one e.	
f: one e	Each A is related to exactly one e.	

f: some e	Each A is related to at least one e.
f: g->h	Each A is related to a relation from g to h.
f: one g lone -> some h	The multiplicities have their usual meanings.  Here, each A is related to exactly one relation relating each g to 1 or more h's, and each h is related to 0 or 1 g.

#### 8.1.5 Functions

Function 121s		
fun Name [parameters] : type {e}	Defines a function, with the given name and (possibly empty) parameters, and producing a relation (or set, or scalar) of the given type.  The result is defined by the expression e, which may reference the parameters.	

#### 8.1.6 Predicates

Predicates 121		
pred Name [parameters] {f}	Defines a predicate, with the given name and (possibly empty) parameters.  A predicate always produces true or false, so no type is needed.  The result is defined by the formula f, which may reference the parameters.	

#### 8.1.7 Facts

Facts 117		
fact {e}	The expression e is a constraint that the analyzer will assume is always true.	
fact Name {e}	You can name a fact if you wish; the analyzer will ignore the name.	

#### 8.1.8 Assertions

Assertions 124		
assert Name {f}	Defines a assertion, with the given name. Assertions take no parameters.  An assertion always produces true or false, so no type is needed.  The result is defined by the formula f.	