



Lecture 20

Causality

Announcements: Part 1

- Homework 7 due Thursday, March 12
 - Midterm on March 13th, 7:10 - 9:00 pm
 - **Now online on Gradescope.com**
 - Must work COMPLETELY by yourself in a quiet room
 - Proctoring in 2050 VLSB if needed
 - You cannot use any resources outside of:
 - Midterm Reference Sheet
 - Blank scratch paper
 - Online textbook
 - Multiple versions - will receive email at 6:00 pm
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Announcements: Part 2

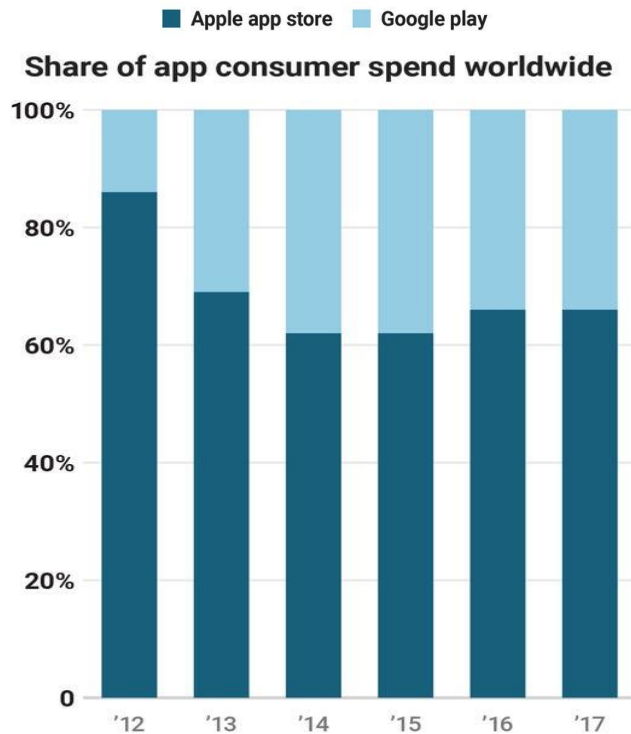
- In-Person Office Hours:
 - Cancelled today & Tuesday
 - Lecture:
 - **Online only**, starting this Wednesday
 - Labs:
 - This week:
 - Review worksheet walk-through posted Wednesday
 - **Next week onwards: in-person labs cancelled**
 - Walk-throughs posted Wednesdays
 - Lab notebooks due Fridays at 11:59pm
 - Lab rooms on campus still available but GSIs remote
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Review: Comparing Two Samples

- Null:
 - In the population, the distributions of the birth weights of the babies in the two groups are the same. (They are different in the sample just due to chance.)
 - Alternative:
 - In the population, the babies of the mothers who smoked weigh less, on average, than the babies of the non-smokers.
- (Demo)
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Importance of Random Assignment

Apple users more willing to pay for apps



Importance of Random Assignment

- iOS users spend 2x as much as Android users on 3rd party apps
 - *Is **higher spending** caused by users owning **iPhone**?*
 - Can't Tell:
 - Users aren't randomly assigned a phone
 - Other factors contribute to their phone purchasing decisions (e.g. income, geography)
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Causality

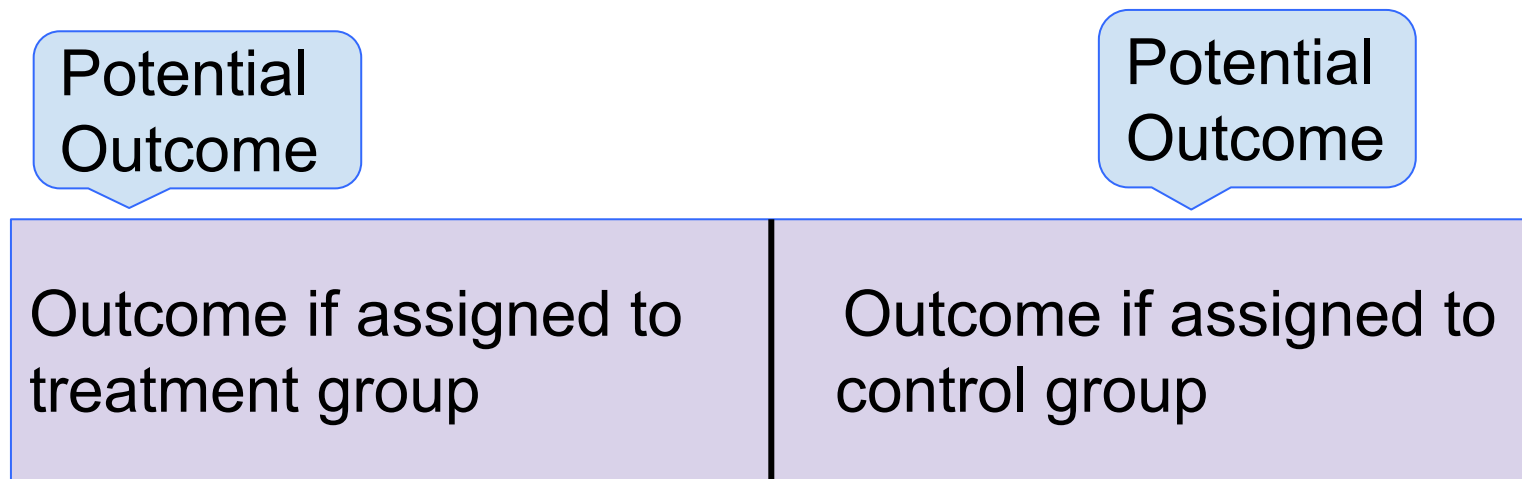
Randomized Controlled Experiment

- Sample A: **control group**
- Sample B: **treatment group**
- **If the treatment and control groups are selected at random, then you can make causal conclusions.**
- Any difference in outcomes between the two groups could be due to
 - chance
 - the treatment

