## CLASS QUIZ: JANUARY 19: MATHEMATICAL INDUCTION

MATH 153, SECTION 55 (VIPUL NAIK)

	name (print clearly in capital letters):
	all these questions, natural number refers to positive integer. In particular, 0 is not considered to b
	al number.
(1)	Suppose S is a subset of the natural numbers with the property that $1 \in S$ and $k \in S \implies k+2 \in S$ . What can we conclude is <b>definitely true</b> about S?  (A) S contains all natural numbers.
	<ul><li>(B) S contains all natural numbers other than 2. It may or may not contain 2.</li><li>(C) S contains all odd natural numbers.</li></ul>
	<ul> <li>(D) S contains all even natural numbers.</li> <li>(E) S does not contain any natural number other than 1.</li> </ul>
	Your answer:
(2)	Suppose $S$ is a subset of the natural numbers with the property that whenever $k \in S$ , we have $k+5 \in S$ . Which of these is the <b>smallest subset</b> $T$ with the property that checking $T \subseteq S$ is sufficient to show that $S$ is the set of all natural numbers?  (A) $\{1,2,3\}$ (B) $\{1,2,3,4\}$ (C) $\{1,2,3,4,5\}$ (D) $\{1,4\}$ (E) $\{1,3,5\}$
	four answer:
(3)	Consider the function $f(x) := a \sin x + b \cos x$ , with $a, b$ nonzero reals. The $n^{th}$ derivative of $f$ is denote $f^{(n)}$ . The association $n \mapsto f^{(n)}$ is periodic, i.e., there is a unique smallest positive integer $f$ such that $f^{(n+h)} = f^{(n)}$ for all $f$ . What is <b>this value</b> of $f$ ?  (A) 1 (B) 2 (C) 3 (D) 4 (E) 5
	Your answer:
	What is the correct <b>general expression</b> for the <b>sum</b> $\sum_{k=2}^{n} \frac{1}{k^2-1}$ for a positive integer $n \geq 2$ ? (A) $\frac{3}{2} - \frac{2n+3}{2(n+1)}$ (B) $\frac{3}{2} - \frac{2n+3}{n(n+1)}$ (C) $\frac{3}{4} - \frac{2n+1}{(n+1)(n+2)}$ (D) $\frac{3}{4} - \frac{2n-1}{2n(n-1)}$ (E) $\frac{3}{4} - \frac{2n+1}{2n(n+1)}$
	Your answer: