





What do you see?



Interactions



Interactions

cow eats grass



(co)Evolution



(co)Evolution

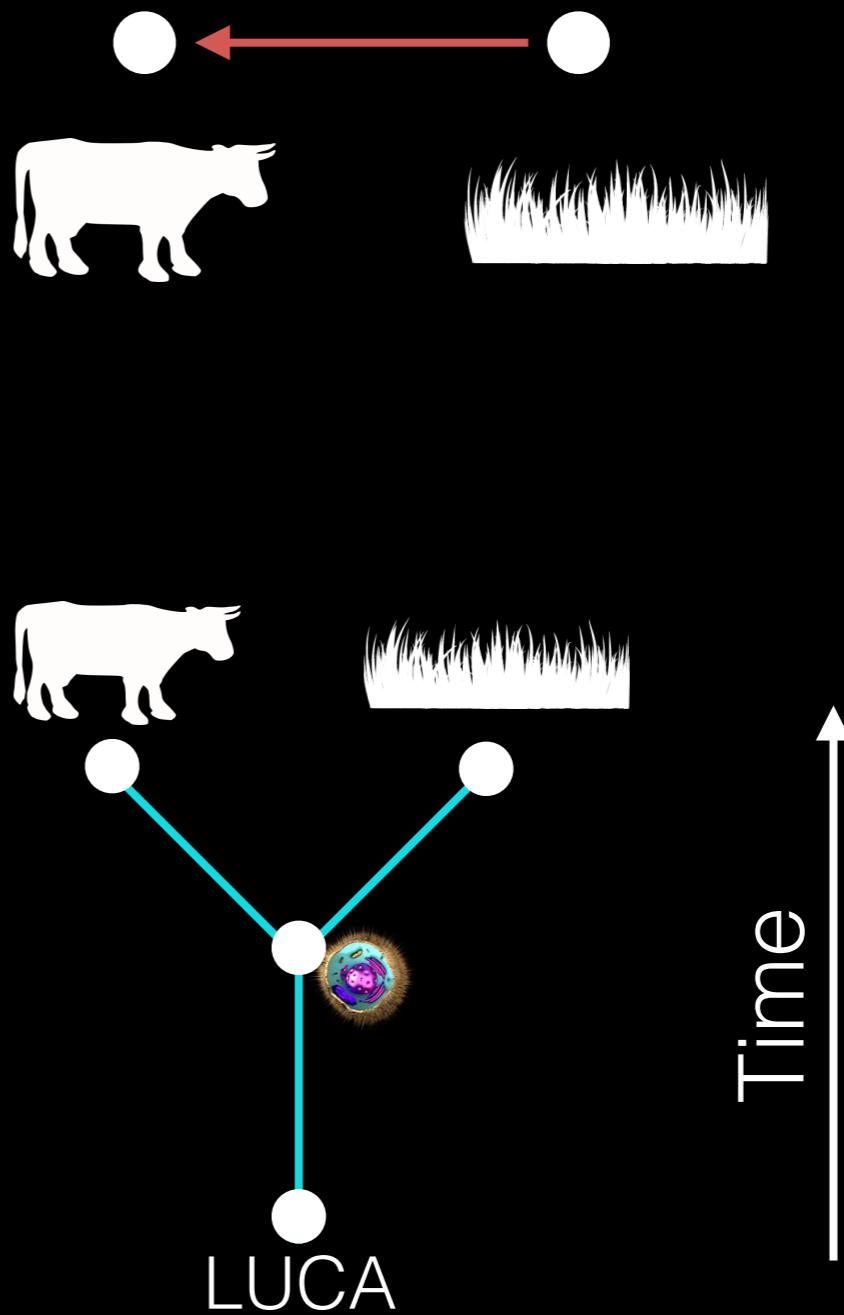
cow's stomach digest grass



How do you write it?

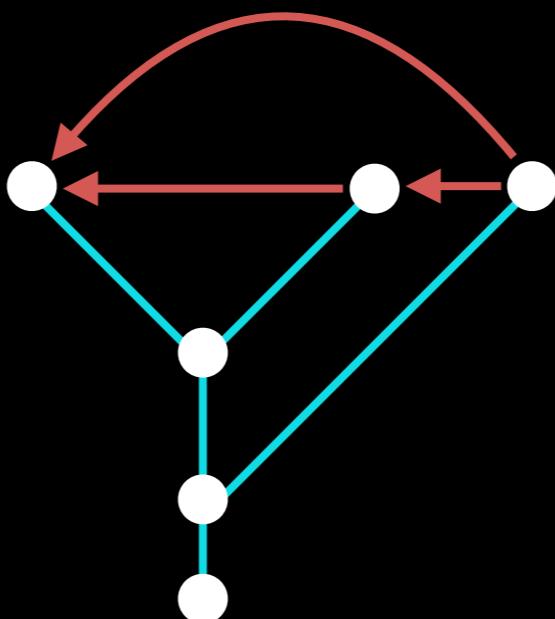
(if you are a mathematician)

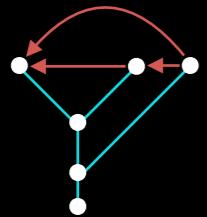




the Web and the Tree

on the interplay between ecological processes and evolutionary histories





the Web and the Tree

on the interplay between ecological
processes and evolutionary histories

Giulio Valentino Dalla Riva

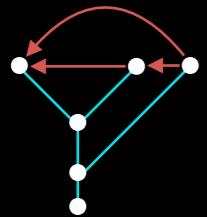
Supervisors:

Mike Steel

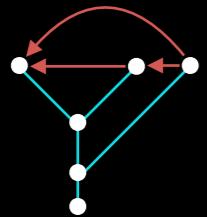
Charles Semple

Daniel Stouffer

University of Canterbury 31 March 2016

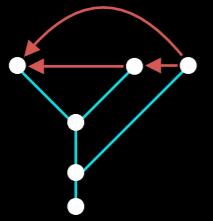


1. Random Dot Product Graphs (Chap. 4)
2. Centrality & Uniqueness (Chaps. 5 & 7)
3. Niche Evolution and Diversity (Chap. 6)

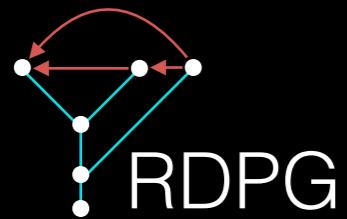


1. Random Dot Product Graphs (Chap. 4)
2. Centrality & Uniqueness (Chaps. 5 & 7)
3. Niche Evolution and Diversity (Chap. 6)

**and skip other work
(sorry coauthors)**



RDPG

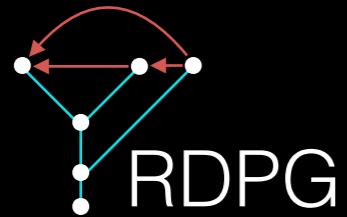


OIKOS SYNTHESISING
ECOLOGY

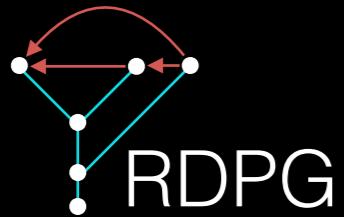
Research

Exploring the evolutionary signature of food webs' backbones using functional traits

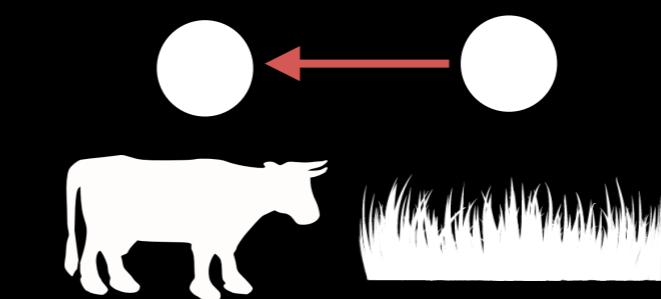
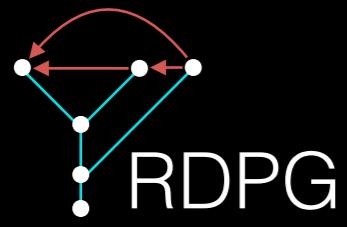
Giulio V. Dalla Riva¹ and Daniel B. Stouffer Issue

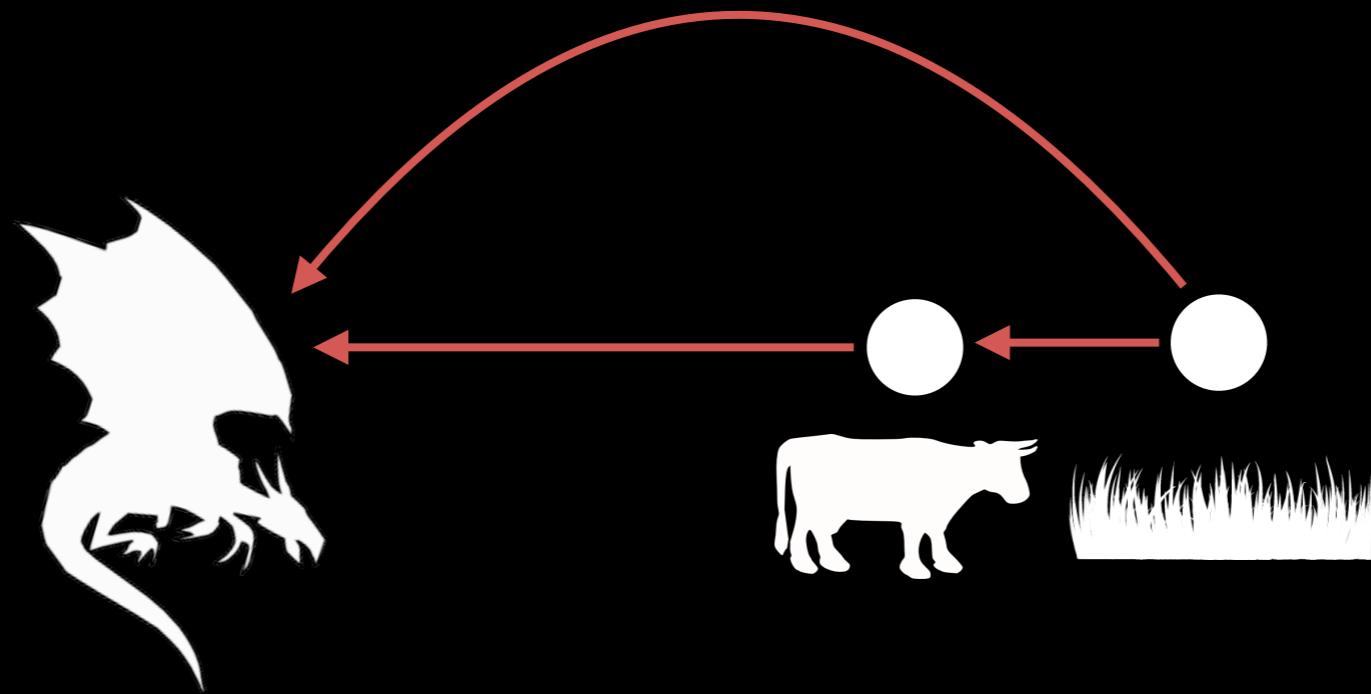
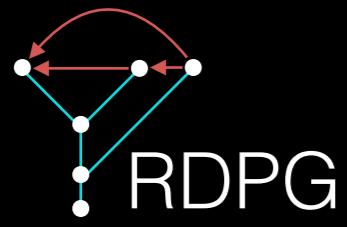


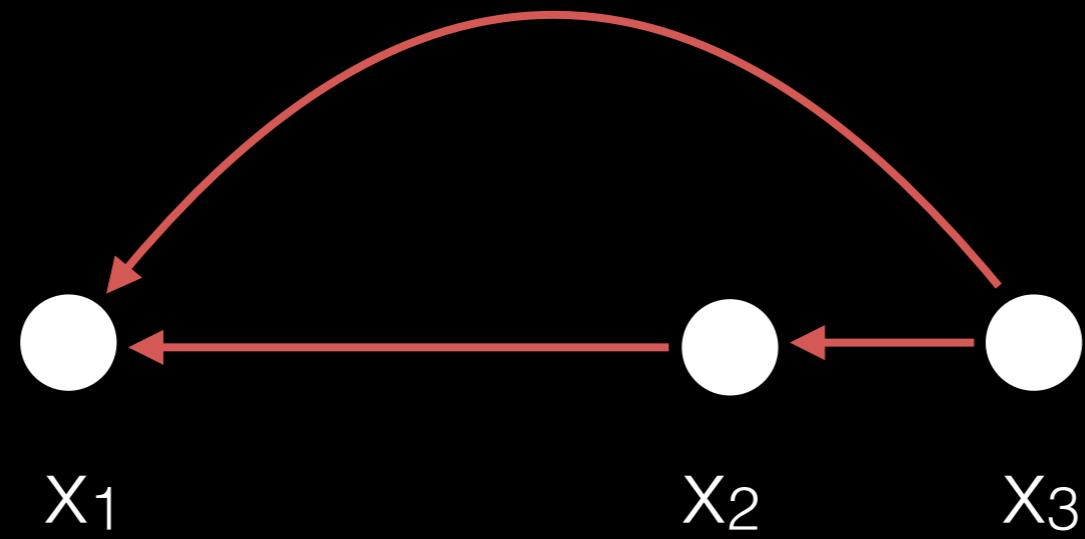
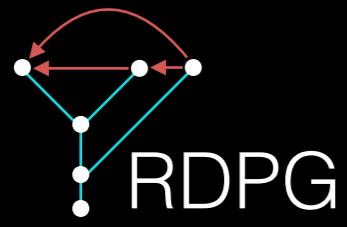
Did evolution leave a trace
in the structure
of ecological networks?

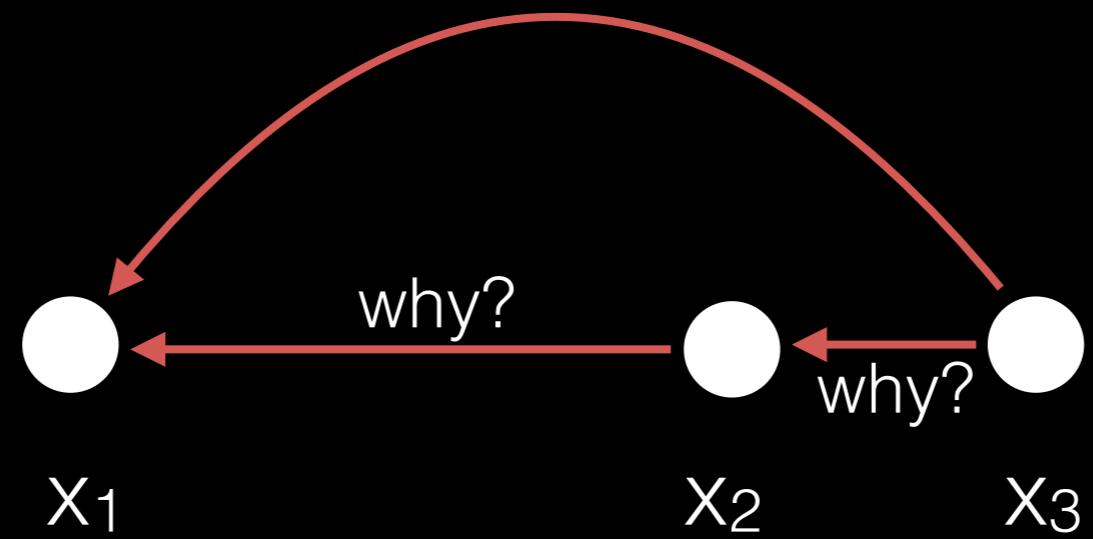
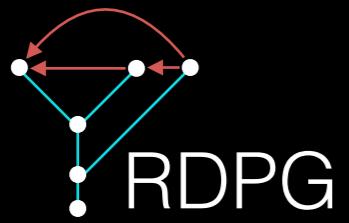


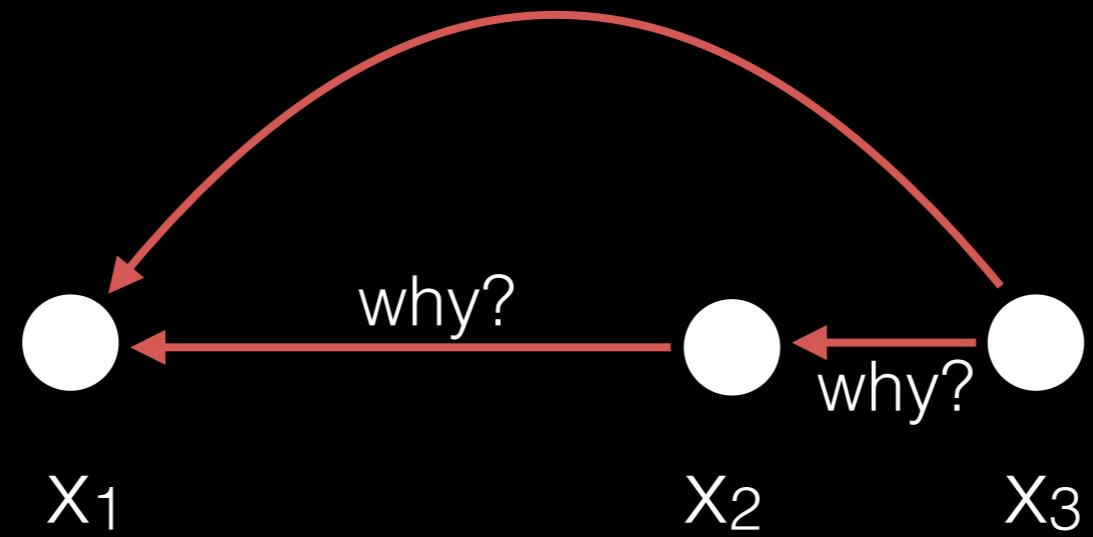
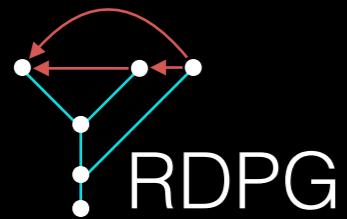
How do we do
phylogenetic comparative analysis
with food webs?



