# Applied SNA with R

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## **Contents**

1	About this book			
2	Introduction	7		
3	R Basics	9		
	3.1 What is R	9		
	3.2 How to install packages	9		
4	Week 1: SNS Study	11		
	4.1 Data preprocessing	11		
	4.2 Creating a network	13		
	4.3 Network descriptive stats	22		
	4.4 Plotting the network in igraph	25		
	4.5 Statistical tests	32		
	4.6 Exponential Random Graph Models	34		
5	Applications	35		
	5.1 Example one	35		
	5.2 Example two	35		
6	Final Words	37		
7	Placeholder	39		
A	Datasets	41		
	A.1 SNS data	41		

4 CONTENTS

# **About this book**

# Introduction

## **R** Basics

- 3.1 What is R
- 3.2 How to install packages

## Week 1: SNS Study

The data can be downloaded from here.

The codebook for the data provided here is in the appendix.

This chapter's goals are:

- 1. Read the data into R,
- 2. Create a network with it,
- 3. Compute descriptive statistics
- 4. Visualize the network

### 4.1 Data preprocessing

### 4.1.1 Reading the data into R

R has several ways of reading data in. You data can be Raw plain files like CSV, tab delimited or specified by column width, for which you can use the readr package; or it can be binary files like dta (Stata), Octave, SPSS, for which foreign can be used; or it could be excel files in which case you should be using readxl. In our case, the data for this session is in Stata format:

```
library(dplyr)
library(magrittr)
library(foreign)
# Reading the data
dat <- foreign::read.dta("03-sns.dta")</pre>
# Taking a look at the data's first 5 columns and 5 rows
dat[1:5, 1:10]
     photoid school hispanic female1 female2 female3 female4 grades1 grades2
##
           1
                                                       0
                                                               0
## 1
                 111
                             1
                                    NA
                                             NA
                                                                       NA
                                                                                NA
## 2
           2
                 111
                             1
                                             NA
                                                      NA
                                                               0
                                                                      3.0
                                                                                NA
## 3
           7
                 111
                             0
                                              1
                                                       1
                                                               1
                                                                      5.0
                                                                               4.5
                                     1
                                              1
                                                       1
                                                                               2.5
## 4
          13
                 111
                             1
                                     1
                                                               1
                                                                      2.5
## 5
          14
                 111
                             1
                                     1
                                              1
                                                       1
                                                              NA
                                                                      3.0
                                                                               3.5
```

## 1 3.5

##

grades3

## 2 NA

## 3 4.0

## 4 2.5

## 5 3.5

### 4.1.2 Creating a unique id for each participant

Now suppose that we want to create a unique id using the school and photo id. In this case, since both variables are numeric, a good way of doing it is to encode the id such that, for example, the last three x numbers are the photoid and the first ones are the school id. To do this we need to take into account the range of the variables. Here, photoid has the following range:

```
(photo_id_ran <- range(dat$photoid))</pre>
```

## [1] 1 2074

As the variable spans up to 2074, we need to set the last 4 units of the variable to store the photoid. Again, we use dplyr to create this variable, and we will call it... id (mind blowing, right?):

```
(dat %<>% mutate(id = school*10000 + photoid)) %>%
head %>%
select(school, photoid, id)
```

```
##
     school photoid
                           id
## 1
        111
                   1 1110001
## 2
        111
                   2 1110002
## 3
        111
                  7 1110007
        111
                  13 1110013
## 4
## 5
        111
                  14 1110014
## 6
        111
                  15 1110015
```

Wow, what happend in the last three lines of code! What is that %>%? Well, that's the piping operator, and it is a very nice way of writing nested function calls. In this case, instead of having write something like

```
dat_filtered$id <- dat_filtered$school*10000 + dat_filtered$photoid
subset(head(dat_filtered), select = c(school, photoid, id))</pre>
```

### 4.2 Creating a network

- We want to build a social network. For that, we either use an adjacency matrix or an edgelist.
- Each individual of the SNS data nomitated 19 friends from school. We will use those nominations to create the social network.
- In this case, we will create the network by coercing the dataset into an edgelist.

### 4.2.1 From survey to edgelist

Let's start by loading a couple of handy R packages for this task.

```
library(tidyr)
library(stringr)
```

Optionally, we can use the tibble type of object which is an alternative to the actual data.frame. This object is claimed to provide *more efficient methods for matrices and data frames*.

```
dat <- as_tibble(dat)</pre>
```

