

Preliminaries

Evolution of Gene  
Function

Mechanistic Machine  
Learning

Proof of Concept

# Predicting of Gene Functions by Leveraging Biological Insights with Mechanistic Machine Learning



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Division of Epidemiology @ University of Utah

Jan 11th, 2023 @ Data Science Seminar

Collaborators: Paul Thomas, Paul Marjoram, Huaiyu Mi, Christopher Williams (USC), Alun Thomas (UofU)

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You can download the slides from <https://ggyv.cl/UofUDS2023>

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But first...

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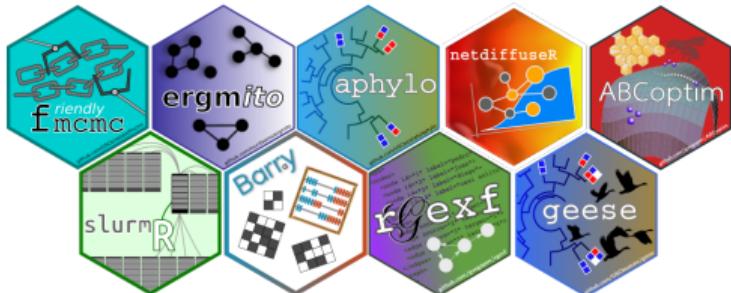
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## George G. Vega Yon's GitHub Stats

⭐ Total Stars Earned:	247
⌚ Total Commits (2022):	2.4k
👉 Total PRs:	111
❗ Total Issues:	228
💻 Contributed to:	33



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- ▶ Scientific software developer (R/C++) with (~ 500K downloads + 9 CRAN packages).

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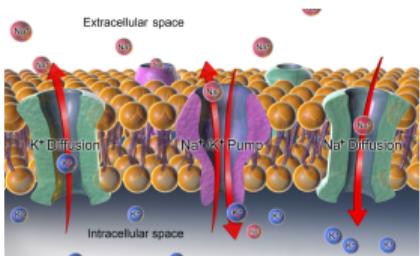
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# Gene Function

Encode the synthesis of genetic products that ultimately are related to a particular aspect of life, for example

## Molecular function

## Active transport



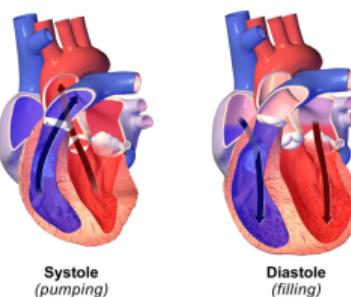
## **Cellular component**

## Mitochondria GO:0004016



## Biological process

## Heart contraction



# Gene Function: the Gene Ontology Project



**GENEONTOLOGY**  
Unifying Biology

- The GO project has  $\sim$  43,000 validated terms,  $\sim$  7.4M annotations on  $\sim$  5,200 species.

**source:** Statistics from <http://pantherdb.org/panther/summaryStats.jsp> and <http://geneontology.org/stats.html>

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- ▶ About  $\sim$  700,000 annotations are on human genes.
- ▶ Only half of the human gene annotations are based on experimental evidence.
- ▶ About  $\sim$  173,000 publications have used the GO.

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# Predicting Gene Function: State-of-the-art

Sequences, phylogenomics, and ML.

- ▶ **BLAST**:<sup>2</sup> Prediction by sequence homology (~ 105,000 citations).

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In the latest CAFA, **none** of the top-performing methods scored an AUC above 0.60, and most were outperformed by BLAST,<sup>19</sup> which annotates using homology based on sequence similarity.

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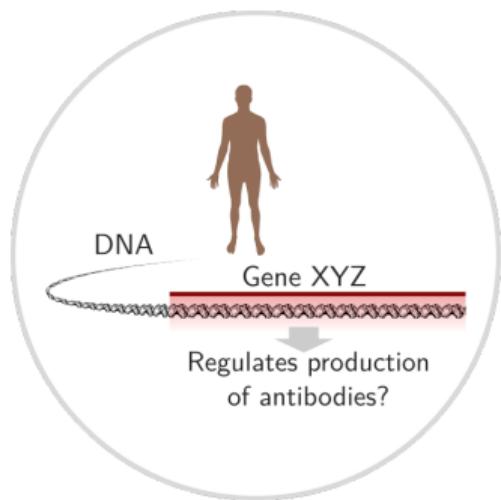
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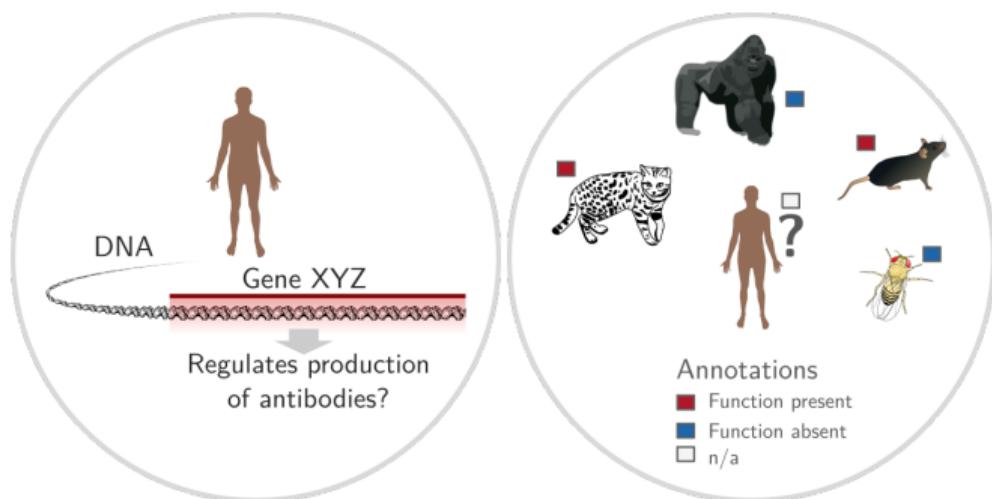
Proof of Concept

Is gene *XYZ* involved in process *ABC*?



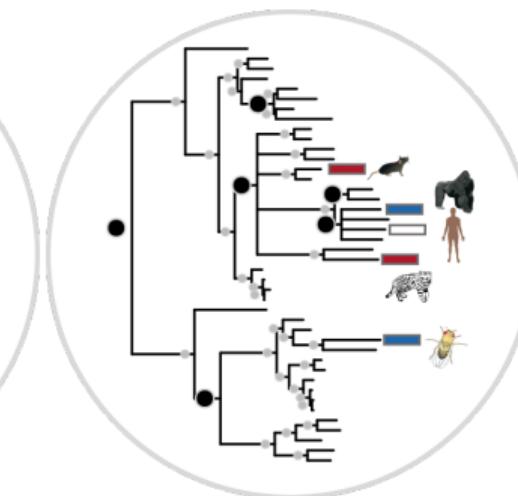
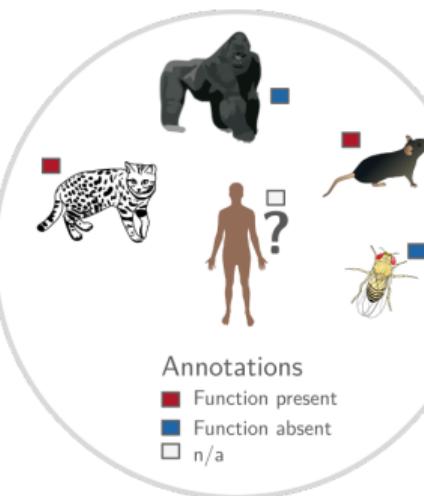
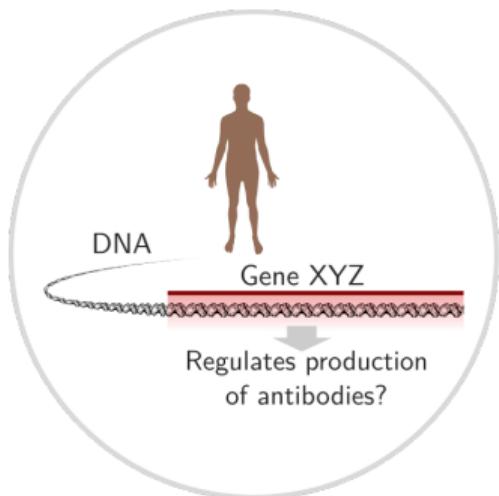
Complex to directly assess

Is gene *XYZ* involved in process *ABC*?



Complex to directly assess But we may know from other species

# Is gene XYZ involved in process ABC?



Complex to directly assess

But we may know from other species

And we further know how these are *evolutionary* connected

Is the human gene **XYZ** involved in process **ABC**, given what we know about that for other *related* species?

## Annotations

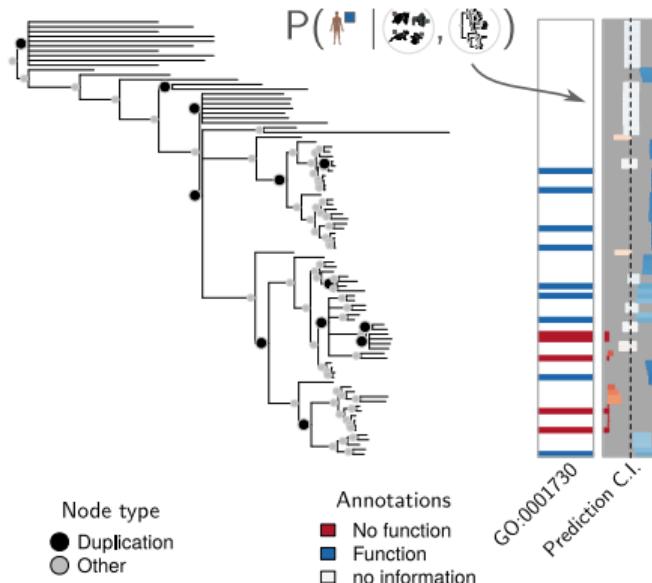
- █ Function present
- █ Function absent
- █ n/a

# Evolution of Gene function (of one function)

Built a big model (lots of trees and annotations) called aphylo:

- ▶ Only two sources of data:

Phylogenetic tree  
(pantherdb.org) and functional  
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(geneontology.org).



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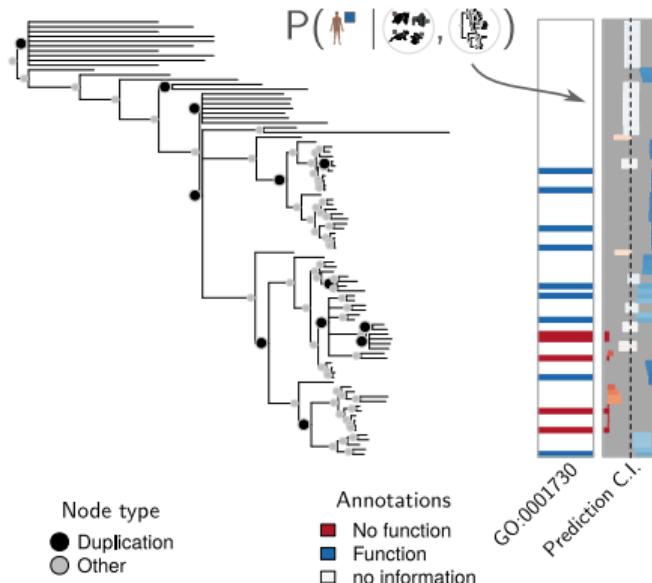
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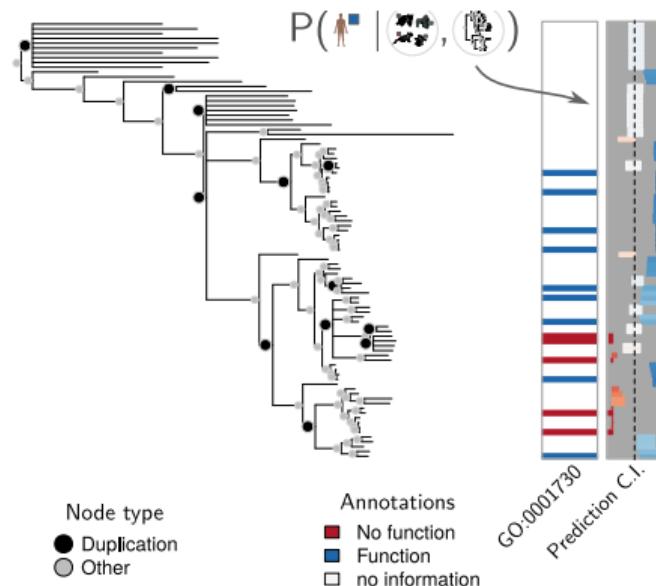
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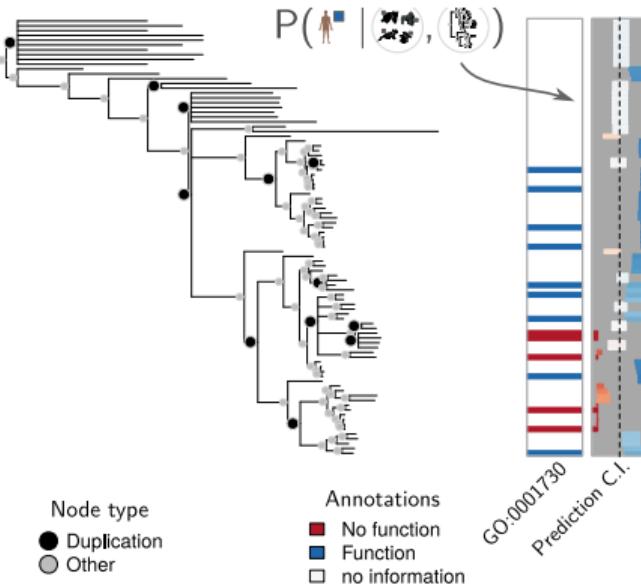
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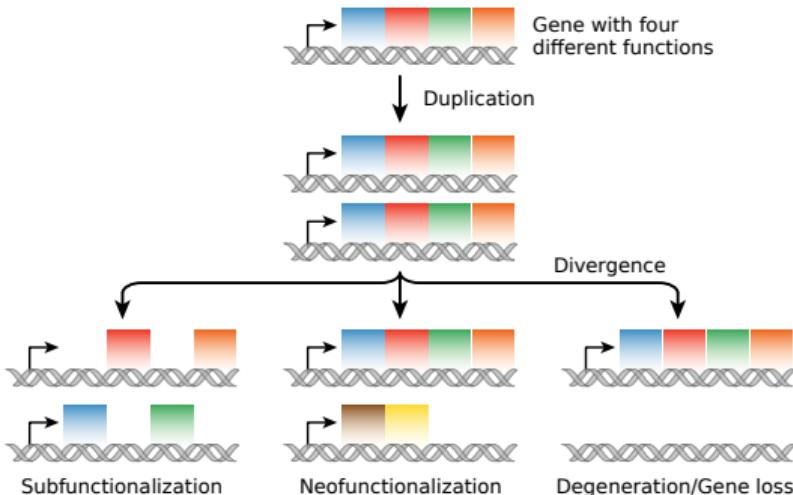
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- ▶ Leverage negative annotation of GO terms (NOT).
- ▶ Use Felsenstein's tree pruning algorithm to compute tree likelihood.
- ▶ Fit pooled models featuring thousands of annotations in hundreds of trees (with split-second prediction capability).



... But what if we wanted to deal with multiple functions?

## Evolution of Gene function (multiple functions)

## Tapping into Evol. Theory

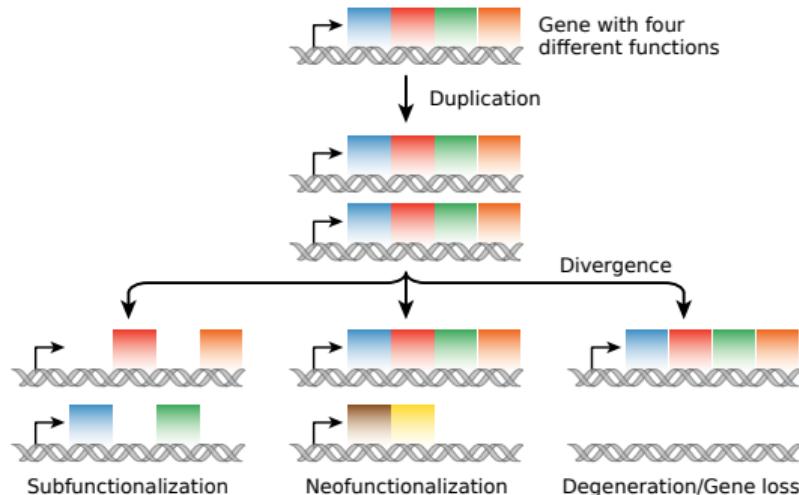


**Figure:** A key part of molecular innovation, gene duplication provides an opportunity for new functions to emerge (wikimedia)

## Evolution of Gene function (multiple functions)

## Tapping into Evol. Theory

- ▶ A fundamental part of Fun. Evol. is Duplication Events.
  - ▶ Furthermore, knowing what happened to gene A (e.g., neofunctionalization) is highly informative to learn about the functional state of B.

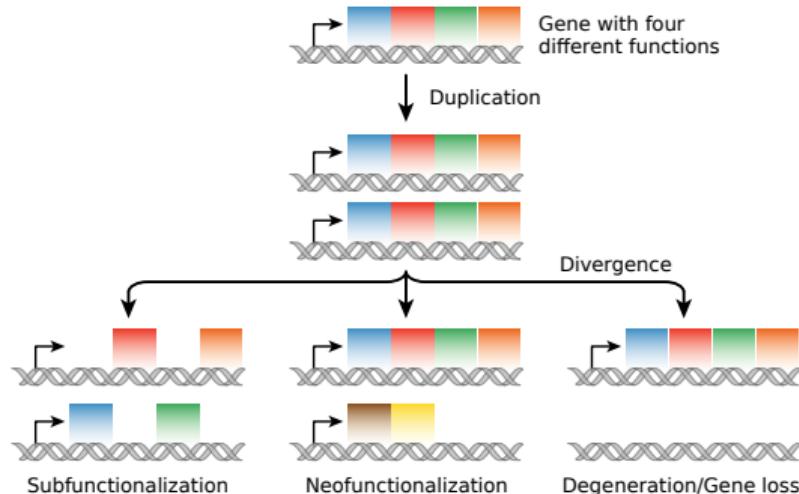


**Figure:** A key part of molecular innovation, gene duplication provides an opportunity for new functions to emerge (wikimedia)

## Evolution of Gene function (multiple functions)

# Tapping into Evol. Theory

- ▶ A fundamental part of Fun. Evolution is Duplication Events.
  - ▶ Furthermore, knowing what happened to gene A (e.g., neofunctionalization) is highly informative to learn about the functional state of B.
  - ▶ One way to model this is using a Markov Transition Model (as in SIFTER).

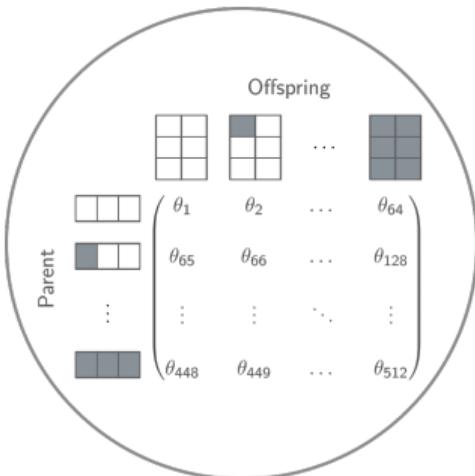


**Figure:** A key part of molecular innovation, gene duplication provides an opportunity for new functions to emerge (wikimedia)

# Evolution of Gene function (multiple functions)

If we wanted to build a model with 3 functions, we would need to estimate...

## Full Markov Transition Matrix



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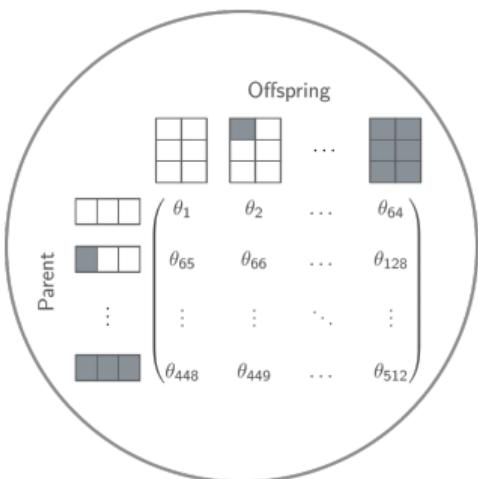
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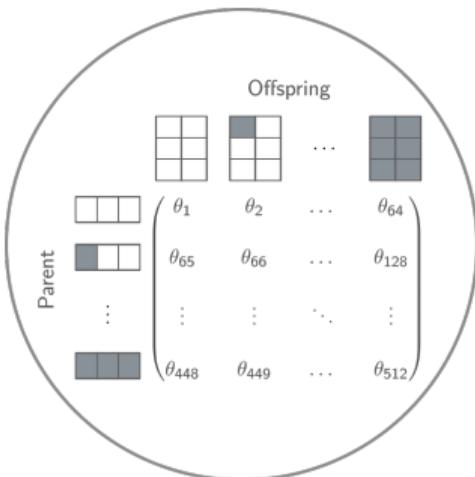
► 512 parameters



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- ▶ 512 parameters
- ▶ Finding this many parameters is not easy.

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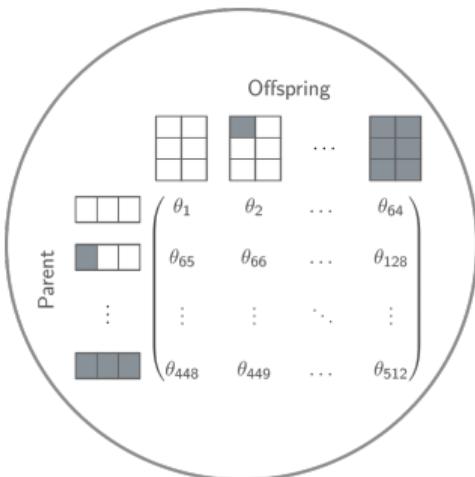
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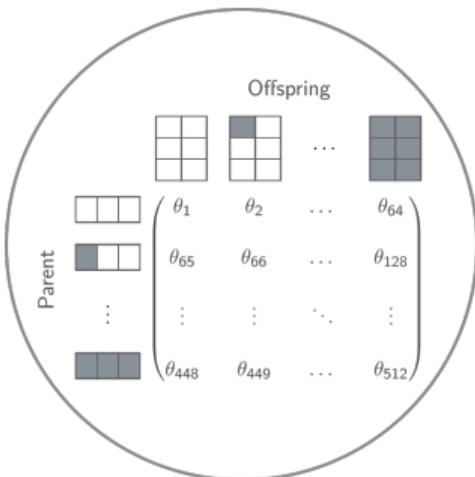


- ▶ 512 parameters
  - ▶ Finding this many parameters is not easy.
  - ▶ Even if you can, interpretation is awkward.

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If we wanted to build a model with 3 functions, we would need to estimate...

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Social Network Analysis may help us...

# Exponential Random Graph Models (ERGMs)

Predicting Gene Functions with Mech. ML

<https://ggy.cl>

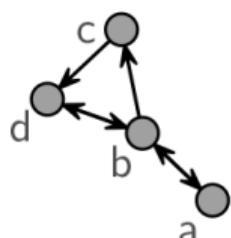
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## Social Network



	a	b	c	d
a				
b				
c				
d				

# Exponential Random Graph Models (ERGMs)

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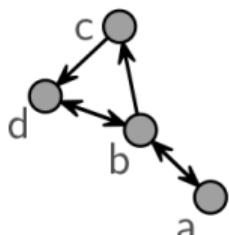
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## Social Network

- ▶ Not about individual ties.



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b				
c				
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# Exponential Random Graph Models (ERGMs)

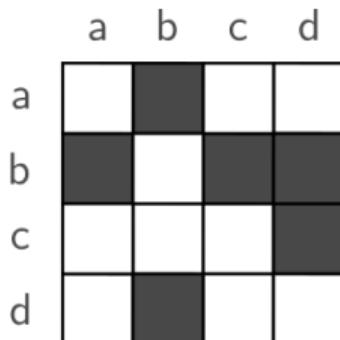
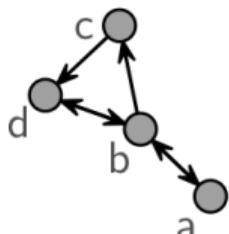
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## Social Network



- ▶ Not about individual ties.
- ▶ Statistical inference on *motifs* (triangles, dyads, homophily, etc.)

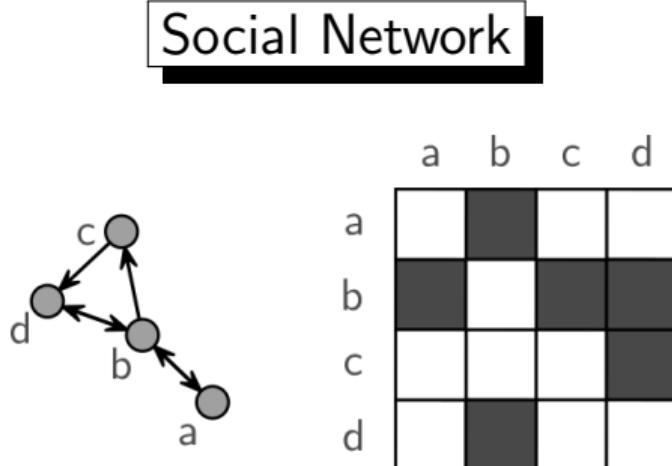
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- ▶ Not about individual ties.
- ▶ Statistical inference on *motifs* (triangles, dyads, homophily, etc.)
- ▶ Literature about ERGMs is vast, a.k.a. a low-hanging fruit.

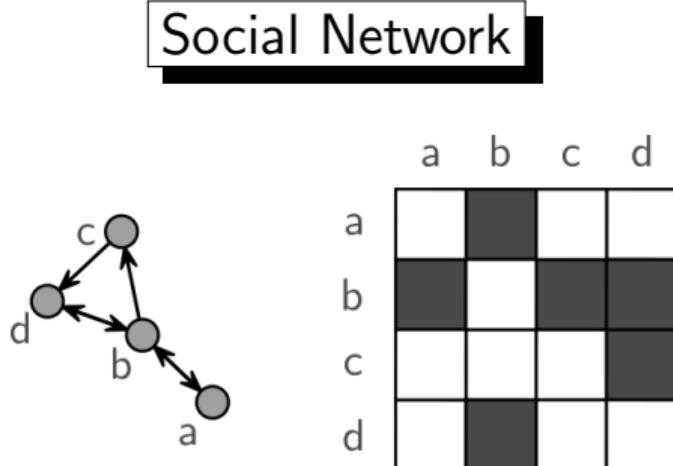
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Ultimately...

**ERGM** ≡ **Modeling binary arrays**

# Exponential Random Graph Models (ERGMs)

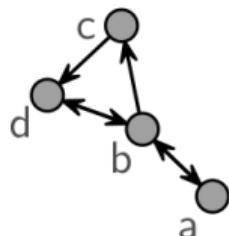
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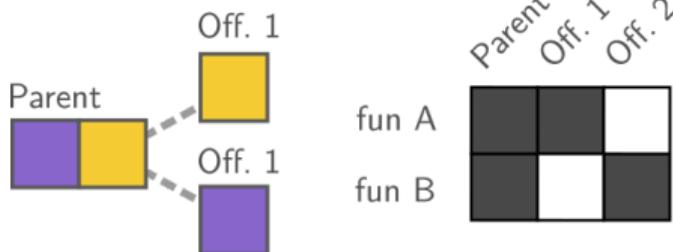
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## Social Network



	a	b	c	d
a				
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## Evolutionary Event



Social Networks are usually represented as **adjacency matrices**, and so can evolutionary events!

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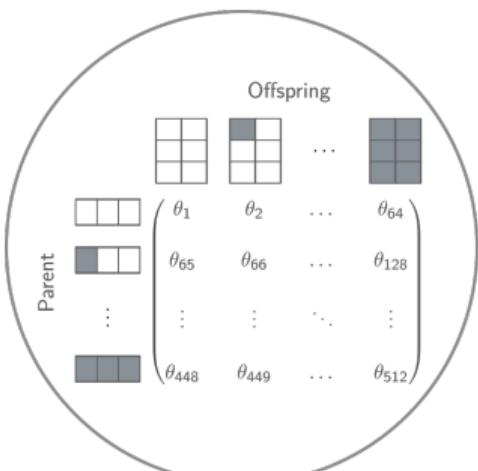
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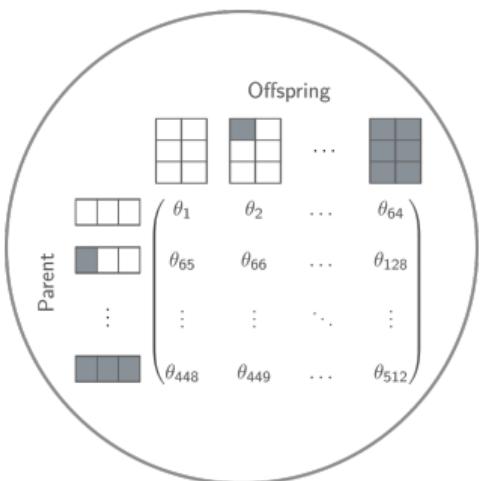


512 parameters

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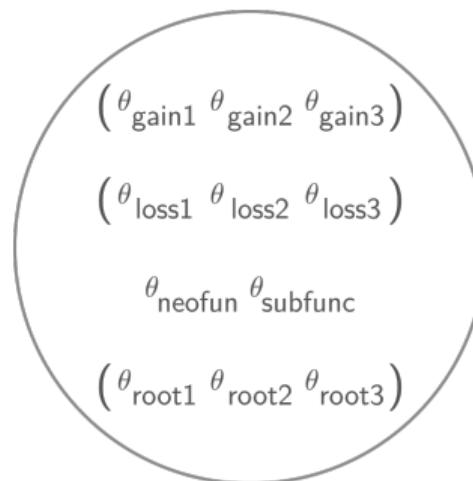
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## Full Markov Transition Matrix



512 parameters

## Sufficient statistics



11 parameters (for example)

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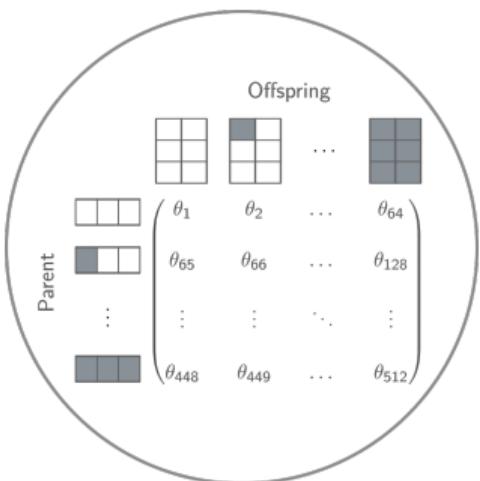
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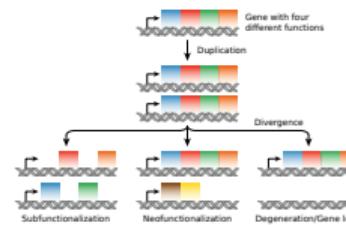
## Sufficient statistics

$$\begin{pmatrix} \theta_{\text{gain}1} & \theta_{\text{gain}2} & \theta_{\text{gain}3} \\ \theta_{\text{loss}1} & \theta_{\text{loss}2} & \theta_{\text{loss}3} \\ \theta_{\text{neofun}} & \theta_{\text{subfunc}} \\ \theta_{\text{root}1} & \theta_{\text{root}2} & \theta_{\text{root}3} \end{pmatrix}$$

Easier to fit  
Easier to interpret

$$\begin{pmatrix} \theta_{\text{gain}1} & \theta_{\text{gain}2} & \theta_{\text{gain}3} \\ \theta_{\text{loss}1} & \theta_{\text{loss}2} & \theta_{\text{loss}3} \\ \theta_{\text{neofun}} & \theta_{\text{subfunc}} \\ \theta_{\text{root}1} & \theta_{\text{root}2} & \theta_{\text{root}3} \end{pmatrix}$$

11 parameters (for example)



Rep.	Description	Definition
	Gain of function	$(1 - x_p) \sum_{n:n \in Off} x_n$
	Loss of function	$x_p \sum_{n:n \in Off} (1 - x_n)$
	Subfunctionalization	$x_p^k x_p^j \sum_{n \neq m} x_n^k (1 - x_n^j) (1 - x_m^k) x_m^j$
	Neofunctionalization	$x_p^k (1 - x_p^j) \sum_{n \neq m} x_n^k (1 - x_n^j) (1 - x_m^k) x_m^j$
	Longest branch gains	$(1 - x_p^k) \mathbf{1} (x_m^k : m = \text{argmax}_n \text{blength}_n)$

Table: Example of sufficient statistics for evolutionary transitions.

# GEESE: GEne functional Evolution using SuficiEncy

I implemented what I just described in a C++ library with a companion R package called geese. The question is: How much do we earn by using these motifs?

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# GEESE: GEne functional Evolution using SuficiEncy

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- ▶ Using 37 phylogenetic trees featuring 401 go annotations.

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- ▶ Fitted both of them using MCMC.
- ▶ Used LOO cross-validation to compute aggregated AUCs and MAE.

# GEESE for predicting gene function (cont.)

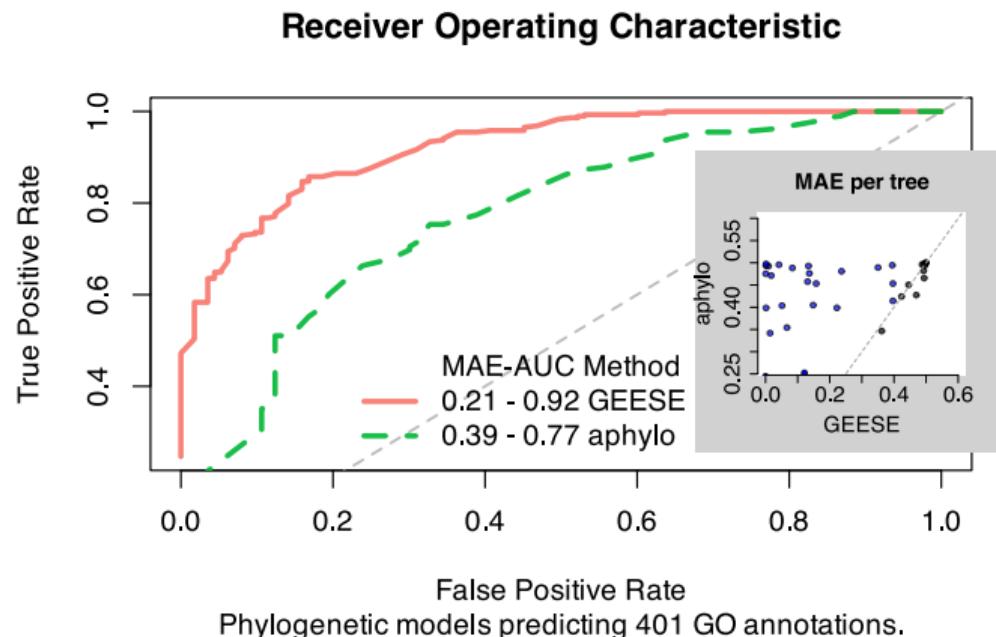
How much can we gain from a joint dist. model?

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Just controlling for preservation (having only one duplicate changing) significantly improves our predictions.

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# Mechanistic Machine Learning: State-of-the-art

- ▶ After all the data pouring, attention to causal inference and mechanistic models is coming back<sup>3,14</sup>
- ▶ Applications in Physics, Chemistry, Biomedical Imaging, and Biology<sup>16,11,7,1</sup> show the benefits of combining the two approaches.

## Mechanistic Models

- ▶ Inference driven (causality)
- ▶ Great for small datasets
- ▶ Not the most accurate

## Machine Learning Models

- ▶ Data-driven (prediction)
- ▶ Lots of points to “learn”
- ▶ Great for big data

**Important:** Mechanistic Machine Learning **is not** domain-knowledge aided feature engineering. You need a whole other model to complement the ML algorithm.

# Three strategies

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**Figure:** “A van Gogh-style painting of an android holding a large biology book in one hand and a computer in another, examining an evolutionary tree that, instead of leaves, have genes.”—DALL-E’s interpretation of my description ([link](#))

# Three strategies

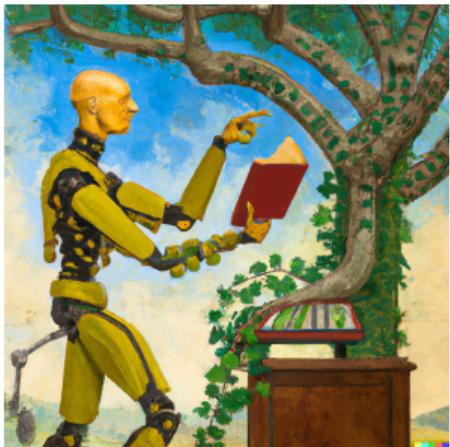
- a. **ML Correction:** Use machine learning to learn the errors of a mechanistic model.

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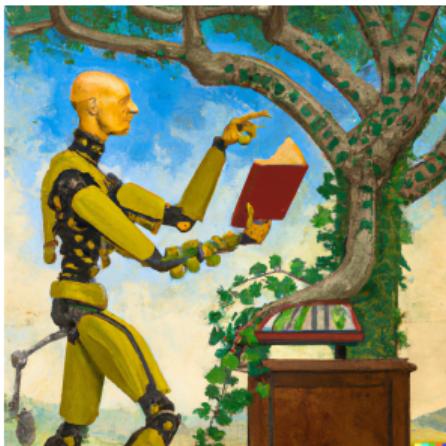
Proof of Concept



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# Three strategies

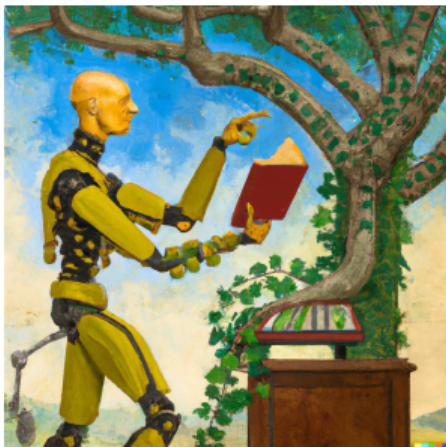
- a. **ML Correction:** Use machine learning to learn the errors of a mechanistic model.
- b. **Mechanistic Feature:** Add mechanistic predictions as a feature of a machine learning model.



**Figure:** “A van Gogh-style painting of an android holding a large biology book in one hand and a computer in another, examining an evolutionary tree that, instead of leaves, have genes.”—DALL-E’s interpretation of my description ([link](#))

# Three strategies

- a. **ML Correction:** Use machine learning to learn the errors of a mechanistic model.
- b. **Mechanistic Feature:** Add mechanistic predictions as a feature of a machine learning model.
- c. **Mechanistic Penalty:** Add constraints to the ML algorithm based on a mechanistic model.

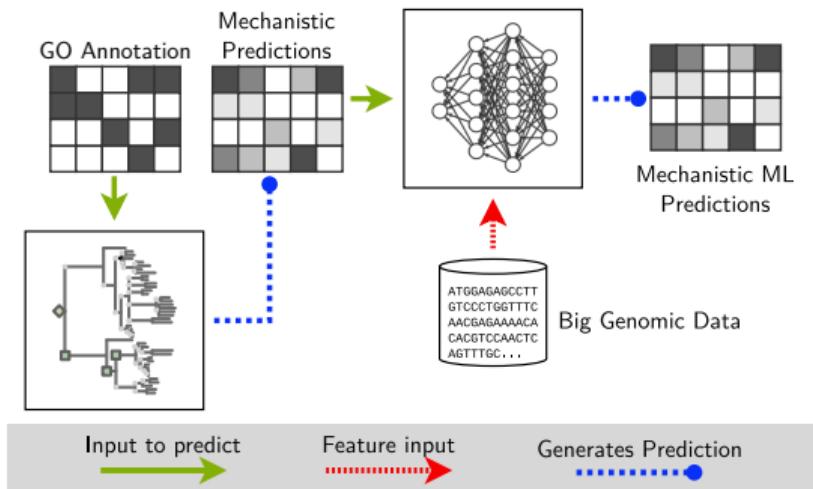


**Figure:** “A van Gogh-style painting of an android holding a large biology book in one hand and a computer in another, examining an evolutionary tree that, instead of leaves, have genes.”—DALL-E’s interpretation of my description ([link](#))

## Three strategies

#### a. ML Correction

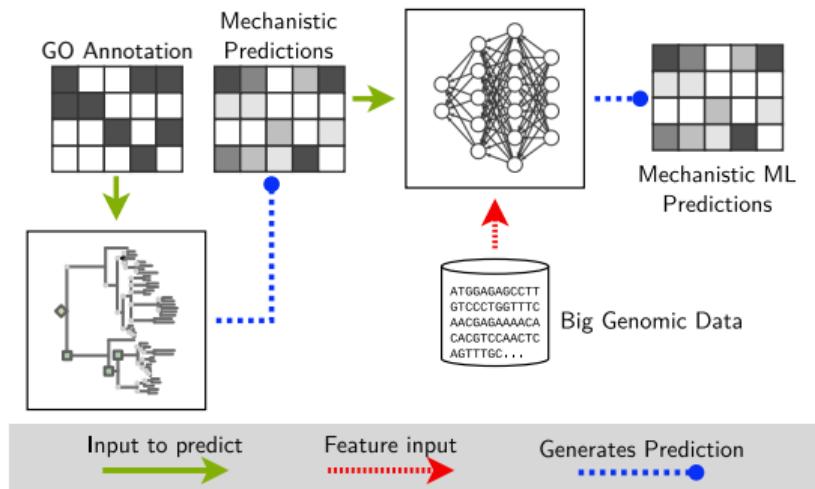
1. Fit the mechanistic model using GEESE



## Three strategies

a. ML Correction

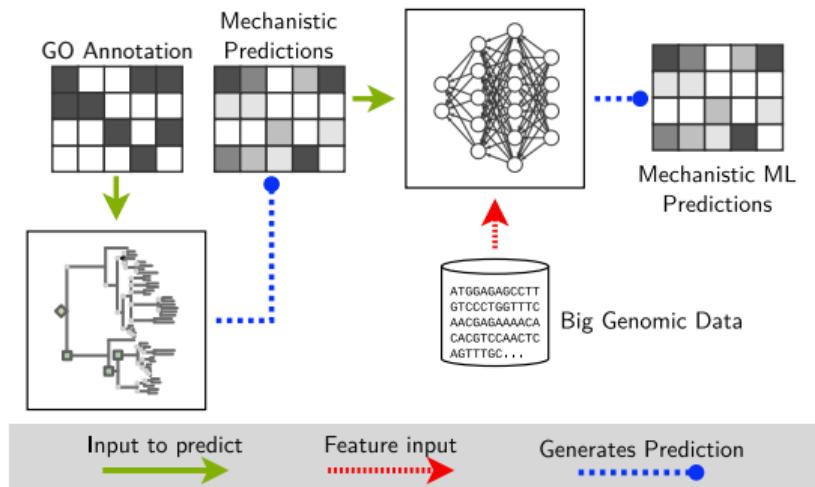
1. Fit the mechanistic model using GEESE
  2. Generate the mechanistic-based predictions,  
 $\hat{y}^{GEESE}$ ,



# Three strategies

## a. ML Correction

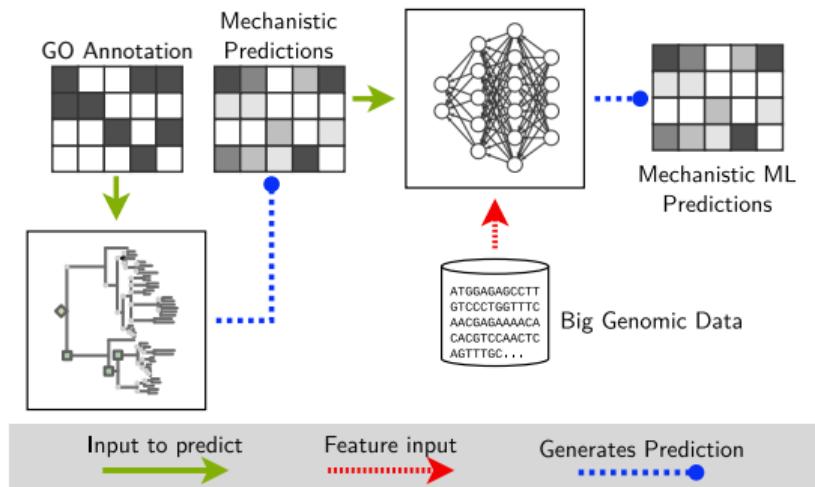
1. Fit the mechanistic model using GEESE
2. Generate the mechanistic-based predictions,  $\hat{y}^{GEESE}$ ,
3. fit an ML model  $f(X, \Omega)$  to predict  $\varepsilon \equiv (y - \hat{y}^{GEESE})$ ,



# Three strategies

#### a. ML Correction

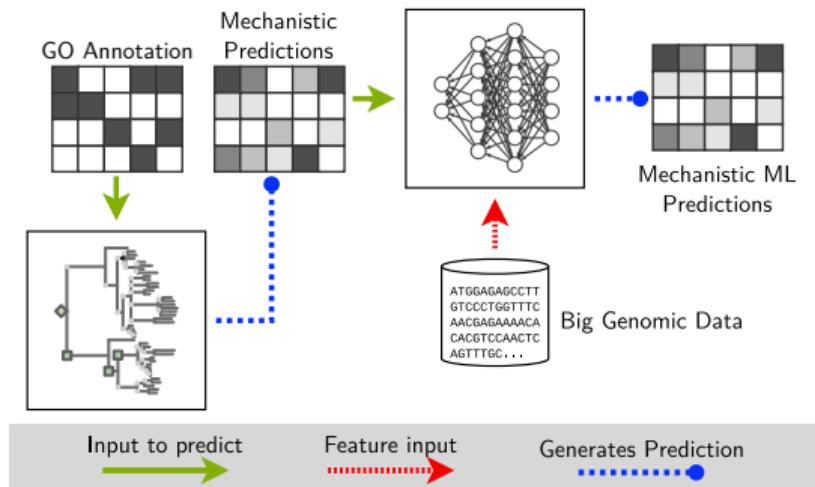
1. Fit the mechanistic model using GEESE
  2. Generate the mechanistic-based predictions,  $\hat{\mathbf{y}}^{GEESE}$ ,
  3. fit an ML model  $f(X, \Omega)$  to predict  $\varepsilon \equiv (\mathbf{y} - \hat{\mathbf{y}}^{GEESE})$ ,
  4. generate the predictions of  $\hat{\varepsilon}$ , and



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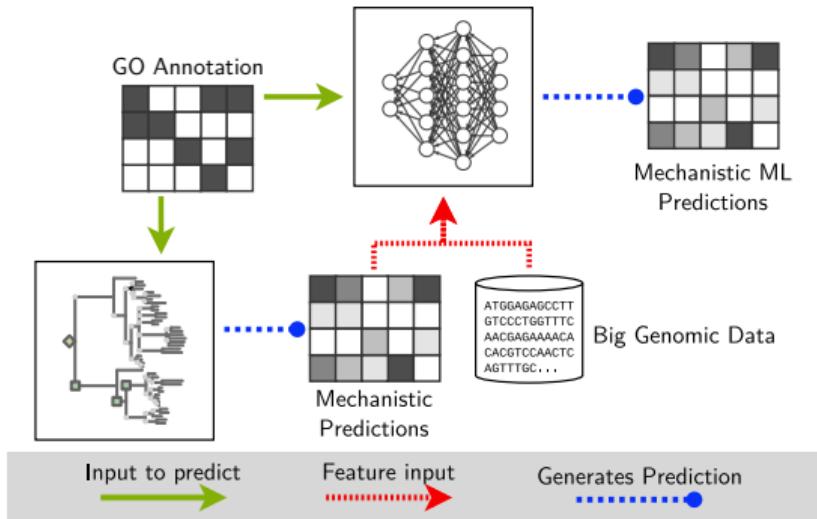
1. Fit the mechanistic model using GEESE
  2. Generate the mechanistic-based predictions,  $\hat{\mathbf{y}}^{GEESE}$ ,
  3. fit an ML model  $f(X, \Omega)$  to predict  $\varepsilon \equiv (\mathbf{y} - \hat{\mathbf{y}}^{GEESE})$ ,
  4. generate the predictions of  $\hat{\varepsilon}$ , and
  5. Compute the Mechanistic-ML predictions as  
 $\hat{\mathbf{y}}^{MML1} \equiv \hat{\mathbf{y}}^{GEESE} + \hat{\varepsilon}$



# Three strategies

#### b. Mechanistic Feature

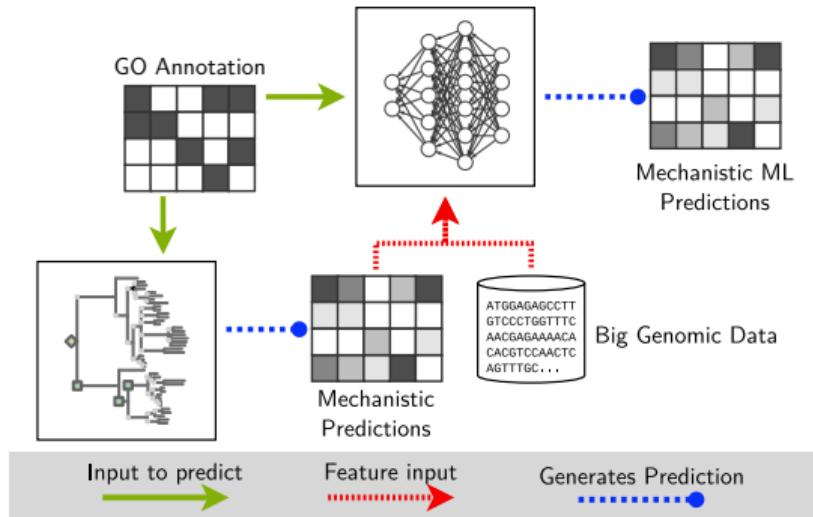
1. Fit the mechanistic model using GEESE,



# Three strategies

## b. Mechanistic Feature

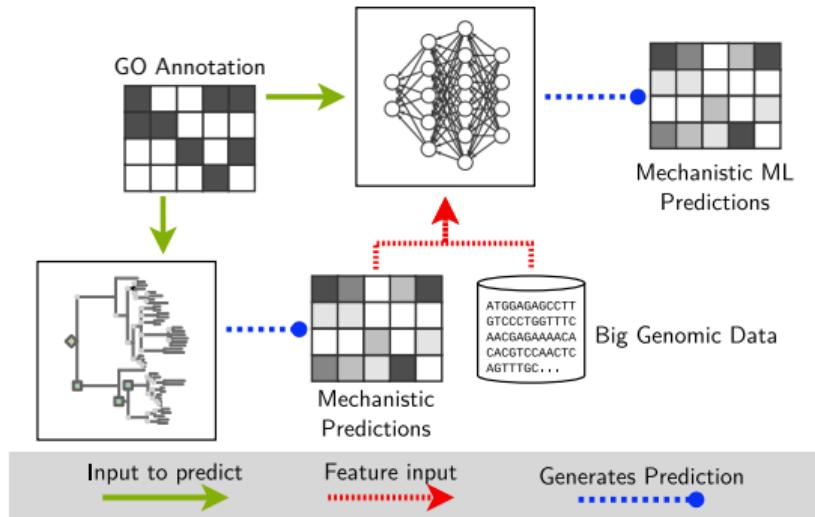
1. Fit the mechanistic model using GEESE,
2. generate the mechanistic-based predictions,  $\hat{y}^{GEESE}$ ,



# Three strategies

#### b. Mechanistic Feature

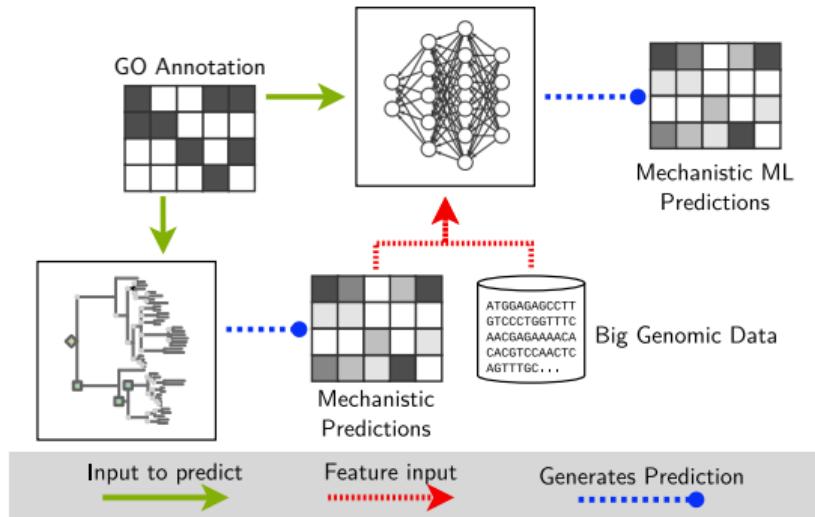
1. Fit the mechanistic model using GEESE,
  2. generate the mechanistic-based predictions,  $\hat{y}^{GEESE}$ ,
  3. fit an ML model that uses the mechanistic predictions as features,  $f(X, \Omega, \hat{y}^{GEESE})$ , and



## Three strategies

#### b. Mechanistic Feature

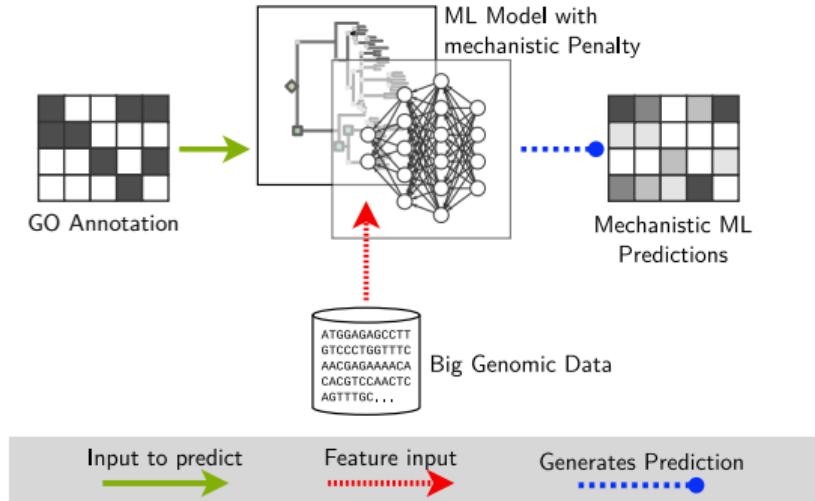
1. Fit the mechanistic model using GEESE,
  2. generate the mechanistic-based predictions,  
 $\hat{y}^{GEESE}$ ,
  3. fit an ML model that uses the mechanistic predictions as features,  $f(X, \Omega, \hat{y}^{GEESE})$ , and
  4. Compute the Mechanistic-ML predictions as  
 $\hat{y}^{MML2} \equiv f(X, \Omega, \hat{y}^{GEESE})$



## Three strategies

### c. Mechanistic Penalty

1. Fit the mechanistic model using GEESE and store the parameter estimates  $\hat{\theta}$ ,



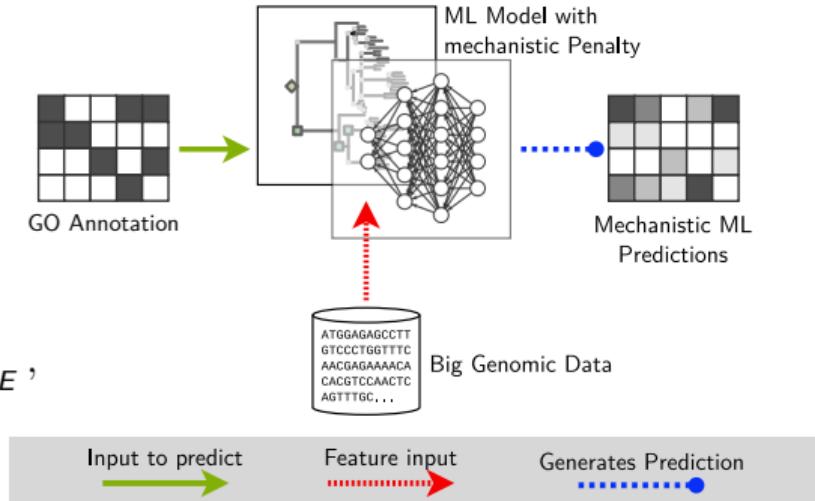
## Three strategies

### c. Mechanistic Penalty

1. Fit the mechanistic model using GEESE and store the parameter estimates  $\hat{\theta}$ ,
  2. minimize the following loss function:

$$L(y^{obs}X, \Omega) - \mathcal{L}(f(y^{obs}X, \Omega))_{GEESE},$$

where  $\mathcal{L}(\cdot)$  is the likelihood function under GEESE.



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# Beyond GO and Trees... Bgee

The **Bgee** project “is a **database** for retrieval and **comparison of gene expression** patterns **across multiple animal species**. It provides an intuitive answer to the question ‘where is a gene expressed?’ and supports research in cancer and agriculture as well as evolutionary biology.” – Bastian et al. [4]

- ▶ Raw expression annotations.
- ▶ Standardized expression scores (so can compare across species/tissues).
- ▶ And also yes/no expression annotations based on the standardized scores.

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## Beyond GO and Trees... Bgee (cont.)

Divergence across species in gene expression levels has been linked to evolutionary events,<sup>13,9</sup> i.e., expression levels clustered phylogenies.

Thinking of different ways to use it as:

- ▶ As an additional feature for our model: “Given the phylo, observed annotations, **and expression levels in  $n$  tissues**, . . .”
- ▶ As 0/1 variable (expression is present/absent) to predict in our model: “Model the evolution of gene function **and expression**.”
- ▶ As part of a prediction model in, say, a Machine Learning Model.

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# What went into the blender

## Data Feats

- ▶ Bgee 15 dataset: approx 7 billion annotations for 1.5 million genes.
- ▶ Our dataset: 1,484 predictions for 1,318 genes.
- ▶ Search by Gene name: 9,923,427 Bgee annotations.

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## Final model

- ▶ 10 GO terms (in a full-Markov model, this is 1 MM params).
- ▶ 278 annotations for 256 genes.
- ▶ 10 GEESE predictions for each gene.
- ▶ 46 Bgee score for gene expression computed as **mean expression score by gene-genus**

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**GO terms:** GO:0004672, GO:0004713, GO:0004867, GO:0005730, GO:0005829, GO:0005886, GO:0006468, GO:0009408, GO:0015020, GO:0060070

**Genus:** Anguilla, Anolis, Astatotilapia, Astyanax, Bos, Branchiostoma, Caenorhabditis, Callithrix, Canis, Capra, Cavia, Cercocetus, Chlorocebus, Danio, Drosophila, Equus, Esox, Felis, Gadus, Gallus, Gasterosteus, Gorilla, Heterocephalus, Homo, Latimeria, Lepisosteus, Macaca, Manis, Meleagris, Microcebus, Monodelphis, Mus, Neolamprologus, Nothobranchius, Ornithorhynchus, Oryctolagus, Oryzias, Ovis, Pan, Papio, Poecilia, Rattus, Salmo, Scophthalmus, Sus, Xenopus

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# Mechanistic ML

We are comparing three models:



Phylogenetic based  
predictions (evolution of  
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# Mechanistic ML

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Linear Prob. model using  
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# Mechanistic ML

We are comparing three models:

GEESE

Bgee

GEESE + Bgee

Phylogenetic based  
predictions (evolution of  
gene function)

Linear Prob. model using  
expression as predictors.

Linear Prob. model using  
expression as predictors  
**and** predictions made by  
GEESE.

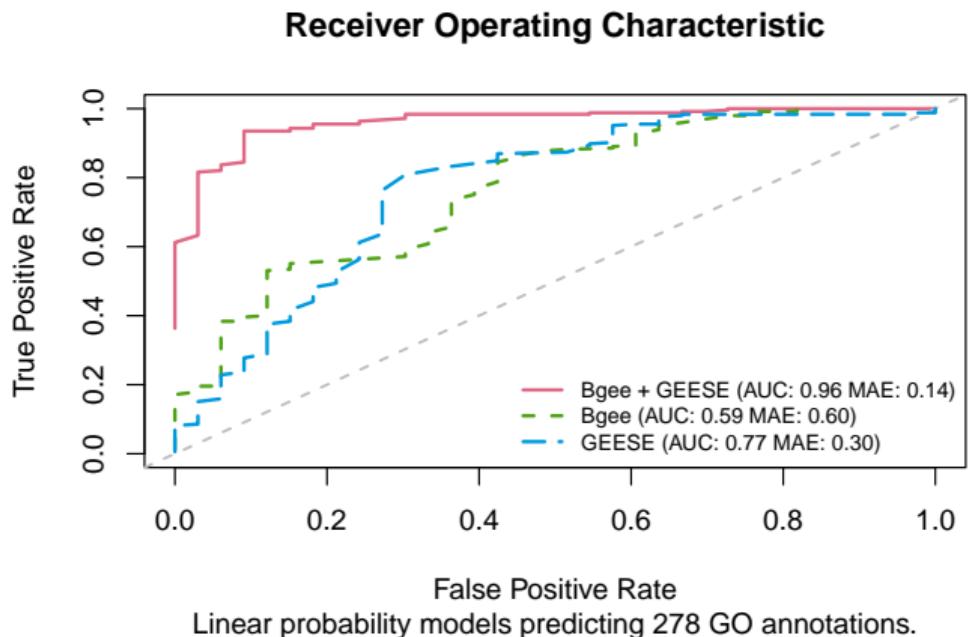
# Mechanistic ML (prelim res.)

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Both AUC and MAE were computed only using predictions for which we knew the true value.

# Discussion

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# Discussion

## Gene function

- ▶ We are racing to discover what genes do.
- ▶ Experimental assessment is expensive (money and time,) → automatic annotations.
- ▶ Many ways to do it (seq. homology, evolutionary theory, ML, etc.)
- ▶ The best methods use ML (pattern discovery)... but none (AFAIK) are based on bio. theory.

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# Discussion

## Gene function

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- ▶ We proposed an Evolutionary model of Gene Function.
  - ▶ This new model, GEESE, uses sufficiency to reduce “Markov complexity.”
  - ▶ We showed it really helps.

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# Discussion

## Gene function

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## Evol. Model

- ▶ We proposed an Evolutionary model of Gene Function.
- ▶ This new model, GEESE, uses sufficiency to reduce “Markov complexity.”
- ▶ We showed it really helps.

## Mechanistic ML

- ▶ Mechanistic Machine Learning (mixing theory-based models with ML) promises improved predictions.
- ▶ I showed an application using gene expression (Bgee).
- ▶ Adding our mechanistic predictions (based on GEESE) boosted quality

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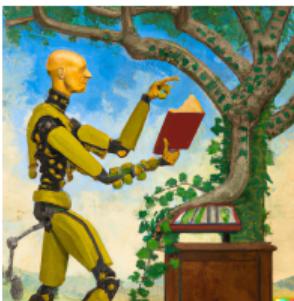
Evolution of Gene Function

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# Thank you!

## Predicting of Gene Functions by Leveraging Biological Insights with Mechanistic Machine Learning



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[george.vegayon@utah.edu](mailto:george.vegayon@utah.edu)  
Division of Epidemiology @ University of Utah

Jan 11th, 2023 @ Data Science Seminar

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# Tree likelihoods: Felsenstein's Pruning algorithm

All possible transitions from  $\mathbf{x}_n$

Transition Probability (ERGM)

$$\mathbb{P}(\tilde{D}_n \mid \mathbf{x}_n, \Theta) = \sum_{\mathbf{x}} \mathbb{P}(\mathbf{x} \mid \mathbf{x}_n) \prod_{m \in \mathcal{O}(n)} \mathbb{P}(\tilde{D}_m \mid \mathbf{x}_m)$$

# Tree likelihoods: Felsenstein's Pruning algorithm

All possible transitions from  $x_n$  → Transition Probability (ERGM)

$$\mathbb{P}(\tilde{D}_n \mid x_n, \Theta) = \sum_x \mathbb{P}(x \mid x_n) \prod_{m \in O(n)} \mathbb{P}(\tilde{D}_m \mid x_m)$$

Model Parameters → Vector of Sufficient Statistics

$$\mathbb{P}(x \mid x_n) = \frac{\exp\{\Theta^t s(x, x_n)\}}{\sum_{x'} \exp\{\Theta^t s(x', x_n)\}}$$

Normalizing Constant → the *lingua franca* of SNA

... I implemented this (and more) on **barry**

# Some computational features of barry