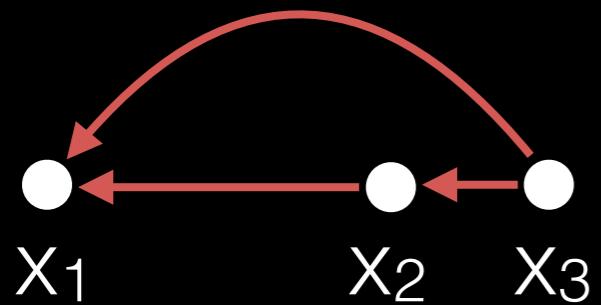
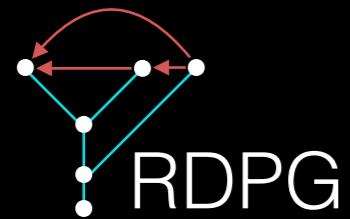








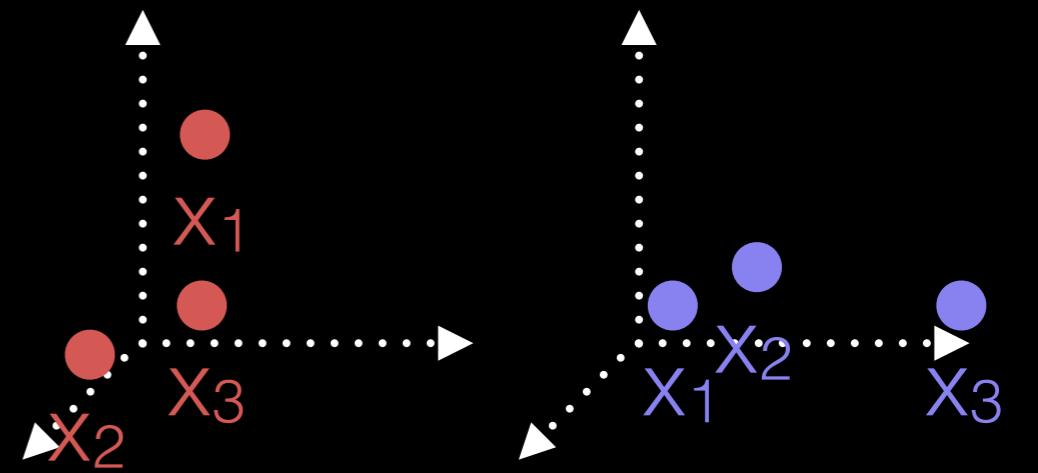
Because *TRAITS*

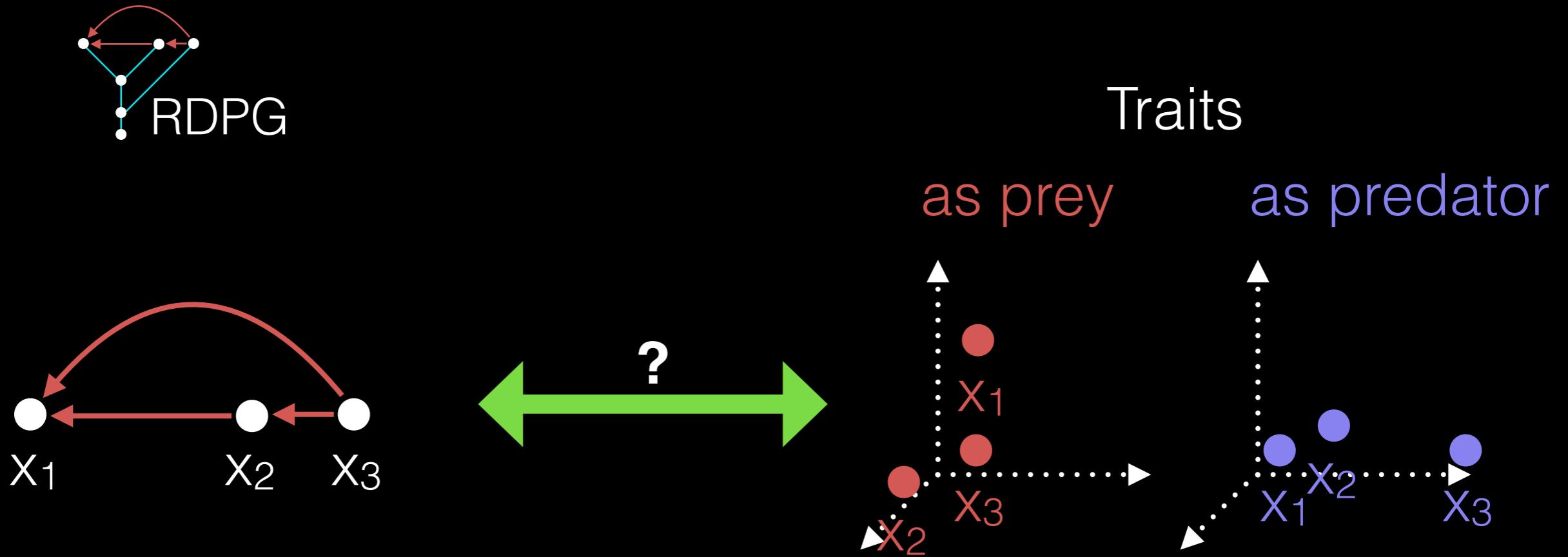


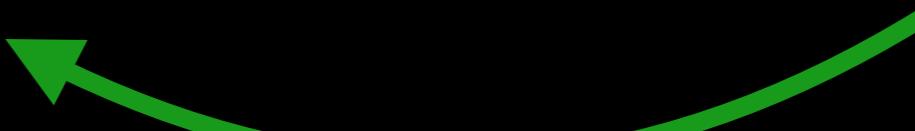
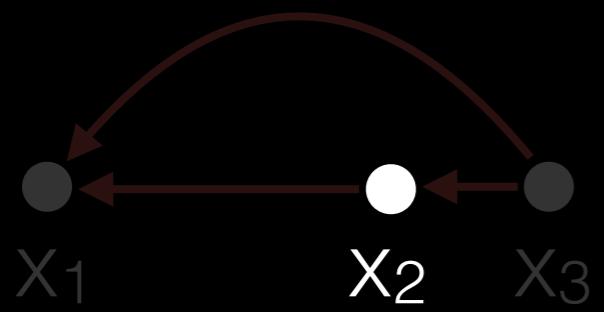
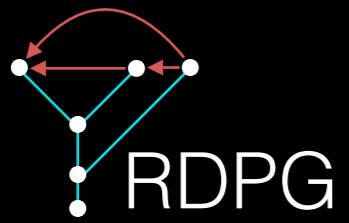
Traits

as prey

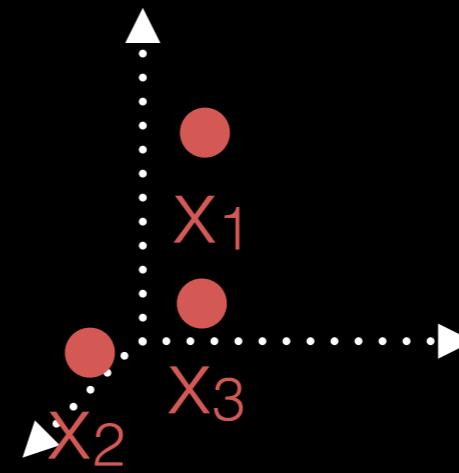
as predator



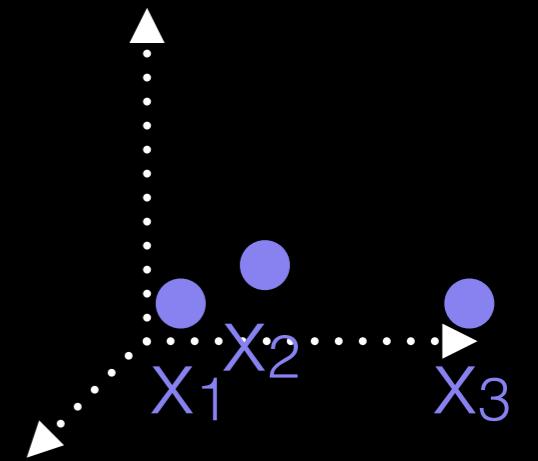


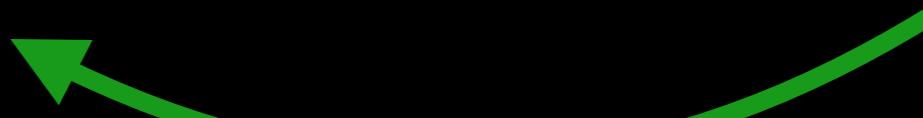
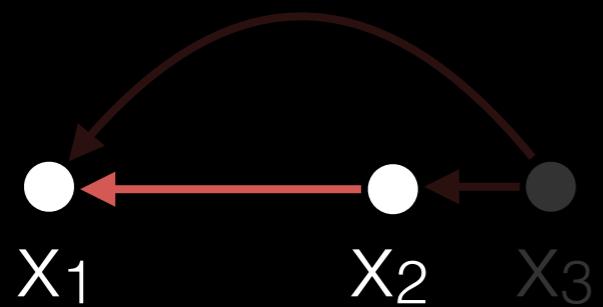
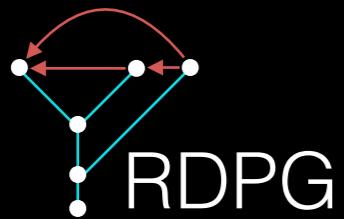


as prey



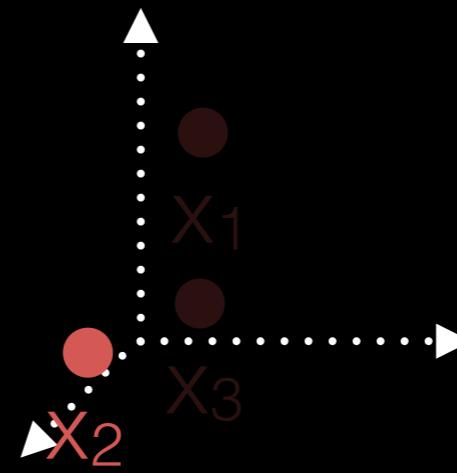
as predator



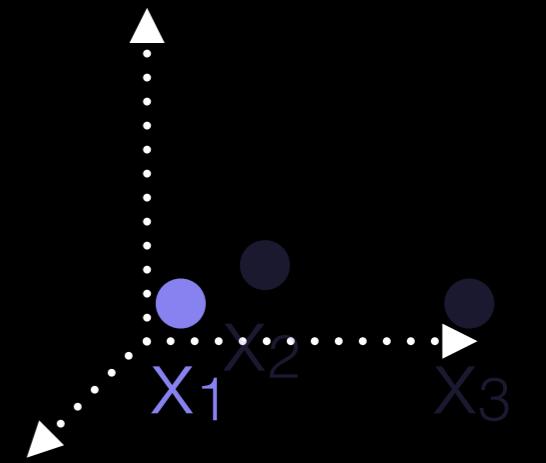


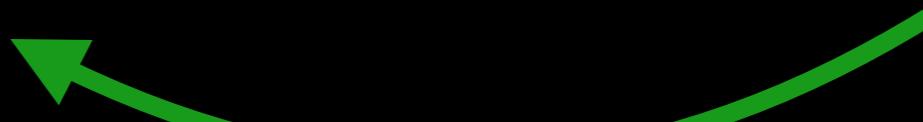
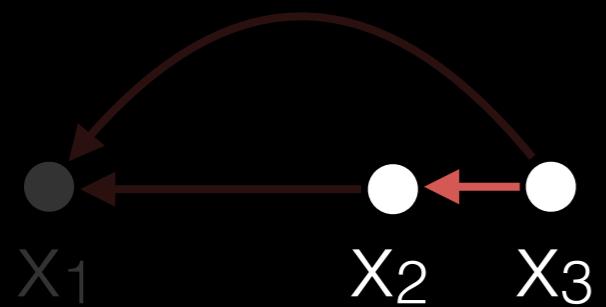
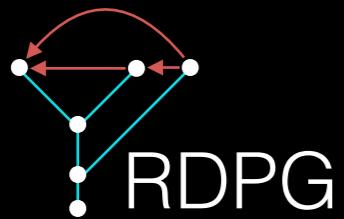
$$\mathbf{P}(x_2 \rightarrow x_1) = x_2 \cdot x_1$$

as prey



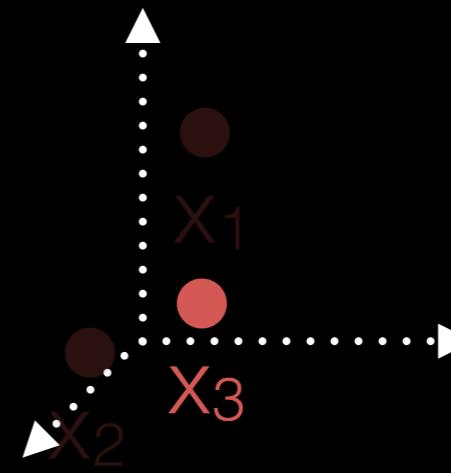
as predator



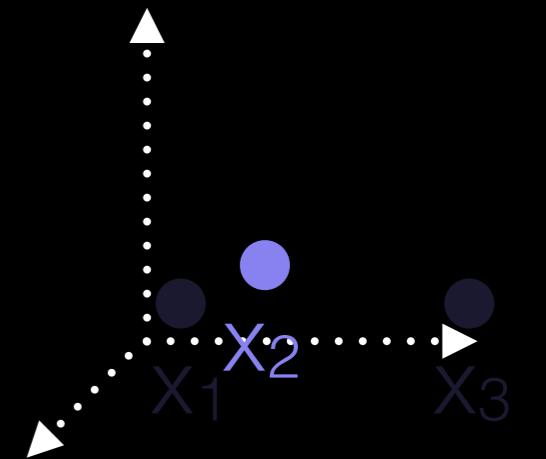


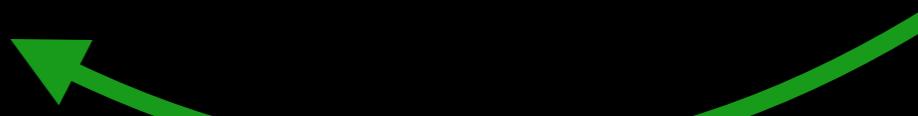
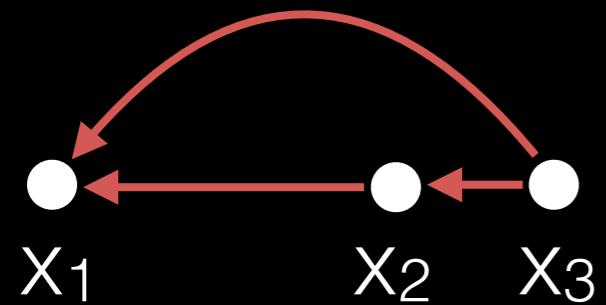
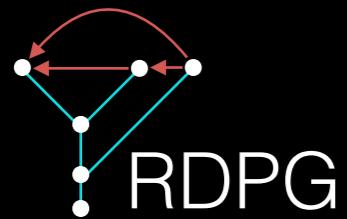
$$\mathbf{P}(x_2 \leftarrow x_3) = x_3 \cdot x_2$$