What I like from tibbles is that when you print them on the console these actually look nice:

dat

```
## # A tibble: 2,164 x 100
##
      photoid school hispanic female1 female2 female3 female4 grades1 grades2
                                                                   <dbl>
##
        <int> <int>
                         <dbl>
                                 <int>
                                          <int>
                                                  <int>
                                                          <int>
                                                                           <dbl>
            1
                 111
                                    NA
                                             NA
                                                      0
                                                              0
                                                                   NA
                                                                           NA
##
   1
                            1.
##
    2
            2
                 111
                            1.
                                     0
                                             NA
                                                     NA
                                                              0
                                                                    3.00
                                                                           NA
            7
                                              1
                                                                            4.50
   3
                 111
                            0.
                                     1
                                                      1
                                                               1
                                                                    5.00
##
                                     1
                                              1
                                                                    2.50
                                                                            2.50
##
   4
           13
                 111
                            1.
                                                      1
                                                               1
                                              1
##
    5
           14
                 111
                            1.
                                     1
                                                      1
                                                              NA
                                                                    3.00
                                                                            3.50
##
   6
           15
                 111
                            1.
                                     0
                                              0
                                                      0
                                                              0
                                                                    2.50
                                                                            2.50
   7
           20
                 111
                                              1
                                                                    2.50
                                                                            2.50
##
                            1.
                                     1
                                                      1
                                                               1
##
   8
           22
                 111
                            1.
                                    NA
                                             NA
                                                      0
                                                              0
                                                                   NA
                                                                           NA
##
   9
           25
                 111
                            0.
                                     1
                                              1
                                                     NA
                                                               1
                                                                    4.50
                                                                            3.50
           27
                                     0
                                             NA
                                                      0
                                                              0
## 10
                 111
                            1.
                                                                    3.50
                                                                           NA
## # ... with 2,154 more rows, and 91 more variables: grades3 <dbl>,
       grades4 <dbl>, eversmk1 <int>, eversmk2 <int>, eversmk3 <int>,
## #
## #
       eversmk4 <int>, everdrk1 <int>, everdrk2 <int>, everdrk3 <int>,
       everdrk4 <int>, home1 <int>, home2 <int>, home3 <int>, home4 <int>,
## #
## #
       sch_friend11 <int>, sch_friend12 <int>, sch_friend13 <int>,
       sch_friend14 <int>, sch_friend15 <int>, sch_friend16 <int>,
## #
## #
       sch_friend17 <int>, sch_friend18 <int>, sch_friend19 <int>,
## #
       sch_friend110 <int>, sch_friend111 <int>, sch_friend112 <int>,
## #
       sch_friend113 <int>, sch_friend114 <int>, sch_friend115 <int>,
```

```
## #
       sch_friend116 <int>, sch_friend117 <int>, sch_friend118 <int>,
## #
       sch_friend119 <int>, sch_friend21 <int>, sch_friend22 <int>,
       sch_friend23 <int>, sch_friend24 <int>, sch_friend25 <int>,
## #
## #
       sch_friend26 <int>, sch_friend27 <int>, sch_friend28 <int>,
## #
       sch_friend29 <int>, sch_friend210 <int>, sch_friend211 <int>,
## #
       sch_friend212 <int>, sch_friend213 <int>, sch_friend214 <int>,
       sch_friend215 <int>, sch_friend216 <int>, sch_friend217 <int>,
## #
       sch_friend218 <int>, sch_friend219 <int>, sch_friend31 <int>,
## #
       sch_friend32 <int>, sch_friend33 <int>, sch_friend34 <int>,
## #
       sch_friend35 <int>, sch_friend36 <int>, sch_friend37 <int>,
## #
       sch_friend38 <int>, sch_friend39 <int>, sch_friend310 <int>,
## #
## #
       sch_friend311 <int>, sch_friend312 <int>, sch_friend313 <int>,
## #
       sch_friend314 <int>, sch_friend315 <int>, sch_friend316 <int>,
       sch_friend317 <int>, sch_friend318 <int>, sch_friend319 <int>,
## #
## #
       sch_friend41 <int>, sch_friend42 <int>, sch_friend43 <int>,
       sch_friend44 <int>, sch_friend45 <int>, sch_friend46 <int>,
## #
## #
       sch_friend47 <int>, sch_friend48 <int>, sch_friend49 <int>,
       sch_friend410 <int>, sch_friend411 <int>, sch_friend412 <int>,
## #
## #
       sch_friend413 <int>, sch_friend414 <int>, sch_friend415 <int>,
## #
       sch_friend416 <int>, sch_friend417 <int>, sch_friend418 <int>,
## #
       sch_friend419 <int>, id <dbl>
# Maybe too much piping... but its cool!
net <- dat %>%
  select(id, school, starts_with("sch_friend")) %>%
  gather(key = "varname", value = "content", -id, -school) %>%
  filter(!is.na(content)) %>%
  mutate(
    friendid = school*10000 + content,
             = as.integer(str_extract(varname, "(?<=[a-z])[0-9]")),</pre>
    year
             = as.integer(str_extract(varname, "(?<=[a-z][0-9])[0-9]+"))
    nnom
```

Let's take a look at this step by step:

First, we subset the data: We want to keep id, school, sch\_friend\*. For the later we
use the function starts\_with (from the tidyselect package). This allows us to select
all variables that starts with the word "sch\_friend", which means that sch\_friend11,
sch\_friend12, ... will all be selected.

```
dat %>%
  select(id, school, starts_with("sch_friend"))
```

```
## # A tibble: 2,164 x 78
            id school sch_friend11 sch_friend12 sch_friend13 sch_friend14
##
##
         <dbl> <int>
                              <int>
                                           <int>
                                                         <int>
                                                                      <int>
    1 1110001.
                  111
                                 NA
                                              NA
                                                                         NA
##
                                                            NA
                                424
                                                                        289
##
    2 1110002.
                  111
                                             423
                                                           426
##
   3 1110007.
                  111
                                629
                                             505
                                                            NA
                                                                         NA
##
  4 1110013.
                  111
                                232
                                             569
                                                            NA
                                                                         NA
   5 1110014.
##
                                582
                                             134
                                                            41
                                                                        592
                  111
##
    6 1110015.
                  111
                                 26
                                             488
                                                            81
                                                                        138
    7 1110020.
                                                                        395
                  111
                                528
                                              NA
                                                           492
##
    8 1110022.
##
                  111
                                 NA
                                              NA
                                                            NA
                                                                         NA
##
    9 1110025.
                  111
                                135
                                             185
                                                           553
                                                                         84
## 10 1110027.
                  111
                                346
                                             168
                                                           559
                                                                          5
## # ... with 2,154 more rows, and 72 more variables: sch_friend15 <int>,
## #
       sch_friend16 <int>, sch_friend17 <int>, sch_friend18 <int>,
## #
       sch_friend19 <int>, sch_friend110 <int>, sch_friend111 <int>,
       sch_friend112 <int>, sch_friend113 <int>, sch_friend114 <int>,
## #
## #
       sch_friend115 <int>, sch_friend116 <int>, sch_friend117 <int>,
## #
       sch_friend118 <int>, sch_friend119 <int>, sch_friend21 <int>,
       sch_friend22 <int>, sch_friend23 <int>, sch_friend24 <int>,
## #
       sch_friend25 <int>, sch_friend26 <int>, sch_friend27 <int>,
## #
## #
       sch_friend28 <int>, sch_friend29 <int>, sch_friend210 <int>,
       sch_friend211 <int>, sch_friend212 <int>, sch_friend213 <int>,
## #
## #
       sch_friend214 <int>, sch_friend215 <int>, sch_friend216 <int>,
## #
       sch_friend217 <int>, sch_friend218 <int>, sch_friend219 <int>,
## #
       sch_friend31 <int>, sch_friend32 <int>, sch_friend33 <int>,
```

```
## #
       sch_friend34 <int>, sch_friend35 <int>, sch_friend36 <int>,
## #
       sch_friend37 <int>, sch_friend38 <int>, sch_friend39 <int>,
       sch_friend310 <int>, sch_friend311 <int>, sch_friend312 <int>,
## #
## #
       sch_friend313 <int>, sch_friend314 <int>, sch_friend315 <int>,
## #
       sch_friend316 <int>, sch_friend317 <int>, sch_friend318 <int>,
## #
       sch_friend319 <int>, sch_friend41 <int>, sch_friend42 <int>,
## #
       sch_friend43 <int>, sch_friend44 <int>, sch_friend45 <int>,
       sch_friend46 <int>, sch_friend47 <int>, sch_friend48 <int>,
## #
## #
       sch_friend49 <int>, sch_friend410 <int>, sch_friend411 <int>,
       sch_friend412 <int>, sch_friend413 <int>, sch_friend414 <int>,
## #
       sch_friend415 <int>, sch_friend416 <int>, sch_friend417 <int>,
## #
       sch_friend418 <int>, sch_friend419 <int>
## #
```

2. Then, we reshape it to *long* format: By transposing all the sch\_friend\* to long. We do this by means of the function gather (from the tidyr package). This is an alternative to the reshape function, and I personally find it easier to use. Let's see how it works:

```
dat %>%
  select(id, school, starts_with("sch_friend")) %>%
  gather(key = "varname", value = "content", -id, -school)
```

```
## # A tibble: 164,464 x 4
##
            id school varname
                                    content
##
         <dbl> <int> <chr>
                                      <int>
    1 1110001.
                  111 sch_friend11
##
                                         NA
##
    2 1110002.
                  111 sch_friend11
                                        424
    3 1110007.
                  111 sch_friend11
##
                                        629
   4 1110013.
                  111 sch_friend11
                                        232
##
   5 1110014.
                  111 sch_friend11
                                        582
##
##
   6 1110015.
                  111 sch_friend11
                                         26
  7 1110020.
                  111 sch_friend11
                                        528
##
## 8 1110022.
                  111 sch_friend11
                                         NA
## 9 1110025.
                  111 sch_friend11
                                        135
## 10 1110027.
                  111 sch_friend11
                                        346
```

```
## # ... with 164,454 more rows
```

In this case the key parameter sets the name of the variable that will contain the name of the variable that was reshaped, while value is the name of the variable that will hold the content of the data (that's why I named those like that). The -id, -school bit tells the function to "drop" those variables before reshaping, in other words, "reshape everything but id and school".