(Demo)

Before the Randomization

- In the population there is one imaginary ticket for each of the 31 participants in the experiment.
- Each participant's ticket looks like this:



The Data

16 randomly picked tickets show:

	Outcome if assigned to control group
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The remaining 15 tickets show:

Outcome if assigned to treatment group	
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The Hypotheses

- **Null:**

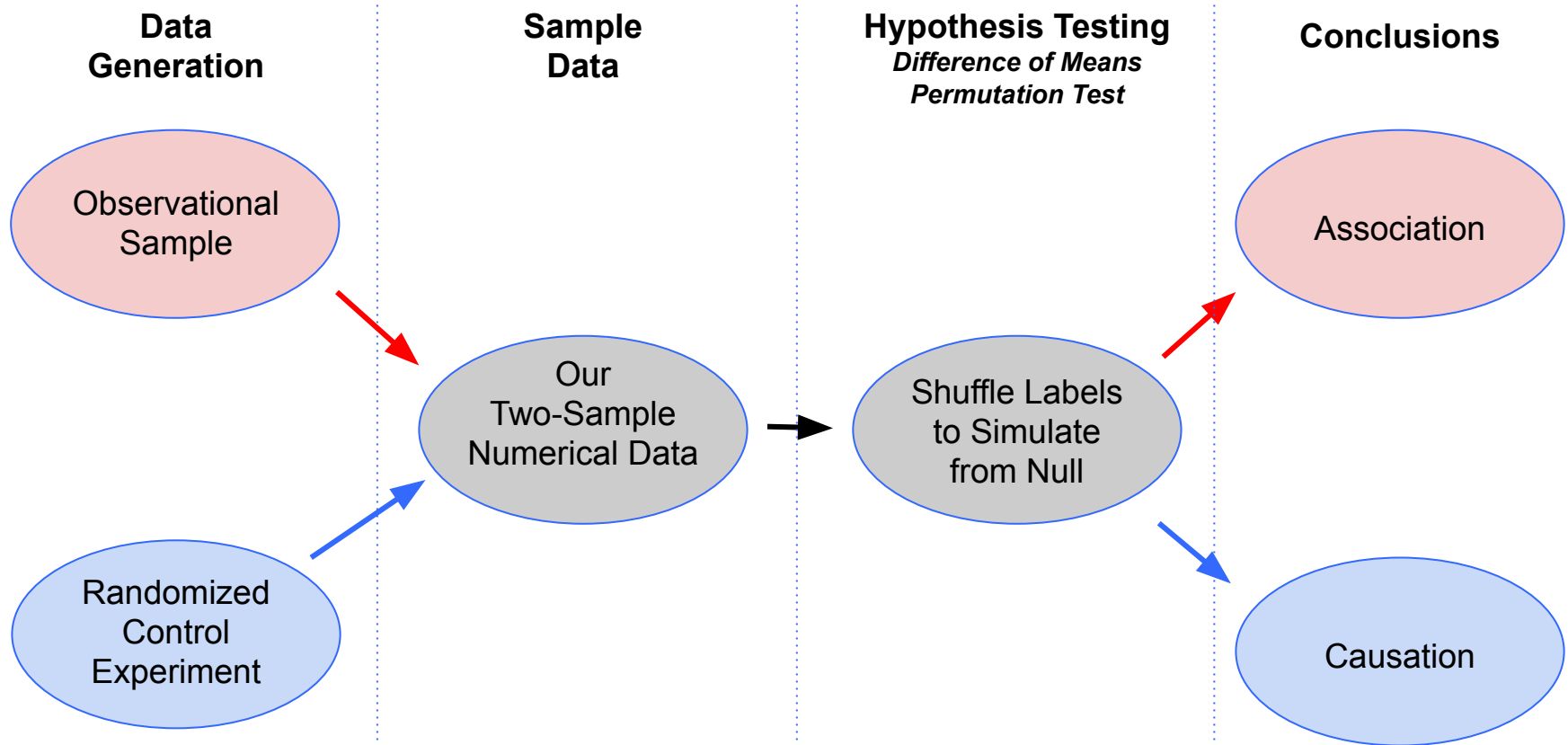
- In the population, the distribution of all potential control scores is the same as the distribution of all potential treatment scores.
- tl;dr the treatment has no effect

- **Alternative:**

- In the population, more of the potential **treatment** scores are 1 (pain improves) than the potential **control** scores.

(Demo)




Random Assignment & Shuffling



An Error Probability

Can the Conclusion be Wrong?

Yes.

	Null is true	Alternative is true
Test favors the null		
Test favors the alternative		

An Error Probability

- The cutoff for the P -value is an error probability.
 - If:
 - your **cutoff is 5%**
 - and the **null hypothesis happens to be true**
 - then there is about a **5% chance** that **your test will reject the null hypothesis**.
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P-value cutoff vs P-value

- P-value cutoff
 - Does not depend on observed data or simulation
 - Decide on it before seeing the results
 - Conventional values at 5% and 1%
 - Probability of hypothesis testing making an error
 - P-value
 - Depends on the observed data and simulation
 - Probability under the null hypothesis that the test statistic is the observed value or further towards the alternative
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