as prey



as predator

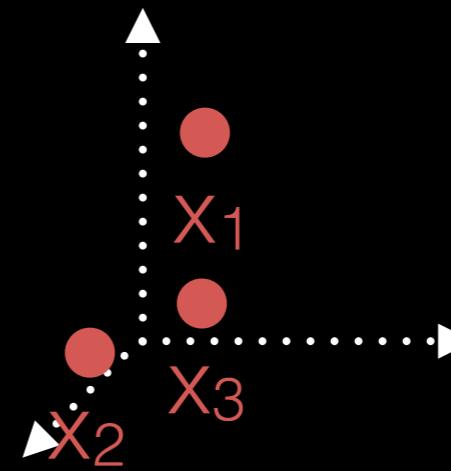




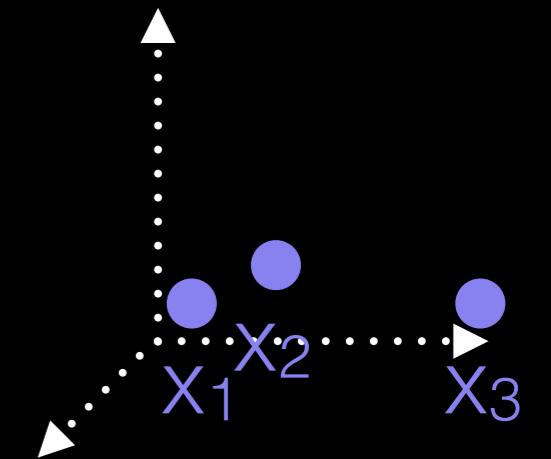
$$M := \mathbf{x} \cdot \mathbf{x}^t$$

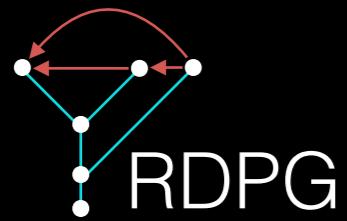
$$M_{ij} = P(x_i \rightarrow x_j)$$

as prey

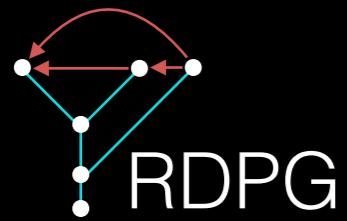


as predator

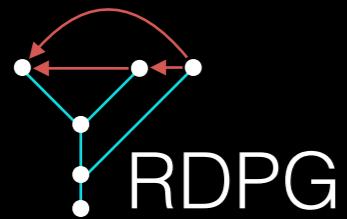




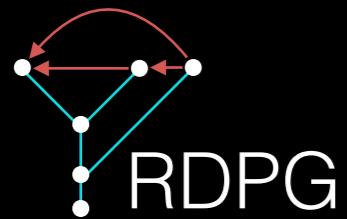
$$P\left(\begin{array}{c} \text{Diagram of } RDPG \\ \text{with nodes } x_1, x_2, x_3 \end{array} \middle| \begin{array}{c} \text{Diagram of } J \\ \text{with nodes } x_1, x_2, x_3 \end{array} \right) =$$



$$P\left(\left. \begin{array}{c} \text{RDPG graph structure} \\ \text{with nodes } x_1, x_2, x_3 \end{array} \right| \begin{array}{c} \text{Input sequence } j \\ \text{with nodes } x_1, x_2, x_3 \end{array} \right) =$$

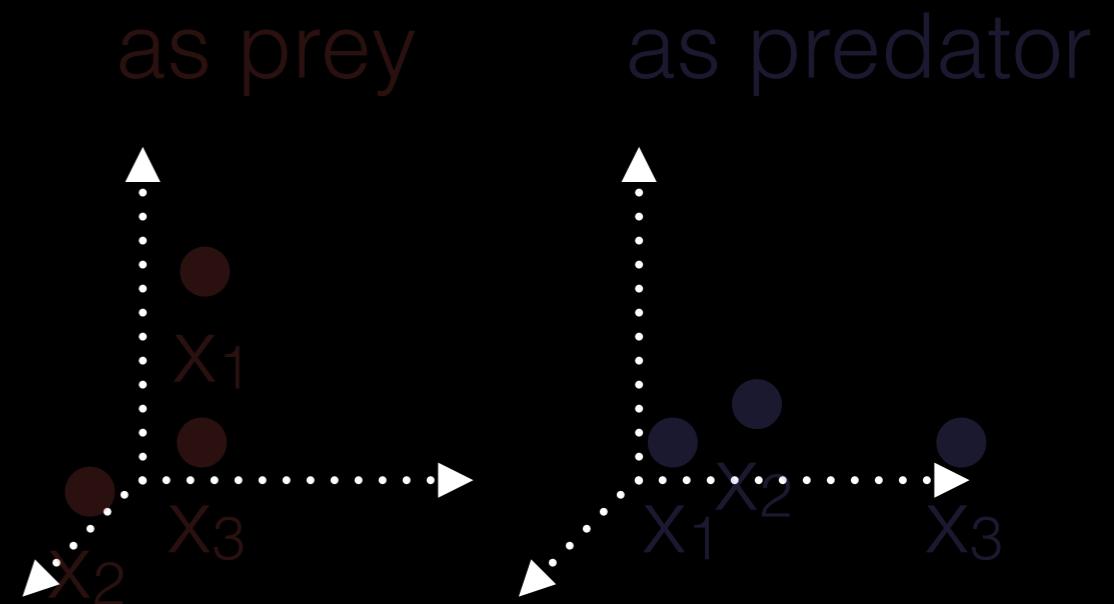
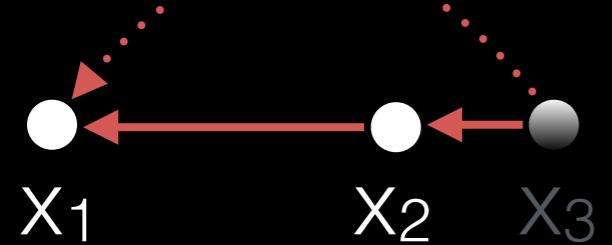
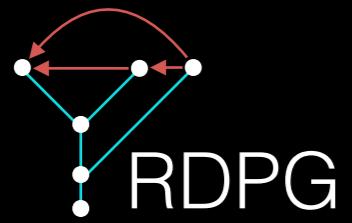


$$P\left(\left. \begin{array}{c} \text{RDPG graph structure} \\ | \\ \text{Three nodes } x_1, x_2, x_3 \end{array} \right| \begin{array}{c} \text{Three red nodes } x_1, x_2, x_3 \\ \text{Three blue nodes } x_1, x_2, x_3 \end{array} \right) = B(A, M)$$

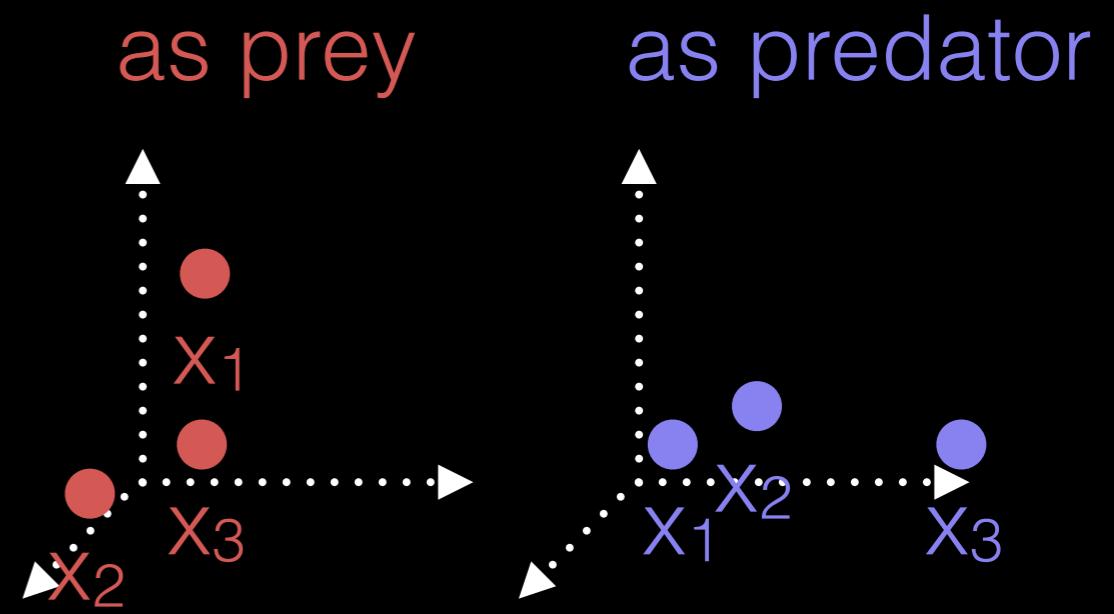
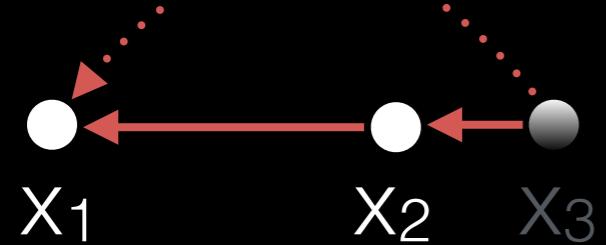
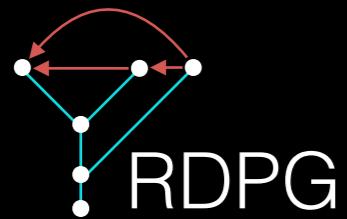


$$P\left(\begin{array}{c} \text{RDPG} \\ | \\ \text{X}_1 \quad \text{X}_2 \quad \text{X}_3 \end{array}\right) = P\left(\begin{array}{c} \text{RDPG} \\ | \\ \text{X}_1 \quad \text{X}_2 \quad \text{X}_3 \end{array}\right)$$

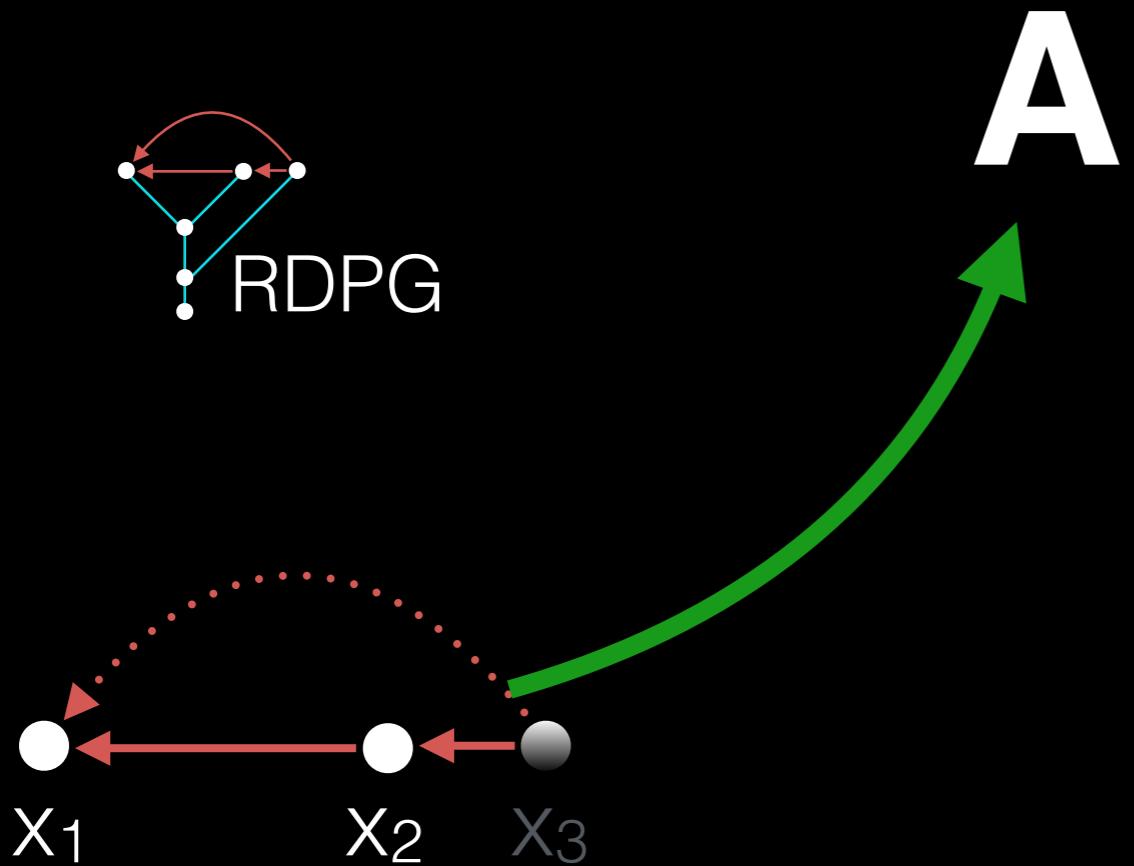
The diagram illustrates two equivalent representations of a probability distribution over a state space. Both sides of the equation show a state transition graph with three states labeled x_1 , x_2 , and x_3 . On the left, the graph is shown with red curved and straight edges. On the right, the graph is shown with red and blue nodes and edges. Above the graph, a vector j is defined with components j_{x_1} , j_{x_2} , and j_{x_3} . The distributions are given as $P(j)$.