Also, notice that we passed from 2164 rows to 19 (nominations) \* 2164 (subjects) \* 4 (waves) = 164464 rows, as expected.

3. As the nomination data can be empty for some cells, we need to take care of those cases, the NAs, so we filter the data:

```
dat %>%
  select(id, school, starts_with("sch_friend")) %>%
  gather(key = "varname", value = "content", -id, -school) %>%
  filter(!is.na(content))
```

```
## # A tibble: 39,561 x 4
##
            id school varname
                                   content
         <dbl> <int> <chr>
##
                                     <int>
   1 1110002.
                  111 sch_friend11
##
                                       424
##
   2 1110007.
                 111 sch_friend11
                                       629
## 3 1110013.
                  111 sch_friend11
                                       232
## 4 1110014.
                  111 sch_friend11
                                       582
##
   5 1110015.
                  111 sch friend11
                                        26
## 6 1110020.
                  111 sch_friend11
                                       528
  7 1110025.
                  111 sch_friend11
##
                                       135
                  111 sch_friend11
## 8 1110027.
                                       346
## 9 1110029.
                  111 sch_friend11
                                       369
## 10 1110030.
                  111 sch_friend11
                                       462
## # ... with 39,551 more rows
```

4. And finally, we create three new variables from this dataset: friendid, year, and nom\_num (nomination number). All this using regular expressions:

```
dat %>%
  select(id, school, starts_with("sch_friend")) %>%
  gather(key = "varname", value = "content", -id, -school) %>%
  filter(!is.na(content)) %>%
  mutate(
    friendid = school*10000 + content,
    year = as.integer(str_extract(varname, "(?<=[a-z])[0-9]")),
    nnom = as.integer(str_extract(varname, "(?<=[a-z][0-9])[0-9]+"))
    )
}</pre>
```

```
## # A tibble: 39,561 x 7
            id school varname
                                   content friendid year nnom
##
         <dbl> <int> <chr>
                                              <dbl> <int> <int>
##
                                     <int>
    1 1110002.
                  111 sch_friend11
                                       424 1110424.
                                                        1
                                                              1
##
    2 1110007.
                  111 sch_friend11
                                       629 1110629.
##
                                                        1
                                                              1
    3 1110013.
                  111 sch_friend11
                                       232 1110232.
##
                                                        1
                                                              1
                  111 sch_friend11
##
   4 1110014.
                                       582 1110582.
                                                        1
                                                              1
   5 1110015.
                  111 sch_friend11
                                        26 1110026.
                                                        1
                                                              1
## 6 1110020.
                  111 sch_friend11
                                       528 1110528.
                                                        1
                                                              1
##
   7 1110025.
                  111 sch_friend11
                                       135 1110135.
                                                        1
                                                              1
## 8 1110027.
                  111 sch_friend11
                                       346 1110346.
                                                        1
                                                              1
## 9 1110029.
                  111 sch_friend11
                                       369 1110369.
                                                        1
                                                              1
## 10 1110030.
                  111 sch_friend11
                                       462 1110462.
                                                        1
                                                              1
## # ... with 39,551 more rows
```

The regular expression (?<=[a-z]) matches a string that is preceded by any letter from a to z, whereas the expression [0-9] matches a single number. Hence, from the string "sch\_friend12", the regular expression will only match the 1, as it is the only number followed by a letter. On the other hand, the expression (?<=[a-z][0-9]) matches a string that is preceded by a letter from a to z and a number from a to a0 to a1; and the expression [0-9]+ matches a string of numbers—so it could be more than one. Hence, from the string "sch\_friend12", we will get 2. We can actually se this

```
str_extract("sch_friend12", "(?<=[a-z])[0-9]")

## [1] "1"

str_extract("sch_friend12", "(?<=[a-z][0-9])[0-9]+")

## [1] "2"</pre>
```

And finally, the as.integer function coerces the returning value from the str\_extract function from character to integer. Now that we have this edgelist, we can create an igraph object

#### 4.2.2 igraph network

For coercing the edgelist into an igraph object, we will be using the graph\_from\_data\_frame function in igraph. This function receives a data frame where the two first columns are sorce(ego) and target(alter), whether is it directed or not, and an optional data frame with vertices, in which's first column should contain the vertex ids.

