



TECHNIQUES DE
GÉNIE AÉROSPATIAL

ENN

ÉCOLE
NATIONALE
D'AÉROTECHNIQUE

$$\frac{\partial}{\partial r} = \frac{1}{r} \frac{\partial}{\partial r} + \frac{\partial^2}{\partial r^2} + \underbrace{\frac{1}{r} \left(\frac{\Delta r}{2} \frac{\partial^2}{\partial r^2} \dots \right) + \left(\frac{\Delta r^2}{12} \frac{\partial^3}{\partial r^3} \dots \right)}_{\text{erreur de troncature}}$$

⇒ schéma consistant.
schéma ordre 1 (Δr exposant 1).

en reprenant le même calcul par l'ordre 2

$$\frac{\partial}{\partial r} = \frac{1}{r} \left(\frac{C_{i+1} - C_{i-1}}{2\Delta r} \right) + \frac{C_{i+1} - 2C_i + C_{i-1}}{\Delta r^2}$$

$$\frac{\partial}{\partial r} = \frac{1}{r 2\Delta r} \left(C_i + \Delta r \frac{\partial}{\partial r} + \frac{\Delta r^2}{2} \frac{\partial^2}{\partial r^2} - (C_i - \Delta r \frac{\partial}{\partial r} + \frac{\Delta r^2}{2} \frac{\partial^2}{\partial r^2} \dots) \right) + \frac{1}{\Delta r^2} \left(C_i + \Delta r \frac{\partial}{\partial r} + \frac{\Delta r^2}{2} \frac{\partial^2}{\partial r^2} - 2C_i + C_i - \Delta r \frac{\partial}{\partial r} + \frac{\Delta r^2}{2} \frac{\partial^2}{\partial r^2} \right)$$

$$\frac{\partial}{\partial r} = \left(\frac{1}{r} \right) \left(\frac{1}{2\Delta r} \right) \left(2\Delta r \frac{\partial}{\partial r} + \frac{\Delta r^2}{3} \frac{\partial^2}{\partial r^2} \dots \right) + \frac{1}{\Delta r^2} \left(\Delta r^2 \frac{\partial^2}{\partial r^2} + \frac{\Delta r^4}{12} \frac{\partial^4}{\partial r^4} \dots \right)$$

$$\frac{\partial}{\partial r} = \left(\frac{1}{r} \right) \left(\frac{\partial}{\partial r} + \frac{\Delta r^2}{6} \frac{\partial^3}{\partial r^3} \dots \right)$$

$$+ \frac{1}{\Delta r^2} \left(\frac{\partial^2}{\partial r^2} \right) + \left(\frac{\Delta r^2}{12} \frac{\partial^4}{\partial r^4} \dots \right)$$

$$\frac{\partial}{\partial r} = \frac{1}{r} \frac{\partial}{\partial r} + \frac{\partial^2}{\partial r^2} + \left[\frac{\Delta r^2}{6} \frac{\partial^3}{\partial r^3} + \frac{\Delta r^2}{12} \frac{\partial^4}{\partial r^4} \dots \right]$$

abandonner
ordre 2
constant