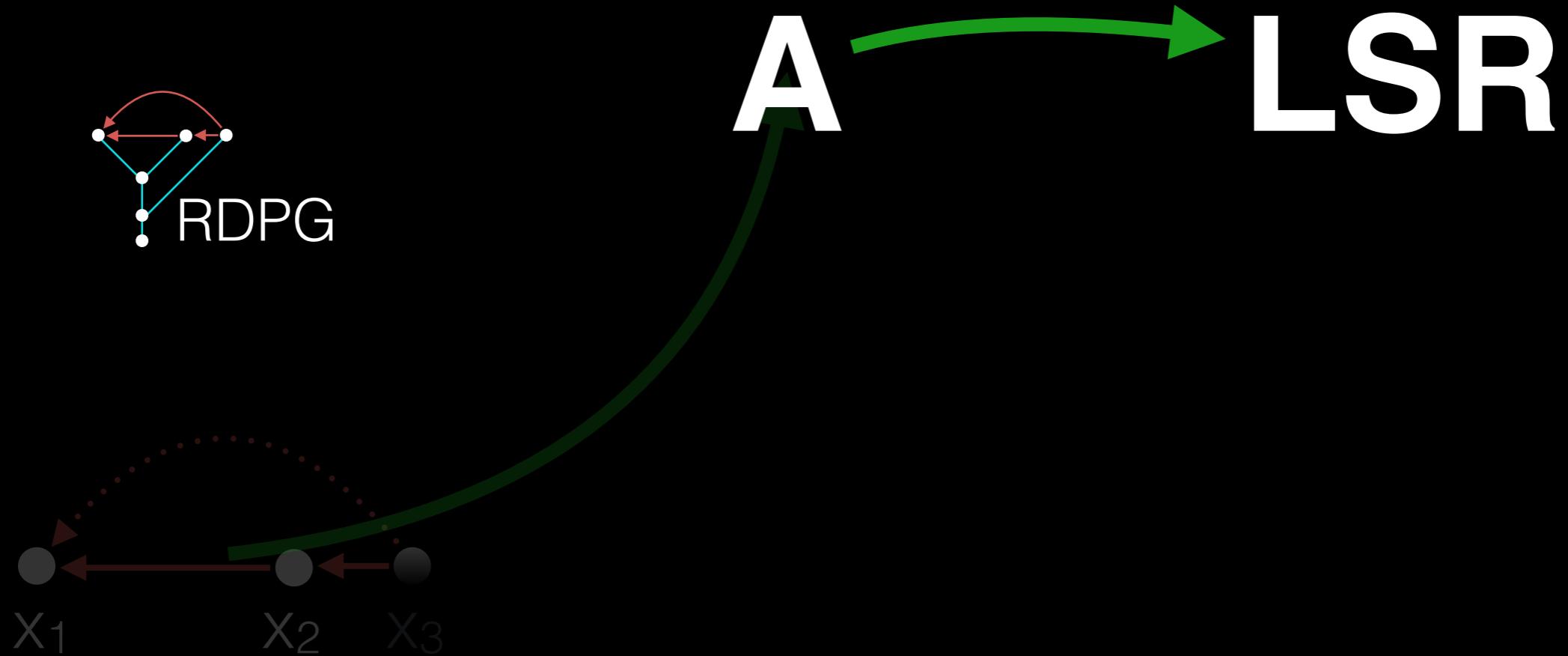


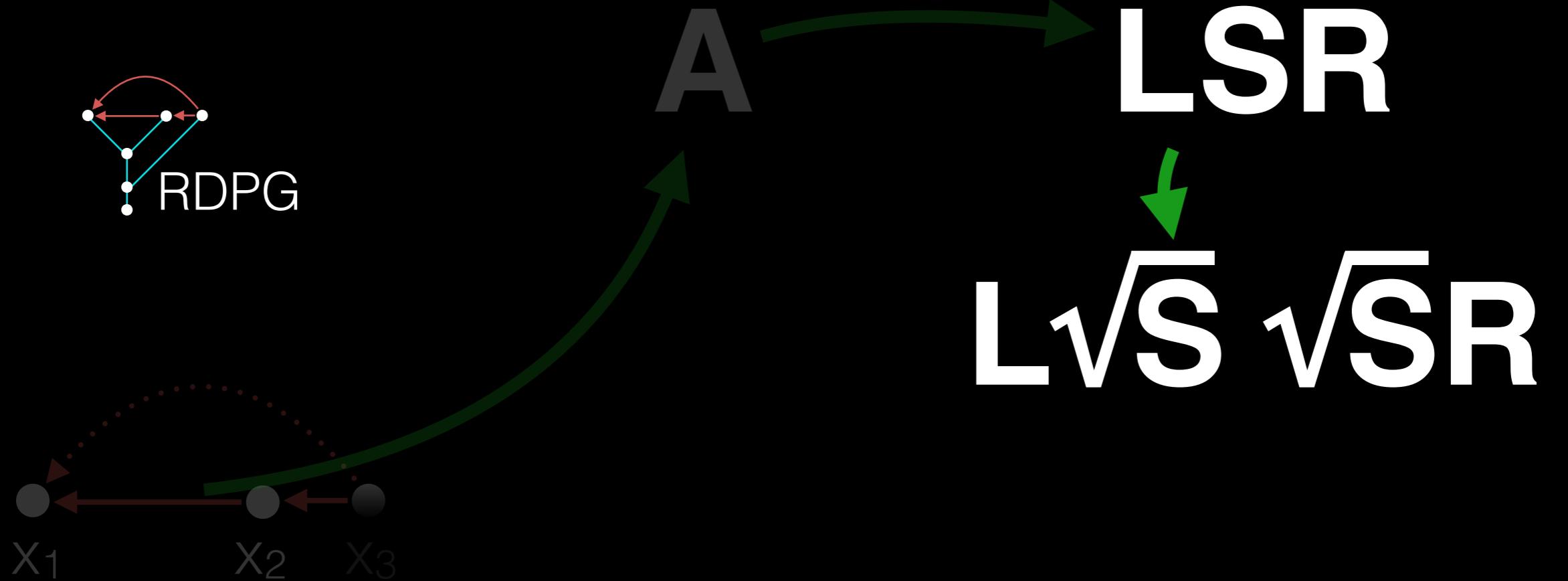
Alas!

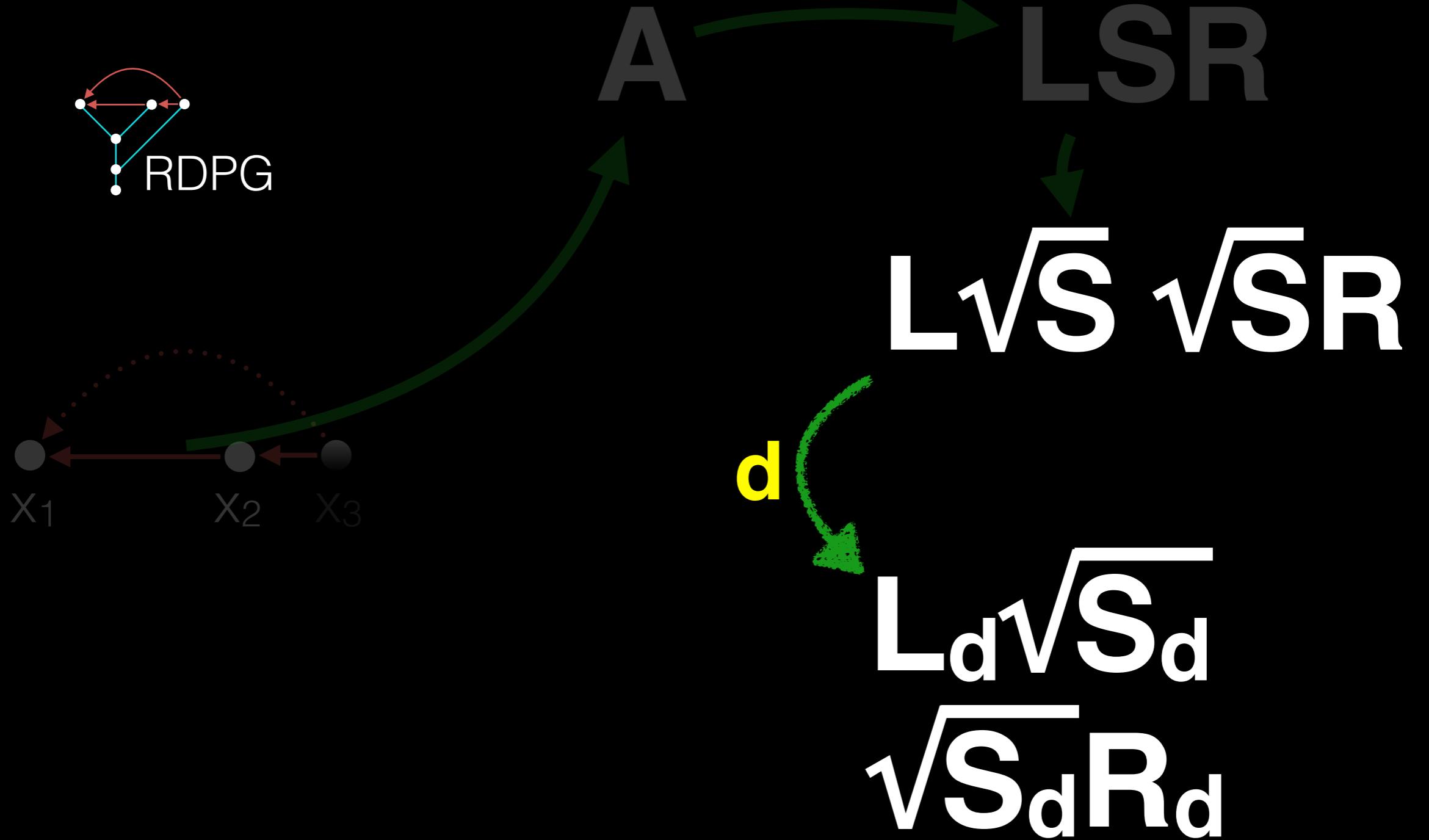


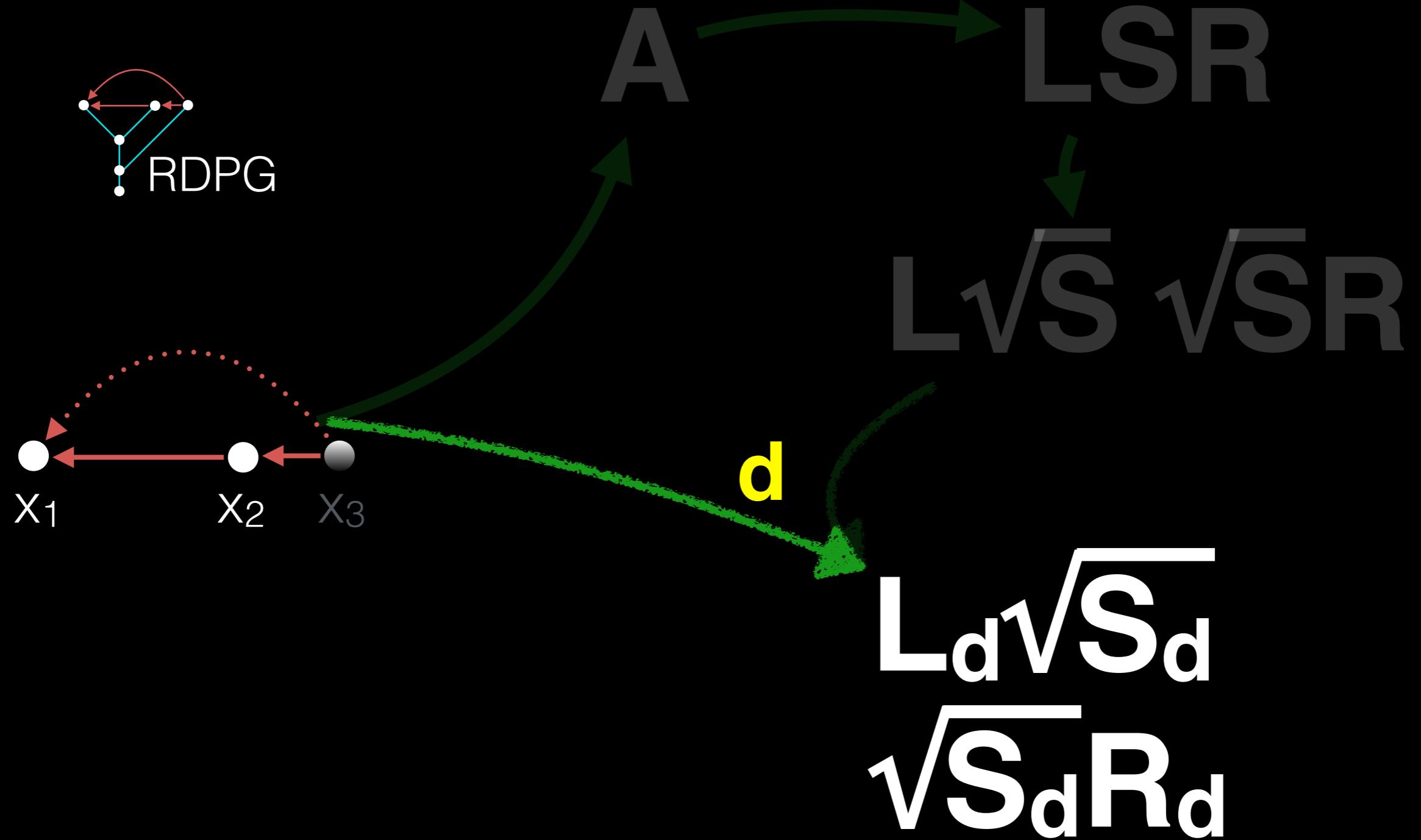
SVD!

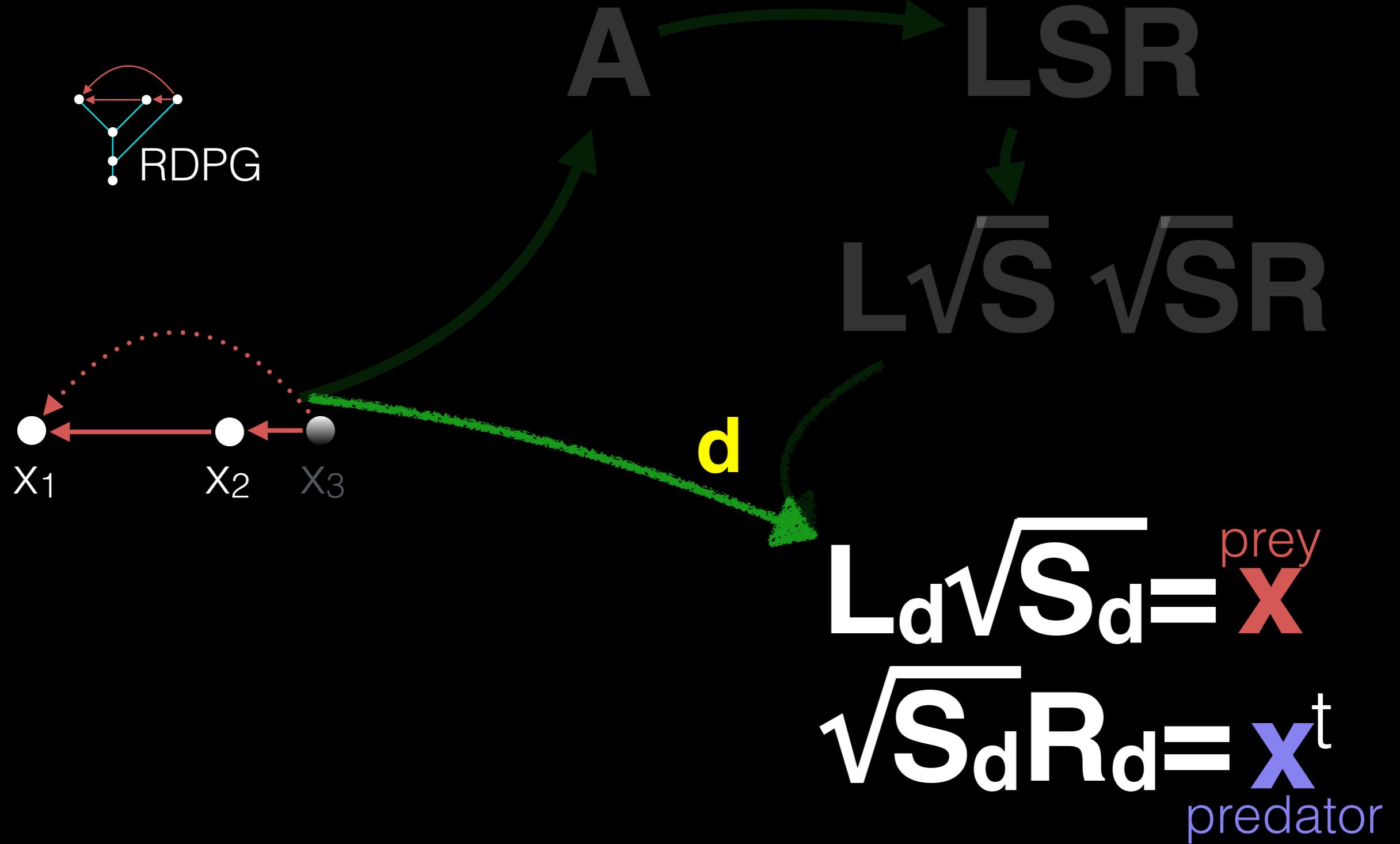


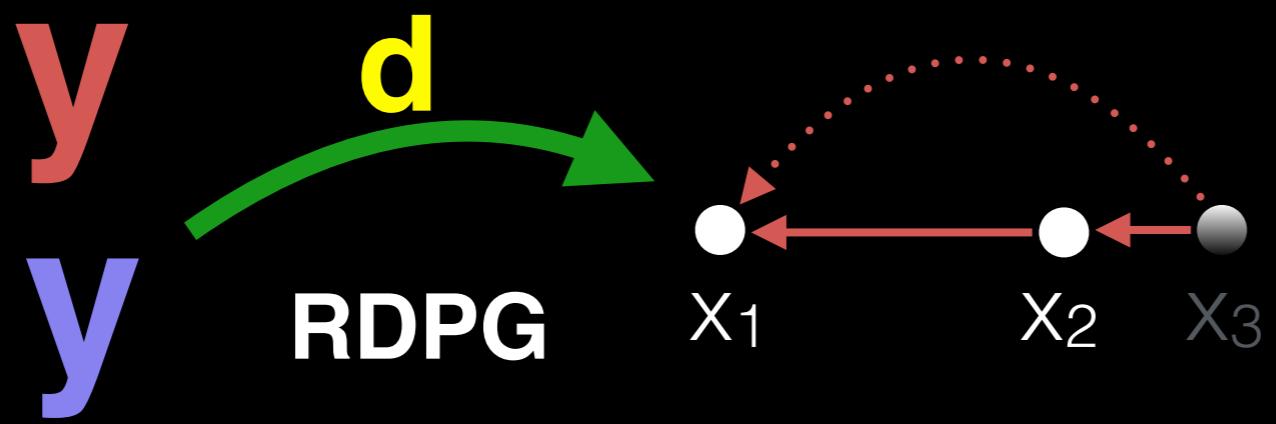
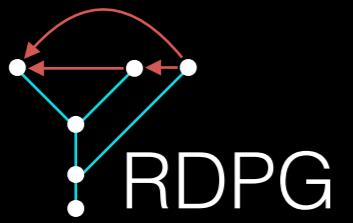