Using the optional vertices argument is a good practice since by doing so you are telling the function what is the set of vertex ids that you are expecting to find. Using the original dataset, we will create a data frame name vertices:

```
vertex_attrs <- dat %>%
select(id, school, hispanic, female1, starts_with("eversmk"))
```

Now, let's now use the function graph\_from\_data\_frame to create an igraph object:

```
library(igraph)

ig_year1 <- net %>%
  filter(year == "1") %>%
  select(id, friendid, nnom) %>%
  graph_from_data_frame(
    vertices = vertex_attrs
)
```

## Error in graph\_from\_data\_frame(., vertices = vertex\_attrs): Some vertex names in edge l

Ups! It seems that individuals are making nominations to other students that were not included on the survery. How to solve that? Well, it all depends on what you need to do! In this case, we will go for the *quietly-remove-em'-and-don't-tell* strategy:

```
ig_year1 <- net %>%
filter(year == "1") %>%

# Extra line, all nominations must be in ego too.
filter(friendid %in% id) %>%

select(id, friendid, nnom) %>%
graph_from_data_frame(
   vertices = vertex_attrs
   )

ig_year1
```

```
## IGRAPH 7532eb5 DN-- 2164 9514 --
## + attr: name (v/c), school (v/n), hispanic (v/n), female1 (v/n),
## | eversmk1 (v/n), eversmk2 (v/n), eversmk3 (v/n), eversmk4 (v/n),
## + edges from 7532eb5 (vertex names):
## [1] 1110007->1110629 1110013->1110232 1110014->1110582 1110015->1110026
## [5] 1110025->1110135 1110027->1110346 1110029->1110369 1110035->1110034
## [9] 1110040->1110390 1110041->1110557 1110044->1110027 1110046->1110030
## [13] 1110050->1110086 1110057->1110263 1110069->1110544 1110071->1110167
## [17] 1110072->1110289 1110073->1110014 1110075->1110352 1110084->1110305
## [21] 1110086->1110206 1110093->1110040 1110094->1110483 1110095->1110043
## + ... omitted several edges
```

So there we have, our network with 2164 nodes and 9514 edges. The next steps: get some descriptive stats and visualize our network.

### 4.3 Network descriptive stats

While we could do all networks at once, in this part we will focus on computing some network statistics for one of the schools only. We start by school 111. The first question that you should be asking your self now is, "how can I get that information from the igraph object?." Well, vertex attributes and edges attributes can be accessed via the V and E functions respectively; moreover, we can list what vertex/edge attributes are available:

```
list.vertex.attributes(ig_year1)

## [1] "name"     "school"     "hispanic" "female1"     "eversmk1" "eversmk2"

## [7] "eversmk3" "eversmk4"

list.edge.attributes(ig_year1)

## [1] "nnom"
```

Just like we would do with data frames, accessing vertex attributes is done via the dollar sign operator \$ together with the V function, for example, accessing the first 10 elements of the variable hispanic can be done as follows:

```
V(ig_year1)$hispanic[1:10]
```

```
## [1] 1 1 0 1 1 1 1 1 0 1
```

Now that you know how to access vertex attributes, we can get the network corresponding to school 111 by identifying which vertices are part of it and pass that information to the induced\_subgraph function:

```
# Which ids are from school 111?
school11lids <- which(V(ig_year1)$school == 111)

# Creating a subgraph
ig_year1_111 <- induced_subgraph(
    graph = ig_year1,
    vids = school11lids
)</pre>
```

The which function in R returns a vector of indices indicating which elements are true. In our

case it will return a vector of indices of the vertices which have the attribute school equal to 111. Now that we have our subgraph, we can compute different centrality measures<sup>1</sup> for each vertex and store them in the igraph object itself:

```
# Computing centrality measures for each vertex
V(ig_yearl_111)$indegree <- degree(ig_yearl_111, mode = "in")
V(ig_yearl_111)$outdegree <- degree(ig_yearl_111, mode = "out")
V(ig_yearl_111)$closeness <- closeness(ig_yearl_111, mode = "total")
V(ig_yearl_111)$betweeness <- betweenness(ig_yearl_111, normalized = TRUE)</pre>
```

From here, we can *go back* to our old habits and get the set of vertex attributes as a data frame so we can compute some summary statistics on the centrality measurements that we just got

```
# Extracting each vectex features as a data.frame
stats <- as_data_frame(ig_yearl_111, what = "vertices")

# Computing quantiles for each variable
stats_degree <- with(stats, {
    cbind(
        indegree = quantile(indegree, c(.025, .5, .975)),
        outdegree = quantile(outdegree, c(.025, .5, .975)),
        closeness = quantile(closeness, c(.025, .5, .975)),
        betweeness = quantile(betweeness, c(.025, .5, .975))
}
stats_degree</pre>
```

```
## indegree outdegree closeness betweeness

## 2.5% 0 0 3.526640e-06 0.000000000

## 50% 4 4 1.595431e-05 0.001879006

## 97.5% 16 16 1.601822e-05 0.016591048
```

The with function is somewhat similar to what dplyr allows us to do when we want to work

<sup>&</sup>lt;sup>1</sup>For more information about the different centrality measurements, please take a look at the "Centrality" article on Wikipedia.

with the dataset but without mentioning its name everytime that we ask for a variable. Without using the with function, the previous could have been done as follows:

```
stats_degree <-
cbind(
  indegree = quantile(stats$indegree, c(.025, .5, .975)),
  outdegree = quantile(stats$outdegree, c(.025, .5, .975)),
  closeness = quantile(stats$closeness, c(.025, .5, .975)),
  betweeness = quantile(stats$betweeness, c(.025, .5, .975))
)</pre>
```

Now we will compute some statistics at the graph level:

```
cbind(
    size = vcount(ig_yearl_111),
    nedges = ecount(ig_yearl_111),
    density = edge_density(ig_yearl_111),
    recip = reciprocity(ig_yearl_111),
    centr = centr_betw(ig_yearl_111)$centralization,
    pathLen = mean_distance(ig_yearl_111)
)
```

```
## size nedges density recip centr pathLen
## [1,] 533 2638 0.009303277 0.3731513 0.02179154 4.23678
```

Triadic census

```
triadic <- triad_census(ig_year1_111)
triadic</pre>
```

```
##
    [1] 24059676
                    724389
                              290849
                                           3619
                                                    3383
                                                              4401
                                                                        3219
    [8]
             2997
                        407
                                   33
                                           836
                                                     235
                                                               163
                                                                         137
## [15]
              277
                         85
```

```
knitr::kable(cbind(
   Pcent = triadic/sum(triadic)*100,
   read.csv("triadic_census.csv")
   ), digits = 2)
```

Pcent	code	description
95.88	003	A,B,C, the empty graph.
2.89	012	A->B, C, the graph with a single directed edge.
1.16	102	A<->B, C, the graph with a mutual connection between two vertices.
0.01	021D	A<-B->C, the out-star.
0.01	021U	A->B<-C, the in-star.
0.02	021C	A->B->C, directed line.
0.01	111D	A<->B<-C.
0.01	111U	A<->B->C.
0.00	030T	A->B<-C, A->C.
0.00	030C	A<-B<-C, A->C.
0.00	201	A<->B<->C.
0.00	120D	A<-B->C, A<->C.
0.00	120U	A->B<-C, A<->C.
0.00	120C	A->B->C, A<->C.
0.00	210	A->B<->C, A<->C.
0.00	300	A<->B<->C, A<->C, the complete graph.

## 4.4 Plotting the network in igraph

### 4.4.1 Single plot

Let's take a look at how does our network looks like when we use the default parameters in the plot method of the igraph object:

#### plot(ig\_year1)

Not very nice, right? A couple of things with this plot:

- 1. We are looking at all schools simultaneously, which does not make sense. So, instead of plotting ig\_year1, we will focus on ig\_year1\_111.
- 2. All the vertices have the same size, and more over, are overalaping. So, instead of using the default size, we will size the vertices by indegree using the degree function, and

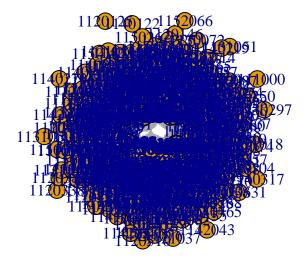


Figure 4.1: A not very nice network plot. This is what we get with the default parameters in igraph.

passing the vector of degrees to vertex.size.<sup>2</sup>

- 3. Given the number of vertices in these networks, the labels are not useful here. So we will remove them by setting vertex.label = NA. Moreover, we will reduce the size of the arrows' tip by setting edge.arrow.size = 0.25.
- 4. And finally, we will set the color of each vertex to be a function of whether the individual is hispanic or not. For this last bit we need to go a bit more of programming:

```
col_hispanic <- V(ig_year1_111)$hispanic + 1
col_hispanic <- coalesce(col_hispanic, 3)
col_hispanic <- c("steelblue", "tomato", "white")[col_hispanic]</pre>
```

Line by line, we did the following:

- 1. The first line added one to all no NA values, so that the 0s (non-hispanic) turned to 1s and the 1s (hispanic) turned to 2s.
- 2. The second line replaced all NAs with the number 3, so that our vector col\_hispanic now ranges from 1 to 3 with no NAs in it.
- 3. In the last line we created a vector of colors. Essentially, what we are doing here is telling R to create a vector of length length(col\_hispanic) by selecting elements by index

<sup>&</sup>lt;sup>2</sup>Figuring out what is the optimal vertex size is a bit tricky. Without getting too technical, there's no other way of getting *nice* vertex size other than just playing with different values of it. A nice solution to this is using netdiffuseR::igraph\_vertex\_rescale which rescales the vertices so that these keep their aspect ratio to a predefined proportion of the screen.

from the vector c("steelblue", "tomato", "white"). This way, if, for example, the first element of the vector col\_hispanic was a 3, our new vector of colors would have a "white" in it.

To make sure we know we are right, let's print the first 10 elements of our new vector of colors together with the original hispanic column:

```
cbind(
  original = V(ig_yearl_111)$hispanic[1:10],
  colors = col_hispanic[1:10]
)
```

```
original colors
##
##
    [1,] "1"
                  "tomato"
    [2,] "1"
                  "tomato"
##
## [3,] "0"
                  "steelblue"
## [4,] "1"
                  "tomato"
## [5,] "1"
                  "tomato"
## [6,] "1"
                  "tomato"
## [7,] "1"
                  "tomato"
                  "tomato"
## [8,] "1"
## [9,] "0"
                  "steelblue"
## [10,] "1"
                  "tomato"
```

With our nice vector of colors, now we can pass it to plot.igraph (which we call implicitly by just calling plot), via the vertex.color argument:

```
# Fancy graph
set.seed(1)
plot(
    ig_year1_111,
    vertex.size = degree(ig_year1_111)/10 +1,
    vertex.label = NA,
    edge.arrow.size = .25,
    vertex.color = col_hispanic
    )
```

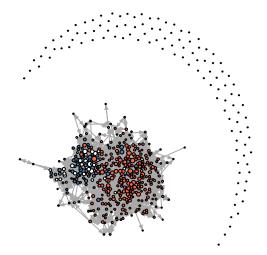


Figure 4.2: Friends network in time 1 for school 111.

Nice! So it does look better. The only problem is that we have a lot of isolates. Let's try again by drawing the same plot without isolates. To do so we need to filter the graph, for which we will use the function induced\_subgraph

```
# Which vertices are not isolates?
which_ids <- which(degree(ig_yearl_111, mode = "total") > 0)

# Getting the subgraph
ig_yearl_111_sub <- induced_subgraph(ig_yearl_111, which_ids)

# We need to get the same subset in col_hispanic
col_hispanic <- col_hispanic[which_ids]</pre>
```

```
# Fancy graph
set.seed(1)
plot(
    ig_year1_111_sub,
    vertex.size = degree(ig_year1_111_sub)/5 +1,
    vertex.label = NA,
    edge.arrow.size = .25,
    vertex.color = col_hispanic
    )
```

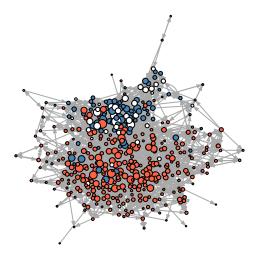


Figure 4.3: Friends network in time 1 for school 111. The graph excludes isolates.

Now that's better! An interesting pattern that shows up is that individuals seem to cluster by whether they are hispanic or not.

We can actually write this as a function so that, instead of us copying and pasting the code n times (supposing that we want to crate a plot similar to this n times). The next subsection does that.

### 4.4.2 Multiple plots

When you are repeating yourself over and over again, it is a good idea to write down a sequence of commands as a function. In this case, since we will be running the same type of plot for all schools/waves, we write a function in which the only things that changes are: (a) the school id, and (b) the color of the nodes.

```
myplot <- function(
  net,
  schoolid,
  mindgr = 1,
  vcol = "tomato",
  ...) {

# Creating a subgraph
  subnet <- induced_subgraph(</pre>
```

```
net,
    which(degree(net, mode = "all") >= mindgr & V(net)$school == schoolid)
  )
  # Fancy graph
  set.seed(1)
  plot(
    subnet,
    vertex.size
                   = degree(subnet)/5,
    vertex.label
                    = NA
    edge.arrow.size = .25,
    vertex.color
                    = vcol,
    . . .
    )
}
```

#### The function definition:

- The myplot <- function([arguments]) {[body of the function]} tells R that we
  are going to create a function called myplot.</li>
- 2. In the arguments part, we are declaring 4 specific arguments: net, schoolid, mindgr, and vcol. These are an igraph object, the school id, the minimum degree that a vertex must have to be included in the plot, and the color of the vertices. Notice that, as a difference from other programming languages, in R we don't need to declare the types that these objects are.
- 3. The elipsis object, ..., is a special object in R that allows us passing other arguments without us specifying which. In our case, if you take a look at the plot bit of the body of the function, you will see that we also added ...; this means that whatever other arguments (different from the ones that we explicitly defined) are passed to the function, these will be passed to the function plot, moreover, to the plot.gexf function (since the subnet object is actually an igraph object). In practice, this implies that we can, for example, set the argument edge.arrow.size when calling myplot, even though we did not included it in the function definition! (See ?dotsMethods in R for more details).

In the following lines of code, using our new function, we will plot each schools' network in the same plotting device (window) with the help of the par function, and add legend with the legend:

```
# Plotting all together
oldpar <- par(no.readonly = TRUE)</pre>
par(mfrow = c(2, 3), mai = rep(0, 4), oma = c(1, 0, 0, 0))
myplot(ig_year1, 111, vcol = "tomato")
myplot(ig_year1, 112, vcol = "steelblue")
myplot(ig_year1, 113, vcol = "black")
myplot(ig_year1, 114, vcol = "gold")
myplot(ig_year1, 115, vcol = "white")
par(oldpar)
# A fancy legend
legend(
  "bottomright",
  legend = c(111, 112, 113, 114, 115),
  pt.bg = c("tomato", "steelblue", "black", "gold", "white"),
  pch
        = 21,
  cex
        = 1,
  bty = "n",
  title = "School"
```

#### So what happend here?

- oldpar <- par(no.readonly = TRUE) This line stores the current parameters for plotting. Since we are going to be changing them, we better make sure we are able to go back!.
- par(mfrow = c(2, 3), mai = rep(0, 4), oma=rep(0, 4)) Here we are setting various things at the same time. mfrow specifies how many *figures* will be drawn and in what order, in particular, we are asking the plotting device to allow for 2\*3 = 6 plots organized in 2 rows and 3 columns, and these will be drawn by row.

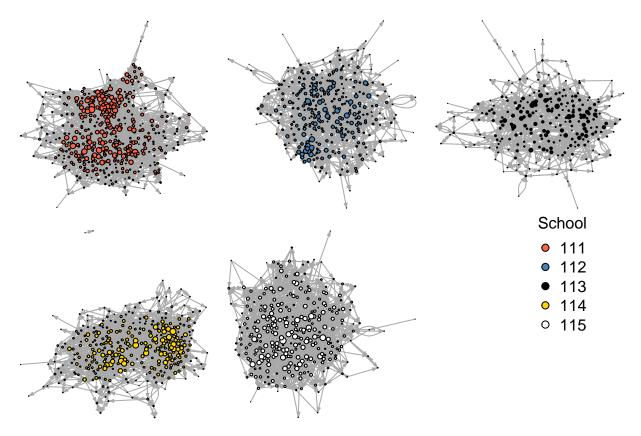


Figure 4.4: All 5 schools in time 1. Again, the graphs exclude isolates.

mai specifies the size of the margins in inches. Setting all margins equal to zero (which is what we are doing now) gives more space to the network itself. The same is true for oma. See ?par for more info.

- myplot(ig\_year1, ...) This is simply calling our plotting function. The neat part of this
  is that, since we set mfrow = c(2, 3), R takes care of distributing the plots in the device.
- par(oldpar) This line allows us to restore the plotting parameters.

### 4.5 Statistical tests

### 4.5.1 Is nomination number correlated with indegree?

Hypothesis: Individuals that on average are among the first nominations of their peers are more popular

```
# Getting all the data in long format
edgelist <- as_long_data_frame(ig_year1) %>%
    as_tibble

# Computing indegree (again) and average nomination number
indeg_nom_cor <- group_by(edgelist, to, to_name, to_school) %>%
    summarise(
    indeg = n(),
    nom_avg = mean(nnom)
) %>%
    rename(
    school = to_school
)

indeg_nom_cor

## # A tibble: 1,561 x 5
```

```
## # Groups: to, to_name [1,561]
##
        to to_name school indeg nom_avg
      <dbl> <chr>
                    <int> <int>
                                  <dbl>
##
## 1
        2. 1110002
                      111
                             22
                                   4.50
  2
        3. 1110007
                      111
                              7
##
                                   5.71
## 3
        4. 1110013
                      111
                              6
                                   5.83
        5. 1110014
                             19
                                  7.47
## 4
                      111
## 5
        6. 1110015
                      111
                             3
                                   6.67
## 6
        7. 1110020
                      111
                              6
                                   6.50
## 7
        9. 1110025
                      111
                             6
                                   4.67
## 8
       10. 1110027
                      111
                             13
                                   4.54
## 9
       11. 1110029
                      111
                             14
                                   7.64
## 10
       12. 1110030
                      111
                                   4.50
                              6
## # ... with 1,551 more rows
```

```
# Using pearson's correlation
with(indeg_nom_cor, cor.test(indeg, nom_avg))

##
## Pearson's product-moment correlation
##
## data: indeg and nom_avg
## t = 5.0502, df = 1559, p-value = 4.933e-07
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## 0.07774571 0.17538115
## sample estimates:
## cor
## 0.1268707
```

## 4.6 Exponential Random Graph Models

```
library(ergm)
```

# **Applications**

- 5.1 Example one
- 5.2 Example two

# **Final Words**

# **Placeholder**

# **Appendix A**

## **Datasets**

## A.1 SNS data

# **Bibliography**