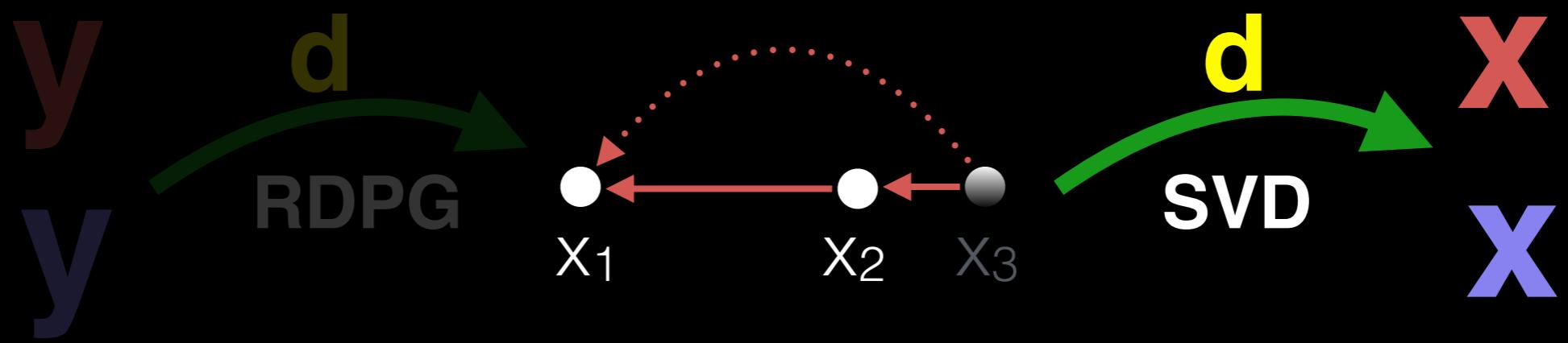
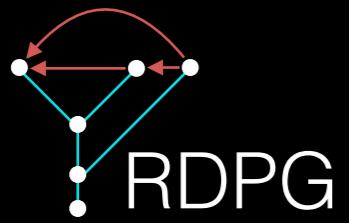


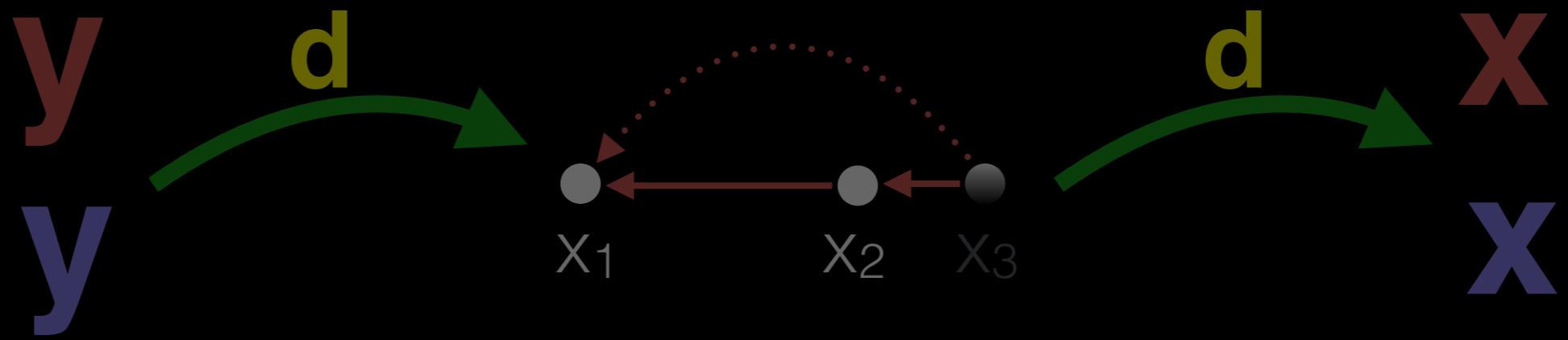
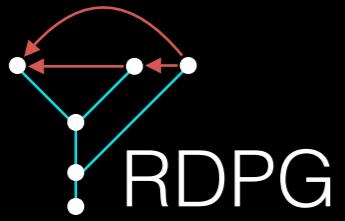




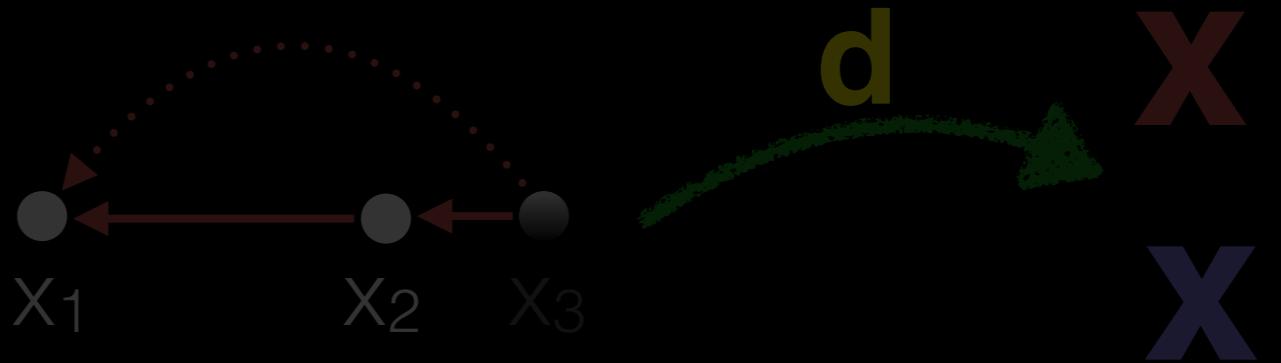
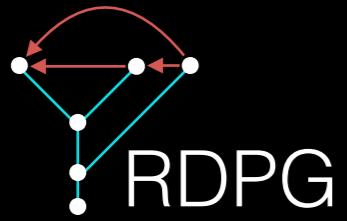




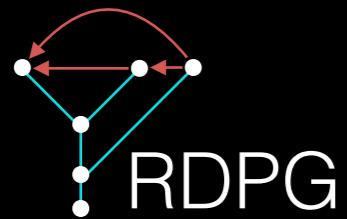




Thm: **X X** are **MLE** of **y y**



we need to choose **d**



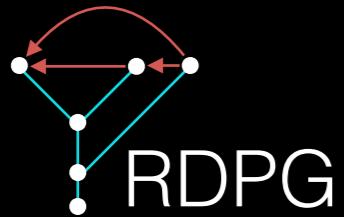
$$P\left(\begin{array}{c} \text{RDPG} \\ | \\ \text{graph LR} \\ | \\ \text{graph LR} \end{array}\right) =$$



\mathbf{x}, \mathbf{x}' unique up to an orthogonal transformation

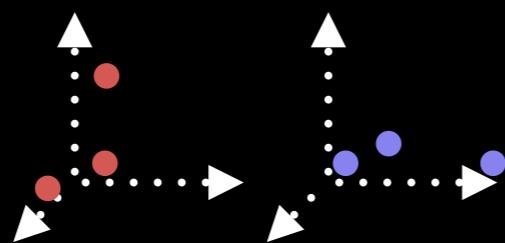


Did evolution leave a trace
in the structure
of ecological networks?

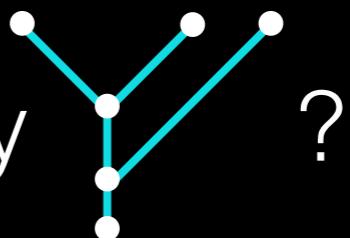


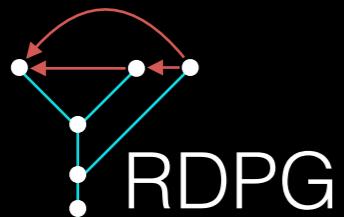
Did evolution leave a trace
in the structure
of ecological networks?

Are

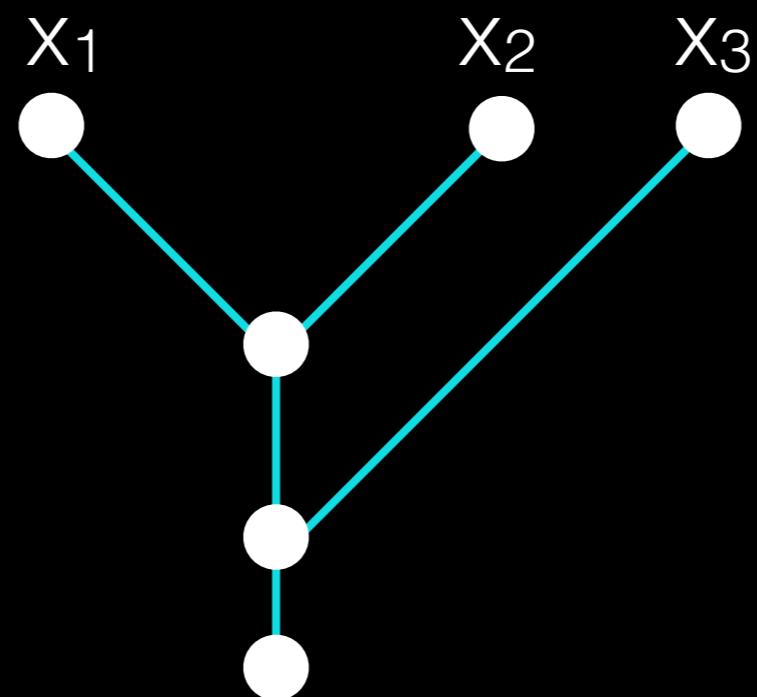


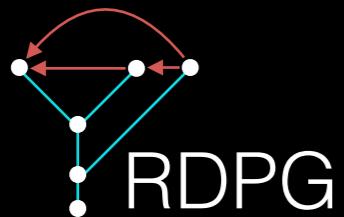
predicted by



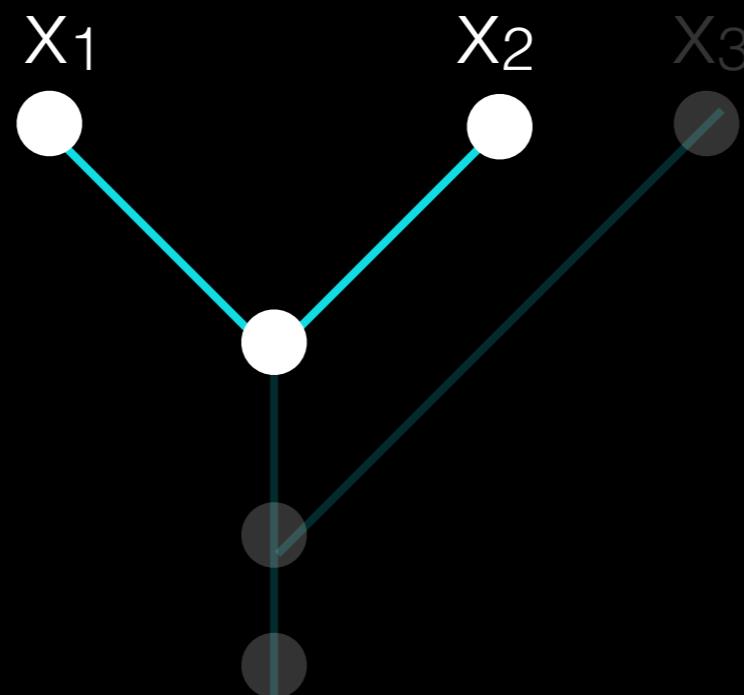


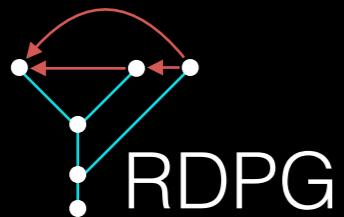
Did evolution leave a trace
in the structure
of ecological networks?



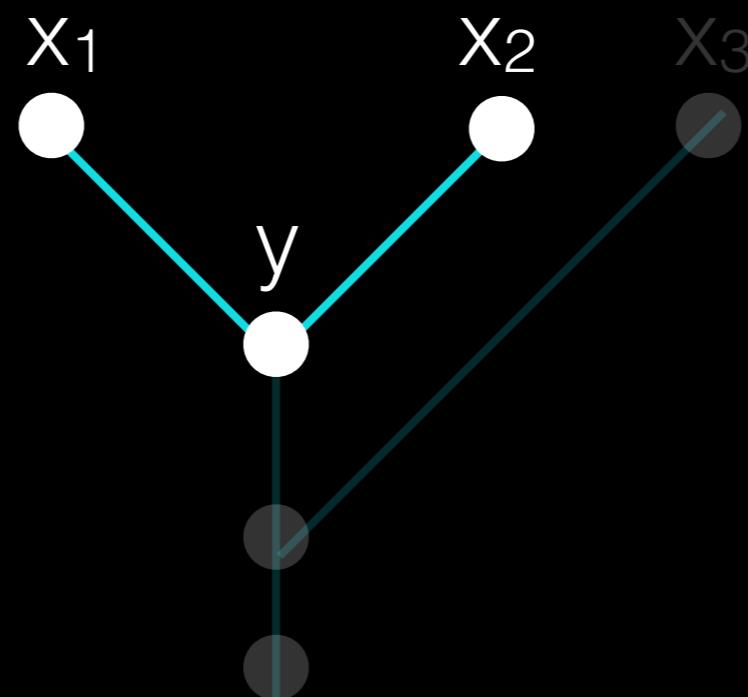


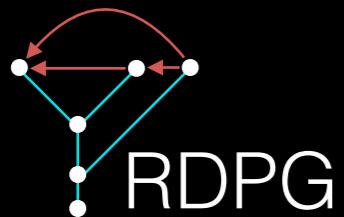
Did evolution leave a trace
in the structure
of ecological networks?



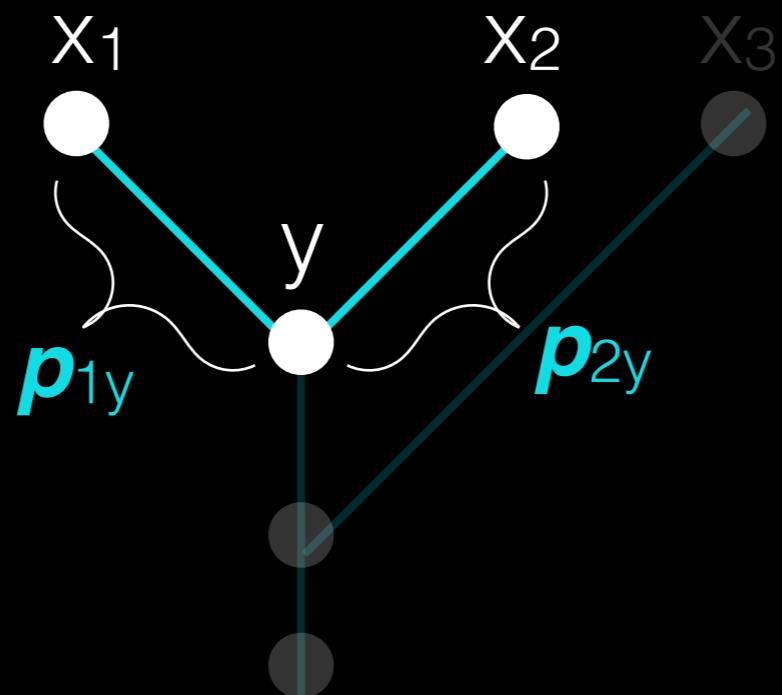


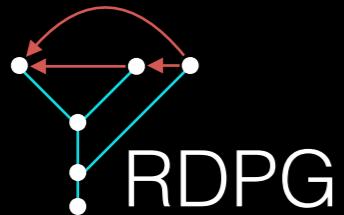
Did evolution leave a trace
in the structure
of ecological networks?



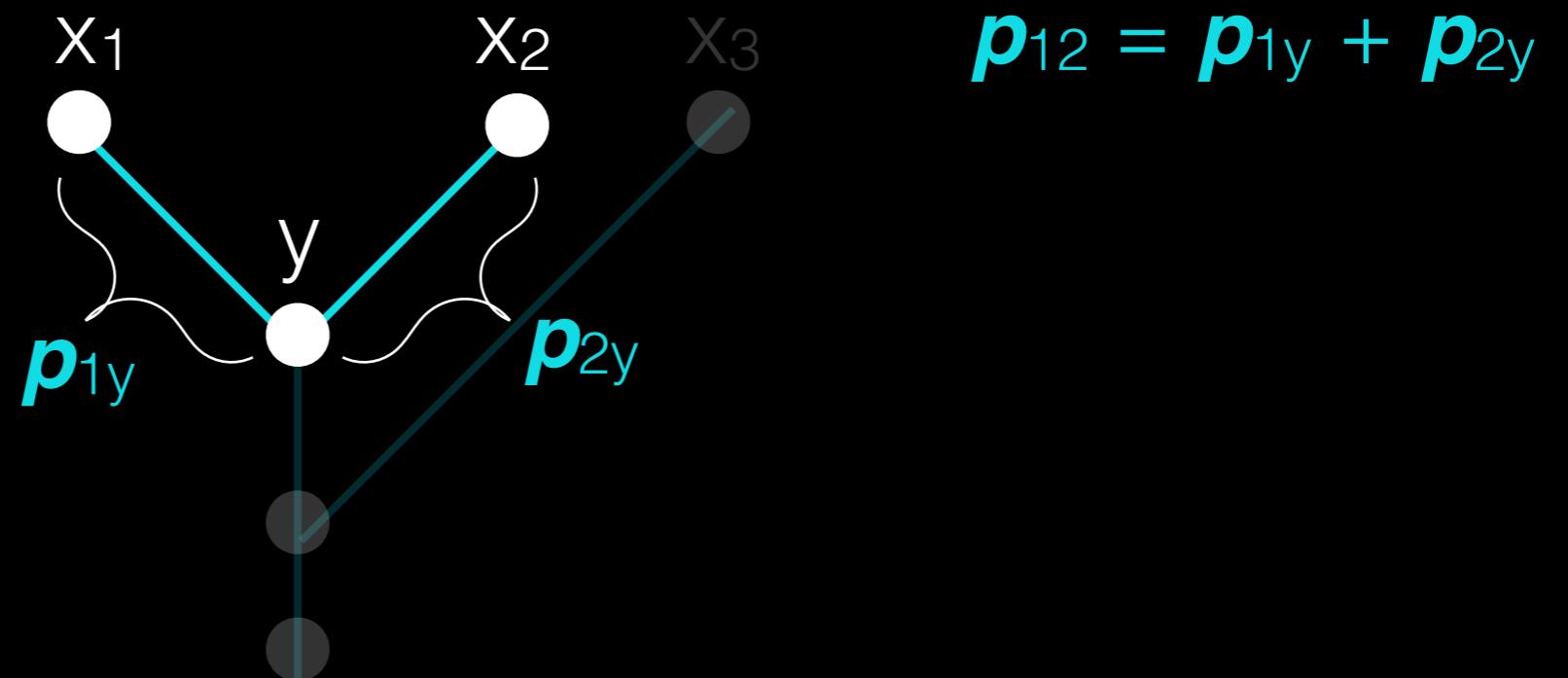


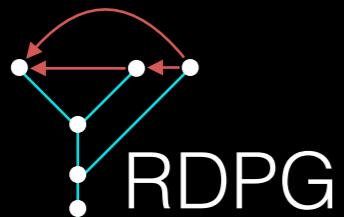
Did evolution leave a trace
in the structure
of ecological networks?



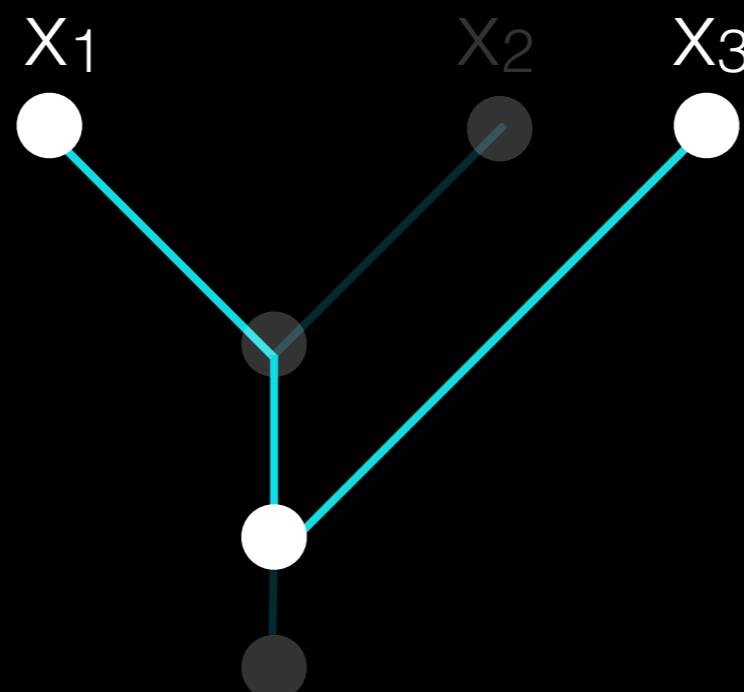


Did evolution leave a trace
in the structure
of ecological networks?



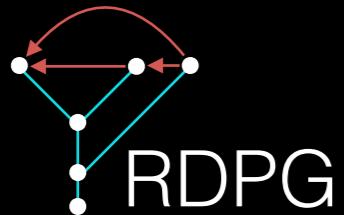


Did evolution leave a trace
in the structure
of ecological networks?

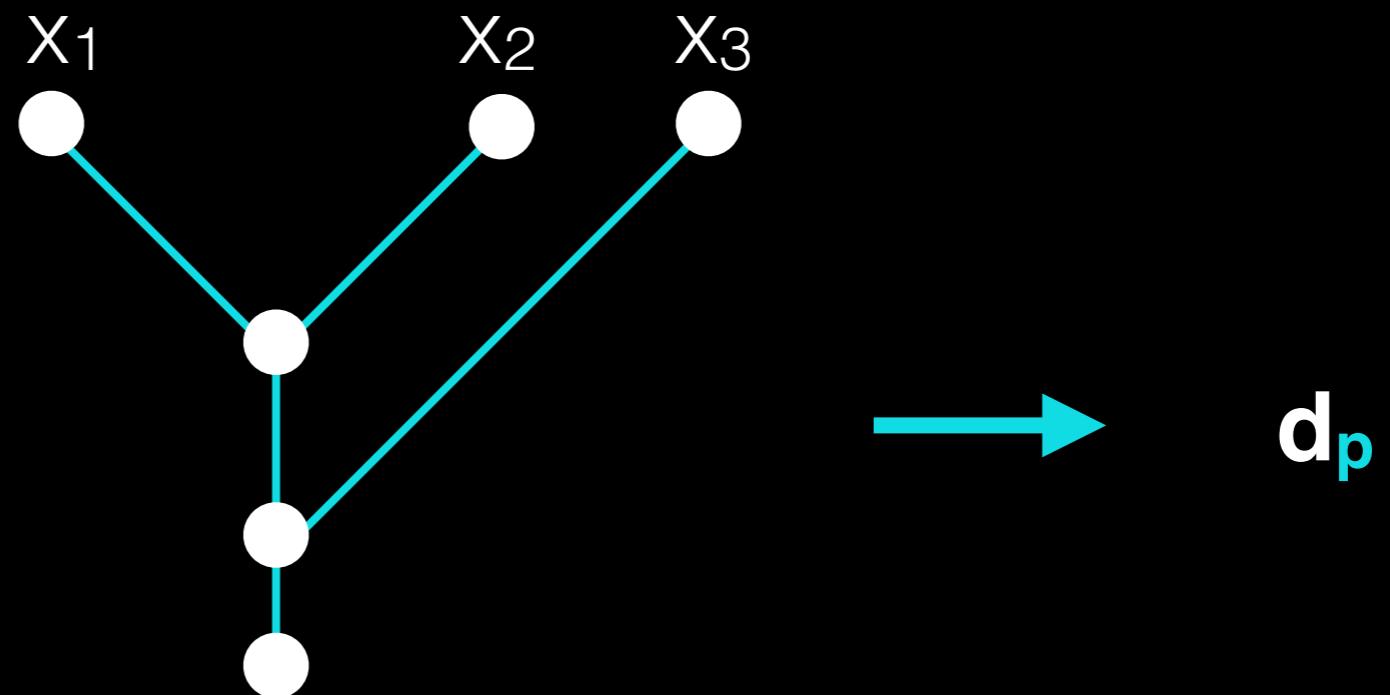


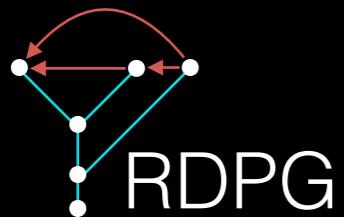
$$p_{12} = p_{1y} + p_{2y}$$

$$p_{13} = \dots$$

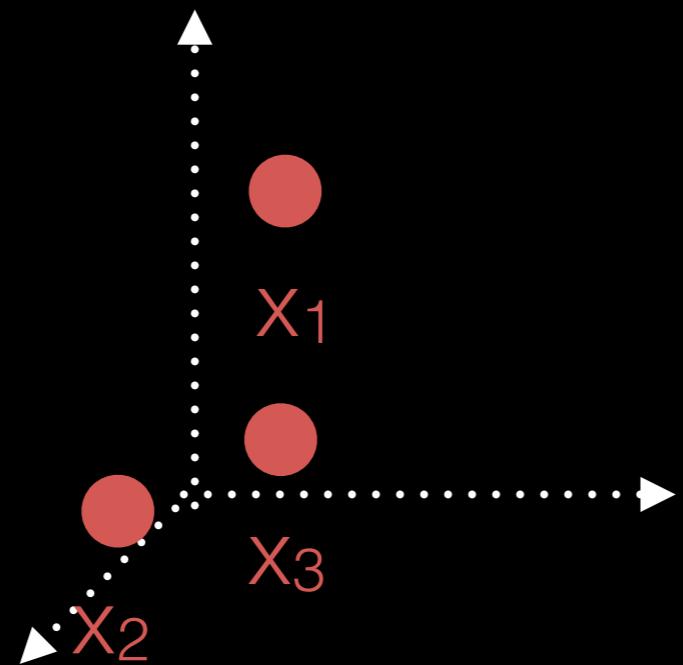


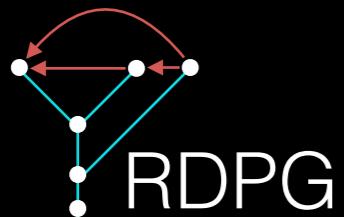
Did evolution leave a trace
in the structure
of ecological networks?



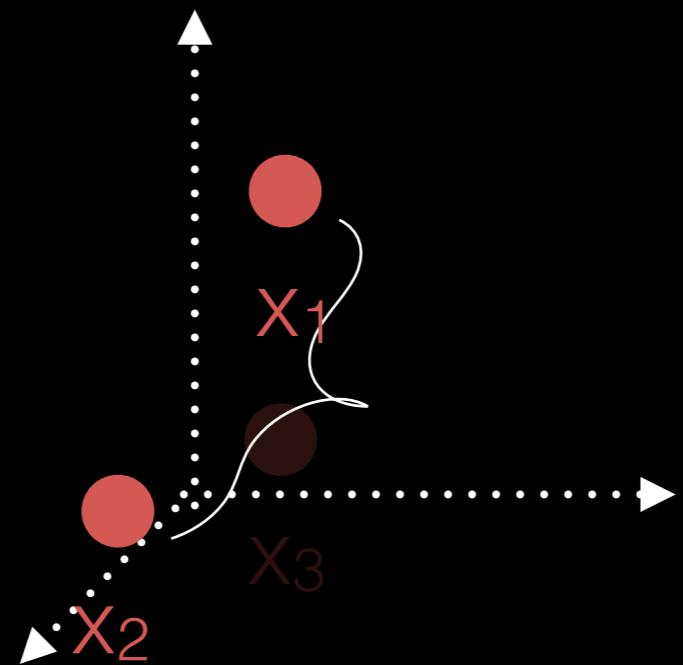


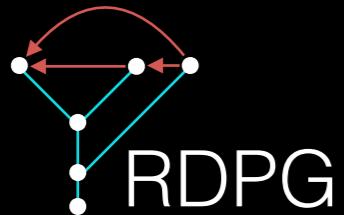
Did evolution leave a trace
in the structure
of ecological networks?



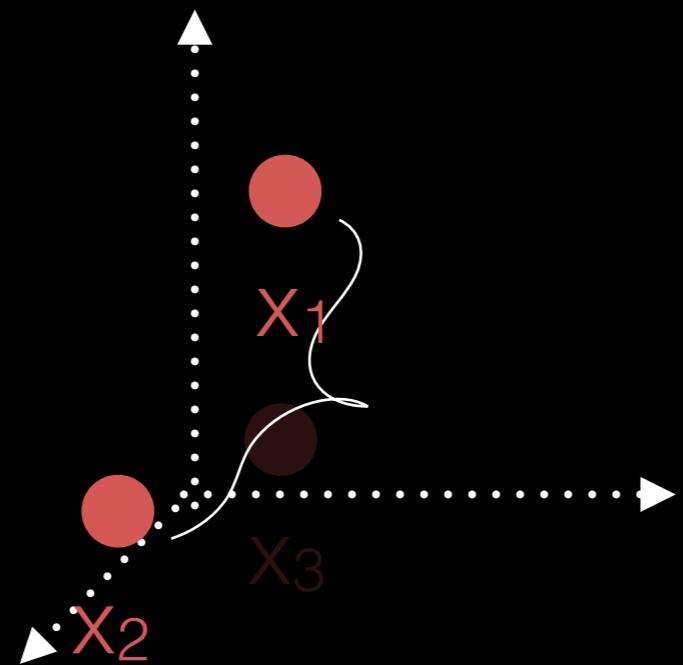


Did evolution leave a trace
in the structure
of ecological networks?

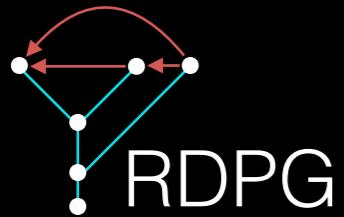




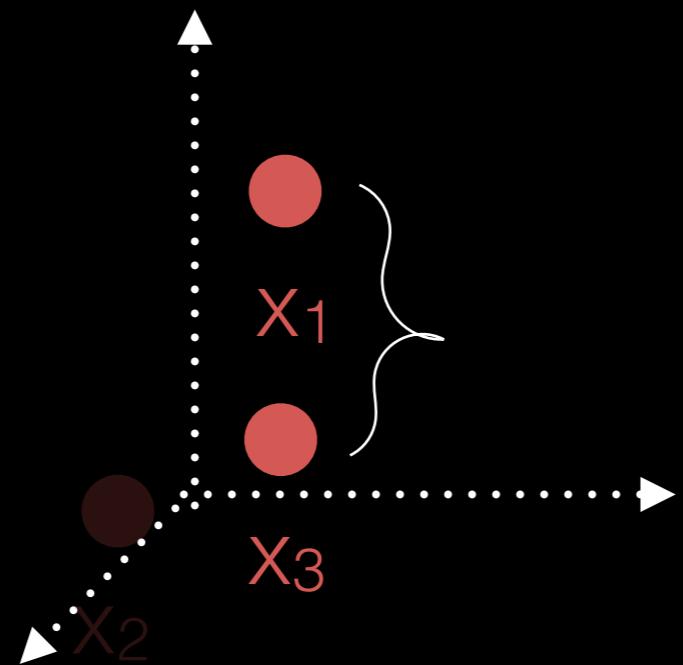
Did evolution leave a trace
in the structure
of ecological networks?



$$\mathbf{x}_{12} = d(x_1, x_2)$$



Did evolution leave a trace
in the structure
of ecological networks?

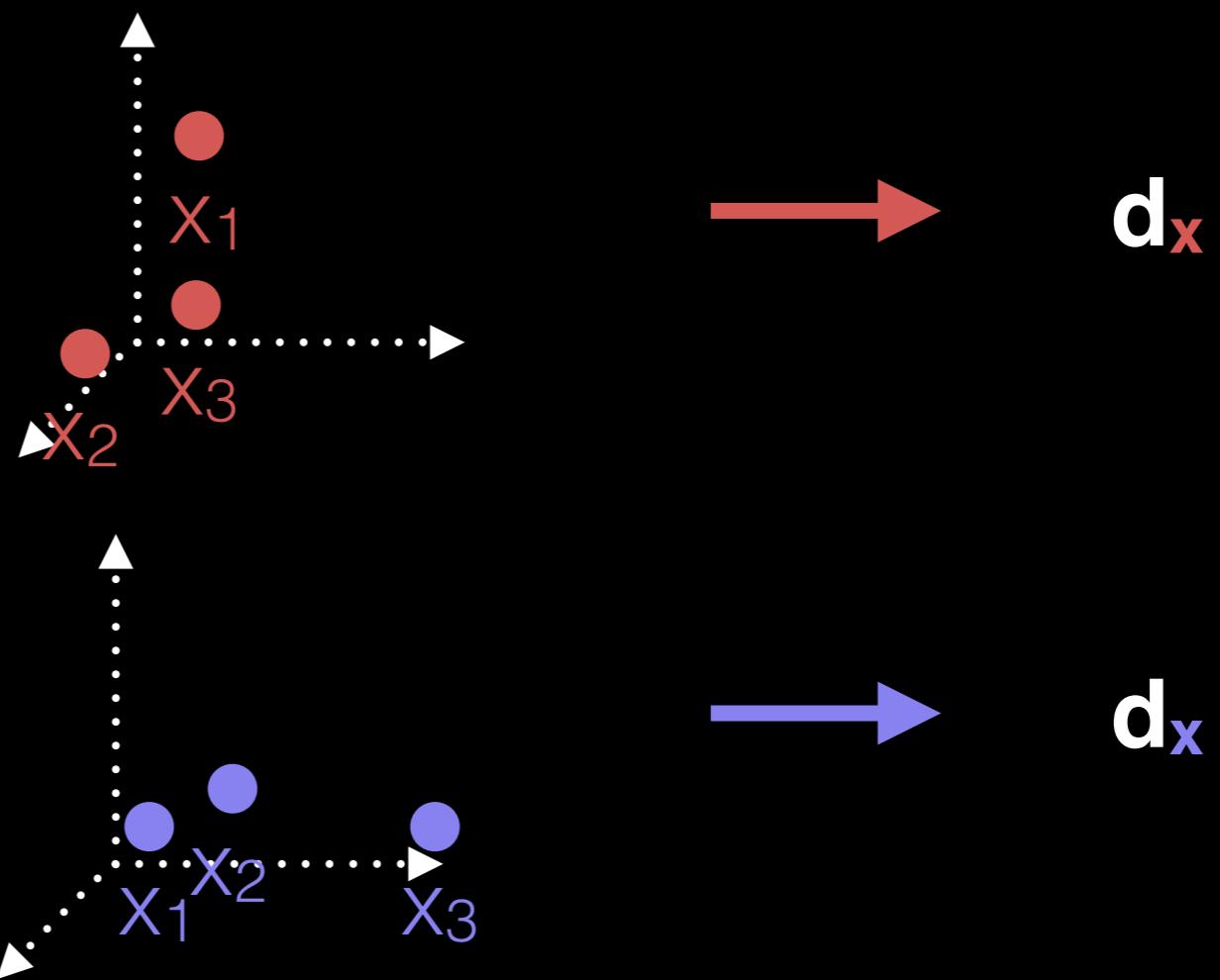


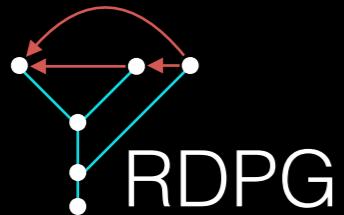
$$\mathbf{x}_{12} = d(x_1, x_2)$$

$$\mathbf{x}_{13} = d(x_1, x_3)$$



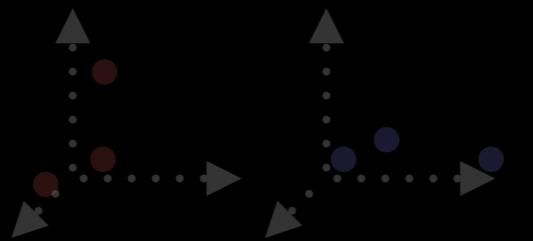
Did evolution leave a trace
in the structure
of ecological networks?



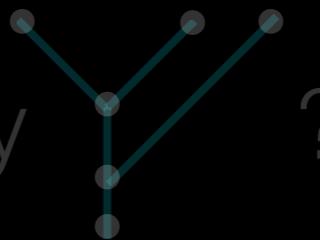


Did evolution leave a trace
in the structure
of ecological networks?

Are



predicted by ?



Are

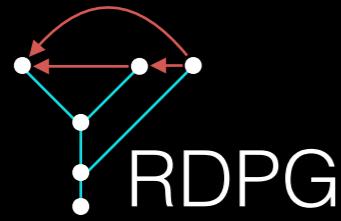
d_x

d_x

predicted by

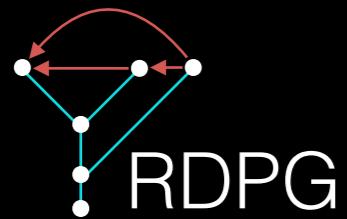
d_p

?

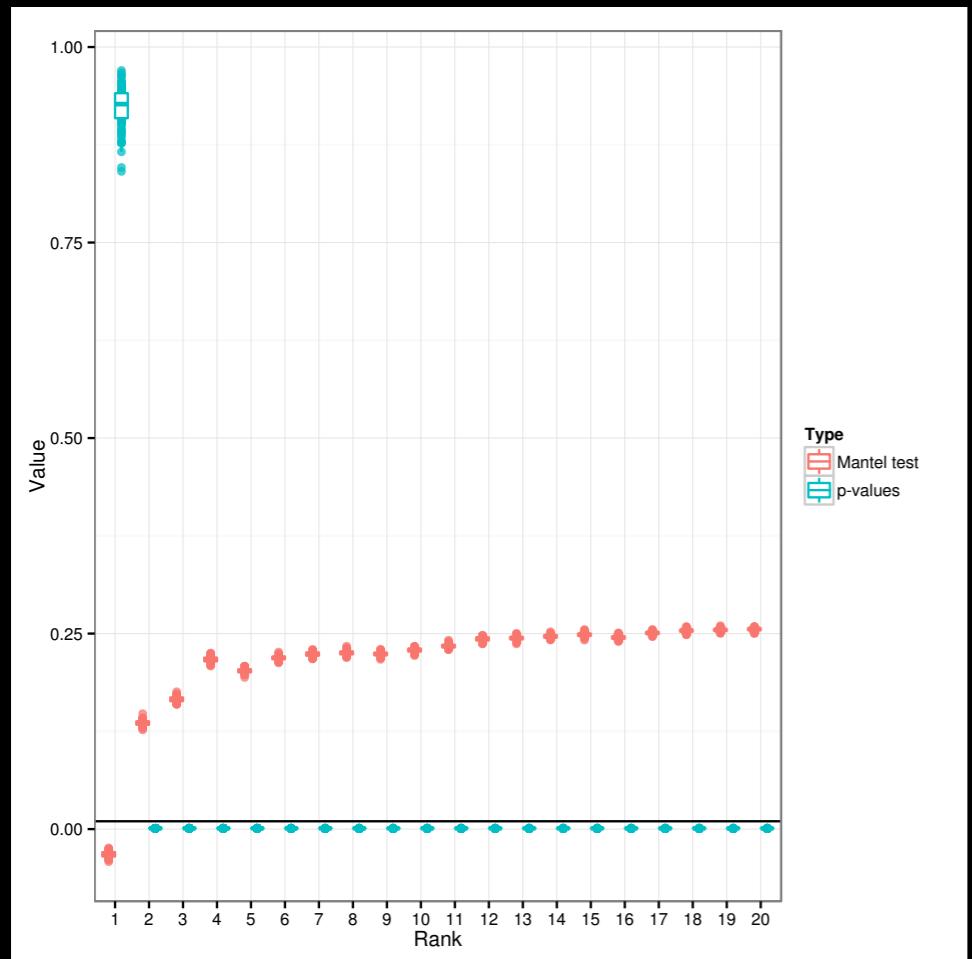


Did evolution leave a trace
in the structure
of ecological networks?

yes

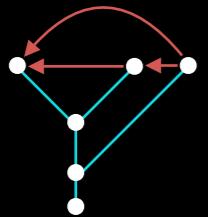


Did evolution leave a trace
in the structure
of ecological networks?



yes, and starting from **d**

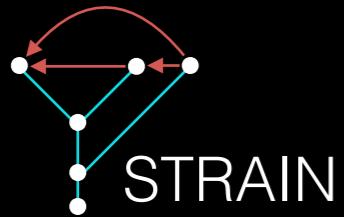
Dalla Riva, G. V. and Stouffer, D. B. (2015), Exploring the evolutionary signature of food webs' backbones using functional traits. Oikos. doi: 10.1111/oik.02305



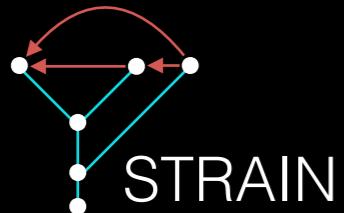
CENTRALITY

with Carey E. Priebe (JHU)

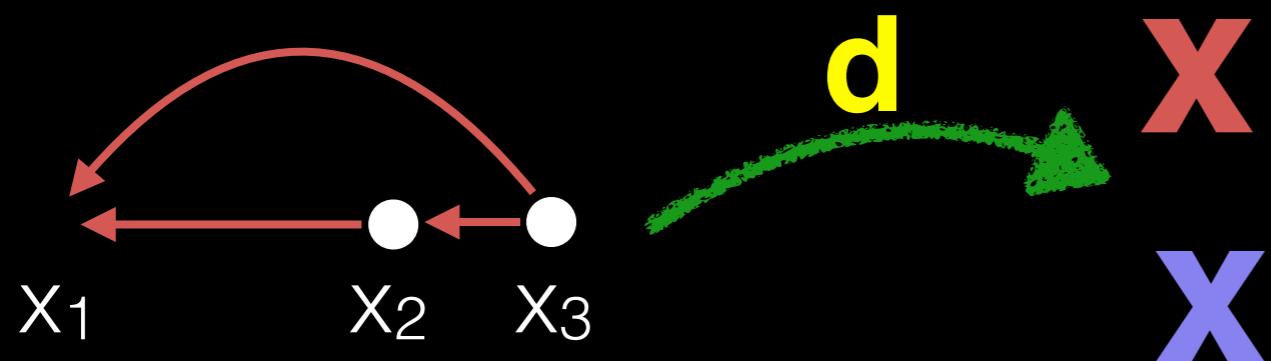
with Arne Ø. Mooers (SFU) and Mike Steel

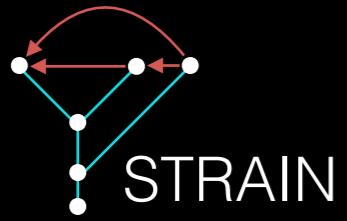


How do we measure
the importance of nodes
in a RDPG framework?

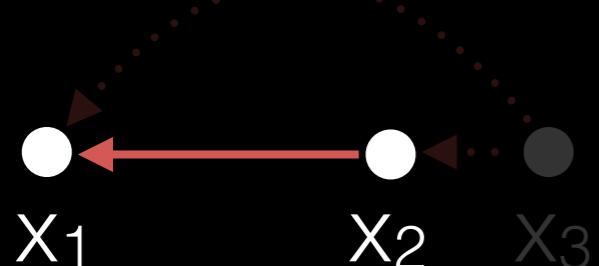
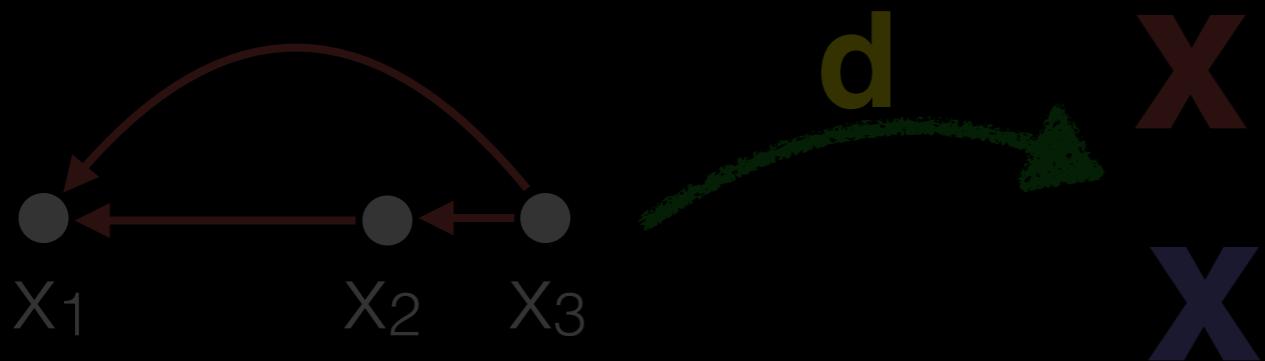


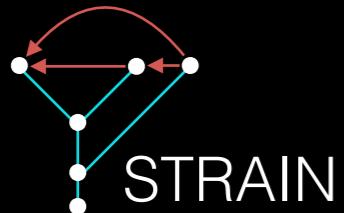
How do we measure
the importance of nodes
in a RDPG framework?



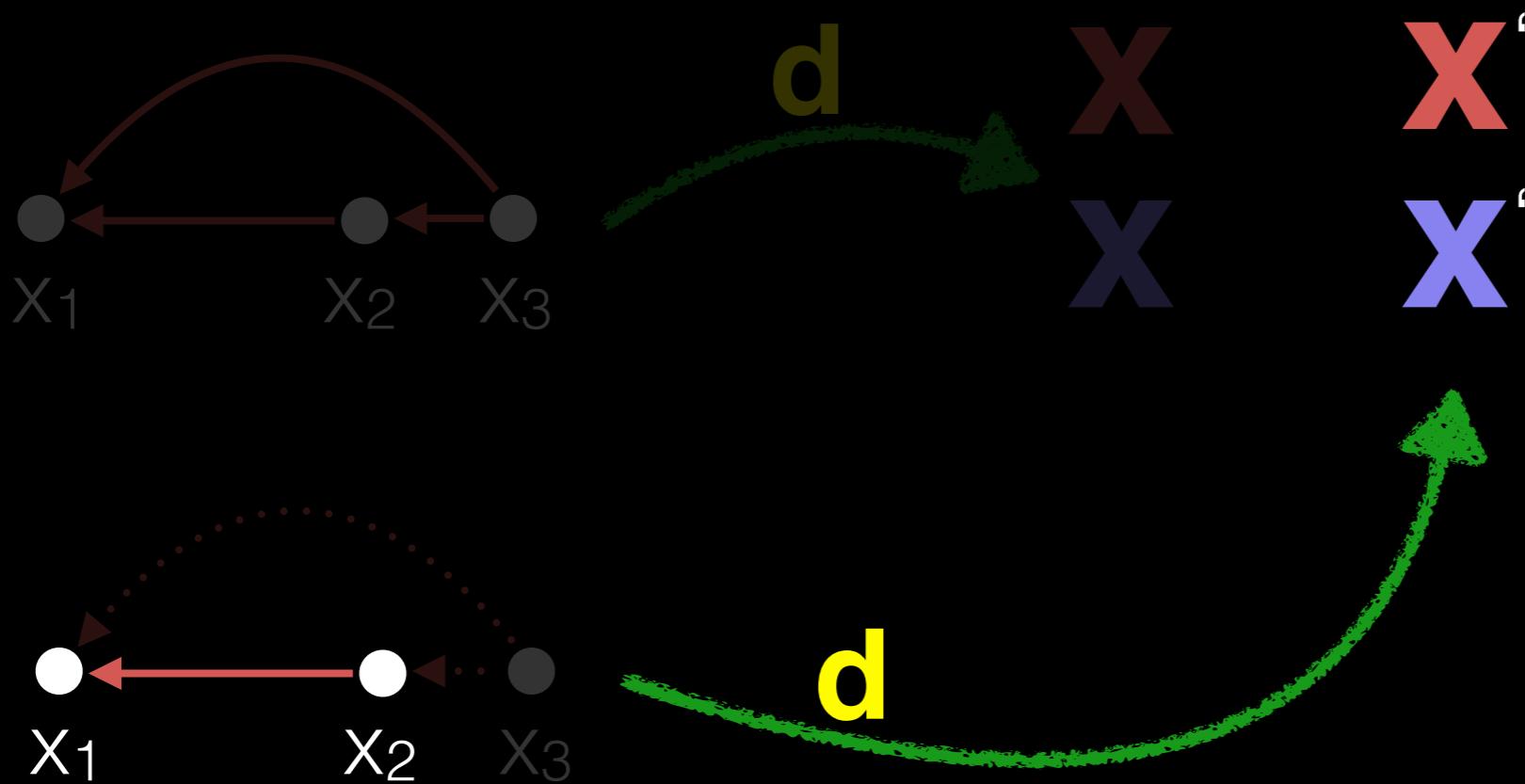


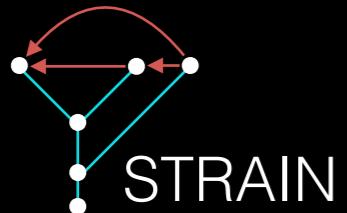
How do we measure
the importance of nodes
in a RDPG framework?



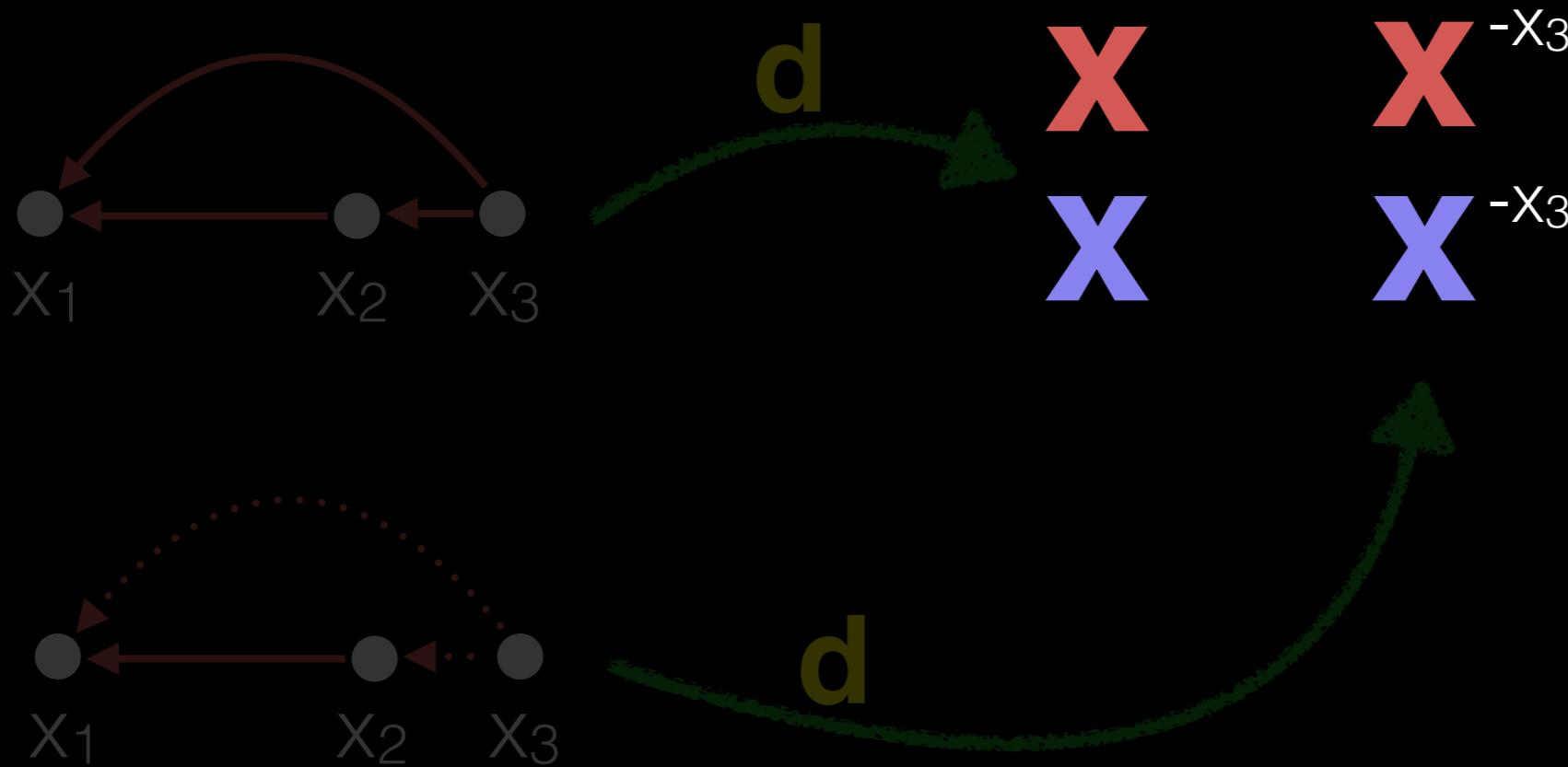


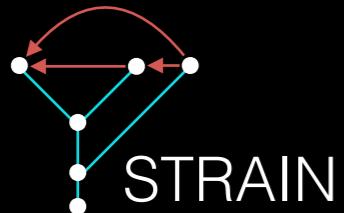
How do we measure
the importance of nodes
in a RDPG framework?



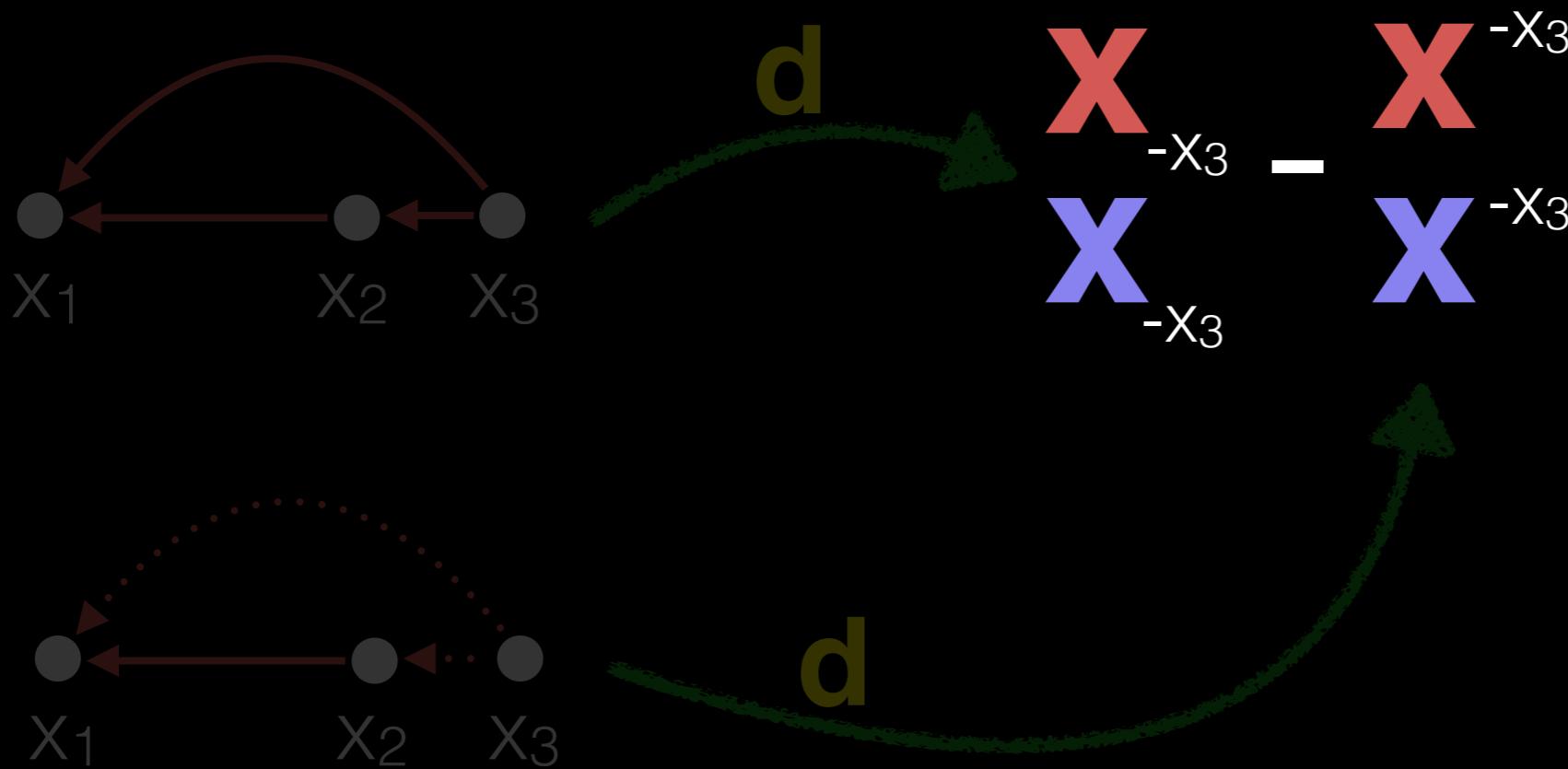


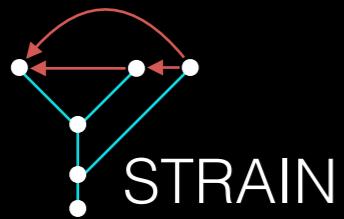
How do we measure
the importance of nodes
in a RDPG framework?



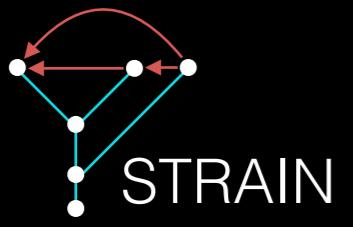


How do we measure
the importance of nodes
in a RDPG framework?

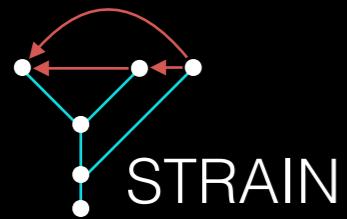




Are ecological unique species
evolutionary distinctive?

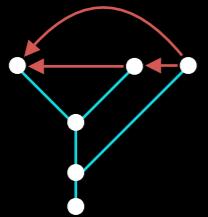


no



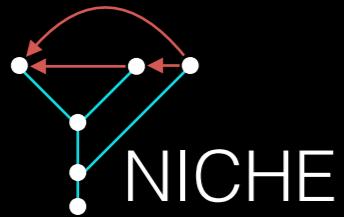
no, but



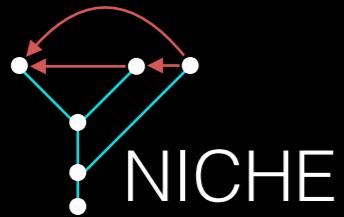


NICHE

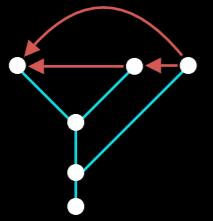
with M Huttchinson, DB Stouffer and M Dehling



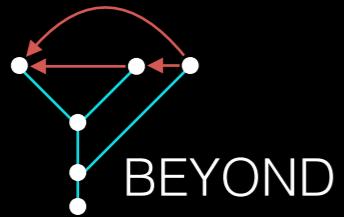
How do species' niches evolve?



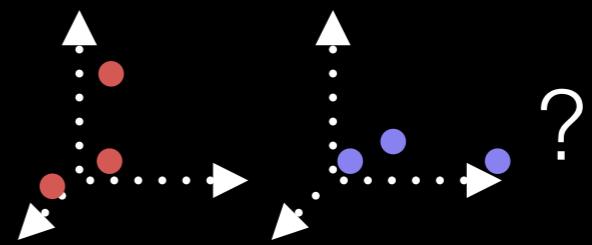
How do we detect the effect
of interactions
in species' evolution?



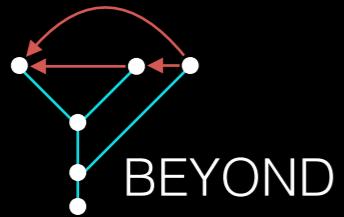
BEYOND



How do species' evolve in



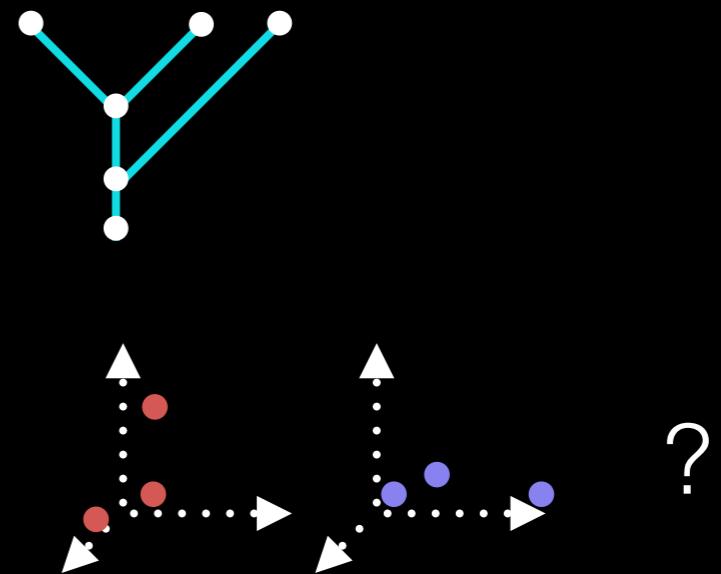
with M Doebeli (UBC)

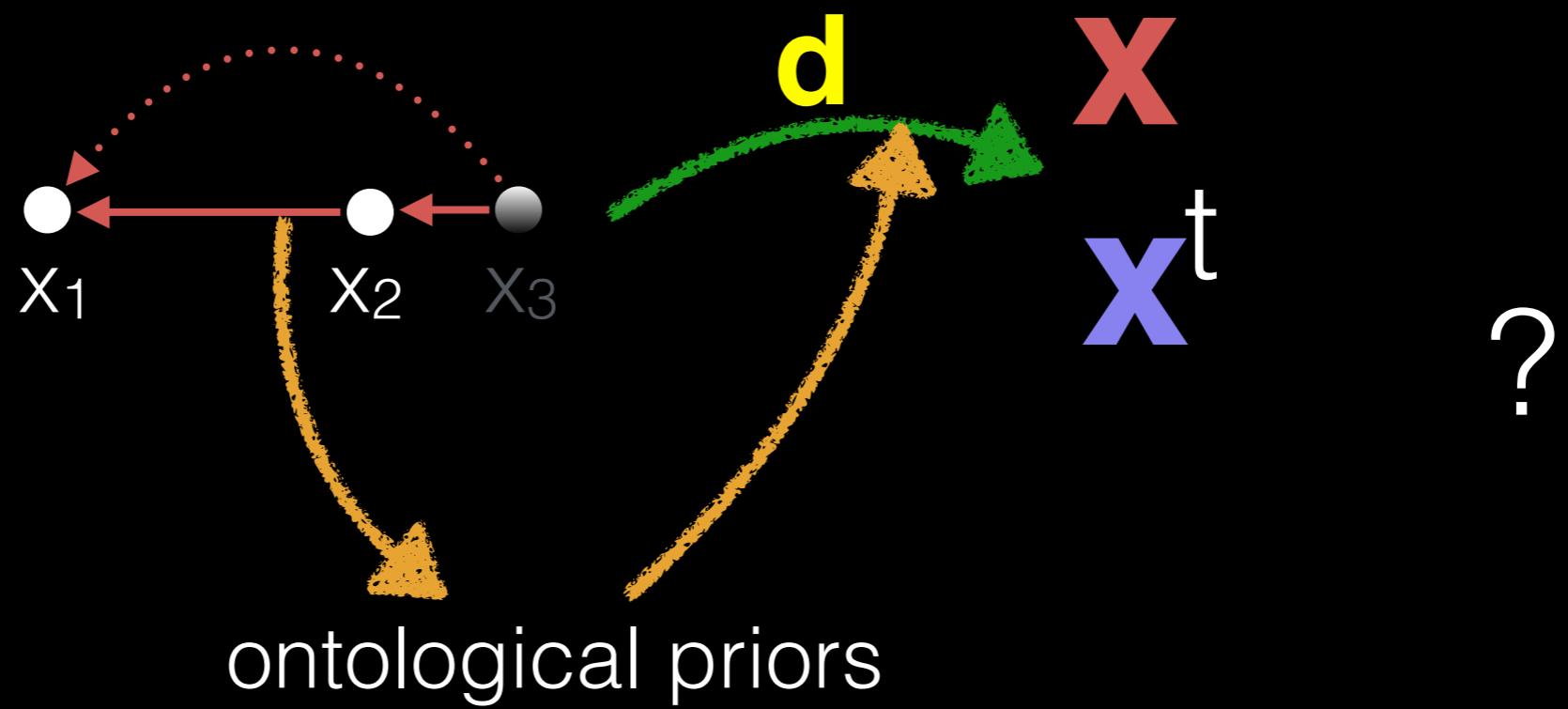
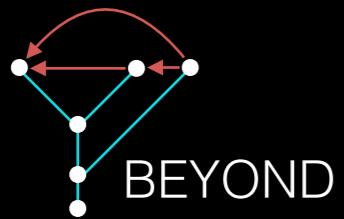


Under which scenarios unique in

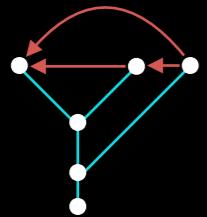
means unique in

with M Doebeli (UBC)





with Carey E Priebe (JHU)



*Because we are all responsible for all
[...] I go for all [...]*

*-Fyodor Dostoyevsky
The Brothers Karamazov*